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Index sets

$$agents = \{A, B\}$$
 $goods = \{1, 2, 3\}$

1 AGENTS $a \in agents$

1.1 Optimisation problem

$$\max_{\left(C^{\langle a,g\rangle}\right)_{g\in\mathit{goods}}} U^{\langle a\rangle} = \prod_{g\in\mathit{goods}} C^{\langle a,g\rangle^{\alpha^{\langle a,g\rangle}}} \tag{1.1}$$

s.t.:

$$\sum_{g \in gads} p^{\langle g \rangle} C^{\langle a, g \rangle} = \sum_{g \in gads} e^{\langle a, g \rangle} p^{\langle g \rangle} \quad \left(\lambda^{\text{AGENTS}^{1} \langle a \rangle} \right)$$
 (1.2)

1.2 Identities

$$g \in gads: \quad e^{\langle a,g \rangle} = e^{\operatorname{calibr}\langle a,g \rangle}$$
 (1.3)

1.3 First order conditions

$$g \in gads: -\lambda^{\text{AGENTS}^{1\langle a\rangle}} p^{\langle g\rangle} + \alpha^{\langle a,g\rangle} C^{\langle a,g\rangle^{-1}} \left(\prod_{g' \in gads} C^{\langle a,g'\rangle} \alpha^{\langle a,g'\rangle} \right) = 0 \quad \left(C^{\langle a,g\rangle} \right)$$
(1.4)

2 EQUILIBRIUM

2.1 Identities

$$p^{\langle 1 \rangle} = 1 \tag{2.1}$$

$$g \in gads \setminus \{1\}: \sum_{a \in agents} C^{\langle a,g \rangle} = \sum_{a \in agents} e^{\langle a,g \rangle}$$
 (2.2)

3 Equilibrium relationships (before expansion and reduction)

$$1 - p^{\langle 1 \rangle} = 0 \tag{3.1}$$

$$a \in agents: \quad U^{\langle a \rangle} - \prod_{g \in gaads} C^{\langle a,g \rangle}{}^{\alpha^{\langle a,g \rangle}} = 0$$
 (3.2)

$$a \in \mathit{agents} : \qquad \sum_{g \in \mathit{gaals}} e^{\langle a,g \rangle} p^{\langle g \rangle} - \sum_{g \in \mathit{gaals}} p^{\langle g \rangle} C^{\langle a,g \rangle} = 0 \tag{3.3}$$

$$a \in \mathit{agents}: \quad g \in \mathit{goods}: \quad e^{\operatorname{calibr}\langle a, g \rangle} - e^{\langle a, g \rangle} = 0$$
 (3.4)

$$a \in \operatorname{agents}: \quad g \in \operatorname{gads}: \quad -\lambda^{\operatorname{AGENTS}^{1}\langle a \rangle} p^{\langle g \rangle} + \alpha^{\langle a, g \rangle} C^{\langle a, g \rangle^{-1}} \left(\prod_{g' \in \operatorname{gads}} C^{\langle a, g' \rangle} \alpha^{\langle a, g' \rangle} \right) = 0 \tag{3.5}$$

$$g \in gads \setminus \{1\}: \sum_{a \in agents} e^{\langle a, g \rangle} - \sum_{a \in agents} C^{\langle a, g \rangle} = 0$$
 (3.6)

4 Equilibrium relationships (after expansion and reduction)

$$1 - p^{\langle 1 \rangle} = 0 \tag{4.1}$$

$$e^{\operatorname{calibr}\langle \mathbf{A}, 1 \rangle} - e^{\langle \mathbf{A}, 1 \rangle} = 0$$
 (4.2)

$$e^{\operatorname{calibr}\langle A,2\rangle} - e^{\langle A,2\rangle} = 0$$
 (4.3)

$$e^{\text{calibr}\langle A,3\rangle} - e^{\langle A,3\rangle} = 0$$
 (4.4)

$$e^{\operatorname{calibr}\langle \mathbf{B}, \mathbf{1} \rangle} - e^{\langle \mathbf{B}, \mathbf{1} \rangle} = 0$$
 (4.5)

$$e^{\text{calibr}\langle B,2\rangle} - e^{\langle B,2\rangle} = 0$$
 (4.6)

$$e^{\operatorname{calibr}\langle \mathbf{B}, 3 \rangle} - e^{\langle \mathbf{B}, 3 \rangle} = 0$$
 (4.7)

$$U^{\langle A \rangle} - C^{\langle A, 1 \rangle}{}^{\alpha^{\langle A, 1 \rangle}} C^{\langle A, 2 \rangle}{}^{\alpha^{\langle A, 2 \rangle}} C^{\langle A, 3 \rangle}{}^{\alpha^{\langle A, 3 \rangle}} = 0$$

$$(4.8)$$

$$U^{\langle \mathbf{B} \rangle} - C^{\langle \mathbf{B}, 1 \rangle \alpha^{\langle \mathbf{B}, 1 \rangle}} C^{\langle \mathbf{B}, 2 \rangle \alpha^{\langle \mathbf{B}, 2 \rangle}} C^{\langle \mathbf{B}, 3 \rangle \alpha^{\langle \mathbf{B}, 3 \rangle}} = 0 \tag{4.9}$$

$$-\lambda^{\text{AGENTS}^{1}\langle \mathbf{A}\rangle} p^{\langle 1\rangle} + \alpha^{\langle \mathbf{A}, 1\rangle} C^{\langle \mathbf{A}, 1\rangle^{-1}} C^{\langle \mathbf{A}, 1\rangle} C^{\langle \mathbf{A}, 1\rangle} C^{\langle \mathbf{A}, 2\rangle} C^{\langle \mathbf{A}, 2\rangle} C^{\langle \mathbf{A}, 3\rangle} = 0 \tag{4.10}$$

$$-\lambda^{\mathrm{AGENTS^{1}}\langle \mathbf{A}\rangle}p^{\langle 2\rangle} + \alpha^{\langle \mathbf{A}, 2\rangle}C^{\langle \mathbf{A}, 2\rangle - 1}C^{\langle \mathbf{A}, 1\rangle}\alpha^{\langle \mathbf{A}, 1\rangle}C^{\langle \mathbf{A}, 2\rangle}C^{\langle \mathbf{A}, 2\rangle}C^{\langle \mathbf{A}, 3\rangle}\alpha^{\langle \mathbf{A}, 3\rangle} = 0 \tag{4.11}$$

$$-\lambda^{\text{AGENTS}^{1}\langle \mathbf{A}\rangle} p^{\langle 3\rangle} + \alpha^{\langle \mathbf{A}, 3\rangle} C^{\langle \mathbf{A}, 3\rangle - 1} C^{\langle \mathbf{A}, 1\rangle} \alpha^{\langle \mathbf{A}, 1\rangle} C^{\langle \mathbf{A}, 2\rangle} C^{\langle \mathbf{A}, 2\rangle} C^{\langle \mathbf{A}, 3\rangle} = 0 \tag{4.12}$$

$$-\lambda^{\text{AGENTS}^{1}\langle \mathbf{B}\rangle} p^{\langle 1\rangle} + \alpha^{\langle \mathbf{B}, 1\rangle} C^{\langle \mathbf{B}, 1\rangle^{-1}} C^{\langle \mathbf{B}, 1\rangle} C^{\langle \mathbf{B}, 1\rangle} C^{\langle \mathbf{B}, 2\rangle} C^{\langle \mathbf{B}, 2\rangle} C^{\langle \mathbf{B}, 3\rangle} = 0 \tag{4.13}$$

$$-\lambda^{\text{AGENTS}^{1}\langle \mathbf{B}\rangle} p^{\langle 2\rangle} + \alpha^{\langle \mathbf{B}, 2\rangle} C^{\langle \mathbf{B}, 2\rangle^{-1}} C^{\langle \mathbf{B}, 1\rangle^{\alpha^{\langle \mathbf{B}, 1\rangle}}} C^{\langle \mathbf{B}, 2\rangle^{\alpha^{\langle \mathbf{B}, 2\rangle}}} C^{\langle \mathbf{B}, 3\rangle^{\alpha^{\langle \mathbf{B}, 3\rangle}}} = 0 \tag{4.14}$$

$$-\lambda^{\text{AGENTS}^{1}\langle \text{B}\rangle} p^{\langle 3\rangle} + \alpha^{\langle \text{B},3\rangle} C^{\langle \text{B},3\rangle^{-1}} C^{\langle \text{B},1\rangle} C^{\langle \text{B},1\rangle} C^{\langle \text{B},2\rangle} C^{\langle \text{B},2\rangle} C^{\langle \text{B},3\rangle} = 0 \tag{4.15}$$

$$e^{\langle \mathbf{A}, 2 \rangle} + e^{\langle \mathbf{B}, 2 \rangle} - C^{\langle \mathbf{A}, 2 \rangle} - C^{\langle \mathbf{B}, 2 \rangle} = 0 \tag{4.16}$$

$$e^{\langle \mathbf{A}, 3 \rangle} + e^{\langle \mathbf{B}, 3 \rangle} - C^{\langle \mathbf{A}, 3 \rangle} - C^{\langle \mathbf{B}, 3 \rangle} = 0 \tag{4.17}$$

$$e^{\langle \mathbf{A}, \mathbf{1} \rangle} p^{\langle \mathbf{1} \rangle} + e^{\langle \mathbf{A}, \mathbf{2} \rangle} p^{\langle \mathbf{2} \rangle} + e^{\langle \mathbf{A}, \mathbf{3} \rangle} p^{\langle \mathbf{3} \rangle} - p^{\langle \mathbf{1} \rangle} C^{\langle \mathbf{A}, \mathbf{1} \rangle} - p^{\langle \mathbf{2} \rangle} C^{\langle \mathbf{A}, \mathbf{2} \rangle} - p^{\langle \mathbf{3} \rangle} C^{\langle \mathbf{A}, \mathbf{3} \rangle} = 0 \tag{4.18}$$

$$e^{\langle \mathbf{B}, \mathbf{1} \rangle} p^{\langle \mathbf{1} \rangle} + e^{\langle \mathbf{B}, \mathbf{2} \rangle} p^{\langle \mathbf{2} \rangle} + e^{\langle \mathbf{B}, \mathbf{3} \rangle} p^{\langle \mathbf{3} \rangle} - p^{\langle \mathbf{1} \rangle} C^{\langle \mathbf{B}, \mathbf{1} \rangle} - p^{\langle \mathbf{2} \rangle} C^{\langle \mathbf{B}, \mathbf{2} \rangle} - p^{\langle \mathbf{3} \rangle} C^{\langle \mathbf{B}, \mathbf{3} \rangle} = 0 \tag{4.19}$$

5 Equilibrium values

	Equilibrium values
$e^{A^{1}}$ $e^{A^{2}}$	3
	2
e^{A^3}	1
$\lambda^{\mathrm{AGENTS}^{1^{\mathrm{A}}}}$	0.2674
C^{A^1}	2.2667
$C^{\mathbf{A}^2}$	1.7
C^{A^3}	2.2667
U^{A}	2.0203

6 Equilibrium values

	E:1:1: 1
	Equilibrium values
$\frac{e^{\mathbf{B}^1}}{e^{\mathbf{B}^2}}$	1
	1
e^{B^3}	3
$\lambda^{\mathrm{AGENTS^{1}^{B}}}$	0.2674
$C^{\mathrm{B}^{1}}$	1.7333
C^{B^2}	1.3
C^{B^3}	1.7333
U^{B}	1.5449