

Index sets

$$HH = \{1, 2\}$$

$$SEC = \{A, B, C\}$$

1 CONSUMER $h \in HH$

1.1 Optimisation problem

$$\max_{(D^{\langle s, h \rangle})_{s \in SEC}} U^{\langle h \rangle} = \left(\sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} \quad (1.1)$$

s.t. :

$$INC^{\langle h \rangle} + \Pi^{\langle h \rangle} = \sum_{s \in SEC} p^{\langle s \rangle} D^{\langle s, h \rangle} \quad \left(\lambda^{\text{CONSUMER}^1 \langle h \rangle} \right) \quad (1.2)$$

1.2 Identities

$$INC^{\langle h \rangle} = L^{\langle h \rangle} + p^k K^{\langle h \rangle} \quad (1.3)$$

$$K^{\langle h \rangle} = k s^{\text{data} \langle h \rangle} \quad (1.4)$$

$$L^{\langle h \rangle} = l s^{\text{data} \langle h \rangle} \quad (1.5)$$

1.3 First order conditions

$$s \in SEC: \quad \lambda^{\text{CONSUMER}^1 \langle h \rangle}_t p_t^{\langle s \rangle} + \alpha^{\langle s, h \rangle} D_t^{\langle s, h \rangle -1+\omega^{-1}(-1+\omega)} \left(\sum_{s \in SEC} \alpha^{\langle s, h \rangle} D_t^{\langle s, h \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad \left(D_t^{\langle s, h \rangle} \right) \quad (1.6)$$

2 FIRM $s \in SEC$

2.1 Optimisation problem

$$\max_{Y^{(s)}, K^{(s)}, L^{(s)}, Y^{VA(s)}, Y^{INT(s)}} \pi^{(s)} = -L^{(s)} - p^k K^{(s)} + p^{(s)} Y^{(s)} - \sum_{\bar{s} \in SEC} \beta^{x(\bar{s}, s)^{-1}} p^{(\bar{s})} Y^{INT(\bar{s})} \quad (2.1)$$

s.t. :

$$Y^{(s)} = Y^{VA(s)} \left(\lambda^{FIRM^1(s)} \right) \quad (2.2)$$

$$Y^{(s)} = Y^{INT(s)} \left(\lambda^{FIRM^2(s)} \right) \quad (2.3)$$

$$Y^{VA(s)} = \gamma^{yva(s)} K^{(s)\beta^k(s)} L^{(s)\beta^l(s)} \left(\lambda^{FIRM^3(s)} \right) \quad (2.4)$$

2.2 Identities

$$\bar{s} \in SEC: \quad X_t^{(\bar{s}, s)} = \beta^{x(\bar{s}, s)^{-1}} Y^{INT_t(\bar{s})} \quad (2.5)$$

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2.3 First order conditions

$$-\lambda^{FIRM^1(s)} - \lambda^{FIRM^2(s)} + p^{(s)} = 0 \quad \left(Y^{(s)} \right) \quad (2.6)$$

$$-p^k + \beta^k(s) \gamma^{yva(s)} \lambda^{FIRM^3(s)} K^{(s)-1+\beta^k(s)} L^{(s)\beta^l(s)} = 0 \quad \left(K^{(s)} \right) \quad (2.7)$$

$$-1 + \beta^l(s) \gamma^{yva(s)} \lambda^{FIRM^3(s)} K^{(s)\beta^k(s)} L^{(s)-1+\beta^l(s)} = 0 \quad \left(L^{(s)} \right) \quad (2.8)$$

$$\lambda^{FIRM^1(s)} - \lambda^{FIRM^3(s)} = 0 \quad \left(Y^{VA(s)} \right) \quad (2.9)$$

$$\lambda^{FIRM^2(s)} - \sum_{\bar{s} \in SEC} \beta^{x(\bar{s}, s)^{-1}} p^{(\bar{s})} = 0 \quad \left(Y^{INT(s)} \right) \quad (2.10)$$

2.4 First order conditions after reduction

$$-p^k + \beta^{k\langle s \rangle} \gamma^{yva\langle s \rangle} \left(p^{\langle s \rangle} - \sum_{\vec{s} \in SEC} \beta^{x\langle \vec{s}, s \rangle - 1} p^{\langle \vec{s} \rangle} \right) K^{\langle s \rangle - 1 + \beta^{k\langle s \rangle}} L^{\langle s \rangle \beta^{1\langle s \rangle}} = 0 \quad (K^{\langle s \rangle}) \quad (2.11)$$

$$-1 + \beta^{1\langle s \rangle} \gamma^{yva\langle s \rangle} \left(p^{\langle s \rangle} - \sum_{\vec{s} \in SEC} \beta^{x\langle \vec{s}, s \rangle - 1} p^{\langle \vec{s} \rangle} \right) K^{\langle s \rangle \beta^{k\langle s \rangle}} L^{\langle s \rangle - 1 + \beta^{1\langle s \rangle}} = 0 \quad (L^{\langle s \rangle}) \quad (2.12)$$

3 EQUILIBRIUM

3.1 Identities

$$\sum_{h \in HH} K^{\langle h \rangle} = \sum_{s \in SEC} K^{\langle s \rangle} \quad (3.1)$$

$$s \in SEC: \quad p_t^{\langle s \rangle} = 1 \quad (3.2)$$

$$h \in HH: \quad \Pi_t^{\langle h \rangle} = \sum_{s \in SEC} \pi^{h\langle h \rangle} \pi_t^{\langle s \rangle} \quad (3.3)$$

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4 Equilibrium relationships (before expansion and reduction)

$$\sum_{h \in HH} K^{\langle h \rangle} - \sum_{s \in SEC} K^{\langle s \rangle} = 0 \quad (4.1)$$

$$h \in HH: \quad -ks^{\text{data}\langle h \rangle} + K^{\langle h \rangle} = 0 \quad (4.2)$$

$$h \in HH: \quad -ls^{\text{data}\langle h \rangle} + L^{\langle h \rangle} = 0 \quad (4.3)$$

$$h \in HH: \quad \Pi^{\langle h \rangle} - \sum_{s \in SEC} \pi^{h\langle h \rangle} \pi^{\langle s \rangle} = 0 \quad (4.4)$$

$$h \in HH: \quad U^{\langle h \rangle} - \left(\sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (4.5)$$

$$h \in HH: \quad -INC^{\langle h \rangle} - \Pi^{\langle h \rangle} + \sum_{s \in SEC} p^{\langle s \rangle} D^{\langle s, h \rangle} = 0 \quad (4.6)$$

$$h \in HH: \quad INC^{\langle h \rangle} - L^{\langle h \rangle} - p^k K^{\langle h \rangle} = 0 \quad (4.7)$$

$$h \in HH: \quad s \in SEC: \quad \lambda^{\text{CONSUMER}^1 \langle h \rangle} p^{\langle s \rangle} + \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle - 1 + \omega^{-1}(-1 + \omega)} \left(\sum_{s \in SEC} \alpha^{\langle s, h \rangle} D^{\langle s, h \rangle \omega^{-1}(-1 + \omega)} \right)^{-1 + \omega(-1 + \omega)^{-1}} = 0 \quad (4.8)$$

$$s \in SEC: \quad -1 + p^{\langle s \rangle} = 0 \quad (4.9)$$

$$s \in SEC: \quad -1 + \beta^{\text{l} \langle s \rangle} \gamma^{\text{yva} \langle s \rangle} \left(p^{\langle s \rangle} - \sum_{\mathbf{s}i \in SEC} \beta^{\text{x} \langle \mathbf{s}i, s \rangle - 1} p^{\langle \mathbf{s}i \rangle} \right) K^{\langle s \rangle \beta^{\text{k} \langle s \rangle}} L^{\langle s \rangle - 1 + \beta^{\text{l} \langle s \rangle}} = 0 \quad (4.10)$$

$$s \in SEC: \quad -p^{\text{k}} + \beta^{\text{k} \langle s \rangle} \gamma^{\text{yva} \langle s \rangle} \left(p^{\langle s \rangle} - \sum_{\mathbf{s}i \in SEC} \beta^{\text{x} \langle \mathbf{s}i, s \rangle - 1} p^{\langle \mathbf{s}i \rangle} \right) K^{\langle s \rangle - 1 + \beta^{\text{k} \langle s \rangle}} L^{\langle s \rangle \beta^{\text{l} \langle s \rangle}} = 0 \quad (4.11)$$

$$s \in SEC: \quad -Y^{\langle s \rangle} + Y^{\text{VA} \langle s \rangle} = 0 \quad (4.12)$$

$$s \in SEC: \quad -Y^{\langle s \rangle} + Y^{\text{INT} \langle s \rangle} = 0 \quad (4.13)$$

$$s \in SEC: \quad -Y^{\text{VA} \langle s \rangle} + \gamma^{\text{yva} \langle s \rangle} K^{\langle s \rangle \beta^{\text{k} \langle s \rangle}} L^{\langle s \rangle \beta^{\text{l} \langle s \rangle}} = 0 \quad (4.14)$$

$$s \in SEC: \quad \pi^{\langle s \rangle} + L^{\langle s \rangle} + p^{\text{k}} K^{\langle s \rangle} - p^{\langle s \rangle} Y^{\langle s \rangle} + \sum_{\mathbf{s}i \in SEC} \beta^{\text{x} \langle \mathbf{s}i, s \rangle - 1} p^{\langle \mathbf{s}i \rangle} Y^{\text{INT} \langle s \rangle} = 0 \quad (4.15)$$

$$s \in SEC: \quad \mathbf{s}i \in SEC: \quad X^{\langle \mathbf{s}i, s \rangle} - \beta^{\text{x} \langle \mathbf{s}i, s \rangle - 1} Y^{\text{INT} \langle s \rangle} = 0 \quad (4.16)$$

5 Equilibrium relationships (after expansion and reduction)

$$-1 + p^{\langle \text{A} \rangle} = 0 \quad (5.1)$$

$$-1 + p^{\langle \text{B} \rangle} = 0 \quad (5.2)$$

$$-1 + p^{\langle \text{C} \rangle} = 0 \quad (5.3)$$

$$-1 + \beta^{\text{l} \langle \text{A} \rangle} \gamma^{\text{yva} \langle \text{A} \rangle} \left(p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{A}, \text{A} \rangle - 1} p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{B}, \text{A} \rangle - 1} p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{C}, \text{A} \rangle - 1} p^{\langle \text{C} \rangle} \right) K^{\langle \text{A} \rangle \beta^{\text{k} \langle \text{A} \rangle}} L^{\langle \text{A} \rangle - 1 + \beta^{\text{l} \langle \text{A} \rangle}} = 0 \quad (5.4)$$

$$-1 + \beta^{\text{l} \langle \text{B} \rangle} \gamma^{\text{yva} \langle \text{B} \rangle} \left(p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{A}, \text{B} \rangle - 1} p^{\langle \text{A} \rangle} - \beta^{\text{x} \langle \text{B}, \text{B} \rangle - 1} p^{\langle \text{B} \rangle} - \beta^{\text{x} \langle \text{C}, \text{B} \rangle - 1} p^{\langle \text{C} \rangle} \right) K^{\langle \text{B} \rangle \beta^{\text{k} \langle \text{B} \rangle}} L^{\langle \text{B} \rangle - 1 + \beta^{\text{l} \langle \text{B} \rangle}} = 0 \quad (5.5)$$

$$-1 + \beta^{l\langle C \rangle} \gamma^{\text{yva}\langle C \rangle} \left(p^{\langle C \rangle} - \beta^{x\langle A, C \rangle} p^{\langle A \rangle} - \beta^{x\langle B, C \rangle} p^{\langle B \rangle} - \beta^{x\langle C, C \rangle} p^{\langle C \rangle} \right) K^{\langle C \rangle \beta^{k\langle C \rangle}} L^{\langle C \rangle -1 + \beta^{l\langle C \rangle}} = 0 \quad (5.6)$$

$$-k s^{\text{data}\langle 1 \rangle} + K^{\langle 1 \rangle} = 0 \quad (5.7)$$

$$-k s^{\text{data}\langle 2 \rangle} + K^{\langle 2 \rangle} = 0 \quad (5.8)$$

$$-l s^{\text{data}\langle 1 \rangle} + L^{\langle 1 \rangle} = 0 \quad (5.9)$$

$$-l s^{\text{data}\langle 2 \rangle} + L^{\langle 2 \rangle} = 0 \quad (5.10)$$

$$-p^k + \beta^{k\langle A \rangle} \gamma^{\text{yva}\langle A \rangle} \left(p^{\langle A \rangle} - \beta^{x\langle A, A \rangle} p^{\langle A \rangle} - \beta^{x\langle B, A \rangle} p^{\langle B \rangle} - \beta^{x\langle C, A \rangle} p^{\langle C \rangle} \right) K^{\langle A \rangle -1 + \beta^{k\langle A \rangle}} L^{\langle A \rangle \beta^{l\langle A \rangle}} = 0 \quad (5.11)$$

$$-p^k + \beta^{k\langle B \rangle} \gamma^{\text{yva}\langle B \rangle} \left(p^{\langle B \rangle} - \beta^{x\langle A, B \rangle} p^{\langle A \rangle} - \beta^{x\langle B, B \rangle} p^{\langle B \rangle} - \beta^{x\langle C, B \rangle} p^{\langle C \rangle} \right) K^{\langle B \rangle -1 + \beta^{k\langle B \rangle}} L^{\langle B \rangle \beta^{l\langle B \rangle}} = 0 \quad (5.12)$$

$$-p^k + \beta^{k\langle C \rangle} \gamma^{\text{yva}\langle C \rangle} \left(p^{\langle C \rangle} - \beta^{x\langle A, C \rangle} p^{\langle A \rangle} - \beta^{x\langle B, C \rangle} p^{\langle B \rangle} - \beta^{x\langle C, C \rangle} p^{\langle C \rangle} \right) K^{\langle C \rangle -1 + \beta^{k\langle C \rangle}} L^{\langle C \rangle \beta^{l\langle C \rangle}} = 0 \quad (5.13)$$

$$U^{\langle 1 \rangle} - \left(\alpha^{\langle A, 1 \rangle} D^{\langle A, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B, 1 \rangle} D^{\langle B, 1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C, 1 \rangle} D^{\langle C, 1 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.14)$$

$$U^{\langle 2 \rangle} - \left(\alpha^{\langle A, 2 \rangle} D^{\langle A, 2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B, 2 \rangle} D^{\langle B, 2 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C, 2 \rangle} D^{\langle C, 2 \rangle \omega^{-1}(-1+\omega)} \right)^{\omega(-1+\omega)^{-1}} = 0 \quad (5.15)$$

$$X^{\langle A, A \rangle} - \beta^{x\langle A, A \rangle} Y^{\text{INT}\langle A \rangle} = 0 \quad (5.16)$$

$$X^{\langle A, B \rangle} - \beta^{x\langle A, B \rangle} Y^{\text{INT}\langle B \rangle} = 0 \quad (5.17)$$

$$X^{\langle A, C \rangle} - \beta^{x\langle A, C \rangle} Y^{\text{INT}\langle C \rangle} = 0 \quad (5.18)$$

$$X^{\langle B, A \rangle} - \beta^{x\langle B, A \rangle} Y^{\text{INT}\langle A \rangle} = 0 \quad (5.19)$$

$$X^{\langle B, B \rangle} - \beta^{x\langle B, B \rangle} Y^{\text{INT}\langle B \rangle} = 0 \quad (5.20)$$

$$X^{\langle B,C \rangle} - \beta^x \langle B,C \rangle^{-1} Y^{\text{INT} \langle C \rangle} = 0 \quad (5.21)$$

$$X^{\langle C,A \rangle} - \beta^x \langle C,A \rangle^{-1} Y^{\text{INT} \langle A \rangle} = 0 \quad (5.22)$$

$$X^{\langle C,B \rangle} - \beta^x \langle C,B \rangle^{-1} Y^{\text{INT} \langle B \rangle} = 0 \quad (5.23)$$

$$X^{\langle C,C \rangle} - \beta^x \langle C,C \rangle^{-1} Y^{\text{INT} \langle C \rangle} = 0 \quad (5.24)$$

$$-Y^{\langle A \rangle} + Y^{\text{VA} \langle A \rangle} = 0 \quad (5.25)$$

$$-Y^{\langle A \rangle} + Y^{\text{INT} \langle A \rangle} = 0 \quad (5.26)$$

$$-Y^{\langle B \rangle} + Y^{\text{VA} \langle B \rangle} = 0 \quad (5.27)$$

$$-Y^{\langle B \rangle} + Y^{\text{INT} \langle B \rangle} = 0 \quad (5.28)$$

$$-Y^{\langle C \rangle} + Y^{\text{VA} \langle C \rangle} = 0 \quad (5.29)$$

$$-Y^{\langle C \rangle} + Y^{\text{INT} \langle C \rangle} = 0 \quad (5.30)$$

$$-Y^{\text{VA} \langle A \rangle} + \gamma^{\text{yva} \langle A \rangle} K^{\langle A \rangle \beta^k \langle A \rangle} L^{\langle A \rangle \beta^1 \langle A \rangle} = 0 \quad (5.31)$$

$$-Y^{\text{VA} \langle B \rangle} + \gamma^{\text{yva} \langle B \rangle} K^{\langle B \rangle \beta^k \langle B \rangle} L^{\langle B \rangle \beta^1 \langle B \rangle} = 0 \quad (5.32)$$

$$-Y^{\text{VA} \langle C \rangle} + \gamma^{\text{yva} \langle C \rangle} K^{\langle C \rangle \beta^k \langle C \rangle} L^{\langle C \rangle \beta^1 \langle C \rangle} = 0 \quad (5.33)$$

$$\lambda^{\text{CONSUMER}^1 \langle 1 \rangle} p^{\langle A \rangle} + \alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle -1+\omega^{-1}(-1+\omega)} \left(\alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,1 \rangle} D^{\langle C,1 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.34)$$

$$\lambda^{\text{CONSUMER}^1 \langle 1 \rangle} p^{\langle B \rangle} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle -1+\omega^{-1}(-1+\omega)} \left(\alpha^{\langle A,1 \rangle} D^{\langle A,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle B,1 \rangle} D^{\langle B,1 \rangle \omega^{-1}(-1+\omega)} + \alpha^{\langle C,1 \rangle} D^{\langle C,1 \rangle \omega^{-1}(-1+\omega)} \right)^{-1+\omega(-1+\omega)^{-1}} = 0 \quad (5.35)$$

$$\lambda^{\text{CONSUMER}^1 \langle 1 \rangle} p^{\langle C \rangle} + \alpha^{\langle C, 1 \rangle} D^{\langle C, 1 \rangle - 1 + \omega^{-1}(-1 + \omega)} \left(\alpha^{\langle A, 1 \rangle} D^{\langle A, 1 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle B, 1 \rangle} D^{\langle B, 1 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle C, 1 \rangle} D^{\langle C, 1 \rangle \omega^{-1}(-1 + \omega)} \right)^{-1 + \omega(-1 + \omega)^{-1}} = 0 \quad (5.36)$$

$$\lambda^{\text{CONSUMER}^1 \langle 2 \rangle} p^{\langle A \rangle} + \alpha^{\langle A, 2 \rangle} D^{\langle A, 2 \rangle - 1 + \omega^{-1}(-1 + \omega)} \left(\alpha^{\langle A, 2 \rangle} D^{\langle A, 2 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle B, 2 \rangle} D^{\langle B, 2 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle C, 2 \rangle} D^{\langle C, 2 \rangle \omega^{-1}(-1 + \omega)} \right)^{-1 + \omega(-1 + \omega)^{-1}} = 0 \quad (5.37)$$

$$\lambda^{\text{CONSUMER}^1 \langle 2 \rangle} p^{\langle B \rangle} + \alpha^{\langle B, 2 \rangle} D^{\langle B, 2 \rangle - 1 + \omega^{-1}(-1 + \omega)} \left(\alpha^{\langle A, 2 \rangle} D^{\langle A, 2 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle B, 2 \rangle} D^{\langle B, 2 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle C, 2 \rangle} D^{\langle C, 2 \rangle \omega^{-1}(-1 + \omega)} \right)^{-1 + \omega(-1 + \omega)^{-1}} = 0 \quad (5.38)$$

$$\lambda^{\text{CONSUMER}^1 \langle 2 \rangle} p^{\langle C \rangle} + \alpha^{\langle C, 2 \rangle} D^{\langle C, 2 \rangle - 1 + \omega^{-1}(-1 + \omega)} \left(\alpha^{\langle A, 2 \rangle} D^{\langle A, 2 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle B, 2 \rangle} D^{\langle B, 2 \rangle \omega^{-1}(-1 + \omega)} + \alpha^{\langle C, 2 \rangle} D^{\langle C, 2 \rangle \omega^{-1}(-1 + \omega)} \right)^{-1 + \omega(-1 + \omega)^{-1}} = 0 \quad (5.39)$$

$$INC^{\langle 1 \rangle} - L^{\langle 1 \rangle} - p^k K^{\langle 1 \rangle} = 0 \quad (5.40)$$

$$INC^{\langle 2 \rangle} - L^{\langle 2 \rangle} - p^k K^{\langle 2 \rangle} = 0 \quad (5.41)$$

$$\Pi^{\langle 1 \rangle} - \pi^{\text{h} \langle 1 \rangle} \pi^{\langle A \rangle} - \pi^{\text{h} \langle 1 \rangle} \pi^{\langle B \rangle} - \pi^{\text{h} \langle 1 \rangle} \pi^{\langle C \rangle} = 0 \quad (5.42)$$

$$\Pi^{\langle 2 \rangle} - \pi^{\text{h} \langle 2 \rangle} \pi^{\langle A \rangle} - \pi^{\text{h} \langle 2 \rangle} \pi^{\langle B \rangle} - \pi^{\text{h} \langle 2 \rangle} \pi^{\langle C \rangle} = 0 \quad (5.43)$$

$$-INC^{\langle 1 \rangle} - \Pi^{\langle 1 \rangle} + p^{\langle A \rangle} D^{\langle A, 1 \rangle} + p^{\langle B \rangle} D^{\langle B, 1 \rangle} + p^{\langle C \rangle} D^{\langle C, 1 \rangle} = 0 \quad (5.44)$$

$$-INC^{\langle 2 \rangle} - \Pi^{\langle 2 \rangle} + p^{\langle A \rangle} D^{\langle A, 2 \rangle} + p^{\langle B \rangle} D^{\langle B, 2 \rangle} + p^{\langle C \rangle} D^{\langle C, 2 \rangle} = 0 \quad (5.45)$$

$$K^{\langle 1 \rangle} + K^{\langle 2 \rangle} - K^{\langle A \rangle} - K^{\langle B \rangle} - K^{\langle C \rangle} = 0 \quad (5.46)$$

$$\pi^{\langle A \rangle} + L^{\langle A \rangle} + p^k K^{\langle A \rangle} - p^{\langle A \rangle} Y^{\langle A \rangle} + \beta^{\text{x} \langle A, A \rangle - 1} p^{\langle A \rangle} Y^{\text{INT} \langle A \rangle} + \beta^{\text{x} \langle B, A \rangle - 1} p^{\langle B \rangle} Y^{\text{INT} \langle A \rangle} + \beta^{\text{x} \langle C, A \rangle - 1} p^{\langle C \rangle} Y^{\text{INT} \langle A \rangle} = 0 \quad (5.47)$$

$$\pi^{\langle B \rangle} + L^{\langle B \rangle} + p^k K^{\langle B \rangle} - p^{\langle B \rangle} Y^{\langle B \rangle} + \beta^{\text{x} \langle A, B \rangle - 1} p^{\langle A \rangle} Y^{\text{INT} \langle B \rangle} + \beta^{\text{x} \langle B, B \rangle - 1} p^{\langle B \rangle} Y^{\text{INT} \langle B \rangle} + \beta^{\text{x} \langle C, B \rangle - 1} p^{\langle C \rangle} Y^{\text{INT} \langle B \rangle} = 0 \quad (5.48)$$

$$\pi^{\langle C \rangle} + L^{\langle C \rangle} + p^k K^{\langle C \rangle} - p^{\langle C \rangle} Y^{\langle C \rangle} + \beta^{\text{x} \langle A, C \rangle - 1} p^{\langle A \rangle} Y^{\text{INT} \langle C \rangle} + \beta^{\text{x} \langle B, C \rangle - 1} p^{\langle B \rangle} Y^{\text{INT} \langle C \rangle} + \beta^{\text{x} \langle C, C \rangle - 1} p^{\langle C \rangle} Y^{\text{INT} \langle C \rangle} = 0 \quad (5.49)$$

6 Calibrating equations

$$-d^{\text{data}\langle\text{B},1\rangle} + D^{\langle\text{B},1\rangle} = 0 \quad (6.1)$$

$$-d^{\text{data}\langle\text{B},2\rangle} + D^{\langle\text{B},2\rangle} = 0 \quad (6.2)$$

$$-d^{\text{data}\langle\text{C},1\rangle} + D^{\langle\text{C},1\rangle} = 0 \quad (6.3)$$

$$-d^{\text{data}\langle\text{C},2\rangle} + D^{\langle\text{C},2\rangle} = 0 \quad (6.4)$$

$$-l^{\text{data}\langle\text{A}\rangle} + L^{\langle\text{A}\rangle} = 0 \quad (6.5)$$

$$-l^{\text{data}\langle\text{B}\rangle} + L^{\langle\text{B}\rangle} = 0 \quad (6.6)$$

$$-l^{\text{data}\langle\text{C}\rangle} + L^{\langle\text{C}\rangle} = 0 \quad (6.7)$$

$$-x^{\text{data}\langle\text{A},\text{A}\rangle} + X^{\langle\text{A},\text{A}\rangle} = 0 \quad (6.8)$$

$$-x^{\text{data}\langle\text{A},\text{B}\rangle} + X^{\langle\text{A},\text{B}\rangle} = 0 \quad (6.9)$$

$$-x^{\text{data}\langle\text{A},\text{C}\rangle} + X^{\langle\text{A},\text{C}\rangle} = 0 \quad (6.10)$$

$$-x^{\text{data}\langle\text{B},\text{A}\rangle} + X^{\langle\text{B},\text{A}\rangle} = 0 \quad (6.11)$$

$$-x^{\text{data}\langle\text{B},\text{B}\rangle} + X^{\langle\text{B},\text{B}\rangle} = 0 \quad (6.12)$$

$$-x^{\text{data}\langle\text{B},\text{C}\rangle} + X^{\langle\text{B},\text{C}\rangle} = 0 \quad (6.13)$$

$$-x^{\text{data}\langle\text{C},\text{A}\rangle} + X^{\langle\text{C},\text{A}\rangle} = 0 \quad (6.14)$$

$$-x^{\text{data}\langle\text{C},\text{B}\rangle} + X^{\langle\text{C},\text{B}\rangle} = 0 \quad (6.15)$$

$$-x^{\text{data}\langle\text{C},\text{C}\rangle} + X^{\langle\text{C},\text{C}\rangle} = 0 \quad (6.16)$$

$$-y^{\text{data}\langle A \rangle} + Y^{\text{VA}\langle A \rangle} = 0 \quad (6.17)$$

$$-y^{\text{data}\langle B \rangle} + Y^{\text{VA}\langle B \rangle} = 0 \quad (6.18)$$

$$-y^{\text{data}\langle C \rangle} + Y^{\text{VA}\langle C \rangle} = 0 \quad (6.19)$$

$$-1 + \beta^{\text{k}\langle A \rangle} + \beta^{\text{l}\langle A \rangle} = 0 \quad (6.20)$$

$$-1 + \beta^{\text{k}\langle B \rangle} + \beta^{\text{l}\langle B \rangle} = 0 \quad (6.21)$$

$$-1 + \beta^{\text{k}\langle C \rangle} + \beta^{\text{l}\langle C \rangle} = 0 \quad (6.22)$$

$$-1 + \pi^{\text{h}\langle 1 \rangle} + \pi^{\text{h}\langle 2 \rangle} = 0 \quad (6.23)$$

$$-1 + \alpha^{\langle A,1 \rangle \omega} + \alpha^{\langle B,1 \rangle \omega} + \alpha^{\langle C,1 \rangle \omega} = 0 \quad (6.24)$$

$$-1 + \alpha^{\langle A,2 \rangle \omega} + \alpha^{\langle B,2 \rangle \omega} + \alpha^{\langle C,2 \rangle \omega} = 0 \quad (6.25)$$

7 Equilibrium values

	Equilibrium values
p^k	1
$\lambda^{\text{CONSUMER}^1}$	-1
$\lambda^{\text{CONSUMER}^2}$	-1
p^A	1
p^B	1
p^C	1
π^A	0
π^B	0
π^C	0
D^{A^1}	52.94
D^{A^2}	64.45
D^{B^1}	11.7
D^{B^2}	30.79
D^{C^1}	18.6
D^{C^2}	43.6
INC^1	83.24
INC^2	138.84
K^1	65.07
K^2	68.77
K^A	38.1
K^B	35.01
K^C	60.73
L^1	18.17
L^2	70.07
L^A	9.44
L^B	31.6
L^C	47.2
Π^1	0
Π^2	0
U^1	83.24
U^2	138.84
X^{A^A}	68.4
X^{A^B}	131.01
X^{A^C}	28.28
X^{B^A}	111.91
X^{B^B}	92.3
X^{B^C}	86.92
X^{C^A}	117.23
X^{C^B}	43.7
X^{C^C}	111.65
Y^A	345.08
Y^B	333.62
Y^C	334.78
Y^{VA^A}	345.08
Y^{VA^B}	333.62
Y^{VA^C}	334.78
Y^{INT^A}	345.08
Y^{INT^B}	333.62
Y^{INT^C}	334.78

8 Parameters of the model

	Parameters
ω	2
α^{A^1}	0.7975
α^{A^2}	0.6813
α^{B^1}	0.3749
α^{B^2}	0.4709
α^{C^1}	0.4727
α^{C^2}	0.5604
β^{k^A}	0.8014
β^{k^B}	0.5256
β^{k^C}	0.5627
β^{l^A}	0.1986
β^{l^B}	0.4744
β^{l^C}	0.4373
$\beta^{x^{AA}}$	5.045
$\beta^{x^{AB}}$	2.5465
$\beta^{x^{AC}}$	11.838
$\beta^{x^{BA}}$	3.0835
$\beta^{x^{BB}}$	3.6145
$\beta^{x^{BC}}$	3.8516
$\beta^{x^{CA}}$	2.9436
$\beta^{x^{CB}}$	7.6343
$\beta^{x^{CC}}$	2.9985
$d^{\text{data}^{B^1}}$	11.7
$d^{\text{data}^{B^2}}$	30.79
$d^{\text{data}^{C^1}}$	18.6
$d^{\text{data}^{C^2}}$	43.6
γ^{yva^A}	11.9486
γ^{yva^B}	10.004
γ^{yva^C}	6.155
ks^{data^1}	65.07
ks^{data^2}	68.77
l^{data^A}	9.44
l^{data^B}	31.6
l^{data^C}	47.2
ls^{data^1}	18.17
ls^{data^2}	70.07
π^{h^1}	0.5
π^{h^2}	0.5
$x^{\text{data}^{AA}}$	68.4
$x^{\text{data}^{AB}}$	131.01
$x^{\text{data}^{AC}}$	28.28
$x^{\text{data}^{BA}}$	111.91
$x^{\text{data}^{BB}}$	92.3
$x^{\text{data}^{BC}}$	86.92
$x^{\text{data}^{CA}}$	117.23
$x^{\text{data}^{CB}}$	43.7
$x^{\text{data}^{CC}}$	111.65
y^{data^A}	345.08
y^{data^B}	333.62
y^{data^C}	334.78