

## Index sets

$$HH = \{1, 2\}$$

$$SEC = \{A, B, C\}$$

## 1 CONSUMER $h \in HH$

### 1.1 Optimisation problem

$$\max_{(D^{\langle s, h \rangle})_{s \in SEC}} U^{\langle h \rangle} = \left( \sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} \quad (1.1)$$

s.t. :

$$INC^{\langle h \rangle} + \Pi^{\langle h \rangle} = \sum_{s \in SEC} p^{\langle s \rangle} D^{\langle s, h \rangle} \quad \left( \lambda^{\text{CONSUMER}^1 \langle h \rangle} \right) \quad (1.2)$$

### 1.2 Identities

$$INC^{\langle h \rangle} = L^{\langle h \rangle} + p^k K^{\langle h \rangle} \quad (1.3)$$

$$K^{\langle h \rangle} = k s^{\text{data} \langle h \rangle} \quad (1.4)$$

$$L^{\langle h \rangle} = l s^{\text{data} \langle h \rangle} \quad (1.5)$$

### 1.3 First order conditions

$$s \in SEC: \quad \lambda^{\text{CONSUMER}^1 \langle h \rangle} p^{\langle s \rangle} + \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle -1+\omega^{-1}(-1+\omega)} \left( \sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad \left( D^{\langle s, h \rangle} \right) \quad (1.6)$$

## 2 FIRM $s \in SEC$

### 2.1 Optimisation problem

$$\max_{Y^{(s)}, K^{(s)}, L^{(s)}, Y^{VA(s)}, Y^{INT(s)}} \pi^{(s)} = -L^{(s)} - p^k K^{(s)} + p^{(s)} Y^{(s)} - Y^{INT(s)} \left( \sum_{\mathbf{s}i \in SEC} \beta^{x(\mathbf{s}i, s)^{-1}} p^{(\mathbf{s}i)} \right) \quad (2.1)$$

s.t. :

$$Y^{(s)} = Y^{VA(s)} \left( \lambda^{FIRM^1(s)} \right) \quad (2.2)$$

$$Y^{(s)} = Y^{INT(s)} \left( \lambda^{FIRM^2(s)} \right) \quad (2.3)$$

$$Y^{VA(s)} = \gamma^{yva(s)} K^{(s)\beta^k(s)} L^{(s)\beta^l(s)} \left( \lambda^{FIRM^3(s)} \right) \quad (2.4)$$

### 2.2 Identities

$$\mathbf{s}i \in SEC: \quad X^{(\mathbf{s}i, s)} = \beta^{x(\mathbf{s}i, s)^{-1}} Y^{INT(s)} \quad (2.5)$$

### 2.3 First order conditions

$$-\lambda^{FIRM^1(s)} - \lambda^{FIRM^2(s)} + p^{(s)} = 0 \quad \left( Y^{(s)} \right) \quad (2.6)$$

$$-p^k + \beta^k(s) \gamma^{yva(s)} \lambda^{FIRM^3(s)} K^{(s)^{-1+\beta^k(s)}} L^{(s)\beta^l(s)} = 0 \quad \left( K^{(s)} \right) \quad (2.7)$$

$$-1 + \beta^l(s) \gamma^{yva(s)} \lambda^{FIRM^3(s)} K^{(s)\beta^k(s)} L^{(s)^{-1+\beta^l(s)}} = 0 \quad \left( L^{(s)} \right) \quad (2.8)$$

$$\lambda^{FIRM^1(s)} - \lambda^{FIRM^3(s)} = 0 \quad \left( Y^{VA(s)} \right) \quad (2.9)$$

$$\lambda^{FIRM^2(s)} - \sum_{\mathbf{s}i \in SEC} \beta^{x(\mathbf{s}i, s)^{-1}} p^{(\mathbf{s}i)} = 0 \quad \left( Y^{INT(s)} \right) \quad (2.10)$$

## 2.4 First order conditions after reduction

$$-p^k + \beta^{k\langle s \rangle} \gamma^{yva\langle s \rangle} \left( p^{\langle s \rangle} - \sum_{\vec{s} \in SEC} \beta^{x\langle \vec{s}, s \rangle - 1} p^{\langle \vec{s} \rangle} \right) K^{\langle s \rangle - 1 + \beta^{k\langle s \rangle}} L^{\langle s \rangle \beta^{1\langle s \rangle}} = 0 \quad (K^{\langle s \rangle}) \quad (2.11)$$

$$-1 + \beta^{1\langle s \rangle} \gamma^{yva\langle s \rangle} \left( p^{\langle s \rangle} - \sum_{\vec{s} \in SEC} \beta^{x\langle \vec{s}, s \rangle - 1} p^{\langle \vec{s} \rangle} \right) K^{\langle s \rangle \beta^{k\langle s \rangle}} L^{\langle s \rangle - 1 + \beta^{1\langle s \rangle}} = 0 \quad (L^{\langle s \rangle}) \quad (2.12)$$

## 3 EQUILIBRIUM

### 3.1 Identities

$$\sum_{h \in HH} K^{\langle h \rangle} = \sum_{s \in SEC} K^{\langle s \rangle} \quad (3.1)$$

$$s \in SEC: \quad p^{\langle s \rangle} = 1 \quad (3.2)$$

$$h \in HH: \quad \Pi^{\langle h \rangle} = \pi^{h\langle h \rangle} \left( \sum_{s \in SEC} \pi^{\langle s \rangle} \right) \quad (3.3)$$

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## 4 Equilibrium relationships (before expansion and reduction)

$$- \sum_{h \in HH} K^{\langle h \rangle} + \sum_{s \in SEC} K^{\langle s \rangle} = 0 \quad (4.1)$$

$$h \in HH: \quad ks^{\text{data}\langle h \rangle} - K^{\langle h \rangle} = 0 \quad (4.2)$$

$$h \in HH: \quad ls^{\text{data}\langle h \rangle} - L^{\langle h \rangle} = 0 \quad (4.3)$$

$$h \in HH: \quad -\Pi^{\langle h \rangle} + \pi^{h\langle h \rangle} \left( \sum_{s \in SEC} \pi^{\langle s \rangle} \right) = 0 \quad (4.4)$$

$$h \in HH: \quad U^{\langle h \rangle} - \left( \sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (4.5)$$

$$h \in HH: \quad -INC^{\langle h \rangle} + L^{\langle h \rangle} + p^k K^{\langle h \rangle} = 0 \quad (4.6)$$

$$h \in HH: \quad -INC^{\langle h \rangle} - \Pi^{\langle h \rangle} + \sum_{s \in SEC} p^{\langle s \rangle} D^{\langle s, h \rangle} = 0 \quad (4.7)$$

$$h \in HH: \quad s \in SEC: \quad \lambda^{\text{CONSUMER}^1 \langle h \rangle} p^{\langle s \rangle} + \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle} \omega^{-1} (-1 + \omega)^{-1} \left( \sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle} \omega^{-1} (-1 + \omega)^{-1} \right)^{-1 + \omega (-1 + \omega)^{-1}} = 0 \quad (4.8)$$

$$s \in SEC: \quad -1 + \beta^{\text{l} \langle s \rangle} \gamma^{\text{yva} \langle s \rangle} \left( p^{\langle s \rangle} - \sum_{\dot{s} \in SEC} \beta^{\text{x} \langle \dot{s}, s \rangle} p^{\langle \dot{s} \rangle} \right) K^{\langle s \rangle} \beta^{\text{k} \langle s \rangle} L^{\langle s \rangle} \beta^{\text{l} \langle s \rangle} = 0 \quad (4.9)$$

$$s \in SEC: \quad 1 - p^{\langle s \rangle} = 0 \quad (4.10)$$

$$s \in SEC: \quad -p^{\text{k}} + \beta^{\text{k} \langle s \rangle} \gamma^{\text{yva} \langle s \rangle} \left( p^{\langle s \rangle} - \sum_{\dot{s} \in SEC} \beta^{\text{x} \langle \dot{s}, s \rangle} p^{\langle \dot{s} \rangle} \right) K^{\langle s \rangle} \beta^{\text{k} \langle s \rangle} L^{\langle s \rangle} \beta^{\text{l} \langle s \rangle} = 0 \quad (4.11)$$

$$s \in SEC: \quad -Y^{\langle s \rangle} + Y^{\text{VA} \langle s \rangle} = 0 \quad (4.12)$$

$$s \in SEC: \quad -Y^{\langle s \rangle} + Y^{\text{INT} \langle s \rangle} = 0 \quad (4.13)$$

$$s \in SEC: \quad -Y^{\text{VA} \langle s \rangle} + \gamma^{\text{yva} \langle s \rangle} K^{\langle s \rangle} \beta^{\text{k} \langle s \rangle} L^{\langle s \rangle} \beta^{\text{l} \langle s \rangle} = 0 \quad (4.14)$$

$$s \in SEC: \quad \pi^{\langle s \rangle} + L^{\langle s \rangle} + p^{\text{k}} K^{\langle s \rangle} - p^{\langle s \rangle} Y^{\langle s \rangle} + Y^{\text{INT} \langle s \rangle} \left( \sum_{\dot{s} \in SEC} \beta^{\text{x} \langle \dot{s}, s \rangle} p^{\langle \dot{s} \rangle} \right) = 0 \quad (4.15)$$

$$s \in SEC: \quad \dot{s} \in SEC: \quad -X^{\langle \dot{s}, s \rangle} + \beta^{\text{x} \langle \dot{s}, s \rangle} Y^{\text{INT} \langle s \rangle} = 0 \quad (4.16)$$

## 5 Equilibrium relationships (after expansion and reduction)

$$-1 + \beta^{\text{l} \langle \text{A} \rangle} \gamma^{\text{yva} \langle \text{A} \rangle} \left( p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{A}, \text{A} \rangle} p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{B}, \text{A} \rangle} p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{C}, \text{A} \rangle} p^{\langle \text{C} \rangle} \right) K^{\langle \text{A} \rangle} \beta^{\text{k} \langle \text{A} \rangle} L^{\langle \text{A} \rangle} \beta^{\text{l} \langle \text{A} \rangle} = 0 \quad (5.1)$$

$$-1 + \beta^{\text{l} \langle \text{B} \rangle} \gamma^{\text{yva} \langle \text{B} \rangle} \left( p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{A}, \text{B} \rangle} p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{B}, \text{B} \rangle} p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{C}, \text{B} \rangle} p^{\langle \text{C} \rangle} \right) K^{\langle \text{B} \rangle} \beta^{\text{k} \langle \text{B} \rangle} L^{\langle \text{B} \rangle} \beta^{\text{l} \langle \text{B} \rangle} = 0 \quad (5.2)$$

$$-1 + \beta^{\text{l} \langle \text{C} \rangle} \gamma^{\text{yva} \langle \text{C} \rangle} \left( p^{\langle \text{C} \rangle} - \beta^{\text{x} \langle \text{A}, \text{C} \rangle} p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{B}, \text{C} \rangle} p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{C}, \text{C} \rangle} p^{\langle \text{C} \rangle} \right) K^{\langle \text{C} \rangle} \beta^{\text{k} \langle \text{C} \rangle} L^{\langle \text{C} \rangle} \beta^{\text{l} \langle \text{C} \rangle} = 0 \quad (5.3)$$

$$1 - p^{\langle A \rangle} = 0 \quad (5.4)$$

$$1 - p^{\langle B \rangle} = 0 \quad (5.5)$$

$$1 - p^{\langle C \rangle} = 0 \quad (5.6)$$

$$k_s^{\text{data}\langle 1 \rangle} - K^{\langle 1 \rangle} = 0 \quad (5.7)$$

$$k_s^{\text{data}\langle 2 \rangle} - K^{\langle 2 \rangle} = 0 \quad (5.8)$$

$$l_s^{\text{data}\langle 1 \rangle} - L^{\langle 1 \rangle} = 0 \quad (5.9)$$

$$l_s^{\text{data}\langle 2 \rangle} - L^{\langle 2 \rangle} = 0 \quad (5.10)$$

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$$-p^k + \beta^{k\langle A \rangle} \gamma^{\text{yva}\langle A \rangle} \left( p^{\langle A \rangle} - \beta^{x\langle A, A \rangle -1} p^{\langle A \rangle} - \beta^{x\langle B, A \rangle -1} p^{\langle B \rangle} - \beta^{x\langle C, A \rangle -1} p^{\langle C \rangle} \right) K^{\langle A \rangle -1 + \beta^{k\langle A \rangle}} L^{\langle A \rangle \beta^{1\langle A \rangle}} = 0 \quad (5.11)$$

$$-p^k + \beta^{k\langle B \rangle} \gamma^{\text{yva}\langle B \rangle} \left( p^{\langle B \rangle} - \beta^{x\langle A, B \rangle -1} p^{\langle A \rangle} - \beta^{x\langle B, B \rangle -1} p^{\langle B \rangle} - \beta^{x\langle C, B \rangle -1} p^{\langle C \rangle} \right) K^{\langle B \rangle -1 + \beta^{k\langle B \rangle}} L^{\langle B \rangle \beta^{1\langle B \rangle}} = 0 \quad (5.12)$$

$$-p^k + \beta^{k\langle C \rangle} \gamma^{\text{yva}\langle C \rangle} \left( p^{\langle C \rangle} - \beta^{x\langle A, C \rangle -1} p^{\langle A \rangle} - \beta^{x\langle B, C \rangle -1} p^{\langle B \rangle} - \beta^{x\langle C, C \rangle -1} p^{\langle C \rangle} \right) K^{\langle C \rangle -1 + \beta^{k\langle C \rangle}} L^{\langle C \rangle \beta^{1\langle C \rangle}} = 0 \quad (5.13)$$

$$-\Pi^{\langle 1 \rangle} + \pi^{h\langle 1 \rangle} \left( \pi^{\langle A \rangle} + \pi^{\langle B \rangle} + \pi^{\langle C \rangle} \right) = 0 \quad (5.14)$$

$$-\Pi^{\langle 2 \rangle} + \pi^{h\langle 2 \rangle} \left( \pi^{\langle A \rangle} + \pi^{\langle B \rangle} + \pi^{\langle C \rangle} \right) = 0 \quad (5.15)$$

$$U^{\langle 1 \rangle} - \left( \alpha^{\langle A, 1 \rangle} D^{\langle A, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B, 1 \rangle} D^{\langle B, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C, 1 \rangle} D^{\langle C, 1 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.16)$$

$$U^{\langle 2 \rangle} - \left( \alpha^{\langle A, 2 \rangle} D^{\langle A, 2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B, 2 \rangle} D^{\langle B, 2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C, 2 \rangle} D^{\langle C, 2 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.17)$$

$$-X^{\langle A, A \rangle} + \beta^{x\langle A, A \rangle -1} Y^{\text{INT}\langle A \rangle} = 0 \quad (5.18)$$

$$-X^{\langle A,B \rangle} + \beta^{\mathbf{x}\langle A,B \rangle} Y^{\text{INT}\langle B \rangle} = 0 \quad (5.19)$$

$$-X^{\langle A,C \rangle} + \beta^{\mathbf{x}\langle A,C \rangle} Y^{\text{INT}\langle C \rangle} = 0 \quad (5.20)$$

$$-X^{\langle B,A \rangle} + \beta^{\mathbf{x}\langle B,A \rangle} Y^{\text{INT}\langle A \rangle} = 0 \quad (5.21)$$

$$-X^{\langle B,B \rangle} + \beta^{\mathbf{x}\langle B,B \rangle} Y^{\text{INT}\langle B \rangle} = 0 \quad (5.22)$$

$$-X^{\langle B,C \rangle} + \beta^{\mathbf{x}\langle B,C \rangle} Y^{\text{INT}\langle C \rangle} = 0 \quad (5.23)$$

$$-X^{\langle C,A \rangle} + \beta^{\mathbf{x}\langle C,A \rangle} Y^{\text{INT}\langle A \rangle} = 0 \quad (5.24)$$

$$-X^{\langle C,B \rangle} + \beta^{\mathbf{x}\langle C,B \rangle} Y^{\text{INT}\langle B \rangle} = 0 \quad (5.25)$$

$$-X^{\langle C,C \rangle} + \beta^{\mathbf{x}\langle C,C \rangle} Y^{\text{INT}\langle C \rangle} = 0 \quad (5.26)$$

$$-Y^{\langle A \rangle} + Y^{\text{VA}\langle A \rangle} = 0 \quad (5.27)$$

$$-Y^{\langle A \rangle} + Y^{\text{INT}\langle A \rangle} = 0 \quad (5.28)$$

$$-Y^{\langle B \rangle} + Y^{\text{VA}\langle B \rangle} = 0 \quad (5.29)$$

$$-Y^{\langle B \rangle} + Y^{\text{INT}\langle B \rangle} = 0 \quad (5.30)$$

$$-Y^{\langle C \rangle} + Y^{\text{VA}\langle C \rangle} = 0 \quad (5.31)$$

$$-Y^{\langle C \rangle} + Y^{\text{INT}\langle C \rangle} = 0 \quad (5.32)$$

$$-Y^{\text{VA}\langle A \rangle} + \gamma^{\text{yva}\langle A \rangle} K^{\langle A \rangle \beta^{\mathbf{k}\langle A \rangle}} L^{\langle A \rangle \beta^{\mathbf{l}\langle A \rangle}} = 0 \quad (5.33)$$

$$-Y^{\text{VA}\langle B \rangle} + \gamma^{\text{yva}\langle B \rangle} K^{\langle B \rangle \beta^{\mathbf{k}\langle B \rangle}} L^{\langle B \rangle \beta^{\mathbf{l}\langle B \rangle}} = 0 \quad (5.34)$$

$$-Y^{\text{VA}\langle C \rangle} + \gamma^{\text{yva}\langle C \rangle} K^{\langle C \rangle} \beta^{\text{k}\langle C \rangle} L^{\langle C \rangle} \beta^{1\langle C \rangle} = 0 \quad (5.35)$$

$$\lambda^{\text{CONSUMER}^1\langle 1 \rangle} p^{\langle A \rangle} + \alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle -1+\omega^{-1}(-1+\omega)} \left( \alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,1 \rangle} D^{\langle C,1 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.36)$$

$$\lambda^{\text{CONSUMER}^1\langle 1 \rangle} p^{\langle B \rangle} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle -1+\omega^{-1}(-1+\omega)} \left( \alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,1 \rangle} D^{\langle C,1 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.37)$$

$$\lambda^{\text{CONSUMER}^1\langle 1 \rangle} p^{\langle C \rangle} + \alpha^{\langle C,1 \rangle} D^{\langle C,1 \rangle -1+\omega^{-1}(-1+\omega)} \left( \alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,1 \rangle} D^{\langle C,1 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.38)$$

$$\lambda^{\text{CONSUMER}^1\langle 2 \rangle} p^{\langle A \rangle} + \alpha^{\langle A,2 \rangle} D^{\langle A,2 \rangle -1+\omega^{-1}(-1+\omega)} \left( \alpha^{\langle A,2 \rangle} D^{\langle A,2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,2 \rangle} D^{\langle B,2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,2 \rangle} D^{\langle C,2 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.39)$$

$$\lambda^{\text{CONSUMER}^1\langle 2 \rangle} p^{\langle B \rangle} + \alpha^{\langle B,2 \rangle} D^{\langle B,2 \rangle -1+\omega^{-1}(-1+\omega)} \left( \alpha^{\langle A,2 \rangle} D^{\langle A,2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,2 \rangle} D^{\langle B,2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,2 \rangle} D^{\langle C,2 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.40)$$

$$\lambda^{\text{CONSUMER}^1\langle 2 \rangle} p^{\langle C \rangle} + \alpha^{\langle C,2 \rangle} D^{\langle C,2 \rangle -1+\omega^{-1}(-1+\omega)} \left( \alpha^{\langle A,2 \rangle} D^{\langle A,2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,2 \rangle} D^{\langle B,2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,2 \rangle} D^{\langle C,2 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.41)$$

$$-INC^{\langle 1 \rangle} + L^{\langle 1 \rangle} + p^{\text{k}} K^{\langle 1 \rangle} = 0 \quad (5.42)$$

$$-INC^{\langle 2 \rangle} + L^{\langle 2 \rangle} + p^{\text{k}} K^{\langle 2 \rangle} = 0 \quad (5.43)$$

$$\pi^{\langle A \rangle} + L^{\langle A \rangle} + p^{\text{k}} K^{\langle A \rangle} - p^{\langle A \rangle} Y^{\langle A \rangle} + Y^{\text{INT}\langle A \rangle} \left( \beta^{\text{x}\langle A,A \rangle -1} p^{\langle A \rangle} + \beta^{\text{x}\langle B,A \rangle -1} p^{\langle B \rangle} + \beta^{\text{x}\langle C,A \rangle -1} p^{\langle C \rangle} \right) = 0 \quad (5.44)$$

$$\pi^{\langle B \rangle} + L^{\langle B \rangle} + p^{\text{k}} K^{\langle B \rangle} - p^{\langle B \rangle} Y^{\langle B \rangle} + Y^{\text{INT}\langle B \rangle} \left( \beta^{\text{x}\langle A,B \rangle -1} p^{\langle A \rangle} + \beta^{\text{x}\langle B,B \rangle -1} p^{\langle B \rangle} + \beta^{\text{x}\langle C,B \rangle -1} p^{\langle C \rangle} \right) = 0 \quad (5.45)$$

$$\pi^{\langle C \rangle} + L^{\langle C \rangle} + p^{\text{k}} K^{\langle C \rangle} - p^{\langle C \rangle} Y^{\langle C \rangle} + Y^{\text{INT}\langle C \rangle} \left( \beta^{\text{x}\langle A,C \rangle -1} p^{\langle A \rangle} + \beta^{\text{x}\langle B,C \rangle -1} p^{\langle B \rangle} + \beta^{\text{x}\langle C,C \rangle -1} p^{\langle C \rangle} \right) = 0 \quad (5.46)$$

$$-INC^{\langle 1 \rangle} - \Pi^{\langle 1 \rangle} + p^{\langle A \rangle} D^{\langle A,1 \rangle} + p^{\langle B \rangle} D^{\langle B,1 \rangle} + p^{\langle C \rangle} D^{\langle C,1 \rangle} = 0 \quad (5.47)$$

$$-INC^{\langle 2 \rangle} - \Pi^{\langle 2 \rangle} + p^{\langle A \rangle} D^{\langle A,2 \rangle} + p^{\langle B \rangle} D^{\langle B,2 \rangle} + p^{\langle C \rangle} D^{\langle C,2 \rangle} = 0 \quad (5.48)$$

$$-K^{\langle 1 \rangle} - K^{\langle 2 \rangle} + K^{\langle A \rangle} + K^{\langle B \rangle} + K^{\langle C \rangle} = 0 \quad (5.49)$$

## 6 Calibrating equations

$$-d^{\text{data}\langle\text{B},1\rangle} + D^{\langle\text{B},1\rangle} = 0 \quad (6.1)$$

$$-d^{\text{data}\langle\text{B},2\rangle} + D^{\langle\text{B},2\rangle} = 0 \quad (6.2)$$

$$-d^{\text{data}\langle\text{C},1\rangle} + D^{\langle\text{C},1\rangle} = 0 \quad (6.3)$$

$$-d^{\text{data}\langle\text{C},2\rangle} + D^{\langle\text{C},2\rangle} = 0 \quad (6.4)$$

$$-l^{\text{data}\langle\text{A}\rangle} + L^{\langle\text{A}\rangle} = 0 \quad (6.5)$$

$$-l^{\text{data}\langle\text{B}\rangle} + L^{\langle\text{B}\rangle} = 0 \quad (6.6)$$

$$-l^{\text{data}\langle\text{C}\rangle} + L^{\langle\text{C}\rangle} = 0 \quad (6.7)$$

$$-x^{\text{data}\langle\text{A},\text{A}\rangle} + X^{\langle\text{A},\text{A}\rangle} = 0 \quad (6.8)$$

$$-x^{\text{data}\langle\text{A},\text{B}\rangle} + X^{\langle\text{A},\text{B}\rangle} = 0 \quad (6.9)$$

$$-x^{\text{data}\langle\text{A},\text{C}\rangle} + X^{\langle\text{A},\text{C}\rangle} = 0 \quad (6.10)$$

$$-x^{\text{data}\langle\text{B},\text{A}\rangle} + X^{\langle\text{B},\text{A}\rangle} = 0 \quad (6.11)$$

$$-x^{\text{data}\langle\text{B},\text{B}\rangle} + X^{\langle\text{B},\text{B}\rangle} = 0 \quad (6.12)$$

$$-x^{\text{data}\langle\text{B},\text{C}\rangle} + X^{\langle\text{B},\text{C}\rangle} = 0 \quad (6.13)$$

$$-x^{\text{data}\langle\text{C},\text{A}\rangle} + X^{\langle\text{C},\text{A}\rangle} = 0 \quad (6.14)$$

$$-x^{\text{data}\langle\text{C},\text{B}\rangle} + X^{\langle\text{C},\text{B}\rangle} = 0 \quad (6.15)$$

$$-x^{\text{data}\langle\text{C},\text{C}\rangle} + X^{\langle\text{C},\text{C}\rangle} = 0 \quad (6.16)$$



$$-y^{\text{data}\langle A \rangle} + Y^{\text{VA}\langle A \rangle} = 0 \quad (6.17)$$

$$-y^{\text{data}\langle B \rangle} + Y^{\text{VA}\langle B \rangle} = 0 \quad (6.18)$$

$$-y^{\text{data}\langle C \rangle} + Y^{\text{VA}\langle C \rangle} = 0 \quad (6.19)$$

$$-1 + \beta^{\text{k}\langle A \rangle} + \beta^{\text{l}\langle A \rangle} = 0 \quad (6.20)$$

$$-1 + \beta^{\text{k}\langle B \rangle} + \beta^{\text{l}\langle B \rangle} = 0 \quad (6.21)$$

$$-1 + \beta^{\text{k}\langle C \rangle} + \beta^{\text{l}\langle C \rangle} = 0 \quad (6.22)$$

$$-1 + \pi^{\text{h}\langle 1 \rangle} + \pi^{\text{h}\langle 2 \rangle} = 0 \quad (6.23)$$

$$-1 + \alpha^{\langle A,1 \rangle \omega} + \alpha^{\langle B,1 \rangle \omega} + \alpha^{\langle C,1 \rangle \omega} = 0 \quad (6.24)$$

$$-1 + \alpha^{\langle A,2 \rangle \omega} + \alpha^{\langle B,2 \rangle \omega} + \alpha^{\langle C,2 \rangle \omega} = 0 \quad (6.25)$$

## 7 Equilibrium values

|                               | Equilibrium values |
|-------------------------------|--------------------|
| $p^k$                         | 1                  |
| $\lambda^{\text{CONSUMER}^1}$ | -1                 |
| $\lambda^{\text{CONSUMER}^2}$ | -1                 |
| $p^A$                         | 1                  |
| $p^B$                         | 1                  |
| $p^C$                         | 1                  |
| $\pi^A$                       | 0                  |
| $\pi^B$                       | 0                  |
| $\pi^C$                       | 0                  |
| $D^{A^1}$                     | 52.94              |
| $D^{A^2}$                     | 64.45              |
| $D^{B^1}$                     | 11.7               |
| $D^{B^2}$                     | 30.79              |
| $D^{C^1}$                     | 18.6               |
| $D^{C^2}$                     | 43.6               |
| $INC^1$                       | 83.24              |
| $INC^2$                       | 138.84             |
| $K^1$                         | 65.07              |
| $K^2$                         | 68.77              |
| $K^A$                         | 38.1               |
| $K^B$                         | 35.01              |
| $K^C$                         | 60.73              |
| $L^1$                         | 18.17              |
| $L^2$                         | 70.07              |
| $L^A$                         | 9.44               |
| $L^B$                         | 31.6               |
| $L^C$                         | 47.2               |
| $\Pi^1$                       | 0                  |
| $\Pi^2$                       | 0                  |
| $U^1$                         | 83.24              |
| $U^2$                         | 138.84             |
| $X^{A^A}$                     | 68.4               |
| $X^{A^B}$                     | 131.01             |
| $X^{A^C}$                     | 28.28              |
| $X^{B^A}$                     | 111.91             |
| $X^{B^B}$                     | 92.3               |
| $X^{B^C}$                     | 86.92              |
| $X^{C^A}$                     | 117.23             |
| $X^{C^B}$                     | 43.7               |
| $X^{C^C}$                     | 111.65             |
| $Y^A$                         | 345.08             |
| $Y^B$                         | 333.62             |
| $Y^C$                         | 334.78             |
| $Y^{VA^A}$                    | 345.08             |
| $Y^{VA^B}$                    | 333.62             |
| $Y^{VA^C}$                    | 334.78             |
| $Y^{\text{INT}^A}$            | 345.08             |
| $Y^{\text{INT}^B}$            | 333.62             |
| $Y^{\text{INT}^C}$            | 334.78             |



## 8 Parameters of the model

|                         | Parameters |
|-------------------------|------------|
| $\omega$                | 2          |
| $\alpha^{A^1}$          | 0.7975     |
| $\alpha^{A^2}$          | 0.6813     |
| $\alpha^{B^1}$          | 0.3749     |
| $\alpha^{B^2}$          | 0.4709     |
| $\alpha^{C^1}$          | 0.4727     |
| $\alpha^{C^2}$          | 0.5604     |
| $\beta^{k^A}$           | 0.8014     |
| $\beta^{k^B}$           | 0.5256     |
| $\beta^{k^C}$           | 0.5627     |
| $\beta^{l^A}$           | 0.1986     |
| $\beta^{l^B}$           | 0.4744     |
| $\beta^{l^C}$           | 0.4373     |
| $\beta^{x^{AA}}$        | 5.045      |
| $\beta^{x^{AB}}$        | 2.5465     |
| $\beta^{x^{AC}}$        | 11.838     |
| $\beta^{x^{BA}}$        | 3.0835     |
| $\beta^{x^{BB}}$        | 3.6145     |
| $\beta^{x^{BC}}$        | 3.8516     |
| $\beta^{x^{CA}}$        | 2.9436     |
| $\beta^{x^{CB}}$        | 7.6343     |
| $\beta^{x^{CC}}$        | 2.9985     |
| $d^{\text{data}^{B^1}}$ | 11.7       |
| $d^{\text{data}^{B^2}}$ | 30.79      |
| $d^{\text{data}^{C^1}}$ | 18.6       |
| $d^{\text{data}^{C^2}}$ | 43.6       |
| $\gamma^{\text{yva}^A}$ | 11.9486    |
| $\gamma^{\text{yva}^B}$ | 10.004     |
| $\gamma^{\text{yva}^C}$ | 6.155      |
| $ks^{\text{data}^1}$    | 65.07      |
| $ks^{\text{data}^2}$    | 68.77      |
| $l^{\text{data}^A}$     | 9.44       |
| $l^{\text{data}^B}$     | 31.6       |
| $l^{\text{data}^C}$     | 47.2       |
| $ls^{\text{data}^1}$    | 18.17      |
| $ls^{\text{data}^2}$    | 70.07      |
| $\pi^{\text{h}^1}$      | 0.5        |
| $\pi^{\text{h}^2}$      | 0.5        |
| $x^{\text{data}^{AA}}$  | 68.4       |
| $x^{\text{data}^{AB}}$  | 131.01     |
| $x^{\text{data}^{AC}}$  | 28.28      |
| $x^{\text{data}^{BA}}$  | 111.91     |
| $x^{\text{data}^{BB}}$  | 92.3       |
| $x^{\text{data}^{BC}}$  | 86.92      |
| $x^{\text{data}^{CA}}$  | 117.23     |
| $x^{\text{data}^{CB}}$  | 43.7       |
| $x^{\text{data}^{CC}}$  | 111.65     |
| $y^{\text{data}^A}$     | 345.08     |
| $y^{\text{data}^B}$     | 333.62     |
| $y^{\text{data}^C}$     | 334.78     |