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#### 1 CONSUMER

#### 1.1 Optimisation problem

$$\max_{K_t^s, C_t, L_t^s, I_t, H_t} U_t = \beta \mathcal{E}_t \left[ U_{t+1} \right] + (1 - \eta)^{-1} \left( (1 - L_t^s)^{1 - \mu} (C_t - persH_t)^{\mu} \right)^{1 - \eta}$$
(1.1)

s.t. :

$$C_t + I_t = \pi_t + K_{t-1}^{\mathrm{s}} r_t + L_t^{\mathrm{s}} W_t \quad \left(\lambda_t^{\mathrm{CONSUMER}^1}\right)$$

$$\tag{1.2}$$

$$K_t^{s} = I_t + K_{t-1}^{s} (1 - \delta) \quad \left(\lambda_t^{\text{CONSUMER}^2}\right)$$
(1.3)

$$H_t = C_{t-1} \quad \left(\lambda_t^{\text{CONSUMER}^3}\right) \tag{1.4}$$

#### 1.2 First order conditions

$$-\lambda_t^{\text{CONSUMER}^2} + \beta \left( (1 - \delta) E_t \left[ \lambda_{t+1}^{\text{CONSUMER}^2} \right] + E_t \left[ \lambda_{t+1}^{\text{CONSUMER}^1} r_{t+1} \right] \right) = 0 \quad (K_t^s)$$
(1.5)

$$-\lambda_t^{\text{CONSUMER}^1} + \beta E_t \left[ \lambda_{t+1}^{\text{CONSUMER}^3} \right] + \mu (1 - L_t^{\text{s}})^{1-\mu} (C_t - persH_t)^{-1+\mu} \left( (1 - L_t^{\text{s}})^{1-\mu} (C_t - persH_t)^{\mu} \right)^{-\eta} = 0 \quad (C_t)$$
(1.6)

$$\lambda_t^{\text{CONSUMER}^1} W_t + (-1 + \mu) (1 - L_t^{\text{s}})^{-\mu} (C_t - persH_t)^{\mu} \Big( (1 - L_t^{\text{s}})^{1-\mu} (C_t - persH_t)^{\mu} \Big)^{-\eta} = 0 \quad (L_t^{\text{s}})$$
(1.7)

$$-\lambda_t^{\text{CONSUMER}^1} + \lambda_t^{\text{CONSUMER}^2} = 0 \quad (I_t)$$
(1.8)

$$-\lambda_t^{\text{CONSUMER}^3} - \mu pers(1 - L_t^s)^{1-\mu} (C_t - persH_t)^{-1+\mu} \left( (1 - L_t^s)^{1-\mu} (C_t - persH_t)^{\mu} \right)^{-\eta} = 0 \quad (H_t)$$
(1.9)

#### 2 FIRM

#### 2.1 Optimisation problem

$$\max_{K_t^d, L_t^d, Y_t} \pi_t = Y_t - L_t^d W_t - r_t K_t^d$$
(2.1)

s.t.:

$$Y_t = Z_t K_t^{\mathrm{d}^{\alpha}} L_t^{\mathrm{d}^{1-\alpha}} \quad \left(\lambda_t^{\mathrm{FIRM}^1}\right) \tag{2.2}$$

### 2.2 First order conditions

$$-r_t + \alpha \lambda_t^{\text{FIRM}^1} Z_t K_t^{\text{d}^{-1+\alpha}} L_t^{\text{d}^{1-\alpha}} = 0 \quad (K_t^{\text{d}})$$

$$(2.3)$$

$$-W_t + \lambda_t^{\text{FIRM}^1} Z_t (1 - \alpha) K_t^{d^{\alpha}} L_t^{d^{-\alpha}} = 0 \quad (L_t^d)$$
(2.4)

$$1 - \lambda_t^{\text{FIRM}^1} = 0 \quad (Y_t) \tag{2.5}$$

#### 2.3 First order conditions after reduction

$$-r_t + \alpha Z_t K_t^{\mathrm{d}^{-1+\alpha}} L_t^{\mathrm{d}^{1-\alpha}} = 0 \quad (K_t^{\mathrm{d}})$$

$$\tag{2.6}$$

$$-W_t + Z_t (1 - \alpha) K_t^{\mathrm{d}^{\alpha}} L_t^{\mathrm{d}^{-\alpha}} = 0 \quad (L_t^{\mathrm{d}})$$

$$(2.7)$$

### 3 EQUILIBRIUM

3.1 Identities

$$K_t^{\mathbf{d}} = K_{t-1}^{\mathbf{s}} \tag{3.1}$$

$$L_t^{\rm d} = L_t^{\rm s} \tag{3.2}$$

#### 4 EXOG

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4.1 Identities

$$Z_t = e^{\epsilon_t^Z + \phi \log Z_{t-1}} \tag{4.1}$$

5 Equilibrium relationships (after reduction)

$$C_{t-1} - H_t = 0 (5.1)$$

$$-\lambda_t^{\text{CONSUMER}^2} + \beta \left( (1 - \delta) E_t \left[ \lambda_{t+1}^{\text{CONSUMER}^2} \right] + E_t \left[ \lambda_{t+1}^{\text{CONSUMER}^2} r_{t+1} \right] \right) = 0$$
 (5.2)

$$-r_t + \alpha Z_t K_{t-1}^{s}^{-1+\alpha} L_t^{s^{1-\alpha}} = 0$$
 (5.3)

$$-W_t + Z_t (1 - \alpha) K_{t-1}^{s} {}^{\alpha} L_t^{s-\alpha} = 0$$
(5.4)

$$-Y_t + Z_t K_{t-1}^{s} {}^{\alpha} L_t^{s1-\alpha} = 0 (5.5)$$

$$Z_t - e^{\epsilon_t^Z + \phi \log Z_{t-1}} = 0 \tag{5.6}$$

$$\lambda_t^{\text{CONSUMER}^2} W_t + (-1 + \mu) \left(1 - L_t^{\text{s}}\right)^{-\mu} (C_t - persH_t)^{\mu} \left( (1 - L_t^{\text{s}})^{1-\mu} (C_t - persH_t)^{\mu} \right)^{-\eta} = 0$$
(5.7)

$$-\lambda_{t}^{\text{CONSUMER}^{2}} - \beta \mu \text{pars} E_{t} \left[ \left( 1 - L_{t+1}^{\text{s}} \right)^{1-\mu} \left( C_{t+1} - \text{pars} H_{t+1} \right)^{-1+\mu} \left( \left( 1 - L_{t+1}^{\text{s}} \right)^{1-\mu} \left( C_{t+1} - \text{pars} H_{t+1} \right)^{\mu} \right)^{-\eta} \right] + \mu \left( 1 - L_{t}^{\text{s}} \right)^{1-\mu} \left( C_{t} - \text{pars} H_{t} \right)^{1-\mu} \left( C_{t} - \text{pars} H_{t} \right)^{\mu} \right)^{-\eta} = 0$$

$$(5.8)$$

$$-C_t - I_t + Y_t = 0 (5.9)$$

$$I_t - K_t^{s} + K_{t-1}^{s} (1 - \delta) = 0 (5.10)$$

$$U_t - \beta E_t \left[ U_{t+1} \right] - (1 - \eta)^{-1} \left( (1 - L_t^s)^{1-\mu} (C_t - prsH_t)^{\mu} \right)^{1-\eta} = 0$$
(5.11)

### 6 Steady state relationships (after reduction)

$$C_{\rm ss} - H_{\rm ss} = 0 \tag{6.1}$$

$$-\lambda_{\rm ss}^{\rm CONSUMER^2} + \beta \left(\lambda_{\rm ss}^{\rm CONSUMER^2} r_{\rm ss} + \lambda_{\rm ss}^{\rm CONSUMER^2} (1 - \delta)\right) = 0 \tag{6.2}$$

$$-r_{\rm ss} + \alpha Z_{\rm ss} K_{\rm ss}^{\rm s}^{-1+\alpha} L_{\rm ss}^{\rm s}^{1-\alpha} = 0 \tag{6.3}$$

$$-W_{\rm ss} + Z_{\rm ss} (1 - \alpha) K_{\rm ss}^{\rm s \alpha} L_{\rm ss}^{\rm s - \alpha} = 0$$
 (6.4)

$$-Y_{\rm ss} + Z_{\rm ss} K_{\rm ss}^{\rm s \alpha} L_{\rm ss}^{\rm s 1-\alpha} = 0 \tag{6.5}$$

$$Z_{\rm ss} - e^{\phi \log Z_{\rm ss}} = 0 \tag{6.6}$$

$$\lambda_{\rm ss}^{\rm CONSUMER^2} W_{\rm ss} + (-1 + \mu) \left(1 - L_{\rm ss}^{\rm s}\right)^{-\mu} \left(C_{\rm ss} - p s H_{\rm ss}\right)^{\mu} \left(\left(1 - L_{\rm ss}^{\rm s}\right)^{1 - \mu} \left(C_{\rm ss} - p s H_{\rm ss}\right)^{\mu}\right)^{-\eta} = 0 \tag{6.7}$$

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$$-\lambda_{\rm ss}^{\rm CONSUMER^2} + \mu (1 - L_{\rm ss}^{\rm s})^{1-\mu} (C_{\rm ss} - persH_{\rm ss})^{-1+\mu} \Big( (1 - L_{\rm ss}^{\rm s})^{1-\mu} (C_{\rm ss} - persH_{\rm ss})^{\mu} \Big)^{-\eta} - \beta \mu pers (1 - L_{\rm ss}^{\rm s})^{1-\mu} (C_{\rm ss} - persH_{\rm ss})^{-1+\mu} \Big( (1 - L_{\rm ss}^{\rm s})^{1-\mu} (C_{\rm ss} - persH_{\rm ss})^{\mu} \Big)^{-\eta} = 0$$

$$(6.8)$$

$$-C_{\rm ss} - I_{\rm ss} + Y_{\rm ss} = 0 ag{6.9}$$

$$I_{\rm ss} - K_{\rm ss}^{\rm s} + K_{\rm ss}^{\rm s} (1 - \delta) = 0$$
 (6.10)

$$U_{\rm ss} - \beta U_{\rm ss} - (1 - \eta)^{-1} \left( (1 - L_{\rm ss}^{\rm s})^{1 - \mu} (C_{\rm ss} - persH_{\rm ss})^{\mu} \right)^{1 - \eta} = 0$$
(6.11)

### 7 Calibrating equations

$$-0.36Y_{\rm ss} + r_{\rm ss}K_{\rm ss}^{\rm s} = 0 (7.1)$$

### 8 Parameter settings

$$\beta = 0.99 \tag{8.1}$$

$$\delta = 0.025 \tag{8.2}$$

$$\eta = 2 \tag{8.3}$$

$$\mu = 0.3 \tag{8.4}$$

$$pers = 0.57 \tag{8.5}$$

$$\phi = 0.95 \tag{8.6}$$

### 9 Steady-state values

	Steady-state values
$\lambda^{\text{CONSUMER}^2}$	0.7116
r	0.0351
C	0.7494
H	0.7494
I	0.2584
$K^{\mathrm{s}}$	10.3356
$L^{\mathrm{s}}$	0.2721
U	-175.4236
W	2.3706
Y	1.0078
Z	1

# 10 The solution of the perturbation

#### 10.1 P

$$\begin{array}{cccc} & C_{t-1} & K_{t-1}^{\mathrm{s}} & Z_{t-1} \\ C & 0.5544 & 0.0151 & 0.1764 \\ K^{\mathrm{s}} & -0.5092 & 0.9817 & 1.1759 \\ Z & 0 & 0 & 0.95 \\ \end{array}$$

#### 10.2 Q

$$\begin{array}{c}
\epsilon^{Z} \\
C \\
K^{s} \\
Z
\end{array}
\left(\begin{array}{c}
0.1857 \\
1.2377 \\
1
\end{array}\right)$$

#### 10.3 R

#### 10.4 S

$$\begin{array}{ccc} & \epsilon^{\rm Z} \\ \lambda^{\rm CONSUMER^2} & \begin{pmatrix} -0.3781 \\ 0.0496 \\ H & 0 \\ I & 1.2377 \\ L^{\rm s} & 0.1753 \\ U & 12.0524 \\ W & 1.8206 \\ Y & 1.4234 \\ \end{pmatrix}$$

# 11 Statistics of the model

### 11.1 Moments

	Steady-state value	Std. dev.	Variance	Loglinear
r	0.0351	0.0046	0	N
C	0.7494	0.0333	0.0011	N
H	0.7494	0.0333	0.0011	N
I	0.2584	0.1077	0.0116	N
$K^{\mathrm{s}}$	10.3356	0.3633	0.132	N
$L^{\mathrm{s}}$	0.2721	0.0164	0.0003	N
U	-175.4236	1.1325	1.2825	N
W	2.3706	0.1719	0.0295	N
Y	1.0078	0.1325	0.0175	N
Z	1	0.0922	0.0085	N

### 11.2 Correlation matrix

	r	C	Н	I	$K^{\mathrm{s}}$	$L^{\mathrm{s}}$	U	W	Y	Z
$\lambda^{\text{CONSUMER}^2}$	-0.8032	-0.9421	-0.7242	-0.8546	-0.7018	-0.861	-0.9737	-0.9722	-0.9318	-0.9048
r	1	0.6233	0.2627	0.9934	0.1395	0.9944	0.9178	0.9204	0.9645	0.9804
C	0.6233	1	0.9106	0.6739	0.826	0.7011	0.8666	0.8652	0.7994	0.7579
H	0.2627	0.9106	1	0.3154	0.8989	0.358	0.5836	0.5818	0.4854	0.4287
I	0.9934	0.6739	0.3154	1	0.2315	0.9968	0.9495	0.9511	0.9826	0.9925
$K^{\mathrm{s}}$	0.1395	0.826	0.8989	0.2315	1	0.2426	0.5211	0.5157	0.3959	0.3318
$L^{\mathrm{s}}$	0.9944	0.7011	0.358	0.9968	0.2426	1	0.9542	0.9562	0.9869	0.9956
U	0.9178	0.8666	0.5836	0.9495	0.5211	0.9542	1	1	0.99	0.978
W	0.9204	0.8652	0.5818	0.9511	0.5157	0.9562	1	1	0.9909	0.9793
Y	0.9645	0.7994	0.4854	0.9826	0.3959	0.9869	0.99	0.9909	1	0.9976
Z	0.9804	0.7579	0.4287	0.9925	0.3318	0.9956	0.978	0.9793	0.9976	1

### 11.3 Autocorrelations

	t-1	t-2	t-3	t-4
r	0.7068	0.4619	0.2614	0.1009
C	0.9106	0.7381	0.5368	0.3373
H	0.9106	0.7381	0.5368	0.3373
I	0.6672	0.4127	0.2174	0.0686
$K^{\mathrm{s}}$	0.9552	0.8509	0.7099	0.5498
$L^{\mathrm{s}}$	0.7157	0.4728	0.2708	0.1076
U	0.7373	0.5093	0.3157	0.1551
W	0.7395	0.5115	0.3169	0.1551
Y	0.7236	0.4858	0.2864	0.1237
Z	0.7133	0.4711	0.2711	0.1098

# 12 Statistics of the model

### 12.1 Moments relative to moments of the reference variable

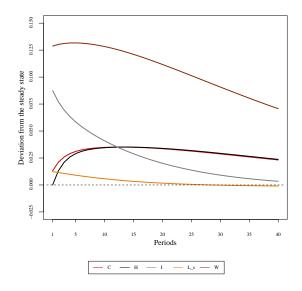
	Steady-state value relative to $Y$	Std. dev. relative to $Y$	Variance relative to $Y$	Loglinear
$\lambda^{ ext{CONSUMER}^2}$	0.7061	0.2894	0.0838	N
r	0.0348	0.0351	0.0012	N
C	0.7436	0.2514	0.0632	N
H	0.7436	0.2514	0.0632	N
I	0.2564	0.8132	0.6612	N
$K^{\mathrm{s}}$	10.2561	2.7424	7.521	N
$L^{\mathrm{s}}$	0.27	0.124	0.0154	N
U	-174.0741	8.5496	73.0965	N
W	2.3524	1.2977	1.6841	N
Y	1	1	1	N
Z	0.9923	0.6958	0.4842	N

### 12.2 Correlations with the reference variable

	$Y_{t-4}$	$Y_{t-3}$	$Y_{t-2}$	$Y_{t-1}$	$Y_t$	$Y_{t+1}$	$Y_{t+2}$	$Y_{t+3}$	$Y_{t+4}$
$\lambda^{ ext{CONSUMER}^2}$	0.0606	-0.1099	-0.3294	-0.6024	-0.9318	-0.7777	-0.6273	-0.4851	-0.3544
r	0.2446	0.3879	0.5562	0.7491	0.9645	0.6134	0.3309	0.1092	-0.0591
C	-0.1308	0.0247	0.2285	0.4854	0.7994	0.8668	0.8036	0.6775	0.5273
H	-0.2439	-0.1308	0.0247	0.2285	0.4854	0.7994	0.8668	0.8036	0.6775
I	0.1926	0.3445	0.5267	0.7398	0.9826	0.6219	0.3489	0.1427	-0.0109
$K^{\mathrm{s}}$	-0.39	-0.2781	-0.115	0.1073	0.3959	0.5704	0.6596	0.6854	0.6651
$L^{\mathrm{s}}$	0.2003	0.3524	0.5342	0.7461	0.9869	0.668	0.4016	0.1854	0.0157
U	0.0534	0.2219	0.4325	0.6881	0.99	0.7536	0.5453	0.3656	0.2138
W	0.0575	0.2257	0.4357	0.6904	0.9909	0.7554	0.5461	0.3647	0.2112
Y	0.1237	0.2864	0.4858	0.7236	1	0.7236	0.4858	0.2864	0.1237
Z	0.1554	0.3142	0.507	0.7349	0.9976	0.6975	0.4461	0.2401	0.0758

# 13 Impulse response functions

# 13.1 Shock $\epsilon^{\mathrm{Z}}$



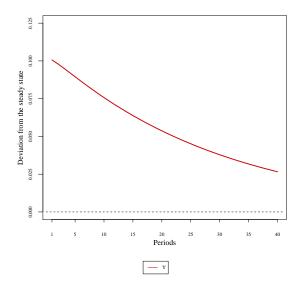


Figure 1: Impulse response function for  $\epsilon^{\mathbf{Z}}$  shock

Figure 2: Impulse response function for  $\epsilon^{\mathbf{Z}}$  shock