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## Answer 1

 $\mathbf{error} = 2 - norm(p - f(t)) \text{ where } p, f(t) \in \mathbb{R}^{100}$ 

p is the vector that consists of the predicted value of the 100 input values evaluated via polynomial fitting.

f(t) is the vector that consists of the actual values of the 100 input values evaluated via the original function  $f(t) = \sin(10t)$ .

## Fitting a 14th degree polynomial to the datapoints with MGS QR factorizatio

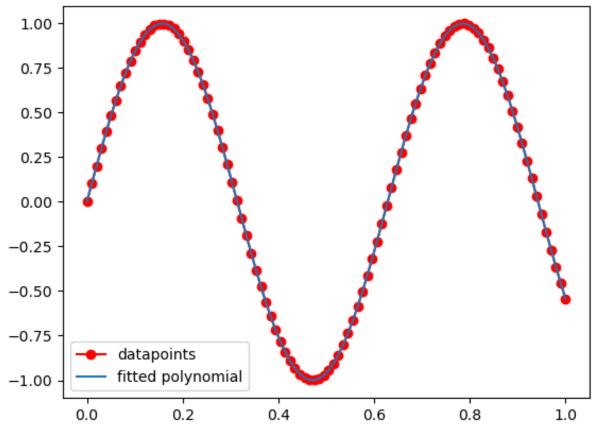


Figure 1: error= 66.47188248164618

ing a 14th degree polynomial to the datapoints with Householder QR factoriz

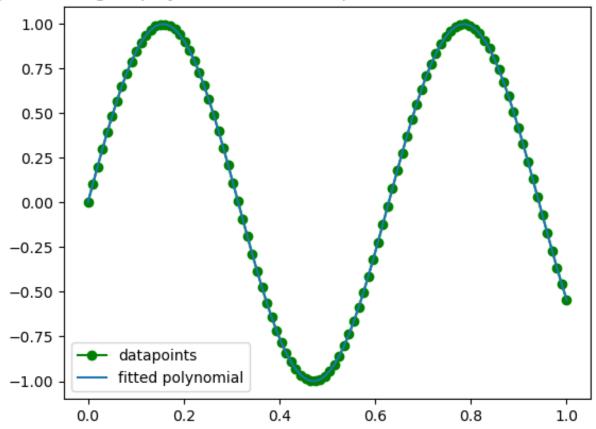


Figure 2: error= 66.47188248158425

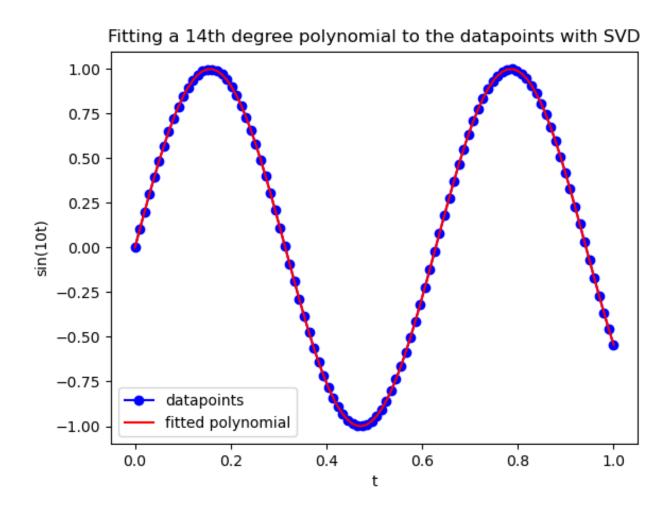


Figure 3: error= 66.47188248158271

## Fitting a 14th degree polynomial to the datapoints with normal equations

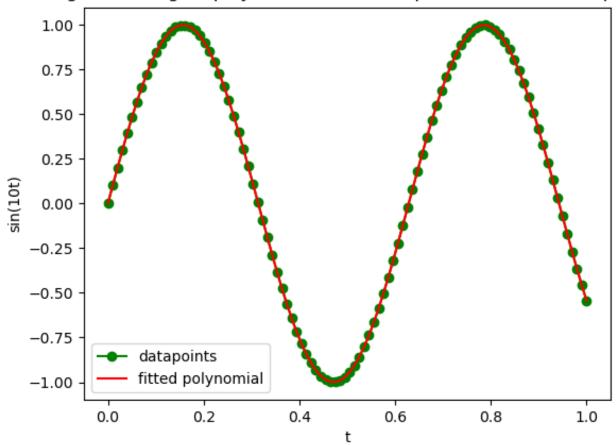


Figure 4: error= 66.47188275756871

## Coefficients of the 14 degree polynomial for the function f(t) = sin(10t) approximation:

	MGS	Householder	normal equations	SVD
$a_0$	4.13e-7	-1.604e-7	0.0000022188	-1.604e-7
$a_1$	9.9998424247	10.0000600749	10.0017959484	10.0000600747
$a_2$	0.0095821262	-0.0031492289	-0.1558430004	-0.0031492228
$a_3$	-166.9113404969	-166.6106191969	-162.496532603	-166.6106192929
$a_4$	3.4840726795	-0.2959493046	-53.2919958934	-0.2959482308
$a_5$	801.5976640372	830.4565467514	1219.9893792245	830.4565385493
$a_6$	199.3841776048	55.2238419012	-1734.0963064463	55.2238843827
$a_7$	-2884.4179382225	-2392.0438688348	3003.4347635999	-2392.0440199592
$a_8$	2979.4731872136	1801.1100507212	-9120.6421024678	1801.1104252418
$a_9$	-4503.7856651089	-2508.830344659	12323.3515274771	-2508.8309956998
$a_{10}$	12907.8718186067	10530.107804164	-2596.3576586784	10530.1085943036
$a_{11}$	-18825.4162729622	-16874.0560276336	-9907.4873359055	-16874.0566831362
$a_{12}$	13836.7980869608	12787.2865803221	-9907.4873359055	12787.2869345805
$a_{13}$	-5133.4271555276	-4800.4499588965	-4908.1733685353	-4800.4500712968
$a_{14}$	774.7959199589	727.5610133192	832.8919068456	727.5610292058

Table 1: Coefficients of the fitted polynomial.

maximum error is 66.47188275756871 occured in Normal equations. minimum error is 66.47188248158271 occured in SVD.

Upto 6 digits after decimal in the values of error, its the same. Thus, we need to set the tolerance more than  $10^{-6}$  to achieve high degree of accuracy to compare among the several methods for solving the least squares problem.