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1 CONSUMER

1.1 Optimisation problem

$$\max_{C_t, L_t^s} U_t = \beta E_t \left[U_{t+1} \right] + (1 - \eta)^{-1} \left(C_t^{\ \mu} (1 - L_t^s)^{1 - \mu} \right)^{1 - \eta} \tag{1.1}$$

s.t.:

$$C_t = \pi_t + L_t^{\mathrm{s}} W_t \quad (\lambda_t^{\mathrm{c}}) \tag{1.2}$$

1.2 First order conditions

$$\beta - \lambda_t^{\mathcal{U}} = 0 \quad (U_t) \tag{1.3}$$

$$-\lambda_t^c + \mu C_t^{-1+\mu} (1 - L_t^s)^{1-\mu} \left(C_t^{\mu} (1 - L_t^s)^{1-\mu} \right)^{-\eta} = 0 \quad (C_t)$$
 (1.4)

$$\lambda_t^{c} W_t + (-1 + \mu) C_t^{\mu} (1 - L_t^{s})^{-\mu} \left(C_t^{\mu} (1 - L_t^{s})^{1 - \mu} \right)^{-\eta} = 0 \quad (L_t^{s})$$
(1.5)

2 FIRM

2.1 Optimisation problem

$$\max_{K_t, L_t^{\rm d}, Y_t, I_t, \pi_t, CapUt_t} \Pi_t = \pi_t + \lambda_t^{\rm c-1} E_t \left[\lambda_{t+1}^{\rm c} \lambda_{t+1}^{\rm U} \Pi_{t+1} \right]$$
(2.1)

s.t.:

$$Y_t = L_t^{\mathrm{d}^{1-\alpha}} Z_t^{1-\alpha} (K_{t-1} C q U t_t)^{\alpha} \quad \left(\lambda_t^{\mathrm{FIRM}^1}\right)$$

$$(2.2)$$

$$K_{t} = I_{t} + K_{t-1} \left(1 - \delta CqU t_{t}^{\omega} \right) \quad \left(\lambda_{t}^{\text{FIRM}^{2}} \right)$$

$$(2.3)$$

$$\pi_t = -I_t - L_t^{\mathrm{d}} W_t + P_t Y_t \quad \left(\lambda_t^{\mathrm{FIRM}^3}\right) \tag{2.4}$$

2.2 First order conditions

$$-\lambda_t^{\text{FIRM}^{\Pi}} + \lambda_{t-1}^{\text{c}}^{-1} \lambda_t^{\text{c}} \lambda_t^{\text{U}} = 0 \quad (\Pi_t)$$
(2.5)

$$-\lambda_{t}^{\text{FIRM}^{2}} + \text{E}_{t} \left[\lambda_{t+1}^{\text{FIRM}^{\Pi}} \left(\lambda_{t+1}^{\text{FIRM}^{2}} \left(1 - \delta C q U t_{t+1}^{\omega} \right) + \alpha \lambda_{t+1}^{\text{FIRM}^{1}} C q U t_{t+1} L_{t+1}^{\text{d}}^{1-\alpha} Z_{t+1}^{1-\alpha} \left(K_{t} C q U t_{t+1} \right)^{-1+\alpha} \right) \right] = 0 \quad (K_{t})$$
(2.6)

$$-\lambda_t^{\text{FIRM}^3} W_t + \lambda_t^{\text{FIRM}^1} (1 - \alpha) L_t^{\text{d}^{-\alpha}} Z_t^{1-\alpha} (K_{t-1} C q U t_t)^{\alpha} = 0 \quad (L_t^{\text{d}})$$

$$(2.7)$$

$$-\lambda_t^{\text{FIRM}^1} + \lambda_t^{\text{FIRM}^3} P_t = 0 \quad (Y_t)$$
 (2.8)

$$\lambda_t^{\text{FIRM}^2} - \lambda_t^{\text{FIRM}^3} = 0 \quad (I_t) \tag{2.9}$$

$$1 - \lambda_t^{\text{FIRM}^3} = 0 \quad (\pi_t) \tag{2.10}$$

$$-\delta\omega K_{t-1}\lambda_t^{\mathrm{FIRM}^2} C_q \mathcal{U} t_t^{-1+\omega} + \alpha K_{t-1}\lambda_t^{\mathrm{FIRM}^1} L_t^{\mathrm{d}^{1-\alpha}} Z_t^{1-\alpha} (K_{t-1} C_q \mathcal{U} t_t)^{-1+\alpha} = 0 \quad (C_q \mathcal{U} t_t)$$

2.3 First order conditions after reduction

$$-\lambda_t^{\text{FIRM}^{\Pi}} + \lambda_{t-1}^{\text{c}}^{-1} \lambda_t^{\text{c}} \lambda_t^{\text{U}} = 0 \quad (\Pi_t)$$

$$(2.12)$$

$$-1 + E_{t} \left[\lambda_{t+1}^{\text{FIRM}^{\Pi}} \left(1 - \delta C q U t_{t+1}^{\omega} + \alpha \lambda_{t+1}^{\text{FIRM}^{1}} C q U t_{t+1} L_{t+1}^{d^{-1-\alpha}} Z_{t+1}^{1-\alpha} \left(K_{t} C q U t_{t+1} \right)^{-1+\alpha} \right) \right] = 0 \quad (K_{t})$$

$$(2.13)$$

$$-W_t + \lambda_t^{\text{FIRM}^1} (1 - \alpha) L_t^{\text{d}-\alpha} Z_t^{1-\alpha} (K_{t-1} C q \mathcal{U} t_t)^{\alpha} = 0 \quad (L_t^{\text{d}})$$

$$(2.14)$$

$$-\lambda_t^{\text{FIRM}^1} + P_t = 0 \quad (Y_t) \tag{2.15}$$

$$-\delta\omega K_{t-1}CqUt_t^{-1+\omega} + \alpha K_{t-1}\lambda_t^{\text{FIRM}^1}L_t^{\text{d}^{1-\alpha}}Z_t^{1-\alpha}(K_{t-1}CqUt_t)^{-1+\alpha} = 0 \quad (CqUt_t)$$

$$(2.16)$$

3 EQUILIBRIUM

3.1 Identities

2

$$P_t = 1 (3.1)$$

$$L_t^{\rm d} = L_t^{\rm s} \tag{3.2}$$

4 EXOG

4.1 Identities

$$Z_t = e^{\epsilon_t^Z + \phi \log Z_{t-1}} \tag{4.1}$$

5 Equilibrium relationships (after reduction)

$$-1 + \beta C_t^{1-\mu} (1 - L_t^{\mathrm{s}})^{-1+\mu} \Big(C_t^{\mu} (1 - L_t^{\mathrm{s}})^{1-\mu} \Big)^{\eta} \mathrm{E}_t \left[\Big(1 - \delta C q U t_{t+1}^{\omega} + \alpha C q U t_{t+1} L_{t+1}^{\mathrm{s}}^{1-\alpha} Z_{t+1}^{1-\alpha} \big(K_t C q U t_{t+1} \big)^{-1+\alpha} \Big) C_{t+1}^{-1+\mu} \Big(1 - L_{t+1}^{\mathrm{s}} \big)^{1-\mu} \Big(C_{t+1}^{\mu} \big(1 - L_{t+1}^{\mathrm{s}} \big)^{1-\mu} \Big)^{-\eta} \right] = 0$$

$$(5.1)$$

$$-W_t + (1 - \alpha) L_t^{s - \alpha} Z_t^{1 - \alpha} (K_{t-1} CqU t_t)^{\alpha} = 0$$
(5.2)

$$-Y_t + L_t^{s^{1-\alpha}} Z_t^{1-\alpha} (K_{t-1} C q U t_t)^{\alpha} = 0$$
(5.3)

$$-Z_t + e^{\epsilon_t^{\mathbf{Z}} + \phi \log Z_{t-1}} = 0 \tag{5.4}$$

$$-\delta\omega K_{t-1} Cqt Ut_t^{-1+\omega} + \alpha K_{t-1} L_t^{s1-\alpha} Z_t^{1-\alpha} (K_{t-1} Cqt Ut_t)^{-1+\alpha} = 0$$
(5.5)

$$(-1+\mu)C_t^{\mu}(1-L_t^s)^{-\mu}\left(C_t^{\mu}(1-L_t^s)^{1-\mu}\right)^{-\eta} + \mu W_t C_t^{-1+\mu}(1-L_t^s)^{1-\mu}\left(C_t^{\mu}(1-L_t^s)^{1-\mu}\right)^{-\eta} = 0$$
(5.6)

$$I_t - K_t + K_{t-1} \left(1 - \delta C q U t_t^{\omega} \right) = 0 \tag{5.7}$$

$$U_t - \beta \mathcal{E}_t \left[U_{t+1} \right] - (1 - \eta)^{-1} \left(C_t^{\mu} (1 - L_t^{s})^{1-\mu} \right)^{1-\eta} = 0$$
 (5.8)

$$-C_{t} + \Pi_{t} + L_{t}^{s}W_{t} - \beta \left(C_{t}^{-1+\mu}\right)^{-1} \left(\left(1 - L_{t}^{s}\right)^{1-\mu}\right)^{-1} \left(\left(C_{t}^{\mu}\left(1 - L_{t}^{s}\right)^{1-\mu}\right)^{-\eta}\right)^{-1} E_{t} \left[\Pi_{t+1}C_{t+1}^{-1+\mu}\left(1 - L_{t+1}^{s}\right)^{1-\mu}\left(C_{t+1}^{\mu}\left(1 - L_{t+1}^{s}\right)^{1-\mu}\right)^{-\eta}\right] = 0$$

$$(5.9)$$

$$-I_{t} - \Pi_{t} + Y_{t} - L_{t}^{s}W_{t} + \beta \left(C_{t}^{-1+\mu}\right)^{-1} \left(\left(1 - L_{t}^{s}\right)^{1-\mu}\right)^{-1} \left(\left(C_{t}^{\mu}\left(1 - L_{t}^{s}\right)^{1-\mu}\right)^{-\eta}\right)^{-1} E_{t} \left[\Pi_{t+1}C_{t+1}^{-1+\mu}\left(1 - L_{t+1}^{s}\right)^{1-\mu}\left(C_{t+1}^{\mu}\left(1 - L_{t+1}^{s}\right)^{1-\mu}\right)^{-\eta}\right] = 0$$
 (5.10)

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6 Steady state relationships (after reduction)

$$-1 + \beta \left(1 - \delta CqU t_{ss}^{\ \ \omega} + \alpha CqU t_{ss}^{\ \ \omega} + \alpha CqU t_{ss}^{\ \ 1-\alpha} Z_{ss}^{\ \ 1-\alpha} (CqU t_{ss}^{\ \ K_{ss}})^{-1+\alpha} \right) C_{ss}^{\ \ -1+\mu} C_{ss}^{\ \ 1-\mu} (1 - L_{ss}^{s})^{-1+\mu} (1 - L_{ss}^{s})^{1-\mu} = 0 \tag{6.1}$$

$$-W_{\rm ss} + (1 - \alpha) L_{\rm ss}^{\rm s - \alpha} Z_{\rm ss}^{1 - \alpha} \left(C q \mathcal{U} t_{\rm ss} K_{\rm ss} \right)^{\alpha} = 0 \tag{6.2}$$

$$-Y_{ss} + L_{ss}^{s}^{1-\alpha} Z_{ss}^{1-\alpha} (CqUt_{ss} K_{ss})^{\alpha} = 0$$
(6.3)

$$-Z_{\rm ss} + e^{\phi \log Z_{\rm ss}} = 0 \tag{6.4}$$

$$-\delta\omega K_{\rm ss} CqU t_{\rm ss}^{-1+\omega} + \alpha K_{\rm ss} L_{\rm ss}^{\rm s}^{1-\alpha} Z_{\rm ss}^{1-\alpha} \left(CqU t_{\rm ss} K_{\rm ss} \right)^{-1+\alpha} = 0 \tag{6.5}$$

$$(-1+\mu)C_{ss}^{\mu}(1-L_{ss}^{s})^{-\mu}\left(C_{ss}^{\mu}(1-L_{ss}^{s})^{1-\mu}\right)^{-\eta} + \mu W_{ss}C_{ss}^{-1+\mu}(1-L_{ss}^{s})^{1-\mu}\left(C_{ss}^{\mu}(1-L_{ss}^{s})^{1-\mu}\right)^{-\eta} = 0$$

$$(6.6)$$

$$I_{\rm ss} - K_{\rm ss} + K_{\rm ss} \left(1 - \delta C q \mathcal{U} t_{\rm ss}^{\ \omega}\right) = 0 \tag{6.7}$$

$$U_{\rm ss} - \beta U_{\rm ss} - (1 - \eta)^{-1} \left(C_{\rm ss}^{\ \mu} (1 - L_{\rm ss}^{\ s})^{1 - \mu} \right)^{1 - \eta} = 0 \tag{6.8}$$

$$-C_{\rm ss} + \Pi_{\rm ss} + L_{\rm ss}^{\rm s} W_{\rm ss} - \beta \Pi_{\rm ss} 1 (1 - L_{\rm ss}^{\rm s})^{-1+\mu} (1 - L_{\rm ss}^{\rm s})^{1-\mu} = 0$$
(6.9)

$$-I_{ss} - \Pi_{ss} + Y_{ss} - L_{ss}^{s} W_{ss} + \beta \Pi_{ss} C_{ss}^{-1+\mu} C_{ss}^{1-\mu} (1 - L_{ss}^{s})^{-1+\mu} (1 - L_{ss}^{s})^{1-\mu} = 0$$

$$(6.10)$$

7 Parameter settings

$$\alpha = 0.36 \tag{7.1}$$

$$\beta = 0.99 \tag{7.2}$$

$$\delta = 0.025 \tag{7.3}$$

$$\eta = 2 \tag{7.4}$$

$$\mu = 0.3 \tag{7.5}$$

 $\omega = 1.45 \tag{7.6}$

 $\phi = 0.95 \tag{7.7}$

8 Steady-state values

| | Steady-state value |
|------------------|--------------------|
| C | 0.7449 |
| CapUt | 0.9284 |
| I | 0.246 |
| K | 10.96 |
| $L^{\mathbf{s}}$ | 0.2673 |
| Π | 11.0707 |
| U | -135.8123 |
| W | 2.3722 |
| Y | 0.9909 |
| Z | 1 |

9 The solution of the 1st order perturbation

Matrix P

$$\begin{array}{cc} K_{t-1} & Z_{t-1} \\ K_t & 0.9758 & 0.0705 \\ Z_t & 0 & 0.95 \end{array} \right)$$

Matrix Q

$$\begin{array}{c} \epsilon^{\rm Z} \\ K \left(\begin{array}{c} 0.0742 \\ I \end{array} \right) \end{array}$$

Matrix R

$$\begin{array}{c} K_{t-1} & Z_{t-1} \\ C_t & 0.2823 & 0.4185 \\ -0.74 & 1.0041 \\ I_t & -1.1491 & 4.5972 \\ L_t^s & -0.2604 & 0.7601 \\ \Pi_t & 0.9893 & 0.0146 \\ U_t & 0.0446 & 0.0408 \\ W_t & 0.1873 & 0.6958 \\ Y_t & -0.0731 & 1.456 \\ \end{array}$$

Matrix S

$$\begin{array}{c} \epsilon^{\rm Z} \\ C \\ C \\ Q \\ U \\ I \\ L^{\rm s} \\ U \\ U \\ W \\ Y \end{array} \begin{array}{c} 0.4405 \\ 1.057 \\ 4.8392 \\ 0.8001 \\ 0.0153 \\ 0.0429 \\ 0.7325 \\ 1.5326 \\ Y \end{array}$$

10 Model statistics

10.1 Basic statistics

| | Steady-state value | Std. dev. | Variance | Loglin |
|------------------|--------------------|-----------|----------|--------|
| \overline{C} | 0.7449 | 0.0408 | 0.0017 | Y |
| CapUt | 0.9284 | 0.1001 | 0.01 | Y |
| I | 0.246 | 0.4485 | 0.2011 | Y |
| K | 10.96 | 0.0245 | 0.0006 | Y |
| L^{s} | 0.2673 | 0.0744 | 0.0055 | Y |
| Π | 11.0707 | 0.0242 | 0.0006 | Y |
| U | -135.8123 | 0.004 | 0 | Y |
| W | 2.3722 | 0.0674 | 0.0045 | Y |
| Y | 0.9909 | 0.1414 | 0.02 | Y |
| Z | 1 | 0.0922 | 0.0085 | Y |

10.2 Correlation matrix

| | C | CapUt | I | K | L^{s} | Π | U | W | Y | Z |
|------------------|---|-------|-------|-------|------------------|--------|-------|-------|-------|-------|
| \overline{C} | 1 | 0.939 | 0.973 | 0.387 | 0.967 | 0.172 | 0.995 | 0.995 | 0.983 | 0.986 |
| CapUt | | 1 | 0.993 | 0.045 | 0.995 | -0.178 | 0.898 | 0.969 | 0.986 | 0.984 |
| I | | | 1 | 0.164 | 1 | -0.06 | 0.944 | 0.991 | 0.999 | 0.998 |
| K | | | | 1 | 0.141 | 0.975 | 0.479 | 0.291 | 0.213 | 0.225 |
| L^{s} | | | | | 1 | -0.083 | 0.936 | 0.988 | 0.997 | 0.996 |
| Π | | | | | | 1 | 0.272 | 0.071 | -0.01 | 0.003 |
| U | | | | | | | 1 | 0.979 | 0.96 | 0.963 |
| W | | | | | | | | 1 | 0.997 | 0.998 |
| Y | | | | | | | | | 1 | 1 |
| Z | | | | | | | | | | 1 |

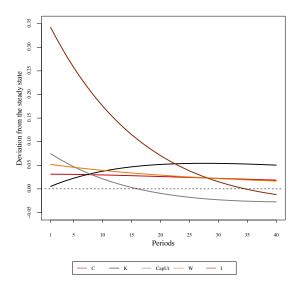
10.3 Cross correlations with the reference variable (Y)

| 10.0 | 10.5 Closs correlations with the reference variable (1) | | | | | | | | | | | |
|--------------|---|-----------|-----------|-----------|-----------|-----------|-------|-----------|-----------|-----------|-----------|-----------|
| | $\sigma[\cdot]$ rel. to $\sigma[Y]$ | Y_{t-5} | Y_{t-4} | Y_{t-3} | Y_{t-2} | Y_{t-1} | Y_t | Y_{t+1} | Y_{t+2} | Y_{t+3} | Y_{t+4} | Y_{t+5} |
| C_t | 0.289 | -0.117 | 0.01 | 0.178 | 0.393 | 0.66 | 0.983 | 0.748 | 0.543 | 0.366 | 0.217 | 0.095 |
| $CapUt_t$ | 0.708 | 0.076 | 0.197 | 0.347 | 0.528 | 0.74 | 0.986 | 0.658 | 0.389 | 0.174 | 0.006 | -0.12 |
| I_t | 3.172 | 0.01 | 0.135 | 0.294 | 0.489 | 0.723 | 0.999 | 0.699 | 0.448 | 0.242 | 0.079 | -0.048 |
| K_t | 0.173 | -0.54 | -0.499 | -0.413 | -0.273 | -0.068 | 0.213 | 0.408 | 0.531 | 0.595 | 0.613 | 0.596 |
| $L_t^{ m s}$ | 0.526 | 0.023 | 0.148 | 0.305 | 0.497 | 0.727 | 0.997 | 0.692 | 0.437 | 0.229 | 0.064 | -0.062 |
| Π_t | 0.171 | -0.549 | -0.535 | -0.484 | -0.386 | -0.232 | -0.01 | 0.255 | 0.436 | 0.548 | 0.603 | 0.614 |
| U_t | 0.029 | -0.171 | -0.046 | 0.124 | 0.344 | 0.621 | 0.96 | 0.758 | 0.575 | 0.414 | 0.275 | 0.156 |
| W_t | 0.477 | -0.061 | 0.065 | 0.23 | 0.438 | 0.692 | 0.997 | 0.732 | 0.504 | 0.314 | 0.157 | 0.032 |
| Y_t | 1 | -0.017 | 0.109 | 0.27 | 0.47 | 0.713 | 1 | 0.713 | 0.47 | 0.27 | 0.109 | -0.017 |
| Z_t | 0.652 | -0.024 | 0.102 | 0.264 | 0.465 | 0.71 | 1 | 0.716 | 0.476 | 0.277 | 0.116 | -0.009 |

10.4 Autocorrelations

| | Lag 1 | Lag 2 | Lag 3 | Lag 4 | Lag 5 |
|------------------|-------|-------|-------|-------|---------|
| \overline{C} | 0.728 | 0.494 | 0.298 | 0.137 | 0.009 |
| CapUt | 0.714 | 0.472 | 0.272 | 0.111 | -0.016 |
| I | 0.712 | 0.468 | 0.268 | 0.107 | -0.019 |
| K | 0.96 | 0.864 | 0.731 | 0.576 | 0.414 |
| L^{s} | 0.711 | 0.468 | 0.268 | 0.106 | -0.02 |
| Π | 0.964 | 0.869 | 0.737 | 0.583 | 0.419 |
| U | 0.743 | 0.518 | 0.326 | 0.165 | 0 |
| W | 0.717 | 0.478 | 0.279 | 0.118 | -0.009 |
| Y | 0.713 | 0.47 | 0.27 | 0.109 | -0.017 |
| Z | 0.713 | 0.471 | 0.271 | 0.11 | -0.016 |

11 Impulse response functions



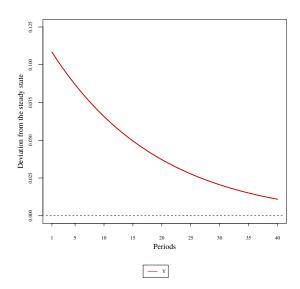


Figure 1: Impulse responses (C,K,CapUt,W,I) to $\epsilon^{\mathbf{Z}}$ shock

Figure 2: Impulse response (Y) to $\epsilon^{\mathbf{Z}}$ shock