

# Lecture 10B: IV: Heterogeneous Effects

*Introduction to Econometrics, Fall 2017*

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## Review the last lecture

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  - When IV satisfy these two assumptions, the causal effect of coefficients of interest, TSLS estimator,  $\beta_{TSLS}$  can be NOT unbiased but **consistent**.
  - The sampling distribution of the TSLS estimator is also normal in large samples, so the general procedures for statistical inference in OLS can be used.

## IV with Heterogeneous Causal Effects: Simple Case

# Introduction :

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  - Men with lottery numbers below a cutoff were eligible for the draft
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- The lottery outcome was random and seems reasonable to suppose that its only effect was on veteran status: exogenous.

## Example: Angrist(1990): heterogeneous effects

- We can classify individuals according to assignment( $Z$ ) and treatment( $X$ ) into four parts

		$Z=0$	
		$D=0$	$D=1$
$Z=1$	$D=0$	Never-taker	Defier
	$D=1$	Complier	Always-taker

Figure 1:



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- Angrist and Imbens(1994) called it as **Local Average Treatment Effect(LATE)**, thus the treatment effect on those that change their behavior under the instrument.

# IV with Heterogeneous Causal Effects: Generalization

# Introduction

- If the population is *heterogeneous*, then the  $i^{th}$  individual now has his or her own causal effect,  $\beta_{1i}$ , then the population regression equation can be written

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- $\beta_{1i}$  is a random variable that, just like  $u_i$ , reflects unobserved variation across individuals.
- The average causal effect is the population mean value of the causal effect,  $E(\beta_{1i})$  which is the expected causal effect of a randomly selected member of the population.

# OLS with Heterogeneous Causal Effects

- If there is heterogeneity in the causal effect and if  $X_i$  is randomly assigned, then the differences estimator is a consistent estimator of the average causal effect.

$$\begin{aligned}
 \hat{\beta}_{ols} &= \frac{s_{XY}}{s_X^2} \xrightarrow{p} \frac{Cov(Y_i, X_i)}{Var(X_i)} = \frac{Cov(\beta_{0i} + \beta_{1i}X_i + u_i, X_i)}{Var(X_i)} \\
 &= \frac{Cov(\beta_{1i}X_i, X_i)}{Var(X_i)} \\
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- Thus, if  $X_i$  is randomly assigned,  $\hat{\beta}_1$  is a *consistent* estimator of the average causal effect  $E(\beta_{1i})$ .



## IV Regression with Heterogeneous Causal Effects

- Specifically, suppose that  $X_i$  is related to  $Z_i$  by the linear model

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- where the coefficients  $\pi_{0i}$  and  $\pi_{1i}$  vary from one individual to the next. And it is the first-stage equation of TSLS with the modification of heterogeneous effect of  $Z$  on  $X$ .

## IV Regression with Heterogeneous Causal Effects

- Then TSLS estimator becomes

$$\hat{\beta}_{2SLS} = \frac{s_{ZY}}{s_{ZX}} \xrightarrow{p} \frac{\sigma_{ZY}}{\sigma_{ZX}} = \frac{E(\beta_{1i}\pi_{1i})}{E(\pi_{1i})}$$

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- The TSLS estimator converges in probability to the ratio of the expected value of the product of  $\beta_{1i}$  and  $\pi_{1i}$  to the expected value of  $\pi_{1i}$ .
- It is a **weighted** average of the individual causal effects  $\beta_{1i}$ . The weights are  $\frac{\pi_{1i}}{E(\pi_{1i})}$ , which measure the relative degree to which the instrument influences whether the  $i_{th}$  individual receives treatment,

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- In other words, TSLS estimator is a consistent estimator of a *weighted average of the individual causal effects*, where the individuals who receive the *most weight* are those for *whom the instrument is most influential*.

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- Aside from these three special cases, in general the local average treatment effect differs from the average treatment effect.

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- The difference arises because each researcher is implicitly estimating a different weighted average of the individual causal effects in the population.
- Recall: **J-test of overidentifying restrictions** can reject if the two instruments estimate different local average treatment effects, even if both instruments are valid. In general neither estimator is a consistent estimator of the average causal effect.



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  - Can one instrument identify the average effect induced by another source of variation?
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- The answer to these questions is usually: **NO**, at least without additional assumptions.

## Some Practical Guides by Angrist and Pischke(2012)

# Practical Guides

## 1 Check IV relevance



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- *Falsification test*: Test the reduced form effect of  $Z_i$  on  $Y_i$  in situations where it is impossible or extremely unlikely that  $Z_i$  could affect  $X_i$ . Because  $Z_i$  can't affect  $X_i$ , then the exclusion restriction

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  - Pick your best single instrument and report just-identified estimates using this one only because just-identified IV is relatively unlikely to be subject to a weak bias.
  - Worry if it is substantially different from what you get using multiple instruments.
  - Check over-identified 2SLS estimates with LIML. LIML is less than precise than 2SIS but also less biased. If the results come out similar, be happy. If not, worry, and try to find stronger instruments.

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- Is this the LATE you would want? Is it a quantify of theoretical interest?

# How to Evaluate IV paper in a simple way?

## ① Relevant: The first stage regression

- Does the author report the first stage regression?
- Does the instrument perform well in the first stage?
- Testable: rule of thumb: first stage  $F > 10$

## ② Exclusion restriction:

- Is the instrument exogenous enough?(the random assignment is the best)
- Would you expect a direct effect of Z on Y
- Not directly testable: Except when equation is overidentified.

## ③ What LATE is being estimated?

- Whose behavior is affected by the instrument?
- Is this the LATE you would want? Is it a quantify of theoretical interest?
- Would other LATEs possible yield different estimates?

# Where Do Valid Instruments Come From?

# Where do we find an IV?

- Generally Speaking

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  - ① Economic Theory/Logics
  - ② Exogenous Source of Variation in  $X$ (natural experiments)

# Where do we find an IV?

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- Result: The estimated effect was three times larger than the effect estimated using OLS.

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- But potential enrollment also fluctuates because parents with young children choose to move into an improving school district and out of one in trouble. She used as her instrument not potential enrollment, but the deviation of potential enrollment from its long-term trend.
- Result: the effect on test scores of class size is small.

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- the number of Rivers: Hoxby(2000)

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- Angrist & Evans(1998): have same sex or different sex children used to estimate the impact of an additional birth on women labor supply.

## Several Applications in China Studies

## Fang et al. (2012)

- Feng et al.(2012) “The Returns to Education in China: Evidence from the 1986 Compulsory Education Law”.



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- Li and Zhang(2007),Liu(2012)- “One Child policy”
- Fang and Zhao(2008)- “Christian in China”: The number of children enrollment in Christian’s primary school per one thousand persons across cities.
- Ying Bai and Ruixue Jia(2014)-“keju” and “the number of small rivers”