

# Limited Asset Market Participation and the Euler Equation Implied Rate

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## Previously: Aggregate Analysis

- Data from NIPA
- Estimated VAR(4) for consumption, inflation, leisure, FFR, ...
- Computed implied interest rates with and without
  1. Habit formation
  2. Nonseparability in consumption and leisure
- Regressed (implied - observed) spread against stance of monetary policy
- Computed impulse response functions for implied rates

# Limited Asset Market Participation

- Inspired by
  - Campbell and Mankiw (1989): estimated half of aggregate consumption undertaken by households who don't optimize
  - Vissing-Jorgensen (2002): estimated EIS separately for stock-, bond-, and non-asset holders
- Aggregate household-level data for bondholders and nonbondholders
- Repeat analysis from before, comparing bondholders and nonbondholders
- **Hypothesis: interest rates implied by bondholders' consumption paths will more resemble observed rates than those from nonbondholders**

# Data

- Consumer Expenditure Survey, 1996.I to 2012.IV
- Rotating panel of representative households, interviewed for 5 quarters (1 practice)
- Very detailed household-level expenditure categories
- Demographic and income data collected in 2nd and 5th interviews

# Bondholder Criteria

- Following Vissing-Jorgensen (2002)
- Asset holdings information only collected in 5th interview
- Positive response to at least one of:
  1. Stock, bonds, and mutual funds category
  2. U.S. savings bond category
- Household classified as bondholder if at least one of:
  1. Same amount of asset as a year ago and positive amount in interview
  2. Lower holdings of asset than a year ago
  3. Increase in holdings by less than reported holdings in interview

# More Specifications

- Following Heathcote et al. (2010):
  - Nondurable consumption := food, clothing, gasoline, household operation, transportation, medical care, recreation, tobacco, and education
- Following Hai et al. (2015):
  - Disposable income := after-tax income
- Following Vissing-Jorgensen (2002):
  - Consumption and income deflated using CPI-U nondurables (2009 dollars)

# More Specifications

- Output less consumption  $:=$  before-tax income - consumption
- Aggregated using CEX-provided population weights
- Inflation, FFR, and CCI series from aggregate analysis
- Log of real consumption seasonally-adjusted by hand

# Household-Level Summary Stats

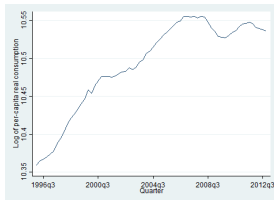
	Bondholders		Nonbondholders	
	Mean	SD	Mean	SD
Consumption	1,774	1,886	1,245	1,339
After-Tax Income	70,641	64,604	48,288	50,043
Hours Worked/Week	41.1	13.1	40.5	12.3
Observations	167,541		1,009,032	
Households	16,959		125,895	

(All dollar amounts nominal)

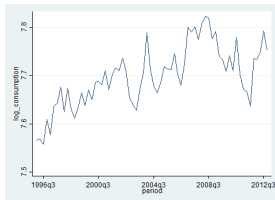


# Volatility Problem

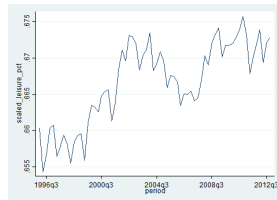
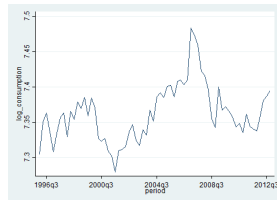
NIPA



CEX Bond



CEX Nonbond



Need much lower risk aversion to accommodate these consumption fluctuations...

# CRRA Implied Rates

- Implied rates computed only from CRRA utility (no habit formation or nonseparability)

$$u(C_t) = \frac{C_t^{1-\alpha}}{1-\alpha}$$

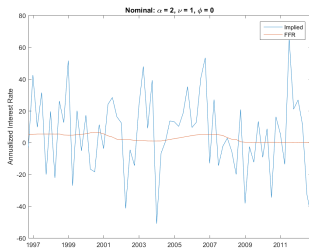
- Euler equation

$$\frac{1}{1+r_t} = \beta \frac{E_t u'(C_{t+1})}{u'(C_t)} = \beta \left( \frac{E_t C_{t+1}}{C_t} \right)^{-\alpha}$$

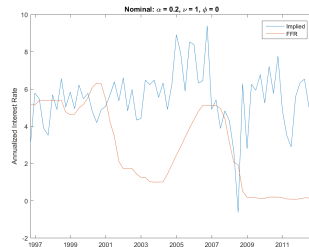
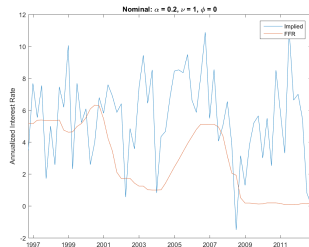
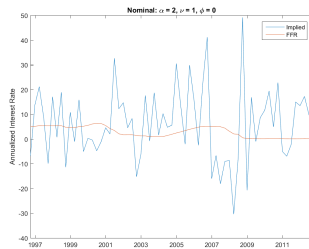
- Coefficient of relative risk aversion  $\alpha$

# Results: Nominal

## Bondholders

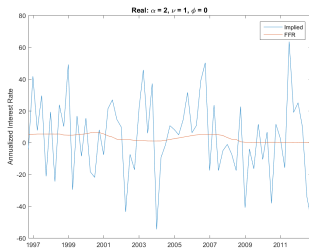


## Nonbondholders

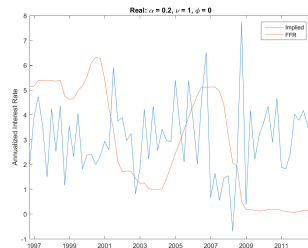
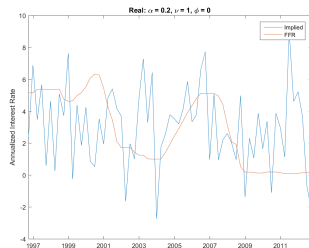
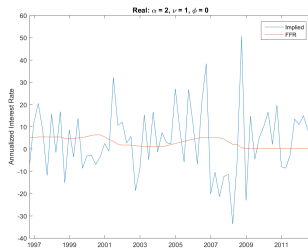


# Results: Real

## Bondholders



## Nonbondholders



## Results: Nominal ( $\alpha = 0.2$ )

	FFR	CEX Bond	CEX Nonbond
Mean	2.83	5.52	5.49
SD	2.19	1.91	1.59
Corr(Implied, FFR)	—	<b>0.193</b>	<b>-0.015</b>
Coef(Spread, FFR)	—	-0.549 (0.199)	-0.647 (0.135)

## Results: Real ( $\alpha = 0.2$ )

	FFR	CEX Bond	CEX Nonbond
Mean	0.353	3.06	3.05
SD	2.58	2.50	1.50
Corr(Implied, FFR)	—	<b>0.235</b>	<b>0.268</b>
Coef(Spread, FFR)	—	-0.527 (0.204)	-0.650 (0.149)

# Conclusions

- Clear difference between bondholders and nonbonders in correlations of nominal rates; no difference for real rates
- Aggregating household-level consumption at quarter level still very noisy
- Small sample size even with most generous definition of bondholders
- EIS ( $= \frac{1}{\alpha}$ ) of 5 not out of the realm of possibility in estimates in literature
- Negative correlation of spread and FFR seems unavoidable
- Results not very conclusive

# References

- Campbell, John Y. and N. Gregory Mankiw (1989) “Consumption, Income, and Interest Rates: Reinterpreting the Time Series Evidence,” *NBER Macroeconomics Annual*.
- Hai, Rong, Dirk Krueger, and Andrew Postlewaite (2015) “On the Welfare Cost of Consumption Fluctuations in the Presence of Memorable Goods,” <http://economics.sas.upenn.edu/~dkrueger/research/Memories.pdf>.
- Heathcote, Jonathan, Fabrizio Perri, and Giovanni L. Violante (2010) “Unequal We Stand: An Empirical Analysis of Economic Inequality in the United States: 1967-2006,” *Review of Economic Dynamics*.
- Vissing-Jorgensen, Annette (2002) “Limited Asset Market Participation and the Elasticity of Intertemporal Substitution,” *Journal of Political Economy*.