

□ Class P: buys_computer = "yes"

□ Class N: buys_computer = "no"

$$Info(D) = I(9,5) = -\frac{9}{14} \log_2\left(\frac{9}{14}\right) - \frac{5}{14} \log_2\left(\frac{5}{14}\right) = 0.940$$

age	p _i	n _i	I(p _i , n _i)
<=30	2	3	0.971
31...40	4	0	0
>40	3	2	0.971

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$$Info_{age}(D) = \frac{5}{14} I(2,3) + \frac{4}{14} I(4,0) + \frac{5}{14} I(3,2) = 0.694$$

$\frac{5}{14} I(2,3)$ means "age <=30" has 5 out of 14 samples, with 2 yes'es and 3 no's.

Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

Similarly, we can get

$$Gain(income) = 0.029$$

$$Gain(student) = 0.151$$

$$Gain(credit_rating) = 0.048$$

$$Info(D) = I(8,4) = -\log(8/12)\log_2(8/12) - (4/12)\log_2(4/12) = 0.9183$$

Infoage(D)

Age	p _i	n _i	I(p _i , n _i)
<=30	2	2	1
31...40	3	0	0
>40	3	2	0.737

$$Infoage(D): 4/12(I(2,2)) + 3/12(I(3,0)) + 5/12(I(3,2)) = 0.64$$

$$Gain(age) = 0.918 - 0.64 = 0.278$$

Infoincome(D)

Income	P _i	N _i	I(p _i , n _i)
High	2	2	1
Medium	4	1	0.722
Low	2	1	0.918

$$Infoincome(D) = 0.864$$

$$Gain(student) = 0.918 - 0.864 = 0.054$$

Infostudent

student	P _i	N _i	I(p _i , n _i)
Yes	5	1	0.65
No	3	3	1

$$Infostudent(D) = 0.825$$

$$Gain(student) = 0.918 - 0.825 = 0.093$$

Infocredit

Credit_rating	Pi	Ni	I(pi,ni)
Fair	6	1	0.592
Excellent	2	3	0.971

Infocredit = 0.749

Gain(credit)= 0.169

Age มีค่าGainมากที่สุดจึงเลือก age เป็น root node

