Generated on 2015-06-13 00:50:27 by gEcon version 0.9.1 (2015-05-19)

Model name: SW\_03

#### 1 CONSUMER

## 1.1 Optimisation problem

$$\max_{C_t, K_t, I_t, B_t, z_t} U_t = \beta E_t \left[ U_{t+1} \right] + \epsilon_t^{b} \left( (1 - \sigma^c)^{-1} \left( C_t - H_t \right)^{1 - \sigma^c} - \omega \epsilon_t^{L} \left( 1 + \sigma^l \right)^{-1} L_t^{s1 + \sigma^l} \right)$$
(1.1)

s.t.:

$$C_t + I_t + B_t R_t^{-1} = D \dot{w}_t - T_t + B_{t-1} \pi_t^{-1} + L_t W_t + K_{t-1} r_t^k z_t - \psi^{-1} r_{ss}^k K_{t-1} \left( -1 + e^{\psi(-1+z_t)} \right) \quad (\lambda_t)$$

$$(1.2)$$

$$K_{t} = K_{t-1} (1 - \tau) + I_{t} \left( 1 - 0.5 \varphi \left( -1 + I_{t-1}^{-1} \epsilon_{t}^{I} I_{t} \right)^{2} \right) \quad (q_{t})$$

$$(1.3)$$

#### 1.2 Identities

$$H_t = hC_{t-1} \tag{1.4}$$

$$Q_t = \lambda_t^{-1} q_t \tag{1.5}$$

#### 1.3 First order conditions

$$-\lambda_t + \epsilon_t^{\mathrm{b}} (C_t - H_t)^{-\sigma^{\mathrm{c}}} = 0 \quad (C_t)$$

$$\tag{1.6}$$

$$-q_t + \beta \left( (1 - \tau) \operatorname{E}_t \left[ q_{t+1} \right] + \operatorname{E}_t \left[ \lambda_{t+1} \left( r_{t+1}^{k} z_{t+1} - \psi^{-1} r_{ss}^{k} \left( -1 + e^{\psi(-1 + z_{t+1})} \right) \right) \right] \right) = 0 \quad (K_t)$$

$$-\lambda_{t} + q_{t} \left(1 - 0.5\varphi \left(-1 + I_{t-1}^{-1} \epsilon_{t}^{I} I_{t}\right)^{2} - \varphi I_{t-1}^{-1} \epsilon_{t}^{I} I_{t} \left(-1 + I_{t-1}^{-1} \epsilon_{t}^{I} I_{t}\right)\right) + \beta \varphi I_{t}^{-2} \mathcal{E}_{t} \left[\epsilon_{t+1}^{I} q_{t+1} I_{t+1}^{2} \left(-1 + I_{t}^{-1} \epsilon_{t+1}^{I} I_{t+1}\right)\right] = 0 \quad (I_{t})$$

$$(1.8)$$

$$\beta E_t \left[ \lambda_{t+1} \pi_{t+1}^{-1} \right] - \lambda_t R_t^{-1} = 0 \quad (B_t)$$
(1.9)

$$\lambda_t \left( K_{t-1} r_t^{k} - r_{ss}^{k} K_{t-1} e^{\psi(-1+z_t)} \right) = 0 \quad (z_t)$$
(1.10)

#### 2 PREFERENCE SHOCKS

2.1 Identities

$$\log \epsilon_t^{\rm b} = \eta_t^{\rm b} + \rho^{\rm b} \log \epsilon_{t-1}^{\rm b} \tag{2.1}$$

$$\log \epsilon_t^{\mathcal{L}} = -\eta_t^{\mathcal{L}} + \rho^{\mathcal{L}} \log \epsilon_{t-1}^{\mathcal{L}} \tag{2.2}$$

#### 3 INVESTMENT COST SHOCKS

3.1 Identities

$$\log \epsilon_t^{\mathrm{I}} = \eta_t^{\mathrm{I}} + \rho^{\mathrm{I}} \log \epsilon_{t-1}^{\mathrm{I}} \tag{3.1}$$

#### 4 WAGE SETTING PROBLEM

4.1 Identities

$$f_t^1 = \beta \xi^{w} E_t \left[ f_{t+1}^1 \left( w_t^{\star - 1} w_{t+1}^{\star} \right)^{\lambda^{w-1}} \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{w}} \right)^{-\lambda^{w-1}} \right] + \lambda_t w_t^{\star} L_t \left( 1 + \lambda^{w} \right)^{-1} \pi_t^{\star^{w} - \lambda^{w-1} (1 + \lambda^{w})}$$

$$(4.1)$$

$$f_t^2 = \beta \xi^{W} E_t \left[ f_{t+1}^2 \left( w_t^{\star - 1} w_{t+1}^{\star} \right)^{\lambda^{W-1} (1 + \lambda^{W}) \left( 1 + \sigma^1 \right)} \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{W}} \right)^{-\lambda^{W-1} (1 + \lambda^{W}) \left( 1 + \sigma^1 \right)} \right] + \omega \epsilon_t^b \epsilon_t^L \left( L_t \pi_t^{\star^{W} - \lambda^{W-1} (1 + \lambda^{W})} \right)^{1 + \sigma^1}$$

$$(4.2)$$

$$f_t^1 = \eta_t^{W} + f_t^2 (4.3)$$

$$\pi_t^{\star^{\mathbf{w}}} = w_t^{\star} W_t^{-1} \tag{4.4}$$

# 5 WAGE EVOLUTION

5.1 Identities

$$1 = (1 - \xi^{\mathbf{w}}) \pi_t^{\star^{\mathbf{w}} - \lambda^{\mathbf{w}} - 1} + \xi^{\mathbf{w}} (W_{t-1} W_t^{-1})^{-\lambda^{\mathbf{w}} - 1} (\pi_t^{-1} \pi_{t-1} \gamma^{\mathbf{w}})^{-\lambda^{\mathbf{w}} - 1}$$

$$(5.1)$$

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#### 6 LABOUR AGGREGATION

#### 6.1 Identities

$$\nu_t^{\mathbf{w}} = (1 - \xi^{\mathbf{w}}) \pi_t^{\star^{\mathbf{w}} - \lambda^{\mathbf{w}} - 1} (1 + \lambda^{\mathbf{w}}) + \xi^{\mathbf{w}} \nu_{t-1}^{\mathbf{w}} \left( W_{t-1} \pi_t^{-1} W_t^{-1} \pi_{t-1} \gamma^{\mathbf{w}} \right)^{-\lambda^{\mathbf{w}} - 1} (1 + \lambda^{\mathbf{w}})$$

$$(6.1)$$

$$L_t = \nu_t^{\mathrm{w}-1} L_t^{\mathrm{s}} \tag{6.2}$$

#### 7 CONSUMER FLEXIBLE

## 7.1 Optimisation problem

$$\max_{C_t^f, K_t^f, I_t^f, B_t^f, z_t^f, L_t^{s^f}} U_t^f = \beta E_t \left[ U_{t+1}^f \right] + \epsilon_t^b \left( (1 - \sigma^c)^{-1} \left( C_t^f - H_t^f \right)^{1 - \sigma^c} - \omega \epsilon_t^L \left( 1 + \sigma^l \right)^{-1} L_t^{s^f} \right)$$
(7.1)

s.t.:

$$C_t^{f} + I_t^{f} + B_t^{f} R_t^{f-1} = B_{t-1}^{f} + D \dot{w}_t^{f} + \Pi_t^{\text{ws}^f} - T_t^{f} + L_t^{\text{s}^f} W_t^{\text{disutil}^f} + K_{t-1}^{f} r_t^{k^f} z_t^{f} - \psi^{-1} r_{\text{ss}}^{k^f} K_{t-1}^{f} \left( -1 + e^{\psi \left( -1 + z_t^f \right)} \right) \quad \left( \lambda_t^f \right)$$

$$(7.2)$$

$$K_t^{f} = K_{t-1}^{f} (1 - \tau) + I_t^{f} \left( 1 - 0.5\varphi \left( -1 + I_{t-1}^{f}^{-1} \epsilon_t^{I} I_t^{f} \right)^2 \right) \quad (q_t^{f})$$

$$(7.3)$$

#### 7.2 Identities

$$H_t^{\mathbf{f}} = hC_{t-1}^{\mathbf{f}} \tag{7.4}$$

$$Q_t^{\mathbf{f}} = \lambda_t^{\mathbf{f}^{-1}} q_t^{\mathbf{f}} \tag{7.5}$$

#### 7.3 First order conditions

$$-\lambda_t^{\mathrm{f}} + \epsilon_t^{\mathrm{b}} \left( C_t^{\mathrm{f}} - H_t^{\mathrm{f}} \right)^{-\sigma^{\mathrm{c}}} = 0 \quad \left( C_t^{\mathrm{f}} \right)$$
 (7.6)

$$-q_t^{f} + \beta \left( (1 - \tau) E_t \left[ q_{t+1}^{f} \right] + E_t \left[ \lambda_{t+1}^{f} \left( r_{t+1}^{k^f} z_{t+1}^{f} - \psi^{-1} r_{ss}^{k^f} \left( -1 + e^{\psi \left( -1 + z_{t+1}^{f} \right)} \right) \right) \right] \right) = 0 \quad (K_t^{f})$$
(7.7)

$$-\lambda_{t}^{\mathrm{f}} + q_{t}^{\mathrm{f}} \left( 1 - 0.5\varphi \left( -1 + I_{t-1}^{\mathrm{f}}^{-1} \epsilon_{t}^{\mathrm{I}} I_{t}^{\mathrm{f}} \right)^{2} - \varphi I_{t-1}^{\mathrm{f}}^{-1} \epsilon_{t}^{\mathrm{I}} I_{t}^{\mathrm{f}} \left( -1 + I_{t-1}^{\mathrm{f}}^{-1} \epsilon_{t}^{\mathrm{I}} I_{t}^{\mathrm{f}} \right) \right) + \beta \varphi I_{t}^{\mathrm{f}-2} \mathbf{E}_{t} \left[ \epsilon_{t+1}^{\mathrm{I}} q_{t+1}^{\mathrm{f}} I_{t+1}^{\mathrm{f}}^{2} \left( -1 + I_{t}^{\mathrm{f}-1} \epsilon_{t+1}^{\mathrm{I}} I_{t+1}^{\mathrm{f}} \right) \right] = 0 \quad \left( I_{t}^{\mathrm{f}} \right)$$

$$(7.8)$$

$$\beta \mathbf{E}_t \left[ \lambda_{t+1}^{\mathbf{f}} \right] - \lambda_t^{\mathbf{f}} R_t^{\mathbf{f}^{-1}} = 0 \quad \left( B_t^{\mathbf{f}} \right) \tag{7.9}$$

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$$\lambda_t^{f} \left( K_{t-1}^{f} r_t^{k^f} - r_{ss}^{k^f} K_{t-1}^{f} e^{\psi(-1+z_t^f)} \right) = 0 \quad (z_t^f)$$
 (7.10)

$$\lambda_t^{\mathbf{f}} W_t^{\text{disutil}^{\mathbf{f}}} - \omega \epsilon_t^{\mathbf{b}} \epsilon_t^{\mathbf{L}} L_t^{\mathbf{s}^{\mathbf{f}} \sigma^{\mathbf{l}}} = 0 \quad \left( L_t^{\mathbf{s}^{\mathbf{f}}} \right)$$
 (7.11)

#### 8 FLEXIBLE MONOPOLISTIC WORKER

#### 8.1 Optimisation problem

$$\max_{W_t^{if}, L_t^{i^{*^f}}} \Pi_t^{\text{ws}^f} = L_t^{i^{*^f}} \left( -W_t^{\text{disutil}^f} + W_t^{i^f} \right)$$
(8.1)

s.t.

$$L_t^{i^{\star^f}} = L_t^f \left( W_t^{i^f} W_t^{f-1} \right)^{\lambda^{w-1} (-1 - \lambda^w)} \quad \left( \lambda_t^{\text{FLEXIBLE}^{\text{MONOPOLISTIC}^{\text{WORKER}^1}}} \right)$$
 (8.2)

8.2 Identities

$$L_t^{i^{\star^f}} = L_t^{i^f} \tag{8.3}$$

8.3 First order conditions

$$L_t^{i^{\star^f}} + \lambda^{w-1} \lambda_t^{\text{FLEXIBLE}^{\text{MONOPOLISTIC}^{\text{WORKER}^1}}} L_t^f W_t^{f-1} \left( -1 - \lambda^w \right) \left( W_t^{i^f} W_t^{f-1} \right)^{-1 + \lambda^{w-1} \left( -1 - \lambda^w \right)} = 0 \quad \left( W_t^{i^f} \right)$$

$$(8.4)$$

$$-\lambda_t^{\text{FLEXIBLE}^{\text{MONOPOLISTIC}^{\text{WORKER}^1}}} - W_t^{\text{disutil}^f} + W_t^{\text{i}^f} = 0 \quad \left(L_t^{\text{i}^{\star^f}}\right)$$
(8.5)

8.4 First order conditions after reduction

$$L_t^{i^{*f}} + \lambda^{w-1} L_t^f W_t^{f-1} \left( -1 - \lambda^w \right) \left( -W_t^{\text{disutil}^f} + W_t^{i^f} \right) \left( W_t^{i^f} W_t^{f-1} \right)^{-1 + \lambda^{w-1} \left( -1 - \lambda^w \right)} = 0 \quad \left( W_t^{i^f} \right)$$
(8.6)

# 9 LABOUR AGGREGATION FLEXIBLE

$$L_t^{s^f} = L_t^{i^f} \tag{9.1}$$

$$L_t^{\mathbf{f}} = L_t^{\mathbf{s}^{\mathbf{f}}} \tag{9.2}$$

## 10 FIRM

#### 10.1 Optimisation problem

$$\max_{K_t^{jd}, L_t^{jd}} t_t^{j} = -r_t^{k} K_t^{j^d} - L_t^{j^d} W_t$$
(10.1)

s.t.

$$Y_t^{\mathbf{j}} = -\Phi + \epsilon_t^{\mathbf{a}} K_t^{\mathbf{j}^{\mathbf{d}} \alpha} L_t^{\mathbf{j}^{\mathbf{d}} 1 - \alpha} \qquad (mc_t)$$

$$(10.2)$$

10.2 First order conditions

$$-r_t^{\mathbf{k}} + \alpha \epsilon_t^{\mathbf{a}} m c_t K_t^{\mathbf{j}^{\mathbf{d}} - 1 + \alpha} L_t^{\mathbf{j}^{\mathbf{d}} - 1 - \alpha} = 0 \quad \left( K_t^{\mathbf{j}^{\mathbf{d}}} \right)$$

$$(10.3)$$

$$-W_t + \epsilon_t^{\mathbf{a}} m c_t (1 - \alpha) K_t^{\mathbf{j}^{\mathbf{d}} \alpha} L_t^{\mathbf{j}^{\mathbf{d}} - \alpha} = 0 \quad \left( L_t^{\mathbf{j}^{\mathbf{d}}} \right)$$

$$(10.4)$$

#### 11 TECHNOLOGY

11.1 Identities

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$$\log \epsilon_t^{\mathbf{a}} = \eta_t^{\mathbf{a}} + \rho^{\mathbf{a}} \log \epsilon_{t-1}^{\mathbf{a}} \tag{11.1}$$

# 12 PRICE SETTING PROBLEM

12.1 Identities

$$g_t^1 = \eta_t^P + g_t^2 (1 + \lambda^P)$$
 (12.1)

$$g_t^1 = \lambda_t \pi_t^* Y_t + \beta \xi^{\mathrm{p}} \pi_t^* \mathcal{E}_t \left[ g_{t+1}^1 \pi_{t+1}^{*-1} \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{\mathrm{p}}} \right)^{-\lambda^{\mathrm{p}-1}} \right]$$
 (12.2)

$$g_t^2 = \beta \xi^{p} E_t \left[ g_{t+1}^2 \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{p}} \right)^{-\lambda^{p-1} (1+\lambda^{p})} \right] + \lambda_t m c_t Y_t$$
(12.3)

# 13 PRICE EVOLUTION

$$1 = \xi^{p} \left( \pi_{t}^{-1} \pi_{t-1}^{\gamma^{p}} \right)^{-\lambda^{p-1}} + (1 - \xi^{p}) \pi_{t}^{\star - \lambda^{p-1}}$$
(13.1)

## 14 FACTOR DEMAND AGGREGATION

# 14.1 Identities

$$K_t^{\mathbf{d}} = K_t^{\mathbf{j}^{\mathbf{d}}} \tag{14.1}$$

$$L_t^{\mathbf{d}} = L_t^{\mathbf{j}^{\mathbf{d}}} \tag{14.2}$$

#### 15 PRODUCT AGGREGATION

#### 15.1 Identities

$$Y_t^{\rm s} = Y_t^{\rm j} \tag{15.1}$$

$$\nu_t^{\mathrm{p}} = (1 - \xi^{\mathrm{p}}) \, \pi_t^{\star - \lambda^{\mathrm{p} - 1} (1 + \lambda^{\mathrm{p}})} + \xi^{\mathrm{p}} \nu_{t-1}^{\mathrm{p}} \left( \pi_t^{-1} \pi_{t-1}^{\gamma^{\mathrm{p}}} \right)^{-\lambda^{\mathrm{p} - 1} (1 + \lambda^{\mathrm{p}})}$$
(15.2)

$$\nu_t^{\mathrm{p}} Y_t = Y_t^{\mathrm{s}} \tag{15.3}$$

# 16 FIRM FLEXIBLE

#### 16.1 Optimisation problem

$$\max_{K_t^{j^{\text{df}}}, L_t^{j^{\text{df}}}} t c_t^{j^{\text{f}}} = -r_t^{k^{\text{f}}} K_t^{j^{\text{df}}} - L_t^{j^{\text{df}}} W_t^{\text{f}}$$
(16.1)

s.t.

$$Y_t^{jf} = -\Phi + \epsilon_t^{a} K_t^{jdf} L_t^{jdf} L_t^{jdf} \qquad (mc_t^f)$$

$$(16.2)$$

#### 16.2 First order conditions

$$-r_t^{\mathbf{k}^{\mathbf{f}}} + \alpha \epsilon_t^{\mathbf{a}} m c_t^{\mathbf{f}} K_t^{\mathbf{j}^{\mathbf{d}^{\mathbf{f}}} - 1 + \alpha} L_t^{\mathbf{j}^{\mathbf{d}^{\mathbf{f}}} 1 - \alpha} = 0 \quad \left( K_t^{\mathbf{j}^{\mathbf{d}^{\mathbf{f}}}} \right)$$

$$(16.3)$$

$$-W_t^{\mathrm{f}} + \epsilon_t^{\mathrm{a}} m c_t^{\mathrm{f}} \left(1 - \alpha\right) K_t^{\mathrm{j}^{\mathrm{df}}} L_t^{\mathrm{j}^{\mathrm{df}}} = 0 \quad \left(L_t^{\mathrm{j}^{\mathrm{df}}}\right)$$

$$(16.4)$$

#### 17 PRICE SETTING PROBLEM FLEXIBLE

#### 17.1 Optimisation problem

$$\max_{Y_t^{\text{f}}, P_t^{\text{j}}} \Pi_t^{\text{ps}^{\text{f}}} = Y_t^{\text{j}^{\text{f}}} \left( -mc_t^{\text{f}} + P_t^{\text{j}^{\text{f}}} \right)$$
(17.1)

s.t.

$$Y_t^{\mathbf{j}^{\mathbf{f}}} = Y_t^{\mathbf{f}} \left( P_t^{\mathbf{f}^{-1}} P_t^{\mathbf{j}^{\mathbf{f}}} \right)^{-\lambda^{\mathbf{p}^{-1}} (1+\lambda^{\mathbf{p}})} \quad \left( \lambda_t^{\text{PRICE}^{\text{SETTING}^{\text{PROBLEM}FLEXIBLE}^1}} \right)$$
(17.2)

#### 17.2 First order conditions

$$-\lambda_t^{\text{PRICE}^{\text{SETTING}^{\text{PROBLEM}^{\text{FLEXIBLE}^1}}} - mc_t^{\text{f}} + P_t^{\text{jf}} = 0 \quad \left(Y_t^{\text{jf}}\right)$$
(17.3)

$$Y_t^{\mathbf{j}^{\mathbf{f}}} - \lambda^{\mathbf{p}-1} \lambda_t^{\mathrm{PRICE}^{\mathrm{SETTING}^{\mathrm{PROBLEM}^{\mathrm{FLEXIBLE}^1}}} P_t^{\mathbf{f}-1} Y_t^{\mathbf{f}} \left(1 + \lambda^{\mathbf{p}}\right) \left(P_t^{\mathbf{f}-1} P_t^{\mathbf{j}^{\mathbf{f}}}\right)^{-1 - \lambda^{\mathbf{p}-1} \left(1 + \lambda^{\mathbf{p}}\right)} = 0 \quad \left(P_t^{\mathbf{j}^{\mathbf{f}}}\right)$$

$$(17.4)$$

#### 17.3 First order conditions after reduction

$$Y_t^{jf} - \lambda^{p-1} P_t^{f-1} Y_t^f (1 + \lambda^p) \left( -mc_t^f + P_t^{jf} \right) \left( P_t^{f-1} P_t^{jf} \right)^{-1 - \lambda^{p-1} (1 + \lambda^p)} = 0 \quad \left( P_t^{jf} \right)$$
(17.5)

## 18 FACTOR DEMAND AGGREGATION FLEXIBLE

#### 18.1 Identities

$$K_t^{\mathbf{d}^{\mathbf{f}}} = K_t^{\mathbf{j}^{\mathbf{d}^{\mathbf{f}}}} \tag{18.1}$$

$$L_t^{\mathbf{d^f}} = L_t^{\mathbf{j^{\mathbf{d^f}}}} \tag{18.2}$$

#### 19 PRODUCT AGGREGATION FLEXIBLE

$$Y_t^{\rm sf} = Y_t^{\rm jf} \tag{19.1}$$

$$Y_t^{\mathbf{f}} = Y_t^{\mathbf{s}^{\mathbf{f}}} \tag{19.2}$$

## 20 PRICE EVOLUTION FLEXIBLE

20.1 Identities

$$P_t^{\rm f} = 1 \tag{20.1}$$

#### 21 GOVERNMENT

21.1 Identities

$$G_t = G^{\text{bar}} \epsilon_t^{G} \tag{21.1}$$

$$G_t + B_{t-1}\pi_t^{-1} = T_t + B_t R_t^{-1}$$
(21.2)

# 22 GOVERNMENT SPENDING SHOCK

22.1 Identities

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$$\log \epsilon_t^{\mathrm{G}} = \eta_t^{\mathrm{G}} + \rho^{\mathrm{G}} \log \epsilon_{t-1}^{\mathrm{G}} \tag{22.1}$$

# 23 GOVERNMENT FLEXIBLE

23.1 Identities

$$G_t^{\rm f} = G^{\rm bar} \epsilon_t^{\rm G} \tag{23.1}$$

$$B_{t-1}^{f} + G_{t}^{f} = T_{t}^{f} + B_{t}^{f} R_{t}^{f-1}$$
(23.2)

## 24 MONETARY POLICY AUTHORITY

$$abbr^{\pi} + \log\left(R_{ss}^{-1}R_{t}\right) = \eta_{t}^{R} + r^{\Delta^{\pi}}\left(-\log\left(\pi_{ss}^{-1}\pi_{t-1}\right) + \log\left(\pi_{ss}^{-1}\pi_{t}\right)\right) + r^{\Delta^{y}}\left(-\log\left(Y_{ss}^{-1}Y_{t-1}\right) + \log\left(Y_{ss}^{-1}Y_{t}\right)\right) + \log\left(Y_{ss}^{-1}Y_{t-1}\right) - \log\left(Y_{ss}^{-1}Y_{t-1}\right)\right) + \rho\log\left(R_{ss}^{-1}R_{t-1}\right) + \rho\log\left(R_$$

$$\log \pi_t^{\text{obj}} = \eta_t^{\pi} + \rho^{\pi^{\text{bar}}} \log \pi_{t-1}^{\text{obj}} + \log \alpha k h r^{\pi^{\text{obj}}} \left( 1 - \rho^{\pi^{\text{bar}}} \right)$$

$$(24.2)$$

# 25 EQUILIBRIUM

#### 25.1 Identities

$$K_t^{\mathbf{d}} = K_{t-1} z_t \tag{25.1}$$

$$L_t = L_t^{\mathrm{d}} \tag{25.2}$$

$$B_t = 0 (25.3)$$

$$D\dot{w}_t = Y_t - L_t^{\mathrm{d}} W_t - r_t^{\mathrm{k}} K_t^{\mathrm{d}} \tag{25.4}$$

# 26 EQUILIBRIUM FLEXIBLE

#### 26.1 Identities

$$K_t^{\mathsf{d}^{\mathsf{f}}} = K_{t-1}^{\mathsf{f}} z_t^{\mathsf{f}} \tag{26.1}$$

$$L_t^{\rm f} = L_t^{\rm d^f} \tag{26.2}$$

$$B_t^{\mathbf{f}} = 0 \tag{26.3}$$

$$D\dot{w}_{t}^{f} = Y_{t}^{f} - L_{t}^{d^{f}} W_{t}^{f} - r_{t}^{k^{f}} K_{t}^{d^{f}}$$
(26.4)

# 27 Equilibrium relationships (after reduction)

$$-q_{t} + \beta \left( (1 - \tau) \operatorname{E}_{t} \left[ q_{t+1} \right] + \operatorname{E}_{t} \left[ \epsilon_{t+1}^{b} \left( r_{t+1}^{k} z_{t+1} - \psi^{-1} r_{ss}^{k} \left( -1 + e^{\psi(-1 + z_{t+1})} \right) \right) \left( C_{t+1} - hC_{t} \right)^{-\sigma^{c}} \right] \right) = 0$$

$$(27.1)$$

$$-q_{t}^{f} + \beta \left( (1 - \tau) E_{t} \left[ q_{t+1}^{f} \right] + E_{t} \left[ e_{t+1}^{b} \left( r_{t+1}^{k^{f}} z_{t+1}^{f} - \psi^{-1} r_{ss}^{k^{f}} \left( -1 + e^{\psi \left( -1 + z_{t+1}^{f} \right)} \right) \right) \left( C_{t+1}^{f} - h C_{t}^{f} \right)^{-\sigma^{c}} \right] \right) = 0$$

$$(27.2)$$

$$-r_t^{k} + \alpha \epsilon_t^{a} m c_t L_t^{1-\alpha} (K_{t-1} z_t)^{-1+\alpha} = 0$$
(27.3)

$$-r_t^{k^f} + \alpha \epsilon_t^a m_t^f L_t^{f^{1-\alpha}} (K_{t-1}^f z_t^f)^{-1+\alpha} = 0$$
 (27.4)

$$-G_t + T_t = 0 (27.5)$$

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$$-G_t + G^{\text{bar}} \epsilon_t^{G} = 0 \tag{27.6}$$

$$-G_t^{\mathbf{f}} + T_t^{\mathbf{f}} = 0 \tag{27.7}$$

$$-G_t^{f} + G^{bar} \epsilon_t^{G} = 0 \tag{27.8}$$

$$-L_t + \nu_t^{\text{w}-1} L_t^{\text{s}} = 0 (27.9)$$

$$-L_t^{s^f} + L_t^f \left( W_t^{i^f} W_t^{f-1} \right)^{\lambda^{w-1} (-1 - \lambda^w)} = 0$$
(27.10)

$$L_t^{\rm sf} - L_t^{\rm f} = 0 (27.11)$$

$$L_t^{s^f} + \lambda^{w-1} L_t^f W_t^{f-1} \left( -1 - \lambda^w \right) \left( -W_t^{disutil^f} + W_t^{i^f} \right) \left( W_t^{i^f} W_t^{f-1} \right)^{-1 + \lambda^{w-1} \left( -1 - \lambda^w \right)} = 0$$
(27.12)

$$\Pi_t^{\text{ws}^f} - L_t^{\text{s}^f} \left( -W_t^{\text{disutil}^f} + W_t^{\text{i}^f} \right) = 0 \tag{27.13}$$

$$\Pi_t^{\text{ps}^f} - Y_t^f \left( -mc_t^f + P_t^{j^f} \right) P_t^{j^f - \lambda^{p-1}(1+\lambda^p)} = 0$$
(27.14)

$$-Q_t + \epsilon_t^{b^{-1}} q_t (C_t - hC_{t-1})^{\sigma^c} = 0$$
(27.15)

$$-Q_t^f + \epsilon_t^{b^{-1}} q_t^f \left( C_t^f - h C_{t-1}^f \right)^{\sigma^c} = 0$$
 (27.16)

$$-W_t + \epsilon_t^{a} mc_t (1 - \alpha) L_t^{-\alpha} (K_{t-1} z_t)^{\alpha} = 0$$
(27.17)

$$-W_t^{f} + \epsilon_t^{a} m c_t^{f} (1 - \alpha) L_t^{f-\alpha} (K_{t-1}^{f} z_t^{f})^{\alpha} = 0$$
(27.18)

$$Y_t^{\rm s} - \nu_t^{\rm p} Y_t = 0 (27.19)$$

$$-Y_t^{f} + Y_t^{s^f} = 0 (27.20)$$

$$-Y_t^{sf} + Y_t^f P_t^{j^{f-\lambda^{p-1}}(1+\lambda^p)} = 0 (27.21)$$

$$\beta E_t \left[ \epsilon_{t+1}^{\rm b} \left( C_{t+1}^{\rm f} - h C_t^{\rm f} \right)^{-\sigma^{\rm c}} \right] - \epsilon_t^{\rm b} R_t^{\rm f-1} \left( C_t^{\rm f} - h C_{t-1}^{\rm f} \right)^{-\sigma^{\rm c}} = 0$$
 (27.22)

$$\beta E_t \left[ \epsilon_{t+1}^b \pi_{t+1}^{-1} (C_{t+1} - hC_t)^{-\sigma^c} \right] - \epsilon_t^b R_t^{-1} (C_t - hC_{t-1})^{-\sigma^c} = 0$$
(27.23)

$$Y_t^{f} P_t^{j^f - \lambda^{p-1}(1+\lambda^p)} - \lambda^{p-1} Y_t^{f} (1+\lambda^p) \left( -mc_t^f + P_t^{j^f} \right) P_t^{j^f - 1 - \lambda^{p-1}(1+\lambda^p)} = 0$$
(27.24)

$$\epsilon_t^{\mathrm{b}} W_t^{\mathrm{disutil}^{\mathrm{f}}} \left( C_t^{\mathrm{f}} - h C_{t-1}^{\mathrm{f}} \right)^{-\sigma^{\mathrm{c}}} - \omega \epsilon_t^{\mathrm{b}} \epsilon_t^{\mathrm{L}} L_t^{\mathrm{s}^{\mathrm{f}} \sigma^{\mathrm{l}}} = 0$$

$$(27.25)$$

$$-1 + \xi^{\mathbf{p}} \left( \pi_t^{-1} \pi_{t-1}^{\gamma^{\mathbf{p}}} \right)^{-\lambda^{\mathbf{p}-1}} + (1 - \xi^{\mathbf{p}}) \pi_t^{\star - \lambda^{\mathbf{p}-1}} = 0$$
 (27.26)

$$-1 + (1 - \xi^{\mathbf{w}}) \left( w_t^{\star} W_t^{-1} \right)^{-\lambda^{\mathbf{w}-1}} + \xi^{\mathbf{w}} \left( W_{t-1} W_t^{-1} \right)^{-\lambda^{\mathbf{w}-1}} \left( \pi_t^{-1} \pi_{t-1} \gamma^{\mathbf{w}} \right)^{-\lambda^{\mathbf{w}-1}} = 0$$
 (27.27)

$$-\Phi - Y_t^{s} + \epsilon_t^{a} L_t^{1-\alpha} (K_{t-1} z_t)^{\alpha} = 0$$
 (27.28)

$$-\Phi - Y_t^{f} P_t^{f^{-\lambda^{P-1}(1+\lambda^{P})}} + \epsilon_t^{a} L_t^{f^{1-\alpha}} (K_{t-1}^{f} z_t^{f})^{\alpha} = 0$$
(27.29)

$$\eta_t^{\mathbf{b}} - \log \epsilon_t^{\mathbf{b}} + \rho^{\mathbf{b}} \log \epsilon_{t-1}^{\mathbf{b}} = 0 \tag{27.30}$$

$$-\eta_t^{\mathcal{L}} - \log \epsilon_t^{\mathcal{L}} + \rho^{\mathcal{L}} \log \epsilon_{t-1}^{\mathcal{L}} = 0 \tag{27.31}$$

$$\eta_t^{\mathcal{I}} - \log \epsilon_t^{\mathcal{I}} + \rho^{\mathcal{I}} \log \epsilon_{t-1}^{\mathcal{I}} = 0 \tag{27.32}$$

$$\eta_t^{\mathbf{w}} - f_t^1 + f_t^2 = 0 (27.33)$$

$$\eta_t^{\mathbf{a}} - \log \epsilon_t^{\mathbf{a}} + \rho^{\mathbf{a}} \log \epsilon_{t-1}^{\mathbf{a}} = 0 \tag{27.34}$$

$$\eta_t^{\rm p} - g_t^1 + g_t^2 (1 + \lambda^{\rm p}) = 0$$
 (27.35)

$$\eta_t^{\mathcal{G}} - \log \epsilon_t^{\mathcal{G}} + \rho^{\mathcal{G}} \log \epsilon_{t-1}^{\mathcal{G}} = 0 \tag{27.36}$$

$$-f_t^1 + \beta \xi^{\mathbf{w}} \mathbf{E}_t \left[ f_{t+1}^1 \left( w_t^{\star - 1} w_{t+1}^{\star} \right)^{\lambda^{\mathbf{w} - 1}} \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{\mathbf{w}}} \right)^{-\lambda^{\mathbf{w} - 1}} \right] + \epsilon_t^{\mathbf{b}} w_t^{\star} L_t \left( 1 + \lambda^{\mathbf{w}} \right)^{-1} \left( C_t - h C_{t-1} \right)^{-\sigma^{\mathbf{c}}} \left( w_t^{\star} W_t^{-1} \right)^{-\lambda^{\mathbf{w} - 1} (1 + \lambda^{\mathbf{w}})} = 0$$
 (27.37)

$$-f_t^2 + \beta \xi^{\mathbf{w}} \mathbf{E}_t \left[ f_{t+1}^2 \left( w_t^{\star - 1} w_{t+1}^{\star} \right)^{\lambda^{\mathbf{w} - 1} (1 + \lambda^{\mathbf{w}}) \left( 1 + \sigma^{\mathbf{l}} \right)} \left( \pi_{t+1}^{- 1} \pi_t^{\gamma^{\mathbf{w}}} \right)^{-\lambda^{\mathbf{w} - 1} (1 + \lambda^{\mathbf{w}}) \left( 1 + \sigma^{\mathbf{l}} \right)} \right] + \omega \epsilon_t^{\mathbf{b}} \epsilon_t^{\mathbf{L}} \left( L_t \left( w_t^{\star} W_t^{- 1} \right)^{-\lambda^{\mathbf{w} - 1} (1 + \lambda^{\mathbf{w}})} \right)^{1 + \sigma^{\mathbf{l}}} = 0$$
 (27.38)

$$-g_t^1 + \beta \xi^{\mathrm{p}} \pi_t^{\star} \mathbf{E}_t \left[ g_{t+1}^1 \pi_{t+1}^{\star^{-1}} \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{\mathrm{p}}} \right)^{-\lambda^{\mathrm{p}-1}} \right] + \epsilon_t^{\mathrm{b}} \pi_t^{\star} Y_t (C_t - hC_{t-1})^{-\sigma^{\mathrm{c}}} = 0$$
 (27.39)

$$-g_t^2 + \beta \xi^{\mathrm{p}} \mathbf{E}_t \left[ g_{t+1}^2 \left( \pi_{t+1}^{-1} \pi_t^{\gamma^{\mathrm{p}}} \right)^{-\lambda^{\mathrm{p}-1}(1+\lambda^{\mathrm{p}})} \right] + \epsilon_t^{\mathrm{b}} m c_t Y_t (C_t - h C_{t-1})^{-\sigma^{\mathrm{c}}} = 0$$
 (27.40)

$$-\nu_t^{\mathbf{w}} + (1 - \xi^{\mathbf{w}}) \left( w_t^{\star} W_t^{-1} \right)^{-\lambda^{\mathbf{w}-1} (1 + \lambda^{\mathbf{w}})} + \xi^{\mathbf{w}} \nu_{t-1}^{\mathbf{w}} \left( W_{t-1} \pi_t^{-1} W_t^{-1} \pi_{t-1}^{\gamma^{\mathbf{w}}} \right)^{-\lambda^{\mathbf{w}-1} (1 + \lambda^{\mathbf{w}})} = 0$$
 (27.41)

$$-\nu_t^{\mathbf{p}} + (1 - \xi^{\mathbf{p}}) \pi_t^{\star - \lambda^{\mathbf{p} - 1}(1 + \lambda^{\mathbf{p}})} + \xi^{\mathbf{p}} \nu_{t-1}^{\mathbf{p}} \left( \pi_t^{-1} \pi_{t-1} \gamma^{\mathbf{p}} \right)^{-\lambda^{\mathbf{p} - 1}(1 + \lambda^{\mathbf{p}})} = 0$$
 (27.42)

$$-K_t + K_{t-1}(1-\tau) + I_t \left(1 - 0.5\varphi \left(-1 + I_{t-1}^{-1} \epsilon_t^{\mathrm{I}} I_t\right)^2\right) = 0$$
(27.43)

$$-K_t^{f} + K_{t-1}^{f} (1 - \tau) + I_t^{f} \left( 1 - 0.5\varphi \left( -1 + I_{t-1}^{f} {}^{-1}\epsilon_t^{I} I_t^{f} \right)^2 \right) = 0$$
 (27.44)

$$U_{t} - \beta E_{t} \left[ U_{t+1} \right] - \epsilon_{t}^{b} \left( (1 - \sigma^{c})^{-1} \left( C_{t} - h C_{t-1} \right)^{1 - \sigma^{c}} - \omega \epsilon_{t}^{L} \left( 1 + \sigma^{l} \right)^{-1} L_{t}^{s + \sigma^{l}} \right) = 0$$
(27.45)

$$U_t^{f} - \beta E_t \left[ U_{t+1}^{f} \right] - \epsilon_t^{b} \left( (1 - \sigma^{c})^{-1} \left( C_t^{f} - h C_{t-1}^{f} \right)^{1 - \sigma^{c}} - \omega \epsilon_t^{L} \left( 1 + \sigma^{l} \right)^{-1} L_t^{s^{f} 1 + \sigma^{l}} \right) = 0$$
(27.46)

$$-\epsilon_{t}^{b}(C_{t} - hC_{t-1})^{-\sigma^{c}} + q_{t}\left(1 - 0.5\varphi\left(-1 + I_{t-1}^{-1}\epsilon_{t}^{I}I_{t}\right)^{2} - \varphi I_{t-1}^{-1}\epsilon_{t}^{I}I_{t}\left(-1 + I_{t-1}^{-1}\epsilon_{t}^{I}I_{t}\right)\right) + \beta\varphi I_{t}^{-2}E_{t}\left[\epsilon_{t+1}^{I}q_{t+1}I_{t+1}^{2}\left(-1 + I_{t}^{-1}\epsilon_{t+1}^{I}I_{t+1}\right)\right] = 0$$

$$(27.47)$$

$$-\epsilon_{t}^{\mathrm{b}}\left(C_{t}^{\mathrm{f}}-hC_{t-1}^{\mathrm{f}}\right)^{-\sigma^{\mathrm{c}}}+q_{t}^{\mathrm{f}}\left(1-0.5\varphi\left(-1+I_{t-1}^{\mathrm{f}}^{-1}\epsilon_{t}^{\mathrm{I}}I_{t}^{\mathrm{f}}\right)^{2}-\varphi I_{t-1}^{\mathrm{f}}^{-1}\epsilon_{t}^{\mathrm{I}}I_{t}^{\mathrm{f}}\left(-1+I_{t-1}^{\mathrm{f}}^{-1}\epsilon_{t}^{\mathrm{I}}I_{t}^{\mathrm{f}}\right)\right)+\beta\varphi I_{t}^{\mathrm{f}}^{-2}\mathrm{E}_{t}\left[\epsilon_{t+1}^{\mathrm{I}}q_{t+1}^{\mathrm{f}}I_{t+1}^{\mathrm{f}}^{2}\left(-1+I_{t}^{\mathrm{f}}^{-1}\epsilon_{t+1}^{\mathrm{I}}I_{t+1}^{\mathrm{f}}\right)\right]=0\tag{27.48}$$

$$\eta_t^{\pi} - \log \pi_t^{\text{obj}} + \rho^{\pi^{\text{bar}}} \log \pi_{t-1}^{\text{obj}} + \log \omega k r^{\pi^{\text{obj}}} \left( 1 - \rho^{\pi^{\text{bar}}} \right) = 0 \tag{27.49}$$

$$-C_t - I_t - T_t + Y_t - \psi^{-1} r_{ss}^k K_{t-1} \left( -1 + e^{\psi(-1+z_t)} \right) = 0$$
(27.50)

$$-abbr^{\pi} + \eta_{t}^{R} - \log\left(R_{ss}^{-1}R_{t}\right) + r^{\Delta^{\pi}}\left(-\log\left(\pi_{ss}^{-1}\pi_{t-1}\right) + \log\left(\pi_{ss}^{-1}\pi_{t}\right)\right) + r^{\Delta^{y}}\left(-\log\left(Y_{ss}^{-1}Y_{t-1}\right) + \log\left(Y_{ss}^{-1}Y_{t}\right)\right) + \log\left(Y_{ss}^{-1}Y_{t-1}\right) - \log\left(Y_{ss}^{-1}Y_{t}\right)\right) + \rho\log\left(R_{ss}^{-1}R_{t-1}\right) + (1-\rho)\left(\log\left(X_{ss}^{-1}X_{t-1}\right) + \log\left(X_{ss}^{-1}X_{t-1}\right)\right)\right) + \rho\log\left(X_{ss}^{-1}X_{t-1}\right) + \log\left(X_{ss}^{-1}X_{t-1}\right) + \log\left(X_{ss}$$

$$-C_t^{f} - I_t^{f} + \Pi_t^{ws^f} - T_t^{f} + Y_t^{f} + L_t^{s^f} W_t^{disutil^f} - L_t^{f} W_t^{f} - \psi^{-1} r_{ss}^{k^f} K_{t-1}^{f} \left( -1 + e^{\psi(-1 + z_t^f)} \right) = 0$$
(27.52)

$$\epsilon_t^{\rm b} \left( K_{t-1} r_t^{\rm k} - r_{\rm ss}^{\rm k} K_{t-1} e^{\psi(-1+z_t)} \right) \left( C_t - h C_{t-1} \right)^{-\sigma^{\rm c}} = 0 \tag{27.53}$$

$$\epsilon_{t}^{b} \left( K_{t-1}^{f} r_{t}^{k^{f}} - r_{ss}^{k^{f}} K_{t-1}^{f} e^{\psi \left( -1 + z_{t}^{f} \right)} \right) \left( C_{t}^{f} - h C_{t-1}^{f} \right)^{-\sigma^{c}} = 0 \tag{27.54}$$

# 28 Steady state relationships (after reduction)

$$-q_{\rm ss} + \beta \left( q_{\rm ss} \left( 1 - \tau \right) + \epsilon_{\rm ss}^{\rm b} \left( r_{\rm ss}^{\rm k} z_{\rm ss} - \psi^{-1} r_{\rm ss}^{\rm k} \left( -1 + e^{\psi(-1 + z_{\rm ss})} \right) \right) \left( C_{\rm ss} - h C_{\rm ss} \right)^{-\sigma^c} \right) = 0$$
 (28.1)

$$-q_{\rm ss}^{\rm f} + \beta \left( q_{\rm ss}^{\rm f} \left( 1 - \tau \right) + \epsilon_{\rm ss}^{\rm b} \left( r_{\rm ss}^{\rm k^{\rm f}} z_{\rm ss}^{\rm f} - \psi^{-1} r_{\rm ss}^{\rm k^{\rm f}} \left( -1 + e^{\psi \left( -1 + z_{\rm ss}^{\rm f} \right)} \right) \right) \left( C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f} \right)^{-\sigma^{\rm c}} \right) = 0 \tag{28.2}$$

$$-r_{\rm ss}^{\rm k} + \alpha \epsilon_{\rm ss}^{\rm a} m c_{\rm ss} L_{\rm ss}^{1-\alpha} (z_{\rm ss} K_{\rm ss})^{-1+\alpha} = 0$$
(28.3)

$$-r_{\rm ss}^{\rm kf} + \alpha \epsilon_{\rm ss}^{\rm a} m c_{\rm ss}^{\rm f} L_{\rm ss}^{\rm f}^{1-\alpha} \left( z_{\rm ss}^{\rm f} K_{\rm ss}^{\rm f} \right)^{-1+\alpha} = 0 \tag{28.4}$$

$$-G_{\rm ss} + T_{\rm ss} = 0 (28.5)$$

$$-G_{\rm ss} + G^{\rm bar} \epsilon_{\rm ss}^{\rm G} = 0 \tag{28.6}$$

$$-G_{\rm ss}^{\rm f} + T_{\rm ss}^{\rm f} = 0 (28.7)$$

$$-G_{\rm ss}^{\rm f} + G^{\rm bar} \epsilon_{\rm ss}^{\rm G} = 0 \tag{28.8}$$

$$-L_{\rm ss} + \nu_{\rm ss}^{\rm w-1} L_{\rm ss}^{\rm s} = 0 \tag{28.9}$$

$$-L_{\rm ss}^{\rm f} + L_{\rm ss}^{\rm f} \left(W_{\rm ss}^{\rm i^f} W_{\rm ss}^{\rm f^{-1}}\right)^{\lambda^{\rm w^{-1}}(-1-\lambda^{\rm w})} = 0$$
(28.10)

$$L_{\rm ss}^{\rm sf} - L_{\rm ss}^{\rm f} = 0$$
 (28.11)

$$L_{\rm ss}^{\rm sf} + \lambda^{\rm w-1} L_{\rm ss}^{\rm f} W_{\rm ss}^{\rm f-1} \left(-1 - \lambda^{\rm w}\right) \left(-W_{\rm ss}^{\rm disutil^{\rm f}} + W_{\rm ss}^{\rm if}\right) \left(W_{\rm ss}^{\rm if} W_{\rm ss}^{\rm f-1}\right)^{-1 + \lambda^{\rm w-1} \left(-1 - \lambda^{\rm w}\right)} = 0 \tag{28.12}$$

$$\Pi_{\rm ss}^{\rm ws^f} - L_{\rm ss}^{\rm sf} \left( -W_{\rm ss}^{\rm disutil^f} + W_{\rm ss}^{\rm if} \right) = 0$$
 (28.13)

$$\Pi_{\rm ss}^{\rm psf} - Y_{\rm ss}^{\rm f} \left( -mc_{\rm ss}^{\rm f} + P_{\rm ss}^{\rm jf} \right) P_{\rm ss}^{\rm jf} = 0 \tag{28.14}$$

$$-Q_{\rm ss} + \epsilon_{\rm ss}^{\rm b}^{-1} q_{\rm ss} (C_{\rm ss} - hC_{\rm ss})^{\sigma^{c}} = 0$$
 (28.15)

$$-Q_{\rm ss}^{\rm f} + \epsilon_{\rm ss}^{\rm b}^{-1} q_{\rm ss}^{\rm f} \left(C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f}\right)^{\sigma^{\rm c}} = 0 \tag{28.16}$$

$$-W_{\rm ss} + \epsilon_{\rm ss}^{\rm a} m c_{\rm ss} \left(1 - \alpha\right) L_{\rm ss}^{-\alpha} \left(z_{\rm ss} K_{\rm ss}\right)^{\alpha} = 0 \tag{28.17}$$

$$-W_{\rm ss}^{\rm f} + \epsilon_{\rm ss}^{\rm a} m c_{\rm ss}^{\rm f} (1 - \alpha) L_{\rm ss}^{\rm f}^{-\alpha} (z_{\rm ss}^{\rm f} K_{\rm ss}^{\rm f})^{\alpha} = 0$$
 (28.18)

$$Y_{\rm ss}^{\rm s} - \nu_{\rm ss}^{\rm p} Y_{\rm ss} = 0 \tag{28.19}$$

$$-Y_{\rm ss}^{\rm f} + Y_{\rm ss}^{\rm s^{\rm f}} = 0 ag{28.20}$$

$$-Y_{\rm ss}^{\rm sf} + Y_{\rm ss}^{\rm f} P_{\rm ss}^{\rm jf}^{-\lambda^{\rm p-1}(1+\lambda^{\rm p})} = 0 \tag{28.21}$$

$$\beta \epsilon_{\rm ss}^{\rm b} \left( C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f} \right)^{-\sigma^{\rm c}} - \epsilon_{\rm ss}^{\rm b} R_{\rm ss}^{\rm f}^{-1} \left( C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f} \right)^{-\sigma^{\rm c}} = 0 \tag{28.22}$$

$$-\epsilon_{\rm ss}^{\rm b} R_{\rm ss}^{-1} (C_{\rm ss} - hC_{\rm ss})^{-\sigma^{\rm c}} + \beta \epsilon_{\rm ss}^{\rm b} \pi_{\rm ss}^{-1} (C_{\rm ss} - hC_{\rm ss})^{-\sigma^{\rm c}} = 0$$
(28.23)

$$Y_{\rm ss}^{\rm f} P_{\rm ss}^{\rm j^{\rm f} - \lambda^{\rm p-1}(1+\lambda^{\rm p})} - \lambda^{\rm p-1} Y_{\rm ss}^{\rm f} (1+\lambda^{\rm p}) \left( -mc_{\rm ss}^{\rm f} + P_{\rm ss}^{\rm j^{\rm f}} \right) P_{\rm ss}^{\rm j^{\rm f} - 1 - \lambda^{\rm p-1}(1+\lambda^{\rm p})} = 0 \tag{28.24}$$

$$\epsilon_{\rm ss}^{\rm b} W_{\rm ss}^{\rm disutil^f} \left( C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f} \right)^{-\sigma^c} - \omega \epsilon_{\rm ss}^{\rm b} \epsilon_{\rm ss}^{\rm L} L_{\rm ss}^{\rm f}^{\sigma^l} = 0 \tag{28.25}$$

$$-1 + \xi^{p} \left( \pi_{ss}^{-1} \pi_{ss}^{\gamma^{p}} \right)^{-\lambda^{p-1}} + (1 - \xi^{p}) \pi_{ss}^{\star - \lambda^{p-1}} = 0$$
(28.26)

$$-1 + (1 - \xi^{\mathbf{w}}) \left( w_{ss}^{\star} W_{ss}^{-1} \right)^{-\lambda^{\mathbf{w}-1}} + \xi^{\mathbf{w}} 1^{-\lambda^{\mathbf{w}-1}} \left( \pi_{ss}^{-1} \pi_{ss}^{\gamma^{\mathbf{w}}} \right)^{-\lambda^{\mathbf{w}-1}} = 0$$
 (28.27)

$$-\Phi - Y_{\rm ss}^{\rm s} + \epsilon_{\rm ss}^{\rm a} L_{\rm ss}^{1-\alpha} (z_{\rm ss} K_{\rm ss})^{\alpha} = 0 \tag{28.28}$$

$$-\Phi - Y_{\rm ss}^{\rm f} P_{\rm ss}^{\rm i^{\rm f}} - \lambda^{\rm p-1} (1+\lambda^{\rm p}) + \epsilon_{\rm ss}^{\rm a} L_{\rm ss}^{\rm f} {}^{1-\alpha} (z_{\rm ss}^{\rm f} K_{\rm ss}^{\rm f})^{\alpha} = 0$$
 (28.29)

$$-\log \epsilon_{\rm ss}^{\rm b} + \rho^{\rm b} \log \epsilon_{\rm ss}^{\rm b} = 0 \tag{28.30}$$

$$-\log \epsilon_{\rm ss}^{\rm L} + \rho^{\rm L} \log \epsilon_{\rm ss}^{\rm L} = 0 \tag{28.31}$$

$$-\log \epsilon_{\rm ss}^{\rm I} + \rho^{\rm I} \log \epsilon_{\rm ss}^{\rm I} = 0 \tag{28.32}$$

$$-f_{\rm ss}^1 + f_{\rm ss}^2 = 0 (28.33)$$

$$-\log \epsilon_{\rm ss}^{\rm a} + \rho^{\rm a} \log \epsilon_{\rm ss}^{\rm a} = 0 \tag{28.34}$$

$$-g_{\rm ss}^1 + g_{\rm ss}^2 (1 + \lambda^{\rm p}) = 0 \tag{28.35}$$

$$-\log \epsilon_{\rm ss}^{\rm G} + \rho^{\rm G} \log \epsilon_{\rm ss}^{\rm G} = 0 \tag{28.36}$$

$$-f_{ss}^{1} + \beta \xi^{w} f_{ss}^{1} 1^{\lambda^{w-1}} \left( \pi_{ss}^{-1} \pi_{ss}^{\gamma^{w}} \right)^{-\lambda^{w-1}} + \epsilon_{ss}^{b} w_{ss}^{\star} L_{ss} \left( 1 + \lambda^{w} \right)^{-1} \left( C_{ss} - h C_{ss} \right)^{-\sigma^{c}} \left( w_{ss}^{\star} W_{ss}^{-1} \right)^{-\lambda^{w-1} (1 + \lambda^{w})} = 0$$
(28.37)

$$-f_{\rm ss}^2 + \omega \epsilon_{\rm ss}^b \epsilon_{\rm ss}^L \left( L_{\rm ss} \left( w_{\rm ss}^{\star} W_{\rm ss}^{-1} \right)^{-\lambda^{\rm w}^{-1} (1+\lambda^{\rm w})} \right)^{1+\sigma^{\rm l}} + \beta \xi^{\rm w} f_{\rm ss}^2 1^{\lambda^{\rm w}^{-1} (1+\lambda^{\rm w}) \left( 1+\sigma^{\rm l} \right)} \left( \pi_{\rm ss}^{-1} \pi_{\rm ss}^{\gamma^{\rm w}} \right)^{-\lambda^{\rm w}^{-1} (1+\lambda^{\rm w}) \left( 1+\sigma^{\rm l} \right)} = 0$$
(28.38)

$$-g_{ss}^{1} + \beta \xi^{p} g_{ss}^{1} \left(\pi_{ss}^{-1} \pi_{ss}^{\gamma^{p}}\right)^{-\lambda^{p-1}} + \epsilon_{ss}^{b} \pi_{ss}^{\star} Y_{ss} \left(C_{ss} - hC_{ss}\right)^{-\sigma^{c}} = 0$$
(28.39)

$$-g_{\rm ss}^2 + \beta \xi^{\rm p} g_{\rm ss}^2 \left(\pi_{\rm ss}^{-1} \pi_{\rm ss}^{\gamma^{\rm p}}\right)^{-\lambda^{\rm p-1}(1+\lambda^{\rm p})} + \epsilon_{\rm ss}^{\rm b} m c_{\rm ss} Y_{\rm ss} (C_{\rm ss} - h C_{\rm ss})^{-\sigma^{\rm c}} = 0$$
(28.40)

$$-\nu_{\rm ss}^{\rm w} + (1 - \xi^{\rm w}) \left(w_{\rm ss}^{\star} W_{\rm ss}^{-1}\right)^{-\lambda^{\rm w}-1} (1 + \lambda^{\rm w}) + \xi^{\rm w} \nu_{\rm ss}^{\rm w} \left(\pi_{\rm ss}^{-1} \pi_{\rm ss}^{\gamma^{\rm w}}\right)^{-\lambda^{\rm w}-1} (1 + \lambda^{\rm w}) = 0 \tag{28.41}$$

$$-\nu_{\rm ss}^{\rm p} + (1 - \xi^{\rm p}) \,\pi_{\rm ss}^{\star - \lambda^{\rm p-1}(1 + \lambda^{\rm p})} + \xi^{\rm p} \nu_{\rm ss}^{\rm p} \left(\pi_{\rm ss}^{-1} \pi_{\rm ss}^{\gamma^{\rm p}}\right)^{-\lambda^{\rm p-1}(1 + \lambda^{\rm p})} = 0 \tag{28.42}$$

$$-K_{\rm ss} + I_{\rm ss} \left( 1 - 0.5\varphi \left( -1 + \epsilon_{\rm ss}^{\rm I} \right)^2 \right) + K_{\rm ss} \left( 1 - \tau \right) = 0 \tag{28.43}$$

$$-K_{\rm ss}^{\rm f} + I_{\rm ss}^{\rm f} \left(1 - 0.5\varphi \left(-1 + \epsilon_{\rm ss}^{\rm I}\right)^{2}\right) + K_{\rm ss}^{\rm f} \left(1 - \tau\right) = 0 \tag{28.44}$$

$$U_{\rm ss} - \beta U_{\rm ss} - \epsilon_{\rm ss}^{\rm b} \left( (1 - \sigma^{\rm c})^{-1} \left( C_{\rm ss} - h C_{\rm ss} \right)^{1 - \sigma^{\rm c}} - \omega \epsilon_{\rm ss}^{\rm L} \left( 1 + \sigma^{\rm l} \right)^{-1} L_{\rm ss}^{\rm s}^{1 + \sigma^{\rm l}} \right) = 0$$
 (28.45)

$$U_{\rm ss}^{\rm f} - \beta U_{\rm ss}^{\rm f} - \epsilon_{\rm ss}^{\rm b} \left( (1 - \sigma^{\rm c})^{-1} \left( C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f} \right)^{1 - \sigma^{\rm c}} - \omega \epsilon_{\rm ss}^{\rm L} \left( 1 + \sigma^{\rm l} \right)^{-1} L_{\rm ss}^{\rm f}^{1 + \sigma^{\rm l}} \right) = 0 \tag{28.46}$$

$$-\epsilon_{\rm ss}^{\rm b}(C_{\rm ss} - hC_{\rm ss})^{-\sigma^{\rm c}} + q_{\rm ss}\left(1 - 0.5\varphi\left(-1 + \epsilon_{\rm ss}^{\rm I}\right)^2 - \varphi\epsilon_{\rm ss}^{\rm I}\left(-1 + \epsilon_{\rm ss}^{\rm I}\right)\right) + \beta\varphi\epsilon_{\rm ss}^{\rm I}q_{\rm ss}\left(-1 + \epsilon_{\rm ss}^{\rm I}\right) = 0 \tag{28.47}$$

$$-\epsilon_{\rm ss}^{\rm b} \left(C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f}\right)^{-\sigma^{\rm c}} + q_{\rm ss}^{\rm f} \left(1 - 0.5\varphi \left(-1 + \epsilon_{\rm ss}^{\rm I}\right)^2 - \varphi \epsilon_{\rm ss}^{\rm I} \left(-1 + \epsilon_{\rm ss}^{\rm I}\right)\right) + \beta \varphi \epsilon_{\rm ss}^{\rm I} q_{\rm ss}^{\rm f} \left(-1 + \epsilon_{\rm ss}^{\rm I}\right) = 0 \tag{28.48}$$

$$-\log \pi_{\rm ss}^{\rm obj} + \rho^{\pi^{\rm bar}} \log \pi_{\rm ss}^{\rm obj} + \log \operatorname{addr}^{\pi^{\rm obj}} \left( 1 - \rho^{\pi^{\rm bar}} \right) = 0 \tag{28.49}$$

$$-C_{ss} - I_{ss} - T_{ss} + Y_{ss} - \psi^{-1} r_{ss}^{k} K_{ss} \left( -1 + e^{\psi(-1 + z_{ss})} \right) = 0$$
(28.50)

$$-abbr^{\pi} + (1 - \rho) \left( \log \pi_{ss}^{obj} - r^{\pi} \log \pi_{ss}^{obj} \right) = 0$$

$$(28.51)$$

$$-C_{\rm ss}^{\rm f} - I_{\rm ss}^{\rm f} + \Pi_{\rm ss}^{\rm ws^{\rm f}} - T_{\rm ss}^{\rm f} + Y_{\rm ss}^{\rm f} + L_{\rm ss}^{\rm f} W_{\rm ss}^{\rm disutil^{\rm f}} - L_{\rm ss}^{\rm f} W_{\rm ss}^{\rm f} - \psi^{-1} r_{\rm ss}^{\rm k^{\rm f}} K_{\rm ss}^{\rm f} \left( -1 + e^{\psi \left( -1 + z_{\rm ss}^{\rm f} \right)} \right) = 0 \tag{28.52}$$

$$\epsilon_{\rm ss}^{\rm b} \left( r_{\rm ss}^{\rm k} K_{\rm ss} - r_{\rm ss}^{\rm k} K_{\rm ss} e^{\psi(-1+z_{\rm ss})} \right) \left( C_{\rm ss} - h C_{\rm ss} \right)^{-\sigma^{\rm c}} = 0$$
(28.53)

$$\epsilon_{\rm ss}^{\rm b} \left( r_{\rm ss}^{\rm f} K_{\rm ss}^{\rm f} - r_{\rm ss}^{\rm f} K_{\rm ss}^{\rm f} e^{\psi \left( -1 + z_{\rm ss}^{\rm f} \right)} \right) \left( C_{\rm ss}^{\rm f} - h C_{\rm ss}^{\rm f} \right)^{-\sigma^{\rm c}} = 0$$
 (28.54)

# 29 Calibrating equations

$$-1.408 + Y_{ss}^{s-1} \left(\Phi + Y_{ss}^{s}\right) = 0 \tag{29.1}$$

$$-1 + \pi_{\rm ss}^{\rm obj} = 0$$
 (29.2)

$$-0.6 + C_{\rm ss}^{\rm f} Y_{\rm ss}^{\rm f^{-1}} = 0 (29.3)$$

$$-0.18 + G_{\rm ss}Y_{\rm ss}^{-1} = 0 (29.4)$$

$$\pi_{\rm ss} - \pi_{\rm ss}^{\rm obj} = 0 \tag{29.5}$$

# 30 Parameter settings

$$\alpha = 0.3 \tag{30.1}$$

$$\beta = 0.99 \tag{30.2}$$

$$\gamma^{\mathrm{w}} = 0.763 \tag{30.3}$$

$$\gamma^{\mathbf{p}} = 0.469 \tag{30.4}$$

$$h = 0.573 (30.5)$$

$$\lambda^{\mathbf{w}} = 0.5 \tag{30.6}$$

$$\omega = 1 \tag{30.7}$$

$$\psi = 0.169 \tag{30.8}$$

$$r^{\pi} = 1.684 \tag{30.9}$$

$$r^{Y} = 0.099 (30.10)$$

$$r^{\Delta^{\pi}} = 0.14 \tag{30.11}$$

$$r^{\Delta^{y}} = 0.159 \tag{30.12}$$

$$\rho^{\rm b} = 0.855 \tag{30.13}$$

$$\rho^{\rm L} = 0.889 \tag{30.14}$$

$$\rho^{\rm I} = 0.927 \tag{30.15}$$

$$\rho^{a} = 0.823 \tag{30.16}$$

$$\rho^{G} = 0.949 \tag{30.17}$$

$$\rho = 0.961 \tag{30.18}$$

$$\rho^{\pi^{\text{bar}}} = 0.924 \tag{30.19}$$

$$\sigma^{c} = 1.353$$
 (30.20)

$$\sigma^{l} = 2.4 \tag{30.21}$$

$$\tau = 0.025 \tag{30.22}$$

$$\varphi = 6.771 \tag{30.23}$$

$$\xi^{W} = 0.737 \tag{30.24}$$

$$\xi^{\rm p} = 0.908 \tag{30.25}$$