

# **Essays on the Economics of Heterogeneity**

**A thesis submitted in partial fulfillment of the requirements  
of the degree of Doctor of Philosophy (Ph.D.) in Economics**

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*To Nadien, who had to lift my spirits more than once over the last four  
years;  
my mother, as I couldn't have made it here without her love and support;  
and Emil, whose laugh carried me through the final stages of this project.*

# Declaration

## **I wish to declare**

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## **Details of collaboration and publications:**

Parts of Chapter 4 were undertaken as joint work with Ryan Weldzius.

**Signature:** Nils-Holger Gudat

**Date:** 28th of July, 2014

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## **Abstract**

The analysis of the effects of heterogeneity on aggregate economic outcomes has seen a resurgence in the recent macroeconomic literature. The exponential increase in computer power over the last decades has allowed researchers to solve ever more complex theoretical models with meaningful heterogeneity along various dimensions, while at the same time bringing ever more granular micro-level data to the table when testing the model predictions.

This thesis explores two varieties of this recent vintage of models of heterogeneity. The first part of the thesis explores the implications of learning about idiosyncratic income risk on the wealth distribution and compares the model results to observed data, with a focus on the effects of changes in cross-sectional income inequality. To this end, income processes with profile heterogeneity are estimated from survey data and then used as inputs for a structural model of household saving, in which households are imperfectly informed about the stochastic process governing the evolution of their lifetime income, but can learn about the underlying parameters. Model results for a standard model are compared to those of a model with consumption habits, while a structural break in the cross-sectional variance of idiosyncratic income growth rates is employed in an attempt to capture the secular rise

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in income inequality observed since the late 1970s and explore its implications for the predicted wealth distribution. The second part of the thesis looks at heterogeneity on the production side of the economy and its implications for international trade. Following an existing approach in the literature, we develop testable implications of the Melitz and Ottaviano (2008) model of trade, in which firms differ in their productivity and have to make production and exporting decisions in the face of costs to trade. Our approach allows us to test the effects of NAFTA on productivity in nine manufacturing sectors in North America and thereby complement and extend the existing literature on the effects of trade liberalisations.

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# Chapter 1

## Introduction

### 1.1 Motivation

Distributional questions are increasingly making a comeback in economics.

### 1.2 Outline

This thesis is structured as follows. Chapter 2 gives an overview of the research on theoretical models of the household wealth distribution in the last two decades. It will highlight the key empirical challenges by presenting stylized facts on the cross sectional wealth distribution in a number of countries and their evolution over time. Then, an overview of existing modeling approaches is presented,

Chapter 3 builds on the discussion in Chapter 2 by constructing a model of learning about idiosyncratic income processes and using it to simulate wealth distributions. As a first step, income processes with profile heterogeneity are estimated for different sub-periods of PSID data from 1968 to 1999 and from

BHPS data in order to assess the stability of the cross-sectional variance of income growth rates across time and labor markets. The estimates are then used as inputs in a structural model of household saving first employed by Guvenen (2007), with the addition of both structural breaks in the cross-sectional variance of growth rates and habits in consumption. The models predictions for the evolution of the US consumer wealth distribution are then benchmarked against data from the Survey of Consumer Finances.

Chapter 4 gives a brief introduction into trade models based on firm-level heterogeneity, before developing an estimable model in the spirit of Chen et al. (2009). The model is then tested on a data set of prices, productivity, and markups for nine manufacturing industries in the Canada, Mexico and the United States over the period of 1994 to 2010. In an extension of the approach of Chen et al. (2009), we also conduct a sub-sample analysis in which we split the same into fixed and free entry industries, based on a measure of firm turnover developed on the basis of prior research.

Chapter 5 concludes the thesis and discusses potential avenues for future research.

## **Chapter 2**

# **Models of the wealth distribution**

### **2.1 Introduction**

The distribution of wealth and income has recently made a comeback to the centre of economic discourse in advanced economies. The ongoing rise of income inequality, observed since the early 1980s especially in Anglo-Saxon countries, has received renewed attention in the public sphere since the financial started taking its toll on living standards across the world. At the same time, the best-selling book by Piketty (2014) led to a surge in interest in the role of capital in the economy, and, by extension, the distribution of wealth, both in the academic literature and the popular press.

While the broader public has only recently picked up on the issues arising around income and wealth distributions, they have sat squarely in the centre of many sub-fields of economics for a long time. The income distribution has long been of interest to labour economists trying to understand the forces shaping the evolution of earnings in the labour market, while at least the accumulation of aggregate

wealth plays a central role in macroeconomic models of economic growth. This chapter, as well as the chapter ??, focuses on the intermediate step that takes us from an income to a wealth distribution - economic models of household saving. When attempting to build a model of the wealth distribution, the first step of course is to get an understanding of the object we want to model. To this end, this chapter starts by presenting stylised facts of the wealth distributions in advanced countries and discusses some of the limitations of the data available. It then builds a simple life-cycle model of consumption and savings to guide the following discussion and fix notation. Using this basic model, different savings motives and their importance in the context of aggregate wealth accumulation are discussed. Following this, the role of income uncertainty and market structure is examined in more detail.

## 2.2 Stylised facts

The most notable and consistent fact that emerges when looking at wealth distributions across all countries and different time periods is that wealth is highly unevenly distributed, much more so than income. This can be readily seen when comparing Gini indices and top shares of income and wealth, as in Table 2.1 or looking at histograms and cdfs of wealth and income distributions as in Figure ??. It is important to note that in producing these aggregate numbers and figures, one necessarily has to make decisions on how exactly to construct measures of income and wealth, which will have to be kept in mind when comparing model predictions with empirical numbers. When constructing an income measure, the obvious starting point are labour earnings, and for many economic applications simply

Table 2.1: Measures of wealth concentration in different data sets.

observing an individual's wages will be enough. When thinking about questions of consumption smoothing though, we are ultimately interested in accounting for all claims on consumption goods available to an individual or household in a given period, and while for most people the largest part of these claims stem from labour earnings, we will also want to account for the effect of government programs (by constructing a post-tax, post-transfer income measure), income from accumulated assets, and potentially even informal insurance arrangements such as inter-vivos transfers between family and friends. In constructing wealth measures, we again have to think closely about the question we are trying to answer when constructing them. If the goal is to account for all productive capital in the economy that can be used in production, a measure of total net wealth aggregating all forms of asset and debt classes, and including some durable consumption goods such as cars. When thinking about the role of wealth in helping the household to smooth out income fluctuations, it might be more appropriate to exclude very illiquid assets such as housing, and look more closely at the role of debt for households which might be at their borrowing constraint and are thus vulnerable to reductions in their borrowing limit, even though their net wealth (including illiquid assets) is positive. Finally, important questions are raised by the existence of various government and private pension schemes, which have to be factored in when constructing measures of a household's lifetime resources, but whose exact value might be uncertain (for the case of defined contribution plans) and not well understood by households themselves.

Figure 2.1: Histograms and cdfs of household net wealth in different data sets.

## 2.3 A workhorse model

The basic model underlying the discussion of savings behaviour and wealth accumulation in this chapter is the life-cycle model of household behaviour dating back to Modigliano and Brumberg (1954)<sup>1</sup>. The model can be written as a single household solving the problem

$$\max_{\{c_{t+j}\}_{j=0}^{T-t}} \sum_{j=0}^{\infty} \delta^{t+j} \mathbb{E}_t [u(c_{t+j}, z_{t+j})] \quad (2.1)$$

subject to

$$a_{t+1} = (1 + r)(a_t + y_t - c_t) \quad (2.2)$$

where  $T$  is the last period of the planning horizon,  $\delta$  is the subjective discount factor,  $u()$  is the instantaneous felicity function – usually assumed to be of the CRRA form,  $\frac{c^{1-\sigma}}{1-\sigma}$ , where  $\sigma$  is the coefficient of relative risk aversion –,  $c$  is consumption,  $a$  are financial assets, which allow the household to transfer resources across time,  $r$  is a one-period interest rate, and  $y$  is income.  $z$  is used as a stand-in variable denoting the fact that households might, in general, care about other things that are not captured by the concept of current consumption; examples would be habits or durable consumption (which break the time-

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<sup>1</sup>A more detailed treatment of the general class of models can be found both in Browning and Crossley (2001) and in Attanasio and Weber (2010), although both papers have their focus on household consumption behaviour rather than wealth accumulation.



separability of the utility function), leisure time, particular classes of assets (such as housing) or bequests left to future generations. While in general,  $T \rightarrow \infty$  is a possibility, and infinite horizon versions – first advocated by Friedman (1957) – of the life-cycle model are widely used in macroeconomic applications, the finite horizon model will be more useful for the following discussion and forms the centrepiece of this thesis for a number of reasons which will become clear as we progress.

## 2.4 Saving motives

When trying to understand wealth distributions through the lens of the model outlined above, the key question is: why do households save? The basic model, in which consumers only care about the time path of instantaneous utility derived from consumption, suggests that households will save if and only if it leads to preferential allocation of consumption over time – they engage in consumption smoothing. As Browning and Crossley (2001) point out, consumption smoothing can happen at different frequencies, depending on the exact set-up of the model. In Modigliano and Brumberg (1954) the main reason saving was the existence of a retirement period, which necessitates consumption smoothing over the life cycle – wealth accumulation during working life to pay for consumption in retirement. The implication of this simple model is that wealth accumulation on the household level solely depends on the length of the retirement period, while in aggregate wealth accumulation crucially hinges on the growth rate of the economy. The crucial assumption that allows Modigliani and Brumberg to focus on consumption smoothing over the life cycle was that of constant income.

## **2.5 Income uncertainty and market structure**

With the assumption of a non-constant income stream, it becomes important to think about the opportunities households have to insure themselves against these fluctuations.

## **2.6 The role of housing**

Campbell and Hercowitz (2005) Yang (2009) Iacoviello (2008)

## **2.7 Closed and open economies**

On the endogeneity of interest rates

## **2.8 Wealth Distribution Papers**

In the last years, many authors have used the increasing possibilities offered by the increase in computing power to derive an additional implication from the broad class of incomplete market models outlined above: a simulated wealth distribution. While there are many practical difficulties in creating model outputs that can reasonably compared to the data collected in surveys (some of which have been alluded to in the above discussion on the definition of wealth), in principle the simulated wealth distribution derived from life-cycle models can be used to calibrate deep parameters of the model, provide an additional test for how well the model is able to capture household savings behaviour, and shed light on which

mechanisms are crucial in driving the evolution of aggregate savings at different parts of the distribution.

An early attempt to use the wealth distribution to estimate the parameters of a life-cycle model of household savings can be found in Cagetti (2003), who uses a simple model similar to the one outlined in equations 2.1 and 2.2. Important additions in his version of the model are a bequest motive – which, *ceteris paribus*, will increase the wealth holdings of elderly households – and a simplified pension system, which guarantees each household a pension depending on their education level, and thereby lowers wealth accumulation during working life. The idea behind the estimation strategy is simple: given a stochastic process for household income, the parameters  $\beta$ ,  $\sigma$  and  $\alpha$  pin down a solution to the household's savings problem which allows one to simulate a theoretical wealth distribution from optimal household behaviour. Therefore, it is possible to use the simulated method of moments to construct an estimator that chooses the triplet  $(\delta, \sigma, \alpha)$  which minimises the distance between empirical moments of the wealth distribution and its simulated counterparts. Given the high skewness of wealth data, Cagetti opts for median wealth by 5-year age group as the moment to match. As has become clear in the previous discussion, a crucial element driving household choices in the model is the income risk they face, making the choice for the stochastic process representing this risk and its calibration a crucial step in modelling wealth distributions. Cagetti opts for a process consisting of a trend growth component common to all households, an age-education component estimated for CEX data, and an MA(1) process representing the stochastic nature of income. With his calibration, Cagetti finds low degrees of persistence, with pronounced heterogeneity across education groups, and high degrees of risk

aversion, implying a significant contribution of precautionary savings to aggregate wealth.

A very similar exercise is performed by Hintermaier and Koeniger (2011), who construct a minimum distance estimator based on the shape of the cross-sectional distribution of wealth at different stages of the life cycle. That is, rather than simply targeting the 50th percentile of wealth holdings as Cagetti (2003), here all percentiles of the wealth distribution from 10 to 90 are considered. The reason for excluding the upper ten percentiles of the distribution are the well-known problems that a simple life-cycle model has in matching the extreme levels of wealth concentration observed at the upper end of the distribution, which might be driven by other motives than the buffer- stock and retirement savings motives included in the model. Increasing the number of moments to match leads to estimates of the discount factor which are an order of magnitude more precise than in Cagetti (2003). The estimate for the discount factor, at  $\hat{\delta} = 0.985$ , is at the upper bound of the estimates in Cagetti (2003), while the estimated risk aversion parameter  $\hat{\sigma} = 1.08$  is only a third to one sixth as large as Cagetti's estimate, depending on the subgroup under consideration.

Hintermaier and Koeniger (2011) Castaneda et al. (2003) Diaz et al. (2003) Floden (2008) Benhabib et al. (2011) De Nardi and Yang (2015)

## 2.9 Conclusion

This chapter provides an overview of stylised facts about the wealth distributions in a number of advanced economies and presents various approaches to build economic models which can account for these stylised facts. It became clear

that while saving for retirement is the main driver of wealth accumulation for large parts of the population, other factors need to be taken into consideration to explain the tails of the distribution and the behaviour of young households. Crucial aspects of an economic model of the wealth distribution are the risks households are facing – both on the income and the expenditure side – and the financial markets available to them to insure themselves against those risks and earn returns on their savings. Finally, the far right tail of the wealth distribution seems to be driven by factors beyond this and it is not clear whether variation in subjective discount factors, entrepreneurial activity, or other factors are best suited to model wealth accumulation at the top.

## **Chapter 3**

# **The effects of profile heterogeneity on estimates of income risk**

### **3.1 Introduction**

As has become clear from the discussion in the previous chapter, a crucial ingredient to any model of household savings is an estimate of the risk that households are facing in the form of their income process. While traditionally researchers have relied on a parsimonious AR(1) specification with a transitory and a persistent shock component, which can be represented as a Markov chain and thus helps to ease the computational burden. Recent research has cast doubt on the ability of this specification to accurately capture the risk faced by households in the labour market though, and advances in computational capabilities have allowed to solve models with larger state spaces, so that there is a renewed interest in estimating richer statistical processes for household income.

Insert discussion of recent papers based on social security data: Guvenen et al. (2015), DeBacker et al. (2013)

### 3.2 A statistical model

To inform the simulations in the following chapter, this thesis will rely on an estimated heterogeneous income profiles (HIP) income process in the spirit of Guvenen (2009). The process to be estimated is of the form

$$y_{h,t}^i = g(\theta_t, \mathbf{X}_{h,t}^i) + \alpha^i + \beta^i h + z_{h,t}^i + \phi \varepsilon_{h,t}^i \quad (3.1)$$

$$z_{h,t} = \rho z_{h-1,t-1} + \pi_t \eta_{h,t}^i \quad (3.2)$$

where  $y_{h,t}^i$  are the log earnings of individual  $i$ , who has  $h$  years of labour market experience in period  $t$ . The function  $g()$  is assumed to be a cubic polynomial in experience, while the individual specific parameters  $\alpha^i$  and  $\beta^i$  – modelled as random variables with mean zero and variance  $\sigma_\alpha^2$  and  $\sigma_\beta^2$ , respectively – capture the cross-sectional profile heterogeneity.  $z_{h,t}^i$  is an AR(1) process with persistence  $\rho$  and innovation variance  $\eta_{h,t}^i$ , which captures persistent shocks to income, while  $\varepsilon_{h,t}^i$  is a purely transitory shock. Both  $\eta^i$  and  $\varepsilon^i$  are mean-zero i.i.d random variables with variances  $\sigma_\eta^2$  and  $\sigma_\varepsilon^2$ , respectively. As discussed above, the variances of both permanent and transitory shocks have seen large swings over the past decades, to capture this we are allowing for time-variation in the innovation variance (denoted  $\pi_t$  for the innovation to the persistent shock component and  $\varphi_t$  for the transitory counterpart).

To estimate the parameters of the model, an equally weighted minimum distance estimator is used to minimise the distance between the empirically observed variance-covariance structure of residual earnings (defined as  $\tilde{y} \equiv y_{h,t}^i - g(\theta_t, \mathbf{X}_{h,t}^i)$ ) and the variance-covariance structure implied by the model. In the present context, this strategy has first been employed by Baker (1997), who estimates a very similar model to the one described above, although the approach has been used before for estimating other models in labour economics, e.g. Abowd and Card (1987). Our model implies theoretical variances and covariances given by:

$$\text{Var}(\tilde{y}_{h,t}^i) = \underbrace{\sigma_\alpha^2 + 2\sigma_{\alpha\beta}h + \sigma_\beta^2}_{\text{contribution of profile heterogeneity}} + \text{Var}(z_{h,t}^i) + \phi_t^2 \sigma_\varepsilon^2 \quad (3.3)$$

$$\text{Cov}(\tilde{y}_{h,t}^i, \tilde{y}_{h+n,t+n}^i) = \underbrace{\sigma_\alpha^2 + 2\sigma_{\alpha\beta}(h+n) + \sigma_\beta^2}_{\text{contribution of profile heterogeneity}} + \text{Var}(z_{h,t}^i) + \phi_t^2 \sigma_\varepsilon^2 \quad (3.4)$$

The empirical variance-covariance matrix underlying the estimation will be obtained by first calculating the covariance of residuals for each age-group in a given year, and then averaging over all age groups present in a given year. The theoretical counterpart is obtained by simply calculating the corresponding variances and covariances from the formulas above, and forming weighted averages over  $h$  with weights corresponding to the relative frequency of age-groups in the empirical data.

### 3.3 Data

As we are interested in the variability of our estimates, we are estimating the process described both on PSID and BHPS data. PSID data has the advantage of



Figure 3.1: Variance of log income and 90/10 percentile width for our sample of BHPS households

providing a very long horizon (37 waves of data covering a total of 45 years), which allows for the analysis of subperiods to examine changes over time. The BHPS, while more limited in time (18 waves of data covering 18 years) serves as a useful comparison, while also providing excellent measures of different measures of household incomes pre- and post taxes and transfers, which enable us to investigate the implications for heterogeneous income processes from The data is taken from all available waves of the PSID, that is years 1968 to 2013 inclusive<sup>2</sup>. For our baseline estimation, to ease comparisons, we stick to the sample selection criteria used in Guvenen (2009), namely:

- Household heads between the ages of 20 and 64 inclusive
- Hourly labour earnings between \$2 and \$400 in 1993 prices
- Hours worked between 520 and 5110

For inclusion in our sample, an individual has to fulfil all of the above conditions for at least 20, not necessarily consecutive, years. These sample selection criteria leave us with 1685 individuals in our final sample<sup>3</sup>. The main variable of interest in the analysis is labour income, for which we use the series of variables starting with V74 in 1968<sup>4</sup>. Hourly earnings are taken from the variable starting with V337 in 1968, while hours worked are taken from the variable starting with V47.

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<sup>2</sup>Note that the PSID income variable refers to income in the previous year, so when we talk about data from, e.g., year 1968, it is implied that we are referring to income in 1967.

<sup>3</sup>To create the longitudinal data set from the PSID cross-sections, we use the excellent *PSIDtools* package (Kohler, 2015)

<sup>4</sup>A complete list of all variables used is available on my GitHub page.

Table 3.1: Results for the PSID sample 1968-1996; Guvenen (2009) refers to published results, Guvenen Matlab to results obtained by running the code available on the journal website, short sample to my own estimation with the 1968-1996 data, full sample to the 1968-2013 data.

	$\rho$	$\sigma_{\eta}^2$	$\sigma_{\varepsilon}^2$	$\sigma_{\alpha}^2$	$\sigma_{\beta}^2$	$\sigma_{\alpha\beta}$
Guvenen (2009), RIP	0.988	0.015	0.061	–	–	–
Guvenen Matlab, RIP	0.935	0.010	0.023	–	–	–
Short sample, RIP	0.951	0.011	0.043	–	–	–
Full sample, RIP	0.920	0.014	0.067	–	–	–
Guvenen (2009), HIP	0.821	0.029	0.047	0.022	0.00038	–0.23
Guvenen Matlab, HIP	0.853	0.013	0.030	0.030	0.00031	–0.30
Short sample, HIP	0.855	0.017	0.018	0.022	0.00030	–0.32
Full sample, HIP	0.839	0.017	0.064	0.047	0.00026	–0.32

### 3.4 Results

## **Chapter 4**

# **The implications of learning about income processes in the face of structural breaks for the household wealth distribution**

### **4.1 Introduction**

What factors can explain the substantial and persistent increase in US household indebtedness over the last three decades? This question has inspired a large literature that has put forward several explanations. On the side of credit supply, the institutional framework plays a central role; Campbell and Hercowitz (2005) emphasize the effects of the liberalization of the US home mortgage market in the early 1980s while Narajabad (2012) points towards improvements in banks' risk assessment capabilities to explain an increase in credit lines available to

households. On the demand side, the most influential view is arguably given by Krueger and Perri (2006) who interpret the expansion of US credit markets as the rational response of consumers borrowing in order to smooth out income shocks, the variance of which has risen over time. However, this view rests on the observed increase in cross-sectional income variation being largely due to a rise in the variance of transitory idiosyncratic shocks, an interpretation that has been called into question by several authors. As an example, Kopczuk et al. (2010) find that the rise in income inequality was almost entirely driven by increases in permanent earnings inequality, with no mitigating effect of mobility across income groups that decreased at the same time as earnings inequality increased. In the same vein, DeBacker et al. (2013) use a confidential panel of tax returns from the IRS to show that all of the rise in the variance of male labour earnings between 1987 and 2009 can be attributed to a rise in the variance of the persistent part of income. In light of these difficulties, the present work aims to examine an additional mechanism that could drive household credit demand – consumption habits. In this regard, this work bears some resemblance to the prominent Rajan (2011) hypothesis that the foundations for the financial crisis of 2007/08 were laid by a credit expansion that mostly benefited low-income households. This also relates to more heterodox, post-Keynesian and Marxist explanations of rising household indebtedness that emphasize the role of debt as a substitute for stagnating or declining real wages in the middle and lower percentiles of the income distribution (see, for example, Barba and Pivetti, 2009), a mechanism of course that would require households to be – at least for some time – oblivious towards the realities of the path of their income stream. Often, behavioural explanations such as conspicuous consumption or household optimization based on a relative income hypothesis are invoked,

examples include Bertrand and Morse (2013), who find empirical support for the hypothesis that consumption of lower income households is influenced by consumption of high income households, and van Treeck (2012), who presents some calculations based on Duesenberry's (1940) relative income hypothesis. Here, we try to frame this argument in terms of an arguably more standard economic model: a life-cycle model with fully optimizing rational households that derive utility from current and past consumption, while facing an uncertain income stream that they learn about over the course of their working life. The basis for the present analysis is a model introduced by Guvenen (2007), in which the income process consists of a permanent stochastic AR(1)-component, as is standard in most of the literature, and an additional deterministic term, that is different across workers and that they have to learn about in order to make precise forecasts of their lifetime income. This uncertainty, coupled with the time-inseparability of consumption introduced by habit formation, can under certain circumstances lead to an increase in the indebtedness even of households with permanently low incomes.

The remainder of this paper is structured as follows: Section (4.2) presents some stylized facts on the developments of the US income and wealth distribution that motivate this work. Section (4.3) lays out the model and gives analytical results for a stripped down version of the model that shed light on the mechanisms through which habit formation can generate higher indebtedness. Section (4.4) presents the results of a quantitative evaluation of the model that is informed by data from the CEX and the SCF. Section (4.5) extends the model to include a labour supply decision and gives results for different assumptions on prior uncertainty, learning behaviour and the specification of the habit formation process. Section (5.5)

discusses the success of different versions of the model in replicating observed data.

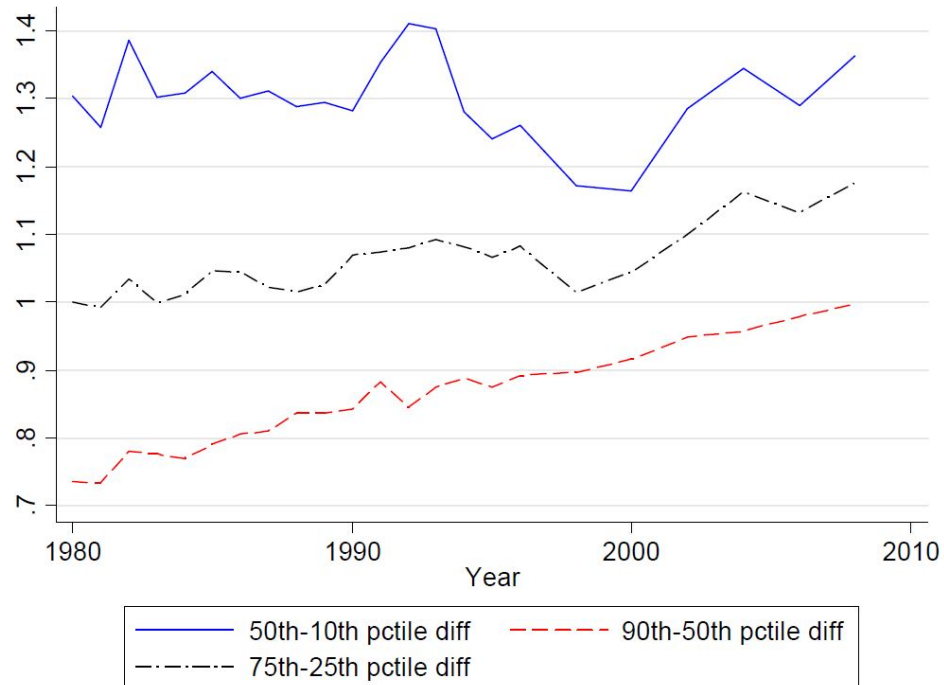
## 4.2 Stylized Facts

The widening inequality in the U.S. income distribution is a well documented feature of the data during at least the last three decades. Numerous studies have examined the secular rise in top incomes (Piketty and Saez, 2003) and the flattening path of middle and lower incomes (Autor et al., 2005) and put forward explanations such as changes in relative demand and supply for different skill levels, the decline of union power, increases in international trade and competition (Ma, 2013) and the fall in the real value of the federal minimum wage<sup>5</sup>. While the exact timing and magnitude of the rise in inequality may differ slightly from one data source to the other and depending on the exact definition of income employed, its existence can be regarded as a consensus in the literature. Figure (4.1) is taken from Attanasio, Hurst and Pistaferri (2012) and shows the evolution of income inequality at different points of the income distribution from 1980 to 2010 based on PSID data. The rise in overall inequality is apparent and can be seen to be mostly driven by a surge in top incomes (even though, as the authors note, PSID data undersamples very rich households and thus most likely understates the rise in top incomes). There exists less consensus about the evolution of consumption inequality over the same period. While early prominent studies such as Krueger and Perri (2006) used CEX data to argue that there has been virtually no increase in consumption inequality and built theoretical models that could account for this puzzle, more recently other authors have found a larger increase in consumption inequality using different data sources that arguably suffer from less measurement error than the aggregate CEX data. Heathcote et al. (2010) use

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<sup>5</sup>Some doubts on the magnitude and timing of the rising inequality are raised by Gordon (2009).

Figure 4.1: Income inequality for three income differentials, 1980-2010, PSID data



CEX spending data to document a very modest increase in consumption inequality, while Aguiar and Bils (2011) use the difference between income and spending in CEX data to document a rise in consumption inequality that is almost as large as the rise in income inequality and Attanasio et al. (2013) argue that, looking at some of the more precisely measured items in the CEX, one finds that consumption inequality has indeed tracked income inequality. For the purpose of this paper, we will use aggregate spending data from the CEX and thus assume that consumption inequality has not risen to the same extent as income inequality while keeping in mind that this is not a foregone conclusion. We will return to this point in the last chapter.

Another well documented feature of the data is the rise in debt holdings of the



private sector. As with the rise in income inequality, this development has been widely noted and discussed with numerous explanations put forward, including changes in the regulatory framework and banking technology that widened credit supply. Most relevant to this work is the demand side argument of Krueger and Perri (2006), who explain the rise in indebtedness with a limited commitment model in which the variance of the transitory component rises and hence more insurance is required, and, indeed, optimal from a welfare perspective. However, as Cordoba (2008) points out, their model produces to empirically unappealing results: for one, wealth holdings are not concentrated at the top of the distribution, and second, the model predicts a large fraction of agents in the economy with negative wealth holdings, when their number really is close to zero in the data. Furthermore, their argument is weakened by a number of studies that find changes in the variance of the permanent component of income shocks to be the driving force behind the rise in income inequality. This is hard to reconcile with the fact that individuals at the lower end of the income distribution are those that increased their debt holdings the most. Figure (4.2) shows the changes in debt holdings for various debt categories calculated from SCF data for 1989 to 2007.

While the large rise in indebtedness for the lowest income group is an artefact of business owners with failed businesses in the data, it is interesting to note that the rise in overall debt has been at least as large for the 20th to 60th percentile as for the highest income percentile. This comes as a surprise if one takes into account the higher income growth rates for individuals in higher income quintile since the early 1980s. Assuming that the dispersion in incomes is mostly driven by an increase in dispersion in the permanent component of income (as suggested by, among others, Kopczuk et al., 2010), a standard life-cycle model would suggest

Figure 4.2: Changes in debt holding by income percentile, 1989-2007, Source: SCF

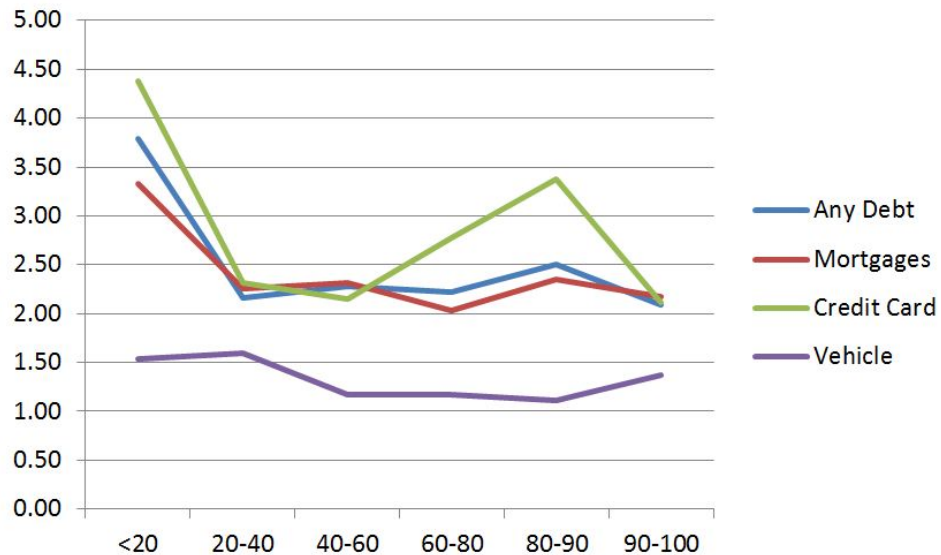


Figure 4.3: Changes in debt holding by income percentile, 1989-2007, Source: SCF

that while high income households should borrow against their higher future income, low income households wouldn't have an incentive to borrow when wages are stagnant. Furthermore, note that the data is not scaled by income, so that debt holdings relative to income have increased a lot more for lower income households, given that their income growth rates over the same period have been lower than those of higher income households. Indeed, Barba and Pivetti (2009) find that instalment loans and credit card debt amount to 59% of disposable income for households in the lowest income quintile of the 2004 SCF, while they amount to only 11% for the highest quintile.

One adjustment margin for households that could explain a decoupling of income and consumption inequality at least over short to medium frequencies is obviously

saving. Saez and Zucman (2014) find that the share of wealth holdings of the bottom 90% of the wealth distribution has fallen from 35% in the mid 1980s to 23% in 2012, citing low growth of middle-class income, financial deregulation leading to predatory lending and behavioral biases in savings decisions as possible explanation. This paper can be seen as an attempt to investigate to what extent imperfect information of agents can account for the observed change in the wealth distribution.

- Increase in the dispersion of wealth holdings that tracked or exceeded the rise in income inequality
- Decreasing aggregate savings rate
- Prevailing misperceptions about future economic situation (Moore 2003)

### 4.3 The Model

The modelling approach draws heavily on the approach in Guvenen (2007) and mostly follows the notation therein. As in Guvenen's work, consumers maximize utility from consumption over the life-cycle while facing an uncertain income stream that consists of a common, known component capturing experience effects, an unknown, individual specific linear term that agents have to learn about, an AR(1) component and a purely transitory shock. The important departure in this work is that consumers also build a stock of habit that enters the utility function multiplicatively, as is standard in the literature to avoid numerical problems with CRRA utility functions (for a discussion, see Carroll (2000)). Consumers maximize

$$E_0 \left[ \sum_{t=0}^T \beta^t \frac{\left( c_t^{1-\gamma} \left( \frac{c_t}{h_t} \right)^\gamma \right)^{1-\sigma}}{1-\sigma} \right] \quad (4.1)$$

s.t.

$$h_{t+1} = (1 - \lambda)h_t + \lambda c_t \quad (4.2)$$

$$a_{t+1} = (1 + r)a_t + y_t - c_t \quad (4.3)$$

$$y_t^i = g(\theta^0, X_t^i) + f(\theta^i, X_t^i) + z_t^i + \epsilon_t^i \quad (4.4)$$

$$a_{t+1} \geq \underline{a} \quad (4.5)$$

where  $c_t$  is consumption in period  $t$ ,  $h_t$  is the habit stock accumulated up to period  $t$ ,  $a_t$  are asset holdings subject to a borrowing constraint  $\underline{a}$  – the specification of which will not be straightforward in this model and requires some further discussion – and  $y_t^i$  is individual income, that can further be broken down into

several parts:

$$y_t^i = g(\theta^0, X_t^i) + f(\theta^i, X_t^i) + z_t^i + \epsilon_t^i$$

where  $g(\theta^0, X_t^i)$  captures age effects and individual specific characteristics such as education,  $z_t^i$  is an autoregressive process of order one, and  $f(\cdot)$  is an individual specific function that plays the decisive role in introducing heterogeneity and learning in the model.

$$f(\theta^i, X_t^i) = \alpha^i + \beta^i t$$

$$z_t^i = \rho z_{t-1}^i + \eta_t^i$$

$$\theta^i \sim N \left[ \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_\alpha^2 & \sigma_{\alpha\beta} \\ \sigma_{\alpha\beta} & \sigma_\beta^2 \end{pmatrix} \right]$$

The parameters  $\alpha$  and  $\beta$  are randomly distributed over the population and govern the evolution of lifetime income over time. Furthermore, they are unknown to individuals upon entering the labor market, meaning that in order to calculate an expected lifetime income to base consumption (and thus, implicitly, habit) choices on, consumers in the model have to hold beliefs over the values of their individual parameters. Here again we follow Guvenen in assuming that these beliefs are updated in a Bayesian fashion, which means beliefs are updated by solving a Kalman filtering problem.

Denoting by  $S_{t+1}^i$  the vector of parameters  $\alpha^i$ ,  $\beta^i$  and  $z_{t+1}^i$  and by  $F$  the coefficient vector in the state space representation, we can derive an optimal forecast based of Bayesian updating for the evolution of the individuals belief about the evolution

of  $S_t^i$  as

$$\hat{S}_{t|t}^i = \hat{S}_{t|t-1}^i + P_{t|t-1} H_t [H_t' P_{t|t-1} H_t + R]^{-1} (y_t^i - H_t' \hat{S}_{t|t-1}^i) \quad (4.6)$$

$$\hat{S}_{t+1|t}^i = F \hat{S}_{t|t}^i \quad (4.7)$$

where  $P_{t|t}$  is the variance-covariance matrix of  $\hat{S}_{t|t}^i$  and  $R$  is the variance of the transitory shock. A similar expression can be derived for the evolution of  $P_{t+1|t}$ :

$$P_{t|t} = P_{t|t-1} - P_{t|t-1} H_t [H_t' P_{t|t-1} H_t + R]^{-1} H_t' P_{t|t-1} \quad (4.8)$$

$$P_{t+1|t} = F P_{t|t} F' + Q \quad (4.9)$$

With  $Q$  denoting the covariance matrix of the innovation in the state space representation of  $\hat{S}_{t+1|t}^i$  (which is basically the innovation in the AR(1) component of earnings). Given this formulation for the evolution of beliefs, we can write the recursive version of our maximization problem as:

$$V_t(a_t, h_t, y_t^i, \hat{S}_{t|t-1}^i) = \max_{\{c_t^i, a_{t+1}^i\}} \left\{ u(c_t, h_t) + \mathbb{E}_t \left[ V_{t+1}(a_{t+1}, h_{t+1}, y_{t+1}^i, \hat{S}_{t+1|t}^i | \hat{S}_{t|t-1}^i) \right] \right\} \quad (4.10)$$

which again has to be solved subject to the constraints 4.2, 4.3, 4.5 and 4.6-4.9.

At the time

It can be shown that<sup>6</sup>, for general specifications of the utility function, the Euler equation of the problem is:

$$u_t^c = \mathbb{E}_t \left[ (1+r) \beta \left[ u_{t+1}^c + \beta (u_{t+2}^h - (1-\lambda) u_{t+2}^c) \right] \beta \left[ u_{t+1}^h - (1-\lambda) u_{t+1}^c \right] \right]$$

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<sup>6</sup>A detailed derivation can be found in Carroll (2000).

### 4.3.1 Computational Algorithm

As described by Guvenen (2007), the model requires a unique construction of the state space to be solved successfully. Here we describe the procedure adapted for our purposes:

1. Draw 100 different  $(\alpha^i, \beta^i)$  combinations from a bivariate normal distribution with mean  $\begin{pmatrix} 2 \\ 0.02 \end{pmatrix}$  and a variance-covariance matrix taken from PSID data. Rank the resulting types by  $\beta$ . For the policy experiment, increase  $\beta^i$  for agents above a cutoff level  $i^*$  at period  $T^*$ .
2. For each type  $i$ , simulate 1000 income histories from  $y_{it} = \alpha^i + \beta^i t + \rho z_{i,t-1} + \epsilon_t^i$
3. Use the Kalman filter to derive, specifying some initial beliefs, a belief vector  $\hat{S}_{t|t}^i$  for each agent at each  $t$ .
4. Divide the space spanned by the derived beliefs,  $[\alpha_{min}, \alpha_{max}] \times [\beta_{min}, \beta_{max}] \times [z_{min}, z_{max}]$ , into 8000 equally sized cubes by taking 21 points along each dimension. At each  $t$ , if any of the  $(\hat{\alpha}^i, \hat{\beta}^i, \hat{z}^i)$  points fall into one of the cubes, assign a grid point to the center of the cube and discard all empty cubes. This will result in  $Q_t$  vectors  $\tilde{S}_t^q = (\hat{\alpha}, \hat{\beta}, \hat{z})^q$ ,  $q = 1, \dots, Q_t$ , where  $Q_t$  is the number of non-empty cubes at  $t$ .
5. To make the income grids consistent with the bounds set by  $(\alpha^i, \beta^i)$ , construct one grid  $y_{grid}^q = [y_{min}^q, y_{max}^q]$  per belief vector  $\tilde{S}_t^q$ , where the bounds are given by  $\exp[H\tilde{S}_t^q \pm 3\sigma(\tilde{y}^q)]$ , with  $\sigma$  taking from the posterior variance of the forecast of  $y$  based on the Kalman filter. Place 8 equidistant nodes on this grid.

6. Construct a wealth grid with 12 points, more densely spaced around the borrowing constraint.
7. Construct a habit grid with 15 points, more densely spaced around average lifetime consumption.
8. Solve the optimization backwards from  $T$  for each  $t$  on a  $[12 \times 15 \times 8 \times Q_t]$  grid.

An issue to consider when imposing the wage structure above is household's relative position in the wage distribution over the life cycle. As Kopczuk et al. (2010) and DeBacker et al. (2013) have shown, the rise in inequality was mostly persistent, and Jantti and Jenkins (2013) show that over ten year periods the largest fraction of households remains in a given income percentile. Further, a number of papers (Card et al. (2013), Bernard and Jensen (1995), Autor et al., 2008) show that a large part of the rise in income inequality can be accounted for by a rise in inequality in pay between firms and industries. Hence, even if households fully understand the changes in the wage structure favoring higher earning occupations, reacting to that change might be impossible to the extent that human capital accumulated over the working life is firm- or occupation specific <sup>7</sup>. For these reasons, we believe that fixing  $\beta$  for each household is not too restrictive.

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<sup>7</sup>In fact, Kambourov and Manovskii (2009) show that households switching occupations are contributing to the flattening of earnings profiles at the lower end of the distribution as the transfer from one occupation to another destroys human capital and hence earnings potential.



## 4.4 Quantitative Results

Given the slow learning induced by the nature of the income process, the initial beliefs of consumers are of crucial importance for consumption decisions in the first periods of live. These in turn determine a habit stock that might (depending on the parameter choice for  $\lambda$ ) have a long lasting effect on the marginal utility of consumption in the following periods. Hence, it is important to explore the sensitivity of results to different initial belief vectors and think about reasonable parametrizations. In a more fully specified model, one could further introduce a trade-off for agents between "comforting" expectations about their own future and the cost attached to acting on overly optimistic preferences, as for example argued by Glaeser (2004), but such a specification would require the introduction of a further unknown parameter in the utility function determining the utility of optimistic expectations and is therefore outside the scope of this work. Instead, we will focus on two baseline cases and explore the sensitivity of results to deviations from this baseline.

The first case assumes that agents entering the labor market in the model at age 25 have formed expectations based on previous observations of wage growth for workers in similar occupations to the one they are entering. Hence, we will assume that someone entering the labor market at, say, the 20th quintile of the wage distribution, will have expectations that were formed on the wage growth of workers in the 20th quintile 10 years prior to the worker entering the labor market. Note that this will have opposite effects on workers entering the labor market in the late 1970s, just before cross-sectional wage dispersion started to increase: while workers in low-skill occupations at the bottom of the wage distribution will

face lower income growth rates than their predecessors, and thus growth rates below their expectations, workers at the high end of the wage distribution will see their incomes grow above expectations for the same reason. Thus, with this parametrization, poorer households will build up habit stocks that are too high relative to lifetime income early in life, with the reverse being true for high income households.

The second baseline case is inspired by the aforementioned research on people's inclination to hold optimistic beliefs as well as survey evidence on the overconfidence of economic actors. One such example would be a Gallup poll (Moore, 2003) in which 31% of respondents declared to expect to be rich at some point in their life, a number that jumps to 51% for the group of 18 to 29 year olds, where *rich* is defined as having an annual income of more than \$120,000 or assets in excess of \$1,000,000. DiPrete (2007) surveys a number of similar polls, compares their results with PSID data and concludes that even accounting for subjective differences in the definition of "being rich", Americans significantly overestimate the opportunity for upward income mobility over their lifetime<sup>8</sup>. A host of similar studies can be found and while one can certainly question whether such obviously unreasonable expectations form the basis for everyday economic decisions, they do point towards a significant amount of unwarranted optimism about the own economic future for a large part of the population. With this in mind, in the second scenario the belief vectors are parametrized to values that exceed the realized growth rates for all income brackets over the entire sample period. While comparing these two cases already gives us a good deal

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<sup>8</sup>Interestingly, this overconfidence seems to have been dampened by the financial crisis, if more recent studies are an indication. Compare, e.g. <http://www.cnbc.com/id/44559645>

of information about the sensitivity of results to the belief vector, in section (5.5) we will also discuss the results using Guvenen's (2007) parametrization to make the model results directly comparable and of experimenting with more extreme values of beliefs.

## 4.5 Extensions

An important part of the mechanism explored quantitatively above was the interaction between profile heterogeneity, initial beliefs and learning, the speed of which in turn depended on the nature of the income process underlying the simulations. Obviously, estimating the model using a more standard income process without profile heterogeneity, as is done in most of the life-cycle literature, would eliminate this mechanism completely, as there would be no meaningful learning about the income process. However, recent work by Hoffmann (2013) shows that specification error in the income process can severely bias econometric results towards either over- or underestimating the importance of profile heterogeneity. Hoffmann proposes a more general and flexible specification, which is still tractable enough to be used in a dynamic programming problem.

## 4.6 Discussion

### 4.6.1 Extensions

- Health inequalities: The model does not account for the fact that there is substantial variation in life-expectancy across the population with a strong correlation between life expectancy and income/asset level. This could lead to higher aggregate savings than in a model that does not account for this fact, as higher income households have to save a larger fraction of income during their working life to insure longevity risk than low income households.

## **Chapter 5**

# **The competitive effects of trade liberalisation in North America: An empirical application of the Melitz and Ottaviano Model**

### **5.1 Introduction**

The economic benefits of free trade are arguably one of the most uncontroversial results of economic research, both theoretically and empirically. However, to this date, free trade is by no means uncontroversial in the public sphere, as is evidenced by the fierce opposition that the proposed transatlantic free trade agreement between the US and Europe is facing. Hence, international trade has remained an active field in economic research, a field which has seen major advancements in the past two decades in incorporating firm-level heterogeneity

coupled with consumer love of variety into trade models that can account for the firm-level responses to increasing trade openness and the large share of intra-industry trade in the international flow of goods and services <sup>9</sup>. This new vintage of trade models predicts additional welfare gains from trade stemming from reallocations of production to more productive firms (as in Melitz, 2003) or increases in firms' efforts to innovate (as in Grossman and Helpman, 1990). To some extent, these new models of trade also help reconcile the unambiguously positive stance of economic researchers on trade liberalization with the public opposition to it – models taking into account explicitly the heterogeneity across agents of firms within a country show that while on aggregate there are significant efficiency gains from free trade, there are also firms and workers who will lose out individually, and can only benefit from a trade liberalization if either the aggregate gains are redistributed in some way to ensure a Pareto improving allocation, or if they can benefit from the reallocation of production to more productive firms by switching to those firms. DixCarneiro (2014) builds a structural model of the Brazilian labor market to estimate the labor market effects of trade liberalization and finds that, depending on the assumptions about capital mobility, the reallocation of workers across sectors can take up to 30 years.

While these new models of international trade are well grounded in empirical evidence coming from micro data, there are surprisingly few tests of the model predictions for aggregate variables which are decisive for the predicted welfare gains from trade. Recently, Arkolakis et al. (2012a,b) call into question the importance of firm-level heterogeneity by showing that in a large class of trade

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<sup>9</sup>A comprehensive survey of trade models with love of variety preferences and firm-level heterogeneity can be found in Melitz and Trefler (2012).

models, the additional welfare gains are fairly small and actually even smaller if consumers don't have CES utility. The response of Melitz and Redding (2013) shows that there is still considerable disagreement over how to theoretically evaluate the additional welfare gains from firm selection, and Costinot and Rodriguez-Clare (2014) review the effects of trade liberalizations in a wider class of new trade models to highlight the importance of the market structure under consideration – depending on whether a one- or multi-sector model is used and the degree of competition assumed, gains from trade are estimated to range from 4% to 40% of non-free-trade welfare. These facts motivate us to test the Melitz-Ottaviano model directly in aggregate data on prices, markups and productivity. To do so, we estimate the effects of trade liberalization on the competitive environment in manufacturing markets of the member countries of the North American Free Trade Agreement (NAFTA). We employ an estimation procedure based on the Melitz and Ottaviano (2008) model introduced by Chen et al. (2009), which to our knowledge is the only empirical application of a model with firm-level heterogeneity on aggregate data. Chen et al. (2009) derive estimable regression equations from the model's equilibrium conditions that allow us to test the effects of trade openness on relative price levels, markups and labor productivities of two trading partners. It is further possible to differentiate between the effects of trade in the short run, which, in the model, refers to an economy without relocation decisions for firms, and in the long run, when firms are free to choose their home market for production. However, as the underlying model is static, no direct results on the time path of the impact of trade liberalization can be obtained. We try to address this issue by dividing our sample in ways that make it more amenable to a model-based estimation. Contrary to Chen et al. (2009), we directly



observe tariff rates between the three countries in our sample and hence use those as a direct measure of trade openness. Additionally, we test for the effects of third-country trade openness on the relative performance of two countries that are linked through trade, predictions for which can be derived from the multi-country version of the Melitz and Ottaviano model. Our dataset comprises of nine manufacturing sectors in Canada, Mexico and the US, covering the time period from the introduction of NAFTA in 1994 up to 2006, which gives us reason to believe that we are able to capture the long run effects of policy changes even in industries with low firm churning rates.

Our findings support the main model predictions, with tariff barriers stifling domestic competition, leading to higher producer prices and markups as well as lower productivity. In the immediate years after the free-trade agreement when tariff barriers are reduced, relative prices and markups decrease as relative productivity increases, thus giving rise to competitive effects. The results in the long-run, however, are not as clear cut, with some effects reversing as predicted by the model while some effects persist. This is also confirmed by directly looking at the reaction of industries with different entry barriers to changes in trade openness.

The paper is organized as follows: Section 5.2 gives a survey of the previous literature assessing the effects of trade liberalizations in general and of NAFTA specifically. Section 5.3 briefly summarizes the Melitz and Ottaviano (2008) model, derives the most important equilibrium conditions and explains the estimation strategy used in Chen et al. (2009). Section 5.4 then presents our

application of the model by giving an overview of the data used and our estimation procedure. The results of our regressions and possible shortcomings as well as extensions of our approach are discussed in Section 5.5; Section 5.6 concludes.

## 5.2 Related Literature

As free trade has been an active topic in economic research since the times of Ricardo, the literature on the welfare gains from trade is immense. Of particular interest to us of course are papers that investigate the economic effects of NAFTA directly, as well as papers that form the theoretical foundation for our estimation strategy.

The effects of free trade in North America have been scrutinized in a large number of papers over the past two decades, starting with work on the predecessor to NAFTA, the 1987 Canada and US free trade agreement (CUSFTA). Head and Ries (1999) document rationalization effects in Canadian plants as a reaction to decreases in Canadian import duties. Trefler (2004), focusing on the CUSFTA, uses a reduced form econometric approach to find large improvements in labor productivity and decreases in employment after the implementation of CUSFTA, coupled with slightly lower import prices and larger volumes of trade. Fukao, Okubo and Stern (2003) derive regression equations from a partial equilibrium model with imperfect competition to estimate the extent to which NAFTA was trade diverting rather than creating and find responses that vary by industry. Romalis (2007) examines both CUSFTA and NAFTA with a strategy based on estimating demand and supply elasticities and finds a large effect of NAFTA on trade volumes, with only minor price changes and, subsequently, only small changes in welfare. Calderon-Madrid and Voicu (2007) use plant-level panel data from Mexico to show that while productivity increases followed the tariff reductions, the responses of plant-level productivity are very unevenly distributed, with larger plants benefiting disproportionately from productivity increases. The

Melitz (2003) model that is at the heart of our analysis is also put to a test with US manufacturing data by Bernard, Jensen and Schott (2006a), who use plant-level data to estimate the effects of changes in the costs of trade, as measured by tariff rates and transportation cost, on productivity growth and firm entry and exit. Their findings confirm the micro-level implications derived from the assumptions on the productivity distribution in Melitz (2003), which we will highlight in the following section. Other papers have used the structure provided by the Melitz and Ottaviano (2008) model to assess the effects of trade liberalization in other parts of the world: Bellone et al. (2008) use price-cost margins of French manufacturing firms to test the models predictions on the effects of market size, import penetration and exporting status on markups and productivity and confirm that all predictions hold. Corcos et al. (2011) estimate structural parameters in order to simulate counterfactual scenarios by changing the costs of trade between countries. Their exercise shows that the firm selection mechanism is crucial for the magnitude of the welfare gains from trade and the potential gains for a country depend on country size as well as remoteness. The paper that is closest to our own work is Chen et al. (2009), who use the equilibrium expressions for prices, markups and productivity from the Melitz-Ottaviano model to estimate the effects of trade liberalization using a dataset that includes data on 10 manufacturing sectors in seven European countries for the period 1989-1999 with country-pair regressions. Their results suggest that trade openness leads to an increase in competitiveness in the short-run with diminishing and at times reversed effects in the long-run, as predicted by the model.

### 5.3 Model and Estimation Equations

The Melitz and Ottaviano (2008) model is a synthesis of the contributions of Melitz (2003), who introduces firm heterogeneity through random draws of a cost parameter for firms entering the market, and Ottaviano et al. (2002), who develop a model with endogenous markups arising from a linear consumer demand system with horizontal product differentiation. The model yields equilibrium conditions that determine a cost cut-off level, i.e. a level of productivity below which firms are not able to compete in the marketplace. This cut-off level uniquely determines all relevant aggregate variables in the model, namely the distribution of prices, markups and productivity. Importantly, the equilibrium conditions of the model economy are different depending on whether firm entry is allowed or not. Without firm entry, the model captures a short-run equilibrium, with the cost cut-offs in two markets given by:

$$N = \bar{N} \left( \frac{c_D}{c_M} \right)^k + \bar{N}^* \frac{1}{\tau^k} \left( \frac{c_D}{c_M^*} \right)^k \quad (5.1)$$

$$N^* = \bar{N}^* \left( \frac{c_D^*}{c_M^*} \right)^k + \bar{N} \frac{1}{(\tau^*)^k} \left( \frac{c_D^*}{c_M} \right)^k \quad (5.2)$$

Here, a star denotes the foreign market,  $\bar{N}$  is the fixed number of incumbents in a market and  $N$  is the number of firms that are producing.  $c_M$  is the upper bound of the distribution of cost draws,  $c_D$  is the cut-off level, i.e. the highest cost draw that allows a firm to earn non-negative profits.  $\tau > 1$  is the iceberg cost of trade faced by foreign companies exporting to the domestic market and can be interpreted as a measure of trade costs, tariffs and other impediments to trade.

The long-run equilibrium of the economy allows for firm entry into a market, so

that the number of firms in a market is now endogenously determined by a zero profit condition for entrants that balances a fixed cost of entry with the expected profits when drawing a cost level from the (known) cost distribution of a country. The equilibrium conditions pinning down the cost cut-off are

$$c_D = \left[ \frac{\phi c_M^k}{L} \frac{1 - (\tau^*)^{-k}}{1 - (\tau \tau^*)^{-k}} \right]^{\frac{1}{k+2}} \quad (5.3)$$

$$c_D^* = \left[ \frac{\phi c_M^k}{L^*} \frac{1 - \tau^{-k}}{1 - (\tau \tau^*)^{-k}} \right]^{\frac{1}{k+2}}, \quad (5.4)$$

where  $L$  is the size of the domestic market. Since all aggregate variables in the Melitz and Ottaviano model are linear functions of the cost cut-off, equations describing the relative price, markup and productivity levels in two countries connected by trade can easily be found by simply dividing the expressions for  $c_D$  by those for  $c_D^*$ . This gives, for the price level in the short run:

$$\left( \frac{\bar{p}}{\bar{p}^*} \right)^k = \left( \frac{c_D}{c_D^*} \right)^k = \left( \frac{c_M}{c_M^*} \right)^k \frac{\bar{N}^*}{\bar{N}} \frac{N}{N^*} \frac{1 + \frac{\bar{N}}{\bar{N}^*} \frac{1}{(\tau^*)^k} \left( \frac{c_M^*}{c_M} \right)^k}{1 + \frac{\bar{N}^*}{\bar{N}} \frac{1}{\tau^k} \left( \frac{c_M}{c_M^*} \right)^k} \quad (5.5)$$

and in the long run:

$$\left( \frac{\bar{p}}{\bar{p}^*} \right)^{(k+2)} = \left( \frac{c_D}{c_D^*} \right)^{(k+2)} = \left( \frac{c_M}{c_M^*} \right)^k \frac{L^*}{L} \frac{1 - \frac{1}{\tau^k}}{1 - \frac{1}{(\tau^*)^k}} \quad (5.6)$$

These two equations capture one of the central predictions of the Melitz and Ottaviano model: asymmetrical trade liberalizations will have opposing effects on competitiveness in the short and the long run. By equation (5.5), lowering trade barriers induces a fall in the cost cutoff, and hence decreases in prices and

markups and increases in productivity. In the long run, however, the effects are reversed, as an increase in trade costs induces firms to choose the relatively more protected market for production, thereby increasing competition in markets that are shielded from foreign firms.

Chen et al. (2009) show that it is possible to substitute out the trade cost term with an openness term that is derived from a measure of foreign firms market share in the domestic market. However, since we are interested in the effect of tariff rates on competitiveness, we use tariff data directly as a proxy for  $\tau$ . This strategy should pick up the effects of tariff rates in our estimation if other determinants of trade openness (e.g. oil prices (Kilian et al., 2009), credit conditions (Chor and Manova, 2012), shared culture and language between countries) do not vary systematically across industries. However, as a first step, we will replicate their analysis exactly in our data set (albeit with different instruments for openness), which requires us to make the same substitution, which is:

$$\frac{1}{\tau^k} \left( \frac{c_M}{c_M^*} \right)^k = \frac{\theta}{1 - \theta} \quad (5.7)$$

Similarly, an expression for the average markup can be derived. The determination of the average markup is equivalent to the one for average prices so expressions for the short- and long-run impacts of openness on markups can readily be derived. Somewhat more problematic is the index for productivity, as the model requires knowledge of a firm's unit costs  $c$ , which are not observable. Chen et al. work around this issue by assuming away differences in capital costs, so that average industry productivity can be approximated by the ratio of nominal wages to labor productivity:  $\bar{c} = \frac{w}{z}$ . If it is additionally assumed that unit

labor costs only depend on nominal wages, the ratio of domestic to foreign labor productivity can be written as:

$$\frac{z}{z^*} = \frac{w}{w^*} \frac{\bar{c}^*}{\bar{c}} \quad (5.8)$$

If the least competitive firm in an industry with a productivity draw at the upper bound of the distribution  $c_M$  has labor productivity  $z_M$  and labor is perfectly mobile between firms, equation (5.8) implies  $\frac{z}{z^*} = \frac{w}{w^*} \frac{c_M^*}{c_M}$ . This relationship can then be used in an analogous fashion as before to construct an expression relating openness to productivity. In the short run, equation (5.8) can be amended to yield:

$$\left(\frac{z}{z^*}\right)^k = \left(\frac{z_M}{z_M^*}\right)^k \frac{(\bar{N}/N)}{(\bar{N}^*/N^*)} \frac{1 + \frac{\bar{N}^*}{\bar{N}} \frac{\theta}{1-\theta}}{1 + \frac{\bar{N}}{\bar{N}^*} \frac{\theta^*}{1-\theta^*}} \quad (5.9)$$

Higher values of  $\theta$  thus lead to higher productivity (conditional on  $\bar{N}/N$ ), as they force lower productivity firms to shut down production. For the long run, equation (5.5) combined with the expression for labor productivity gives:

$$\left(\frac{z}{z^*}\right)^{k+2} = \left(\frac{w}{w^*}\right)^2 \frac{L}{L^*} \left(\frac{z_M}{z_M^*}\right)^k \frac{1 - \frac{\theta}{1-\theta}}{1 - \frac{\theta^*}{1-\theta^*}} \quad (5.10)$$

Larger markets exhibit higher labor productivity, while the effects of  $\theta$  and  $\theta^*$  are the opposite of those in the short-run.

### 5.3.1 The Role of Market Entry

Following the arguments in Trefler (2004), we want to exploit the nature of NAFTA being close to a natural experiment and hence try to identify the effect of the



policy measures (i.e. the changes in tariff rates) separately from the effects of trade openness in general. There is evidence that trade openness – measured by the import penetration of a certain country or industry, as in Chen et al. (2009) – is affected by a number of external forces, including oil prices (Kilian et al., 2009), credit conditions (Chor and Manova, 2012), shared culture and language between countries and many more. Therefore, we deconstruct the iceberg costs of trade into two parts:  $\tau^{lh} = \frac{Tr^{lh}}{\theta^{lh}}$ , where  $Tr^{lh} > 1$  is the tariff rate for trade between countries  $l$  and  $h$  and  $\theta^{lh} > 1$  captures the additional costs of trade imposed by the aforementioned factors. Then, the import penetration can be viewed as a measure of  $\theta^{lh}$ , as in Chen et al. (2009), while a carefully constructed tariff measure can directly account for the effect of NAFTA-mandated changes in the trade environment. Obviously, the import penetration in a sector depends on the tariff measure as well, so an instrumental variable approach has to be taken in order to identify this effect. We defer the discussion of the construction of the tariff measure and the choice of instruments to the following chapter. Prior work of Bernard et al. (2006b) suggests that tariff rates throughout the 1980s, at an average level between four and five percent, accounted for about the same fraction of trade costs as costs directly attached to shipping the good, i.e. freight and insurance, so we expect them to have a sizable impact on trade flows between countries and hence the competitive environment.

As we have seen in the exposition of the Melitz and Ottaviano model above, there is one crucial caveat in taking the model to the data: due to the static nature of the model, the comparative static results just compare one steady state

with another, while being silent about the transitional dynamics. The estimation strategy of Chen et al. (2009) tries to account for this by estimating an error correction model to identify the long-run separately from the short-run, but their results – just as ours – are mixed for the long run and it cannot be ruled out that this is due to the estimation procedure. Therefore, we try to address this issue in a more direct way: as short- and long-run in the model differ only in the possibility of firm entry, we separate industries into those with a fixed number of firms and those with low entry barriers. This distinction then gives us industries that represent the short- and long-run and we can directly investigate whether the coefficients on the relevant variables differ significantly<sup>10</sup>. This approach, however, leads to two issues that need to be addressed before implementation. First, it is not *a priori* obvious how to measure the entry conditions in an industry; while the theoretical model uses the number of firms, this could in practice either refer to firms or to establishments (i.e. different production sites run by the same parent company), or even to employees, as firms in the model use unit labor input. Second, there is no reason to believe that different measures of entry and exit dynamics are exogenous with respect to trade openness – indeed in the model trade openness is a key factor in the entry decision of firms, but in the real world there might be various other factors that might lead to industries being asymmetrically affected by a change in trade costs, hence biasing our results. To tackle both these issues, we aim to construct a robust measure of industry dynamics by aggregating multiple studies that examine firm and employment turnover in Canada, Mexico and the United States as well as Europe over different

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<sup>10</sup>We were inspired to do so by Head and Ries (1999) who use the classification to test competing theories of trade that rely on different market structures.

Table 5.1: Market Structure measures used, numbers in percent

Study	Subject	Highest Turnover	Lowest Turnover
Dunne et al. (1988)	Entry Rates (4-yearly) U.S. 63-82	Instruments (60.3) Lumber (49.70) Printing (49.0)	Leather (29.4) Food Processing (23.9) Tobacco (20.5)
Samianego (2008)	Entry Rates (yearly) Europe 97-04	Paper, printing, software (15.6) Textiles (11.9) Petroleum and Coal (11.9)	Chemicals (9.5) Plastics (9.4) Food Products (9.1)
Brown (2004)	Employment renewal Canada 73-96	Plastic (79.5) Furniture (79.4) Fabricated Metals (77.2)	Primary Metals (33.6) Paper (32.4) Tobacco (4.2)
Foster et al. (2006)	Job creation (yearly) U.S. 72-98	Lumber (11.8) Apparel (11.2) Miscellaneous (11.0)	Paper (5.9) Petroleum (5.9) Tobacco (5.1)
Baldwin et al. (1994)	Job turnover (yearly) Canada 73-86	Furniture (26.5) Machinery (26.3) Lumber (25.7)	Petroleum (14.1) Primary Metals (13.5) Paper (10.7)
Baldwin et al. (1994)	Job turnover (yearly) U.S. 73-86	Lumber (27.2) Apparel (25.5) Leather (22.5)	Petroleum (14.6) Chemicals (14.0) Paper (13.3)

time periods. With this, we hope to identify those industries that are either very dynamic or very static over a broad set of different measures, regions and time periods. Table ?? gives an overview of the studies used and a glance at their respective results, showing considerable variation in the dynamics of entry and job creation in different manufacturing sectors.

In order to aggregate the different studies, we compute percentile-based rankings of the industries for each study (to account for the different number

of industries across studies) and then average the percentiles across studies. Based on these average percentiles, we can then split the sample according to the short- and long-run distinction made in the model: those industries above the 60th percentile are taken to represent the dynamic, "free entry" sample and thus the long run, while those industries below the 40th percentile are taken to represent the short run. This procedure leads us to split the sample three-ways: Food, Beverages and Tobacco, Textiles as well as Chemicals, Fuels, Plastics, Rubber fall into the long run category, Machinery and Transportation Equipment, Manufacturing not else classified and Wood and Cork make up the short run category. The three remaining industries (Paper and Printing, Basic and Manufactured Metal Products and Other Non-Metallic Mineral Products) are too close to the median to be classified either way and are thus dropped from the sample<sup>11</sup>.

A little thought experiment may clarify the role that market entry effects play in muddling the distinction between short- and long-run equilibria. The Melitz and Ottaviano (2008) model yields opposing predictions on the effects of trade liberalization on country-level economic variables such as prices, productivity and mark-ups. The reason for the differences, as we have seen, lies in the assumptions on market structure: there are two different equilibria depending on whether

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<sup>11</sup>Due to different classification systems, the aggregation of studies was not always exact and some industry groups are quite heterogeneous when sub-industries are considered. For further details on the aggregation see Appendix B

entry into a market is allowed. We repeat them here for convenience:

$$\begin{aligned} c_D^k &= c_M^k \frac{\bar{N}^*}{N^*} \left( 1 + \frac{\bar{N}}{\bar{N}^*} \frac{\theta^*}{1 - \theta^*} \right) \\ c_D^{k+2} &= \frac{\phi c_M^k}{\Upsilon L} \left( 1 - \frac{\theta^*}{1 - \theta^*} \right) \end{aligned}$$

In model terms, only one of these two equations holds at any given time, and it is posited that the first equation captures the short run effects of trade liberalization, while in the long run firms are allowed to enter the markets and the effects of trade barriers are determined by the second equation. No further assumptions on the nature of the firm's entry decisions or capital adjustment costs are made that could help separate short- from long run. However, in reality, it seems to be more natural to assume that there is a gradual evolution from one equilibrium to the other, and this view is borne out by data on firm entry and exits showing that in a given year, only between five and ten percent of firms in a given industry are new entrants, while over longer horizons this figure goes up to 80 percent. Hence, it seems to be reasonable to model the transition from the short- to the long run equilibrium by introducing a parameter  $\alpha$  that governs the fraction of firms entering an industry. The effects of this parameter are most clear on the productivity side, given that firms cannot change their productivity level, the new productivity distribution will be a weighted average of new entrants' and existing firms' productivity. As the examples in Chen et al. are formulated with respect to relative prices, and we are using their notation, we will discuss the effects of limited firm entry in the price level case as well. The argument carries through if one is ready to assume a nominal rigidity that prevents incumbents from re-optimizing their prices, similar to the assumptions made in New Keynesian monetary models. Similar to the

productivity level, the price level is then a weighted average of new and old prices (for simplicity, here we abstract from substitution effects induced by the new relative prices of new and old producers):

$$\begin{aligned}\bar{p} &= \alpha \bar{p}^{LR} + (1 - \alpha) \bar{p}^{SR} \\ &= \alpha c_D^{LR} + (1 - \alpha) c_D^{SR} \\ &= \alpha \left( \frac{\phi c_M^k}{\Upsilon L} \left( 1 - \frac{\theta^*}{1 - \theta^*} \right) \right)^{\frac{1}{k+2}} + (1 - \alpha) \left( c_M^k \frac{1}{\frac{\bar{N}}{N} \left( 1 + \frac{\bar{N}^*}{N} \frac{\theta}{1 - \theta} \right)} \right)^{\frac{1}{k}}\end{aligned}$$

where the second line drops the constant linking price level and cost cut-off for notational simplicity. It can easily be seen that the introduction of the  $\alpha$  parameter makes the expression for the price level hugely complicated and eliminates the possibility to cancel out most constant terms by using relative prices as was done in Chen et al. (2009). Obviously, the above expression is impossible to take to the data in the hope of identifying any of the parameters.

Let's consider a simplified version of the above. Assume that relative prices levels in the short- and long run, respectively, are given by:

$$\begin{aligned}\frac{\bar{p}^{SR}}{\bar{p}^{*SR}} &= \left( \frac{c_M}{c_M^*} \right)^k \frac{(\bar{N}^*/N^*)}{(\bar{N}/N)} \frac{\rho^*}{\rho} \\ \frac{\bar{p}^{LR}}{\bar{p}^{*LR}} &= \left( \frac{c_M}{c_M^*} \right)^k \frac{L^*}{L} \frac{(1 - \rho^*)}{(1 - \rho)}\end{aligned}$$

This is a simplified version of the equilibrium conditions in Chen et al. using the notation of Melitz and Ottaviano in which trade freeness is measured by  $\rho \in (0, 1)$ . It captures the main essence of the model, in the short run relative prices depend on the number of firms and negatively on trade freeness (increasing  $\rho$  will decrease

$\bar{p}$ ), while in the long country size matters and prices depend positively on trade freeness (increasing  $\rho$  decreases  $1 - \rho$  and thus increases  $\bar{p}$ ). Now assume further, that price setting decisions and substitution behavior of consumer is such that we can aggregate *relative* price levels in the same way we aggregated individual price levels before. Then:

$$\begin{aligned}\frac{\bar{p}}{\bar{p}^*} &= \alpha \frac{\bar{p}^{LR}}{\bar{p}^{*LR}} + (1 - \alpha) \frac{\bar{p}^{SR}}{\bar{p}^{*SR}} \\ &= \alpha \left( \left( \frac{c_M}{c_M^*} \right)^k \frac{L^* (1 - \rho^*)}{L (1 - \rho)} \right) + (1 - \alpha) \left( \left( \frac{c_M}{c_M^*} \right)^k \frac{(\bar{N}^*/N^*) \rho^*}{(\bar{N}/N) \rho} \right)\end{aligned}$$

Here, the fundamental identification problem becomes apparent: in the first term on the right hand side of the equation, the effect of  $\rho$  on  $\bar{p}$  is positive, while in the second term it is negative. However, the size and sign of the composite effect will be governed by  $\alpha$ , which is unobservable. In order to estimate the effects of trade openness on prices, we have to control for firms entry behavior. While this might well be endogenous to changes in trade policy, it is reasonable to assume that different industries have different entry conditions due to fixed costs inherent in the business model. We can try to exploit this variation in entry conditions by sorting businesses according to the ease of entry; then, *ceteris paribus*, an industry with lower barriers to entry should exhibit a response to trade liberalization along the lines that the model predicts for the long run equilibrium (as the value of  $\alpha$  increases,  $\bar{p}$  approaches  $\bar{p}^{LR}$ ), while an industry with high entry barriers subject to the same trade liberalization should see a very different reaction.

One way to alleviate this problem is by trying to use information on  $\alpha$  in the estimation. Splitting the sample based on our aggregated turnover measures can be seen as a crude approximation to this, as can be the construction of dummy

variables for high and low turnover industries. The most direct way, however, would be to use information on industry turnover rates directly. Obviously, this brings back the very same endogeneity problems we described above that were one reason to aggregate the studies in the first place, which makes it important to instrument for entry and exit rates in industries using turnover measurements for different periods than the one considered in the estimation. The variable construction will be explained in more detail in the next section.

## 5.4 Application

Starting from the equations for prices, productivity and markups derived within the Melitz-Ottaviano framework, we can derive estimable log-linearized equations analogous to those in Chen et al. The estimation equation for prices is given by:

$$\begin{aligned} \Delta \ln \left( \frac{\bar{p}_{it}}{\bar{p}_{it}^*} \right) = & \beta_0 + \beta_1 \Delta \ln \tau_{it} + \beta_2 \Delta \ln \tau_{it}^* + \beta_3 \Delta \ln D_{it} + \beta_4 \Delta \ln D_{it}^* \\ & + \gamma \left[ \ln \left( \frac{\bar{p}_{it-1}}{\bar{p}_{it-1}^*} \right) + \delta_0 + \delta_1 \ln L_{t-1} + \delta_2 \ln L_{t-1}^* + \delta_3 \ln \tau_{i,t-1} + \delta_4 \ln \tau_{i,t-1}^* \right] + \varepsilon_{ijt} \end{aligned} \quad (5.11)$$

In the above equation, the number of firms serving the domestic market,  $N$ , has been replaced by the more readily observable number of domestic firms producing for the domestic market,  $D$ , where  $D = N \left( \frac{c_D}{c_M} \right)^k$ . The short-run dynamics are estimated in the first part of the equation, with regressors expressed in first differences. The long run is represented by the term in brackets. From the perspective of this model, we would expect  $\beta_1 > 0$ , an increase in domestic import tariffs increases relative prices in the short-run, and correspondingly  $\beta_2 > 0$ . The



model predicts a dampening effect of the number of domestic firms on domestic prices, which should be reflected by  $\beta_3 < 0$ , and the opposite for foreign firms,  $\beta_4 < 0$ . As we expect the coefficient on the error correction term,  $\gamma$ , to be negative, a reversal the

As previously discussed, all aggregate variables (prices, markups, productivity) are ultimately functions of the cost-cutoff level  $c_D$ , leading to very similar estimation equations for our three dependent variables. The equation markups is:

$$\begin{aligned} \Delta \ln \left( \frac{\bar{\mu}_{it}}{\bar{\mu}_{it}^*} \right) = & \beta_0 + \beta_1 \Delta \tau_{it} + \beta_2 \Delta \tau_{it}^* + \beta_3 \Delta \ln \theta_{it} + \beta_4 \Delta \ln \theta_{it}^* + \beta_5 \Delta \ln D_{it} + \beta_6 \Delta \ln D_{it}^* \\ & + \gamma \left[ \ln \left( \frac{\bar{\mu}_{it-1}}{\bar{\mu}_{it-1}^*} \right) + \delta_0 + \delta_1 \ln L_{t-1} + \delta_2 \ln L_{t-1}^* + \delta_3 \tau_{i,t-1} + \delta_4 \tau_{i,t-1}^* \right] + \varepsilon_{ijt} \end{aligned} \quad (5.12)$$

The effect of tariffs, openness, number of firms and market size on productivity is estimated by:

$$\begin{aligned} \Delta \ln \left( \frac{\bar{z}_{it}}{\bar{z}_{it}^*} \right) = & \beta_0 + \beta_1 \Delta \tau_{it} + \beta_2 \Delta \tau_{it}^* + \beta_3 \Delta \ln D_{it} + \beta_4 \Delta \ln D_{it}^* \\ & + \gamma \left[ \ln \left( \frac{\bar{z}_{it-1}}{\bar{z}_{it-1}^*} \right) + \delta_0 + \delta_1 \ln L_{t-1} + \delta_2 \ln L_{t-1}^* + \delta_3 \tau_{i,t-1} + \delta_4 \tau_{i,t-1}^* \right. \\ & \left. + \delta_5 \ln w_{i,t-1} + \delta_6 \ln w_{i,t-1}^* \right] + \varepsilon_{ijt} \end{aligned} \quad (5.13)$$

where  $\delta_7$  and  $\delta_8$  capture the effects of changes in nominal wages in the long run. The intercepts  $\beta_0$  are introduced to capture differences in country-specific technology as Chen et al. depart from the baseline Melitz-Ottaviano model by allowing for such differences. While in the baseline, these vary by country-pair,

we check the robustness of the specification by allowing fixed effects at a sectoral level.

### 5.4.1 Preferential Trade Liberalization

The model results and estimation equations presented so far all referred to a unilateral trade liberalization in a simplified two-country setup<sup>12</sup>. While making the exposition clearer and helping to elicit the effects at work in the model, this setup is clearly not an accurate description of the reality of trade relationships in modern industrialized economies. Taking the United States as an example, while the two other countries in our data set, Canada and Mexico, are its largest trading partners, they only account for 16.6 and 13.5% of all US trade by value, respectively<sup>13</sup>. Even the largest 30 US trading partners only account for about 86% of US trade, highlighting the fragmented nature of international trade. While the Melitz-Ottaviano model can be extended to an arbitrary number of countries, it is clearly not feasible to assemble a data set on all trade partners of the NAFTA countries. We do however want to recognize the multi-country structure of NAFTA by taking into account third country effects of trade barriers. Here, NAFTA can be interpreted as a preferential liberalization of Mexico *vis-a-vis* the US and Canada, as Mexico had the highest tariff barriers to start off with. In the three country case, we expect the country with the lowest sum of bilateral trade barriers to have the lowest cost cutoff, as it becomes the best export hub. To account for this, we amend equations 5.11, 5.12 and 5.13 by including the relevant third country

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<sup>12</sup>Note that a bilateral trade liberalization – changing  $\tau$  and  $\tau^*$  by the same amount – would not lead to the discussed short- and long run changes in cost cutoffs for two countries, but instead to a decline in the cost cutoffs in both countries both in the short and the long run.

<sup>13</sup>See Top U.S. Trade Partners, U.S. International Trade Administration

tariffs. The estimation equation for the effects of trade barriers on prices then becomes:

$$\begin{aligned} \Delta \ln \left( \frac{\bar{p}_{it}}{\bar{p}_{it}^*} \right) = & \beta_0 + \beta_1 \Delta \ln \tau_{it} + \beta_2 \Delta \ln \tau_{it}^* + \beta_3 \Delta \ln \tau_{it}^{ht} + \beta_4 \Delta \ln \tau_{it}^{th} + \beta_5 \Delta \ln \tau_{it}^{ft} + \beta_6 \Delta \ln \tau_{it}^{th} \\ & + \beta_7 \Delta \ln D_{it} + \beta_8 \Delta \ln D_{it}^* + \beta_9 \Delta \ln D_{it}^t \\ & + \gamma \left[ \ln \left( \frac{\bar{p}_{it-1}}{\bar{p}_{it-1}^*} \right) + \delta_0 + \delta_1 \ln L_{t-1} + \delta_2 \ln L_{t-1}^* + \delta_3 \ln L_{t-1}^t + \delta_4 \ln \tau_{i,t-1} \right. \\ & \left. + \delta_5 \ln \tau_{i,t-1}^* + \delta_6 \Delta \ln \tau_{it}^{ht} + \delta_7 \Delta \ln \tau_{it}^{th} + \delta_8 \Delta \ln \tau_{it}^{ft} + \delta_9 \Delta \ln \tau_{it}^{th} \right] + \varepsilon_{ijt} \end{aligned} \quad (5.14)$$

where now  $h$  is the domestic economy,  $f$  is the foreign economy, and, with a slight abuse of notation, a  $t$  superscript denotes the third country for each country pair (e.g. when estimating the Canada-US relationship,  $\tau^{th}$  are Mexican tariffs on Canadian goods, while  $\tau^{ht}$  are Canadian tariffs on Mexican goods). Both the equations for markups and productivity will be amended accordingly.

### 5.4.2 Dataset

The database we utilize covers the period 1994-2006 for NAFTA member countries – Canada, Mexico, and the US – and nine manufacturing sectors. For our factory gate price data, we use the producer price index (PPI) as reported by CANSIM, the Banco de Mexico, and the U.S. Bureau of Labor Statistics, respectively. All indices are normalized to equal 100 in 2003. While the majority of the manufacturing data collected is reported at the two-digit level according to ISIC Rev. 3, we aggregate all data according to NACIS in order to keep consistency throughout the

analysis (see Table 5.4 for the manufacturing classification breakdown). While the main part of our analysis rests on data aggregated at the two-digit level, we were also able to assemble a data set at the four-digit level, which we will use to check the robustness of our results.

The value of markups is not easily observable, and thus we follow the calculation as outlined in the recent literature on industrial organization, and similarly used by Chen et al. (2009), although with a subtle modification. We compute average markups as the ratio of sectoral turnover relative to total variable costs, which are computed as the sum of intermediate inputs and labor costs as reported by the OECD STAN database.<sup>14</sup> Due to the unavailability of data on sectoral turnover, we use sectoral production as a proxy. While turnover may be slightly higher than production<sup>15</sup> in a given year if all of the produced goods are sold along with any stored goods from previous years, according to the OECD these measures will converge in the long term. Fixed costs are excluded from the calculation, as they will cause a negative bias between markups and openness. As the number of foreign firms increases due to a decrease in trade costs, the market share for domestic producers falls; because this will spread fixed costs across a smaller share of production, average total costs will increase contemporaneously (Chen et al., 2009).

Labor productivity is calculated as the ratio between real value added and total employment. Value added is reported by the OECD STAN database, while employment data is provided by LABORSTA, the statistical department of the International Labor Organization (ILO).

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<sup>14</sup>In contrast, Chen et al. (2009) calculate average markups as the ratio of turnover relative to the sum of the costs of materials, consumables, and staff costs.

<sup>15</sup>Production represents the value of goods produced in a year, whether they are sold or stocked.

The main explanatory variable in this analysis is the tariff imposed on foreign products. The simple average for tariffs disaggregated at the two-digit level (ISIC Rev. 2) imposed on the bi-lateral trading partners within NAFTA were taken from the World Integrated Trade Solution (WITS), which is a resource developed by the World Bank. The changes in import tariffs across all industries for each country-pair are illustrated in Figures 5.1 – 5.6, including the maximum and minimum tariff for each year. The tariffs imposed by the U.S. on Canadian and Mexican goods, and those imposed by Canada on Mexican and U.S. goods approached zero by 1999–2000, while the Mexican imposed tariffs fluctuated drastically throughout the time period, with some tariffs reaching 30%. The average, maximum, and minimum tariffs by country and sector are also detailed in Table 5.3, as well as the other main variables in this analysis.

To construct the openness variable, we calculate the ratio of imports relative to the sum of imports and domestic production, as in Chen et al. (2009). The bilateral trade data for each country-pair comes from the OECD STAN database and measured in current USD. Domestic production is calculated as the difference between total sectoral output and exports. The sectoral output data are also taken from the OECD STAN database (measured in current units of national currency) and converted to current USD using the OECD-reported exchange rates. In order to check the reliability of our measure of openness, we also use the UPenn openness index.

As discussed in the previous section, for all of the log-linearized equations, we replace the number of firms serving the domestic market,  $N$ , with the number of domestic firms producing for the domestic market,  $D$ . Unfortunately, this data is not available for all three countries during the specified time period, and thus

we utilize the number of establishments, which will always be higher than the firm count as each firm may have multiple establishments. As long as the average number of establishments per firm remains constant, this should not present a problem, as our model is estimated in first differences. It is however not obvious that this relationship will remain constant in response to a trade liberalization. In fact, the main channel through which welfare gains arise in the model is the reallocation of production from unproductive to more productive firms, with less productive firms exiting the market and more productive firms expanding. If this displacement happens through larger firms taking over establishments of less productive ones, we would expect the number of establishments to stay constant, while the number of domestic producers falls (i.e. the number of establishments per firm increases). If on the other hand larger firms are simply able to expand production in existing establishments, this effect would be absent.

The control variables used in the regressions include nominal wages and size of the economy, both of which are provided by LABORSTA. Wages are disaggregated according to ISIC Rev. 3 and reported in national currency units per hour for all wage earners (as before, we convert all data into ISIC Rev. 2 and current USD). For the size of the economy  $L$ , we utilize the total economically active population for manufacturing. Moreover, there are missing values for the US and Mexico<sup>16</sup> and thus we use interpolated data for these years.

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<sup>16</sup>We use interpolated data for the years 1999, 2001, and 2003 for the US, and 1992, 1994, 1996, 1998, 2001-2003 for Mexico.

### 5.4.3 Estimation

As outlined at the beginning of Section 5.4, we follow the estimation strategy of Chen et al. (2009); however, while they use changes in domestic and foreign import penetration in sector  $i$  at time  $t$  as the main explanatory variables for changes in price, markups, and labor productivity, we use this as a control variable and instead rely on the domestic tariff rate ( $\tau$ ) imposed on foreign goods imported from the trading partner and the foreign tariff rate ( $\tau^*$ ) imposed on domestic goods exported to the trading partner as the main explanatory variables. To test the competitive effects of trade liberalization, we use the difference in differences approach with fixed-effects on the country-pair, industry, and year. In the short run we use the log first-difference in the explanatory and dependent variables, whereas we use a lag operator on the explanatory variables and an error correction term to estimate the dynamics in the long run. Moreover, because our variables are stationary in a unit root sense and serially correlated, we utilize a panel-specific AR(1) autocorrelation structure and perform our regressions using a Generalized Least Squares estimation strategy.

Table 5.2 outlines the comparative statics for the theoretical model, with subscript  $sr$  denoting the "short run" and  $lr$  denoting the "long run". Notice that in the long run theory suggests that the pro-competitive effects are reversed and actually take an anti-competitive nature as firms are able to relocate to new markets. Interestingly, as we will exhibit in the following section, our analysis does not provide the same long-run dynamics.

Table 5.2: Comparative Statics – Model Predictions

Regressor	Dependent Variables					
	$\bar{p}_{sr}$	$\bar{p}_{lr}$	$\mu_{sr}$	$\mu_{lr}$	$z_{sr}$	$z_{lr}$
$\tau$	+	–	+	–	–	+
$\tau^*$	–	+	–	+	+	–
$D$	–		–		+	
$D^*$	+		+		–	
$L$		–		–		+
$L^*$		+		+		–

## 5.5 Results & Discussion

Tables 5.5, 5.6 and 5.7 present our results on the short-run effects of trade liberalization on prices, markups and productivity, respectively. Column (1) in each table presents the results from our theoretical estimations in equations 5.11, 5.12, and 5.13, respectively. Beginning with table 5.5, we see that the signs on the tariff measures are as predicted – a decrease in the domestic tariff will decrease the relative price in the short-run – but only the foreign tariff measure is significant. The measure of openness, on the other hand, is as predicted in the model and both coefficients are significant at the 1% level. Finally, contrary to the model's predictions the number of firms serving the domestic market does not have any effect on prices. The results for this model specification on markups are similar, with the openness measure as predicted and significant and no effect from the change in domestic firms (see Table 5.6); in this case, however, the change in the domestic tariff is positive as predicted and significant at the 10% level, whereas the foreign tariff rate has the opposite effect than the model predicts, albeit insignificant. Finally, Table 5.7 shows the effects on industry productivity with different results than predicted by the model. Although the domestic tariff



measure is positive and significant, we see that the openness measures have the opposite effect than the model predicts and are highly significant; an increase in domestic import penetration actually brings about a *decrease* in productivity in the short-run.

Columns (2) and (3) are modified to include the log first-difference in relative tariffs and openness, as well as the log first-difference in the lagged dependent variable.

In the short run, the signs for all short-run effects of tariff reductions are as predicted and highly significant. Table 5.5 presents the effects of tariff reductions on prices in the short run. A decrease in domestic tariffs causes a decrease in relative prices, whereas foreign tariffs actually increase prices. The openness variables that are the main explanatory variable in Chen et al. (2009) are not significant when the tariffs are included, as the tariff provides a more accurate measure of openness between the country-pair; it should be noted, however, that the signs on the openness variable follow the predicted signs from the model when tariffs are excluded from the regression analysis.

Similar to relative prices, Table 5.6 focuses on price markups, and suggests that a decrease in domestic tariffs will likewise decrease domestic markups, with profit margins actually increasing with foreign tariffs. While the coefficients are no longer significant, the signs still match the predicted theory and hold with the different model specifications. In contrast, Table 5.7 focuses on labor productivity, and suggests that domestic tariff reductions will increase productivity, with foreign tariffs causing the opposite effect.

The main contribution of this paper comes from the long-run effects of trade liberalization as presented in Tables 5.8, 5.9, and 5.10. Table 5.8 focuses on

the long-run effects of liberalization on relative prices. While the sign on the coefficient in question (i.e., lagged domestic tariffs) is positive, which is in direct contrast to the theory of Melitz and Ottaviano (2009), the results are not significant. However, the market size ( $L$ ) has a positive and highly significant effect on relative prices in the long-run, thus contradicting theory that the most productive firms will relocate to a less competitive market and the short-run gains from trade will converge back to their equilibrium levels. As firms leave the market, relative prices remain low according to this analysis.

While the sign on tariffs was in contrast to the theory, the competitive effect of trade openness on relative markups (as presented in Table 5.9) does follow the theory of Melitz and Ottaviano, with decreasing tariffs causing an increase in relative markups in the long-run. Moreover, now the size of the market ( $L$ ) has a negative impact on markups, which supports the anti-competitive effects in the long-run when firms have the option to relocate to a less competitive market.

Finally, Table 5.10 presents the results for the long-run effects of tariff reductions on labor productivity. Similar to the theoretical predictions, labor productivity is reversed in the long run.

While the estimation results of Chen et al. on country-pairs within the European Union followed those predicted by the model of Melitz and Ottaviano, the long-run results in this analysis were in contradiction to the theory with regards to prices; however, the models predictions do hold for relative markups and productivity. The estimation results for the short-run follow the model's predictions and are highly significant.

## 5.6 Conclusion

The only empirical application of the Melitz–Ottaviano (2008) model to date suggested that the long–run effects of trade liberalization are anti–competitive, that is, there will be a reversal in any competitive gains as firms are allowed to move to new markets. However, largely due to the year restrictions in their database, the results from Chen et al. (2009) are insignificant in the long run, and thus merely suggestive. While this paper replicates their analysis with only minor conceptual changes, our use of NAFTA as a defining multilateral trade agreement and the 12–years of data available after its implementation, provides new insights into the long–run dynamics of international trade agreements. While the theory suggests a reversal of competitive effects in the aggregate, this paper illustrates that the competitive effects are merely assuaged, but certainly not reversed. This adds credence to the pro–liberalization camp of policy makers who argue for the social welfare improving competitive effects of trade liberalization in the short–, medium–, and long term.

## **5.7 Appendix A: Figures, Summary Statistics, Results**

Figure 5.1: Canadian Tariff on Mexican Goods

Figure 5.2: Canadian Tariff on U.S. Goods

Figure 5.3: Mexican Tariff on Canadian Goods

Figure 5.4: Mexican Tariff on U.S. Goods

Figure 5.5: U.S. Tariff on Canadian Goods

Figure 5.6: U.S. Tariff on Mexican Goods

Table 5.3: Summary Statistics

Statistic	N	Mean	St. Dev.	Min	Max
exp_f	702	76,233,571,691.000	198,643,966,085.000	399,038,863	1,890,000,000,000
gdp_can	594	908.568	278.187	536.500	1,370.640
gdp_mex	594	1,036.795	315.456	560.660	1,566.310
gdp_usa	594	9,807.745	2,991.049	5,482.130	14,498.930
cpi_can	675	79.697	12.487	56.340	100.000
cpi_mex	675	48.219	32.559	1.560	100.000
cpi_usa	675	75.546	14.894	50.300	100.000
open_ind_can	810	59.378	12.446	37.550	75.580
open_ind_mex	810	34.822	17.307	13.210	62.320
open_ind_usa	810	22.673	3.691	17.190	30.970
ppi_mex	810	57.485	51.438	0.100	276.590
tau_s_can_mex	540	1.829	3.193	0.000	17.780
tau_s_can_usa	540	2.440	5.051	0.000	26.440
tau_s_mex_can	405	8.654	8.751	0.000	30.530
tau_s_mex_usa	405	7.611	8.552	0.000	28.800
tau_s_usa_can	621	0.994	1.780	0.000	10.600
tau_s_usa_mex	621	1.717	2.654	0.000	11.810

## **5.8 Appendix B: Conversion Table**

## **5.9 Appendix C: Regression Results**



Table 5.4: Manufacturing Sectors: ISIC Rev. 3 to ISIC Rev. 2 Conversion

ISIC Rev. 3	ISIC Rev. 2
D15: Foods, products, and beverages D16: Tobacco products	31: Food, beverages, and tobacco
D17: Textiles D18: Wearing apparel, dressing and dyeing of fur D19: Tanning and dressing of leather, manufacture of luggage, handbags, saddlery, harness and footwear	32: Textile, wearing apparel, and leather industries
D20: Wood and of products of wood and cork, except furniture; manufacture of articles of straw and plaiting materials	33: Wood and Wood Products, Including Furniture
D21: Paper and paper products D22: Publishing, printing, and reproduction of recorded media	34: Paper and paper products, printing and publishing
D23: Coke, refined petroleum products and nuclear fuel D24: Chemicals and chemical products D25: Rubber and plastics products	35: Chemical, petroleum, coal, rubber and plastic products
D26: Other non-metallic mineral products	36: Non-metallic mineral products, except products of petroleum and coal
D27: Basic metals	37: Basic Metal Industries
D28: Fabricated metal products, except machinery and equipment D29: Machinery and equipment n.e.c. D30: Office, accounting and computing machinery D31: Electrical machinery and apparatus n.e.c. D32: Radio, television and communication equipment and apparatus D33: Medical, precision and optical instruments, watches and clocks D34: Motor vehicles, trailers and semi-trailers D35: Other transport equipment	38: Fabricated metal products, machinery and equipment
D36: Manufacture of furniture; manufacturing n.e.c. D37: Recycling	39: Other Manufacturing Industries

Table 5.5: Prices (Short Run), all country pairs

	Dependent variable:	
	$\Delta \log \left( \frac{p}{p^*} \right)$	
	(1)	(2)
$\Delta \log \tau_t$	0.002 (0.002)	0.002 (0.002)
$\Delta \log \tau_t^*$	-0.003* (0.002)	-0.003 (0.002)
$\Delta \log \theta_t$	-0.106*** (0.014)	-0.104*** (0.015)
$\Delta \log \theta_t^*$	0.247*** (0.023)	0.248*** (0.024)
$\Delta \log D_t$	0.015 (0.025)	0.016 (0.025)
$\Delta \log D_t^*$	-0.034 (0.134)	-0.084 (0.153)
Observations	320	320
R <sup>2</sup>	0.371	0.379
Note: *p<0.1; **p<0.05; ***p<0.01 Fixed effects for country pair		

Table 5.6: Markups (Short Run), all country pairs

	Dependent variable:			
	$\Delta \log \left( \frac{\mu}{\mu^*} \right)$			
	(1)	(2)	(3)	(4)
$\Delta \log \tau_t$	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)	0.001 (0.001)
$\Delta \log \tau_t^*$	0.00003 (0.001)	0.00003 (0.001)	0.0002 (0.001)	0.0002 (0.001)
$\Delta \log \theta$			-0.024*** (0.005)	-0.024*** (0.006)
$\Delta \log \theta^*$			0.028*** (0.009)	0.028*** (0.009)
$\Delta \log D_t$	-0.003 (0.009)	-0.002 (0.009)	-0.005 (0.009)	-0.003 (0.009)
$\Delta \log D_{t-1}$	0.049 (0.050)	0.006 (0.056)	0.037 (0.049)	-0.008 (0.055)
Observations	306	306	302	302
R <sup>2</sup>	0.009	0.006	0.109	0.107
Note: *p<0.1; **p<0.05; ***p<0.01 Fixed effects for country pair				

Table 5.7: Productivity (Short Run), all country pairs

	Dependent variable:			
	$\Delta \log \left( \frac{z}{z^*} \right)$			
	(1)	(2)	(3)	(4)
$\Delta \log \tau_t$	0.007 (0.005)	0.007 (0.006)	0.009** (0.004)	0.009** (0.004)
$\Delta \log \tau_t^*$	-0.006 (0.005)	-0.006 (0.005)	-0.003 (0.004)	-0.003 (0.004)
$\Delta \log \theta_t$	-0.415 (0.264)	-0.389 (0.283)		
$\Delta \log \theta_t^*$	0.767* (0.425)	0.681 (0.482)		
$\Delta \log D_t$			-0.329*** (0.035)	-0.322*** (0.036)
$\Delta \log D_t^*$			0.656*** (0.057)	0.660*** (0.059)
diff(log(firms.h))			-0.012 (0.061)	-0.012 (0.062)
diff(log(firms.f))			0.428 (0.333)	0.359 (0.380)
Observations	324	324	320	320
R <sup>2</sup>	0.027	0.023	0.428	0.432

Note:

\* p<0.1; \*\* p<0.05; \*\*\* p<0.01  
Fixed effects for country pair

Table 5.8: Prices (Long Run), all country pairs

	<i>Dependent variable:</i>			
	$\Delta \log \left( \frac{p_t}{p_t^*} \right)$			
	(1)	(2)	(3)	(4)
$\Delta \log \tau_t$	-0.0004 (0.001)	-0.001 (0.001)	0.0003 (0.001)	-0.001 (0.001)
$\Delta \log \tau_t^*$	-0.002* (0.001)	-0.002 (0.001)	-0.003** (0.001)	-0.003* (0.001)
$\Delta \log \theta$			-0.048*** (0.011)	-0.049*** (0.012)
$\Delta \log \theta^*$			0.040* (0.020)	0.071** (0.033)
$\Delta \log D_t$	0.013 (0.016)	0.031* (0.019)	0.011 (0.016)	0.043** (0.018)
$\Delta \log D_t^*$	-0.040 (0.091)	-0.031 (0.104)	-0.025 (0.091)	-0.030 (0.106)
$\log \left( \frac{p_{t-1}}{p_{t-1}^*} \right)$	-0.279*** (0.011)	-0.263*** (0.013)	-0.270*** (0.014)	-0.233*** (0.021)
$\log \tau_{t-1}$	0.001 (0.001)	0.001 (0.001)	0.002* (0.001)	0.001 (0.002)
$\log \tau_{t-1}^*$	-0.002* (0.001)	-0.002 (0.002)	-0.003*** (0.001)	-0.002 (0.002)
$\log \theta_{t-1}$			-0.012** (0.006)	-0.005 (0.011)
$\log \theta_{t-1}^*$			0.012** (0.006)	0.017 (0.025)
$\log D_{t-1}$	0.0004 (0.005)	0.040** (0.020)	0.003 (0.005)	0.069*** (0.021)
$\log D_{t-1}^*$	0.001 (0.004)	0.088* (0.045)	-0.0005 (0.004)	0.082* (0.045)
$\log L_{t-1}$	-0.082 (0.150)	-0.175 (0.156)	-0.135 (0.148)	-0.323** (0.160)
$\log L_{t-1}^*$	0.061 (0.152)	0.132 (0.153)	0.128 (0.151)	0.251 (0.154)
Observations	324	324	320	320
R <sup>2</sup>	0.731	0.751	0.753	0.776

Note:

\*p<0.1; \*\*p<0.05; \*\*\*p<0.01  
Fixed effects for country pair

Table 5.9: Markups (Long Run), all country pairs

	Dependent variable:			
	$\Delta \log \left( \frac{\mu}{\mu^*} \right)$			
	(1)	(2)	(3)	(4)
$\Delta \log \tau$	0.001 (0.001)	0.0004 (0.001)	0.001 (0.001)	0.0005 (0.001)
$\Delta \log \tau^*$	0.001 (0.001)	0.001 (0.001)	0.00002 (0.001)	0.0003 (0.001)
$\Delta \log \theta$			-0.032*** (0.006)	-0.027*** (0.006)
$\Delta \log \theta^*$			0.048*** (0.010)	0.095*** (0.016)
$\Delta \log D_t$	-0.0004 (0.009)	0.012 (0.008)	-0.004 (0.009)	0.006 (0.007)
$\Delta \log D_t^*$	0.027 (0.053)	-0.055 (0.050)	0.034 (0.051)	-0.063 (0.047)
$\log \left( \frac{\mu_{t-1}}{\mu_{t-1}^*} \right)$	0.010 (0.007)	-0.460*** (0.042)	0.003 (0.007)	-0.454*** (0.039)
$\tau_{t-1}$	-0.001 (0.001)	-0.002** (0.001)	-0.001 (0.001)	-0.002** (0.001)
$\tau_{t-1}^*$	0.001 (0.001)	0.001* (0.001)	-0.0001 (0.001)	0.001 (0.001)
$\log \theta_{t-1}$			-0.010*** (0.003)	-0.010* (0.005)
$\log \theta_{t-1}^*$			0.008** (0.003)	0.037*** (0.010)
$L_{t-1}$	-0.156* (0.080)	-0.128* (0.068)	-0.255*** (0.080)	-0.185*** (0.066)
$L_{t-1}^*$	0.139* (0.081)	0.104 (0.068)	0.230*** (0.081)	0.138** (0.068)
Observations	306	306	302	302
R <sup>2</sup>	0.040	0.332	0.183	0.491

Note: \* p<0.1; \*\* p<0.05; \*\*\* p<0.01  
Fixed effects for country pair

Table 5.10: Productivity (Long Run), all country pairs

	Dependent variable:			
	$\Delta \log \left( \frac{z}{z^*} \right)$			
	(1)	(2)	(3)	(4)
$\Delta \log \tau_t$	0.0002 (0.005)	-0.001 (0.004)	0.004 (0.004)	0.003 (0.004)
$\Delta \log \tau_t^*$	0.001 (0.005)	0.004 (0.005)	-0.001 (0.005)	0.002 (0.005)
$\Delta \log \theta$			-0.245*** (0.040)	-0.214*** (0.042)
$\Delta \log \theta^*$			0.574*** (0.070)	0.451*** (0.131)
$\Delta \log D_t$	-0.428* (0.246)	0.409* (0.221)	-0.179 (0.210)	0.262 (0.208)
$\Delta \log D_t^*$	0.336 (0.393)	-0.427 (0.358)	0.167 (0.345)	-0.175 (0.353)
$\log \left( \frac{z_{t-1}}{z_{t-1}^*} \right)$	-0.145*** (0.016)	-0.348*** (0.022)	-0.089*** (0.015)	-0.308*** (0.033)
$\log \tau_{t-1}$	-0.008 (0.006)	-0.009* (0.005)	-0.007 (0.005)	-0.006 (0.005)
$\log \tau_{t-1}^*$	0.006 (0.005)	0.013** (0.005)	0.0004 (0.005)	0.006 (0.005)
$\log \theta_{t-1}$			-0.012 (0.021)	-0.092** (0.043)
$\log \theta_{t-1}^*$			-0.010 (0.021)	0.119 (0.078)
$\log L_{t-1}$	0.569 (0.623)	-1.531*** (0.559)	-0.523 (0.539)	-1.625*** (0.538)
$\log L_{t-1}^*$	-0.777 (0.636)	1.740*** (0.568)	0.198 (0.547)	1.416*** (0.543)
$\log w_{t-1}$	0.160** (0.063)	0.181** (0.090)	0.068 (0.058)	0.216** (0.100)
$\log w_{t-1}^*$	-0.230*** (0.069)	-0.584*** (0.117)	-0.063 (0.062)	-0.129 (0.142)
Observations	324	324	320	320
R <sup>2</sup>	0.290	0.543	0.510	0.613

Note: \* p<0.1; \*\* p<0.05; \*\*\* p<0.01  
Fixed effects for country pair or industry/country pair

## Chapter 6

## Conclusion

Throughout this thesis, an outline of affine term structure models is provided. This particular class of term structure models has been made very popular in recent years due to its ability to capture the dynamics of yields both across their time series and cross-section and its ease in imposing the absence of arbitrage, allowing in turn the obtention of adaptable risk premia specifications. Affine term structure models have the advantage of allowing various extensions, in a wide range, to their basic primary setup, asserting their importance in the literature. However, difficulties do arise in their estimation and in the interpretation of the latent factors used. This thesis addresses both problems by utilizing a specific structure to the factor loadings, known as the Nelson-Siegel method. The estimation of this term structure model not only circumvents the global optimum issues but further provides some interpretation to the factors, given the level, slope and curvature factors of the Nelson-Siegel interpolation are not only intuitive in their nature, but also have reliable macroeconomic links.

The present thesis introduces and employs dynamic term structure models

to macroeconomic and financial research questions. More precisely, this study initially pertains to financial markets by establishing a tie between interest rates and exchange rates. The study follows by concerning itself with macroeconomic objectives, by exploiting the relationship between yields and inflation.

In a first instance, this study exploits a theoretical relationship between interest rates and exchange rates, namely the uncovered interest rate parity, with the aim to extract currency risk premia through a bilateral affine term structure model with stochastic volatility. The method proposed consists of developing an affine Arbitrage-Free class of dynamic Nelson-Siegel term structure models (AFNS) with stochastic volatility to obtain the domestic and foreign discount rate variations, which in turn are used to derive a representation of exchange rate depreciations. The manipulation of no-arbitrage restrictions allows to endogenously capture currency risk premia. The estimation exercise comprises of a state-space analysis using the Kalman filter. The imposition of the Dynamic Nelson-Siegel (DNS) structure allows for a tractable and robust estimation, offering significant computational benefits, whilst no-arbitrage restrictions enforce the model with theoretically appealing properties. Empirical findings suggest that estimated currency risk premia are able to account for the forward premium puzzle.

In a second instance, inflation expectations and inflation risk premia are derived using a shadow rate class of term structure models. In response to the recent financial crisis, the Bank of England reduced short term interest rates to 0.5%. With such low short term rates, traditional term structure models are likely to be inappropriate for estimating inflation expectations and risk premia, because expectations based on such models might implicitly violate the zero lower



bound condition. In this segment both the nominal and real UK term structure of interest rates are studied, using the dynamic term structure model introduced by, which imposes the non-negativity of nominal short maturity rates. Estimates of the term premia, inflation risk premia and market-implied inflation expectations are provided. Findings indicate that the zero lower bound specification is necessary to reflect countercyclicality in nominal term premia projections and that medium and long term inflation expectations have been contained within narrower bounds since the early 1990s, suggesting monetary policy credibility after the introduction of inflation targeting.

For my future research projects, I wish to draw from the analysis and discussion of this thesis and elaborate further on this strand of the literature, this time emphasizing on the joint effect of monetary economics and finance on asset prices, financial markets and monetary policy. Two main perspectives emerge within my research agenda. A potential project, that inclines more towards macroeconomic concepts, consists in building an extension of the two above-mentioned models by constructing a Taylor rule type of model which would further extend to include growth. Furthermore, an alternative suggests to further exploit the interaction between macroeconomic and financial data to explore a gap in the literature. Specifically, the study includes providing an economic interpretation to the latent factors, used in the state-space representation, by venturing towards macro-finance models and high frequency data. This analysis is built on the prior belief that assets are affected by macroeconomic conditions but simultaneously suffer from microstructure phenomena.

Notwithstanding the extensions listed above, it is crucial to note that the most important message to draw from this thesis is that the literature on risk

premia is still at its infancy due to the striking complexity involved in estimating an unobservable variable which nonetheless contains a very rich informational content. In turn, in future research, I wish to investigate the sensitivity of the price of risk, and consequently of risk premia, to different specifications in the mean reversion matrix of the states' dynamics. The aim is to determine a preferred specification for dynamic term structure models using a Bayesian shrinkage estimation approach.

To conclude, this thesis builds a spherical account of the versatility of affine models by implementing them to distinct monetary finance applications. Several of the pending issues in the literature are addressed and the grounds for future interesting questions are paved.

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