
UM-SJTU JOINT INSTITUTE
INTRODUCTION TO CRYPTOGRAPHY
(VE475)

PROJECT REPORT

GROUP 1

BITCOIN

Name: Liu Niyiqu	ID: 516370910118
Name: Xiang Zhiyuan	ID: 516370910118
Name: Zhu Hanqi	ID: 515370910113
Name: Li Ruohan	ID: 515370910083

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1 Introduction

1.1 Traditional Coins and Banks

Long time ago, in a trading system, participants would exchange their goods or services without medium of change. It is not efficient because it is hard to find a pair participant who exactly has the corresponding desire. Then, people start to use precious metal as medium of change due to its stability and rarity. Later, currency is invented to work as medium of change, which contributes to the foundation of a modern society. Trade becomes easier with currency. In current society, electric trade start to grow rapidly, in which people can merchandise goods and services not using currency but money stored in banks or online payments such as Alipay.

This electric trade is innovative when it enables long-distance and quick trade globally. However, this kind of currency still requires credit endorsement from countries and banks. If Alice transfers her money to a bank, then the bank first verifies that the money are of authority, and provides Alice some promise that she can take away her money or directly transfer the money to others. Bob who is going to accept money from Alice, would get the transferred amount from the bank about the amount he get. In this simple transition procedure, bank plays an important role as a middleman as well as provide credit endorsement for both sides.

There are problems in this common trade scheme.

- The cost is high. Bank would ask both sides in the trade for handling fee as income of the bank.
- It is slow. The service requires time to check user's information and complete the procedures.
- It is not anonymous.
- Trade between countries and areas are harder to complete. This involves problems of exchange rate.

1.2 Creation of Bitcoins

In 2008, Satoshi Nakamoto published a paper "Bitcoin: A Peer-to-Peer Electronic Cash System", putting forward a kind of electronic cash system constructed on the basis of cryptography. Instead of traditional credit endorsement of countries and banks, Satoshi uses cryptography as the basis of cash system. Satoshi states that "A purely peer-to-peer version of electronic

cash would allow online payments to be sent directly from one party to another without going through a financial institution.”[1] In his design, people can trade with others with bitcoins peer to peer with no third parties, and the safety is still ensured. This is a cash system with no extra cost, perfect speed, anonymity and totally no threshold.

Especially in the society with giant number of commerce on the Internet, financial institutes as third parties are essential to deal with electronic payments. This commerce model depends on trust and costs a number of transaction cost. Satoshi proposes ”a solution to the double-spending problem using a peer-to-peer distributed timestamp server to generate computational proof of the chronological order of transactions.”[1] The system is computationally secure because only when the attacker node can control more CPU power than all the other users collectively worldwide. It is impossible in cryptography.

The number of bitcoins is limited so as not to reduce their value. A user can mine bitcoins by running the program. The complexity is very high and the number of bitcoins mined in a period of time is certain. When user mine the solution, all the other users can get to know. It is hard to find, but easy to verify. The number of bitcoins remaining to be mined is reducing. In total, there are no more than 21 million bitcoins. [1]

2 Fundamentals in Cryptography

As is illustrated before, bitcoins are constructed on the foundation of Cryptography. In this section, some basic cryptography concepts and working principles are explained.

2.1 Hash Functions

A hash function is used to map an arbitrary-length data into a data of fixed length. It also verifies the properties:

- The hashing result is efficiently computed for any input.
- It is computationally infeasible to discover two values x and x' such that $x \neq x'$ and $h(x) = h(x')$. This property is called ”Collision Resistant”.

The properties of hash function can protect the original information, prevent information being tampered, verify authentication and etc. It is a general concept while various hash functions have wide applications in cryptography as well as in the world of bitcoins.

2.2 Merkle Tree

Merkle tree is a special form of hash function, which has wide applications in peer-to-peer transition. Merkle tree allows efficient and secure verification for data of large size. In a merkle tree, every leaf node is hash result of a block of information. The leaves of a merkle tree are the hash results of the blocks of the original data. Then, hashing goes upwards. Nodes in a merkle tree are the hashing result of its respective children. This procedure continues until the root of merkle tree is obtained. Usually, a merkle tree is a binary tree.

In a peer-to-peer network, Merkle Tree is used to make sure that data blocks received are not corrupted or replaced with great efficiency.

2.3 Digital Signature

Digital signature typically composes of three parts:

- Key generation.

Select the private key randomly.

- Signing.

A signature is produce by assigning a message with the private key.

- Verifying.

Verify whether there is authentication with signature, public key and message.

There two important properties of digital signature: (1) the authenticity of a digital signature can be verifies with the corresponding public key; (2) is is computationally infeasible to generate a signature which can be verified by the public key without knowing the corresponding private key.

2.4 SHA-256 Signature

SHA is the simplified form of "Secure Hash Algorithm". SHA-2 is a set of cryptographic hash functions design with MerkleDamgrd structure. SHA-256 is one hash function in SHA-2. These functions share similar structure. SHA-256 computes with 32-bit words. It has great performance on security and efficiency.

2.5 RIPEMD160

RIPEMD is the simplified form of "RIPE Message Digest", and it represents a set of cryptographic hash functions with MerkleDamgrd construction. RIPEMD160 is one reversed and strengthened version in this family, and it is commonly used for academy. It is designed for longer hash results with safety. RIPMED160 can produce 160-bit hash digest.

2.6 Base58Check Encoding

Instead of Base64, in bitcoin Base58 Encoding is adopted. The number 0, uppercase letters O,I, lower case letter i and special symbols +,/ are eliminated from the base. The reason why not taking the number ans letters is these may look extremely similar in some fonts, and Satoshi hopes to obtain visually identitital strings. This base also provides the possibility for double click in most applications.

3 Transaction

3.1 Overview

One important thing of which Bitcoin currency is very different from common cash is that, what you receive will not add up or mix up together. The Bitcoin system is like a public account book, it writes:

Bob pays Alice 2 BTC
Alice pays you 1 BTC
You pay Bob 0.5 BTC
...

how much bitcoin you have is not a total number, but all the payments that you receive from others according to your address, or say your public key. The payments are independent and will not mix up, and whenever you spend bitcoin, the amount you pay others is just from the previous payments you received previously.

Of course, a real transaction in Bitcoin system is no as simple as a sentence saying who pays whom how much. A transaction is mainly composed of the following parts:

- Input refers to which output (or outputs) does the currency that you want to send comes from.

- The output is the amount sent to the bitcoin address (via standard transactions) and a set of rules for unlocking the output amount. In Bitcoin terms, the output is called "unspent transaction output" or UTXO. Any bitcoin amount we receive is locked at the receiving address.
- Metadata, including transaction ID, transaction format version, number of input amounts, number of output amounts, lock time, and size of transaction (in bytes).

A transaction can have multiple inputs or outputs. For multiple outputs, we take the example at the beginning, and assume that you just enter the Bitcoin world, so all you received is from Alice's payment to you, and you want to pay Bob 0.5BTC. As mentioned before, bitcoin is not like cash in the wallet, you are not deducting 0.5BTC from 1BTC that you have, but dividing the 1BTC to two separate outputs: one is 0.5BTC to Bob, the other is the rest of the bitcoins, say your "change". The output back to you could be less than 0.5BTC, with some of it sparing to a "transaction fee" (see also Section 4). Multiple inputs are even easier to think of: if you are paying Bob 0.5BTC, you can use two outputs from previous confirmed transactions to your address, like "Alice pays you 0.1BTC" and "John pays you 0.4BTC", or "Alice pays you 0.3BTC" and "John pays you 0.3BTC", in this way you'll have two inputs and two outputs.

3.2 Bitcoin Wallet

Before entering Bitcoin market, you must have a "wallet" of bitcoin. This wallet does not store any bitcoin you own, but stores your public and private keys. Bitcoin exchanges use the software to generate these two keys for you and put them in your wallet.

According to the Bitcoin protocol, the length of the public key is 512 bits. Since the length is quite long and inconvenient to display or spread, the public key will be hashed using SHA-256 hashing and then RIPEMD-160 thus to generate an address. The address is encoded by Base58 into one string composed of English letters and numbers and its length is fixed to 160 bits, which is easier for displaying and spreading. Briefly speaking, a transaction is bitcoin's transferring from one address to another. When some other party pays you bitcoin, they only need to know your wallet address and make payment to the address.

In later transaction steps, the wallet address will be certified by a private key.

The public key can be known to all, but the private key should be kept secret. If the private key is stolen by others, they can use your identity and transfer the bitcoin to their own wallet.

3.3 Process and Verify the Transaction

The Bitcoin protocol stipulates that in a certain transaction case, in addition to the transaction amount, the payer must also provide the following data:

- Hash of the last transaction(s), so the source of this amount of bitcoins is clarified.
- The address of both the payer and the receiver.
- Payer's public key.
- The digital signature generated by the payer's private key.

The payer will also need to inform all the nodes in the Bitcoin network to let them verify the transaction. The verification steps include:

1. Finding the previous transaction(s) and confirm the payer's bitcoin source. This ensures that you have enough bitcoin to complete the transaction. Since all the bitcoin transaction records are public, this step is quite clear and easy to complete.
2. Calculating the signature of the payer's public key and confirming that it is consistent with the payer's address. This ensures that the public key truly exists.
3. Using the public key to unlock the digital signature. This ensures that the private key is true, so that no one is using other's public key to forge transactions.

3.4 Adding Transaction to Block

After verifying the transaction, the whole transaction is still not fully completed. Once a transaction is verified, the information of this transaction should be added to a block, and the block can be connected to a blockchain. If one wants to tamper with a transaction, all the blocks in the blockchain need changing, and this is basically impossible (Section 5).

In the procedure of adding a transaction to block, three hashes are involved. First is the hash of the transaction itself. As mentioned above, a

transaction may contain multiple inputs and outputs. By arranging these inputs and outputs and hashing them, a unique hash value of a transaction can be obtained. Second is the Merkle hash root of all transactions in the current block. The third one is the block hash, when hashing the whole block, the Merkle hash root is used as a parameter, so that the information of all transactions is reflected in the hash of a block.

4 Mining

4.1 Definition of Mining

The bitcoin is a decentralized cryptocurrent. No authorities are present to authenticate each transaction. Thus the burden of verifying transactions and gathering valid transactions lies to the miners. The ultimate goal of a miner is to constitute a block by solving a mathematical problem, which will be described in the next section. To compensate the computational power spent by the miner, some bitcoins are given to the first miner that create a new block. Also, the payer in a transaction may specify a transaction fee that will be given to the miner.

4.2 Mathematics of Mining

4.2.1 Proof of Work

The cost function is define as

$$\begin{aligned}\mathcal{F} : \mathcal{S} \times \mathbb{N}^* \times \mathbb{N}^* &\longrightarrow \{\text{True}, \text{False}\} \\ (s, D, x) &\longmapsto \mathcal{F}(s, D, x)\end{aligned}$$

The set \mathcal{S} is the set of strings. $D \in \mathbb{N}^*$ is the difficulty level of this problem and x is called a nonce. $\mathcal{F}(s, D, x)$ returns true if and only if $\text{Hash}(A|D|x)$ starts with D zeros.

In the case of bitcoin, the hash function SHA-256 is used. In practice, s and D is fixed, the process of proof of work is to find a nonce x such that $\mathcal{F}(s, D, x)$ returns true. An simplified example of proof of work is shown in Fig. 1. In this process the nonce x is chosen in the order of the natural numbers.

4.2.2 Mining a New Block

The mining process is to solve the problem given by proof of work. At a given time, a node would gather transactions and form a block. To add this

```

"Hello, world!0" => 1312af178c253f84028d480a6adc1e25e81caa44c749ec81976192e2ec934c64
"Hello, world!1" => e9afc424b79e4f6ab42d99c81156d3a17228d6e1eef4139be78e948a9332a7d8
"Hello, world!2" => ae37343a357a8297591625e7134cbea22f5928be8ca2a32aa475cf05fd4266b7
...
"Hello, world!4248" => 6e110d98b388e77e9c6f042ac6b497cec46660deef75a55ebc7cfd65cc0b965
"Hello, world!4249" => c004190b822f1669cac8dc37e761cb73652e7832fb814565702245cf26ebb9e6
"Hello, world!4250" => 0000c3af42fc31103f1fdc0151fa747ff87349a4714df7cc52ea464e12dcd4e9

```

Figure 1: Example of a proof of work. [2]

block to the block chain, the node has to solve the following problem:

Looking for a nonce x such that: $Hash(s|x) < \text{target}$

$s = s_1|s_2|s_3|s_4|s_5$

$s_1 = \text{version}$

$s_2 = \text{hash of previous block}$

$s_3 = \text{hash of merkle root}$

$s_4 = \text{timestamp}$

$s_5 = \text{target}$

A block is composed of a block header and a block body. The block header is defined as $s|x$. Once a suitable nonce x is found, the miner is can publish this block and add it to the block chain.

4.2.3 Adjustment of Difficulties

Let T be random variable that represents the time required to mine a new block. The bitcoin protocol specifies that

$$E[T] = \tau_0 = 600 \quad [\text{seconds}]$$

But the computational power of the miner may differ, so the difficulty level is adjusted once 2016 blocks are mined (two weeks) to make $E[T] = 600$. The formula is given by

$$D_{\text{new}} = D_{\text{old}} \cdot \frac{t}{2016 \cdot \tau_0}$$

t is the time spent to mine the last 2016 blocks.

The random variable T follows a exponential distribution

$$f_T(x) = \alpha e^{-\alpha x}$$

$$\alpha = \frac{1}{600} \quad [\text{seconds}^{-1}]$$

4.3 General Procedure of Mining

1. Alice gathers the transactions and put them in a block (a block can contain approximately 4,000 transactions)
2. Alice tries to solve the proof of work by finding a suitable nonce x
3. If Alice is the first one to mine a new block, she may announce the block to the public and add it to the block chain
4. If in the process of mining, a new block is mined by Bob. Alice abandons her block and restart step 1.

4.4 The Byzantine Generals' Problem

A number of Byzantine Generals each has his own computer. They communicate through Internet to devise a plan to attack king's army. Only with a joint forces between the generals can they beat the king's army. However, several generals are spies deplored by the king. They would try to sabotage the proposed good plans. In this situation, the Byzantine General's Problem is given by how to agree upon a feasible plan to attack the king's army, given the condition that most of the generals (more than half in the case of bitcoin) are honest.

In the set up of bitcoin, the Byzantine Generals' Problem is solved by the mining process at the cost of computational power (electricity). With the hard "inverse hash" step in the proof of work, the bitcoin system guarantees that no malicious user can double spend their bitcoins or forge a transaction, as will be shown in the next section.

4.5 Possible Attacks Prevented by the Mining Process

Now Eve has ten bitcoins and she proposes transactions to both Bob and Alice to give them ten bitcoins each. In the meantime, there are two miners Charlie and Manuel.

1. Eve announces a 10-bitcoin-transaction to both Bob and Alice. (She only has 10 bitcoins left)
2. Charlie first receives Eve's transaction to Alice, so he ignores Eve's transaction request to Bob.
3. Due to delay of the Internet, Manuel first receives Eve's transaction to Bob. So he ignores Eve's transaction request to Alice.

4. Charlie and Manuel gather some transactions and both start to mine a block.
5. Without lose of generality, let's assume Manuel beats Charlie and solve the proof of work problem. Manuel happily add this new block to block chain.
6. Then Charlie would abandon his block. While gathering transactions for a new block, he would ignore Eve's transaction request because Eve's has already gave her remaining 10 bitcoins to Bob in the previous block mined by Manuel.

Eve failed to double spend her bitcoin. She now tries to forge bitcoin transactions to make her rich. The only way she can forge bitcoins is to alter previous transaction records. To do so, she would have to recalculate a block.

1. In a block B_i , there is a transaction record that Eve paid 10 bitcoins to Bob
2. Eve discard this record. Then she need to solve the proof of work problem again for this block.
3. Eve solves this block. However since the block chain is a linked chain, she would have to recalculate all the subsequent blocks.

From the above discussion, we can see that Eve can only commit forgery if she has more computational powers than all the other honest parties in the mining pool, since we always take the longest chain to be the correct one.

5 Definition of Blockchain

Blockchain, by definition, is a growing list of records that are linked using cryptography, these records are also called as blocks. The beginning of the blockchain, which is the first block in this blockchain, is called as genesis block, every new generated block is then linked to the last block in the chain. For different blockchain, it may have different block structure, and different way to link the blocks. In cryptocurrency bitcoin, a special blockchain serves as the public ledger for all transactions on the network.

Thus, when implementing a blockchain, the most important things are the structure of the block, and how to link the blocks.

In this part, I'll explain the block structure of the blockchain in bitcoin, and how these blocks are linked.

5.1 Merkle Tree

Before introducing the structure of block in bitcoin, I'll first introduce what is Merkle tree.

By definition, Merkle tree, also called as hash tree, is a tree in which every leaf node is the hash of a data block, this data block could be a file or a set of files, while for the nodes that further up in the tree, they are the hashes of their respective children. And most hash tree implementation are binary, that means their structure is a binary tree, each node can at most have two children.

For example, in Fig 1, it shows a structure of a binary hash tree. In this hash tree, it has four leaf nodes: Hash 0-0, Hash 0-1, Hash 1-0 and Hash 1-1. And we can see, for each leaf node, it contains a hash of a corresponding Data Block. For example, for Hash 0-0, it contains $hash(L1)$, which is the hash of the Data Block L1. And for the upper nodes, like Hash 0, since Hash 0-0 and Hash 0-1 are its children, so the value contained in Hash 0 node is $hash(Hash\ 0-0 \parallel Hash\ 0-1)$. In the same way, we can get the value contained in Hash 1 node is $hash(Hash\ 1-0 \parallel Hash\ 1-1)$. At last, we get the root node of this hash tree, Top Hash contains $hash(Hash\ 0 \parallel Hash\ 1)$. Usually, we call the value of Top hash node as Merkle root hash of the Merkle tree.

Since we have learned from the course, a well performed hash function should have four properties: easy to compute, collision resistant, pre-image resistant and second pre-image resistant. And in Merkle tree, each time we calculate the hash value of a node, we are actually reinforcing the security of its children, in other words, the Merkle root hash is a hash value which contains all the information in Data Blocks. Thus, if any Data Block has been modified by even one bit, the Merkle root hash of the Merkle tree will be totally changed.

In this case, Merkle tree can be used to verify any kind of data stored, handled and transferred in and between computers, make sure the received data is undamaged and unaltered, also, is not fake.

5.2 Block Structure

Now that we have understood the concept of Merkle tree, and this will help us to have a better understanding of the structure of block in bitcoin system

The block in bitcoin system is made up of two parts: block header and block body.

Usually, we will define the hash of the block header as the hash of the whole block.

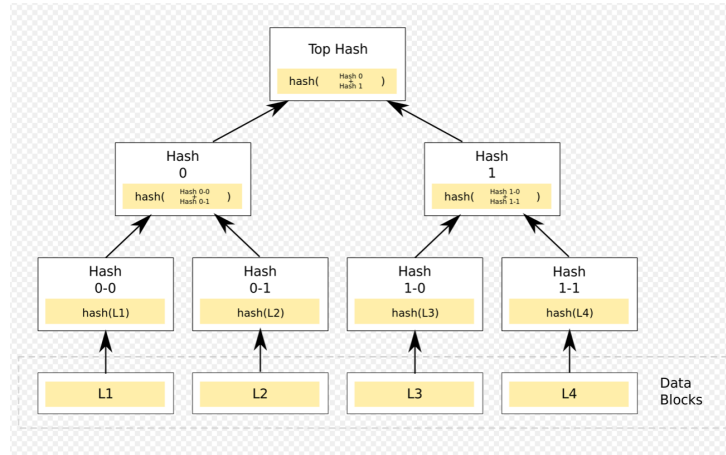


Figure 2: A Binary Merkle Tree.[5]

Block header is made up of the following parts:

1. version: this part record the version of the block header, which can be used to update the protocols and software.
2. prevBlockHash: this part will record the cryptographic hash of previous block.
3. merkleRoot: this part will record the value of Merkle root hash of the Merkle tree of all the transactions in this block.
4. time: this part will record the creation timestamp of this block.
5. difficultyTarget: this part will record the difficulty target of this block.
6. nonce: this part will record the nonce that used to verify the proof-of-work of this block.

And the block body is used to store the informations about transactions. On average, one block could store 500 transaction in its block body. In bitcoin system, the block body is made up of the following parts:

1. numTransactionsBytes: this part record the number of bytes that are used to store information about transactions.
2. numTransactions: this part record the number of transactions stored in this block.
3. transactions: this part will be used to store transactions.

I will further explain why the block in bitcoin's blockchain is formed in this way, especially for the block header.

For the preBlockHash part in the block header, actually this will enable us to find the previous block by its unique hash value, and thus establish a connection between them. More details will be covered in next part, Block Linking.

And for the merkleRoot in block header, just as I have introduced before, Merkle tree can be used to verify any kind of data stored, handled and transferred in and between computers, make sure the received data is undamaged and unaltered, also, is not fake. The block will store transactions in its block body, thus, by placing all transactions into a Merkle tree and attach its Merkle root hash into the header, everyone could basing on the Merkle root hash to verify the authenticity and reliability of all the transactions in the block.

For the time part in block header, it will contain the timestamp of the creation of the block, thus it can be used to prove all transactions stored in this block should be broadcast before this timestamp.

For the difficultyTarget and nonce, these parts are related to the creation of this block, and will be covered in Mining part, so we won't explain them here.

For the block body, it contains all the transactions in the block, and all the details about the structure of transactions have been covered in Transactions part.

5.3 Block Linking

In this part I will explain how the blocks in bitcoin's blockchain is linked, and why we choose to link the blocks in this way.

As we have mentioned in last part, in the bitcoin system, all blocks will record the hash of previous block in its block header, and according to the definition of hash, we know that each block in a blockchain will have a unique hash, thus, the hash of the previous block is like an address, which allows us to trace back to the previous block, and by repeatedly doing this, we will eventually go back to the genesis block and cover the whole chain. This is how these block are linked to form a chain.

But why don't we just number each block, and record the corresponding number of the previous block into the block header?

The reason is that, by linking blocks in this way, we can prevent the blocks from being modified or being tampered with, thus we don't need a trusted third party to verify the security or authenticity of the block together with the transactions stored in it.

As I have mentioned, the hash of a block is the hash of its block header, and for each block, it will record the hash of previous block in its block header, that means if you modify one block, since the hash of that block also changes, you need to modify all the blocks after this, otherwise when you broadcast your falsified blockchain, other nodes in the network will fail the verification, and this falsified blockchain won't be accepted by the other nodes in the network. And in a later introduction, we will further explain why it is theoretically impossible for one to modify a block and all the other blocks after it to deceive other nodes in the network.

6 Application of Blockchain

Now we have already understand what is transactions in bitcoin system, and what is blockchain, how a new block is generated in bitcoin system. Thus, in this part, we will explain how the entire bitcoin system could solve some hard problems so that it can be accepted by lots of people and become one of the most widely accepted cryptocurrencies.

6.1 Double Spending Problem

One of the hard problem faced by many cryptocurrencies is that, how could cryptocurrency system prevent a node from double spending his money.

For example, in bitcoin system, as we have learned, if user A want to have a transaction with user B, he wants to spend 5 bitcoins to buy something from B, he will create a new transaction basing on the previous transactions, and broadcast this transactions to the whole network, and waiting for some miners to accept this transaction and packet it into the blocks they are building. However, the problem is, if A only owns 5 bitcoins, but he also makes a transaction with C at the same time, and he wants to spend another 5 bitcoins to buy something from C, though he doesn't own enough bitcoins, but he broadcast these two transactions to the whole network nearly at the same time or within a very short time period, so how could the whole network figures out which transaction is valid, and which one is invalid?

This problem won't happen in the current monetary system. Why? Because if you are using paper money, since you cannot divide a paper into two parts and make each of them still be valuable, the double spending would never happen. Even if you are not using paper money, this problem is still impossible to happen, because there exist a trusted third party in real life, for example, the bank, or the government, every transaction you made with others will be transmit to them, and they will record every transaction of

you, and if they received two transactions from you, they will basing on the received time to accept the first transaction, and for the second one, they will check you money, and find out that you don't have enough money, so the second transaction will be canceled.

However, as we have mentioned, bitcoin system is decentralized, there exist no such kind of trusted third party. Thus, how could the network solve this problem?

Actually, there exist a rule in bitcoin system, that is every node in the network will select the longest block chain as the correct one. Thus, when A broadcast two transactions, some nodes or miners in the network will first receive A's transaction with B, and after they verify this transaction, they will store this transaction into their own ledgers, so when they received A's transaction with C, they check and find A doesn't own enough money, so they will discard that transaction. And other nodes or miners in the network who received A's transaction with C first, they will accept this transaction and discard another one. In this case, part of the nodes or miners will accept one transaction, while the others will accept another transaction. That is when the whole system diverges.

However, this situation won't last for a long time. As we have mentioned, every node in the network will select the longest block chain as the correct one and accept it. If, after a short time (according to what we have introduced in Mining part, at most after 10 mins), one of the miners in the network fortunately find out the new block, then this problem will be solve. If this lucky miner accept A's transaction with B and packet this transaction into new block, then a longer blockchain appears, so all the nodes in the network, no matter which transaction they accepted in the past, they will accept this longest blockchain and working on it, in this case, A's transaction with B is accepted by the blockchain, while the other transaction is rejected. And the same, if this lucky miner accept A's transaction with C, then the blockchain will contain A's transaction with C, and the other transaction is rejected.

And you may ask, what if two lucky miners find out the new block nearly at the same time? If so, then all the other miners will record both blockchains for the time being, and each miner will select one of the two blockchains and basing on it to dig the next block. In this situation, part of the miners in the network will work on the first blockchain, while the others will work on the second blockchain, a temporary fork appears. This fork will end once a new block is found and one of the blockchains becomes longer, otherwise the fork will continue or even more forks will appear. But since the probability of two miners find a same new block is very very small, usually the fork won't last for a long time.

In a conclusion, with the help of blockchain, bitcoin system could perfectly

solve double spending problem.

References

- [1] Nakamoto, Satoshi. "Bitcoin: A peer-to-peer electronic cash system." (2008).
- [2] Retrieved from en.bitcoin.it/wiki/Main_Page
- [3] Grunspan, Cyril and Prez-Marco, Ricardo. "Double spend races." *arXiv preprint arXiv: 1702.02867*.(2017)
- [4] Shirriff, Ken. "Bitcoins the hard way: Using the raw Bitcoin protocol." www.righto.com/2014/02/bitcoins-hard-way-using-raw-bitcoin.html *Ken Shirriff's Blog* (2014).
- [5] Retrieved from https://en.wikipedia.org/wiki/Merkle_tree
- [6] Retrieved from <https://en.wikipedia.org/wiki/Bittorrent>
- [7] Retrieved from https://en.wikipedia.org/wiki/Digital_signature
- [8] Retrieved from <https://en.wikipedia.org/wiki/RIPEMD>