## The FARM Felix Annotated Reference Manual

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## Chapter 1

## Introduction

This reference is a guide to the Felix programming language. It is not the usual reference because Felix differs from other systems in that most of the grammar is part of the library, in user space. In principle then, separating the library from the core language is impossible: if anything the core language is defined by the compiler intermediate abstract machine, details of little interest to most programmers.

Furthermore even that characterisation is weak, because considerable functionality is actually embodied in the run time library. For example the compiler knows what a service request is, but it has no idea what an fthread is. It knows what a generator is, and it knows which generators perform yields, but it has no idea what an iterator is, despite the fact these are effectively a core language feature.

Therefore, our presentation cannot be complete, it cannot be precise, and it cannot replace actually reading the library code. Felix is a highly mutable language, major new features can often be introduced without touching the compiler.

For example a complete set of primitive types with their base operations cannot be presented, because, with a couple of exceptions there aren't any such types. Instead, most primitive types are introduced without knowledge of the compiler, by creating bindings to C++ in library code; these bindings defined the type name and some operations on the types in terms of C++.

# ${f Part\ I}$ ${f Scripting}$

Felix is primarily a scripting language, meaning, it is intended for writing a program in one file and immediately running it. It's hard to define what this means but the lack of separate interfaces is one of the things that makes writing script simpler.

Although out of logical order, we present the basic statements, expressions, and definitions first, because together with examples that is enough to get most programmers writing script.

Felix code, like most other languages, is compiled before execution. However it differs from many other systems which compile to byte code and interpret it: Felix uses C++ as its bytecode, and compiles it to machine binary and executes that. Compilation times are slower, but the run time performace is better.

## Chapter 2

## Language Features

- higher order functions, procedures, and coroutines
- parametric polymorphism
- type constraints
- typeclass based polymorphism
- overloading
- generics
- row polymorphism
- tuple, record and struct product types
- sum, variant and union sum types
- rich pattern matching
- regular expressions
- java like object sublanguage
- circuit based coroutines
- platform independent asynchronous socket I/O
- platform independent pre-emptive threading
- direct embedding of C and C++
- can be embedded in framework idle loops
- generates fast binary programs and libraries
- $\bullet\,$  run scripts directly without make files

## Chapter 3

## The flavour of Felix

Although this is a reference manual, it seems wise to show the flavour of the scripting subsystem with examples, and what could be a better starting point than:

```
println "Hello World";
```

#### 3.1 Simple calculations

To perform a simple numerical calculation using a function:

```
fun hypot (x:double, y:double) => sqrt (x^2 + y^2);
var x = 4.0;
var y = 5.0;
var d = hypot (x,y);

println$
   "Hypotenuse of triangle base " + x.str +
   ", side " + y.str " is " +
   d.str
;
```

A better looking way:

```
fun hypot (x:double, y:double) => \sqrt{x^2+y^2};
```

encoded like this:

```
fun hypot (x:double, y:double) => \(\sqrt \(x^2 + y^2\)\);
```

#### 3.2 Yielding Generators

To calculate the number of rabbits using a yielding generator:

```
gen rabbits () = {
  var generation = 1;
  var last_gen = 1;
  var this_gen = 2;
  while true do
    yield (generation, this_gen);
    last_gen <-> this_gen;
    this_gen += last_gen;
    done
}

var fibonacci = rabbits;

for i in 1..10 do
    var bunnies = fibonacci();
    println$ bunnies;
done
```

#### 3.3 Fibres

To parse text into words, using a coroutine pipeline. First a producer of characters:

```
proc char_stream (s:string) (out:%>char) {
  for c in s perform write (out,c);
  write (out,char "");
}
```

and now a transducer that converts a character stream into a word stream:

```
proc words (inp:%<char, out:%>string) {
  while true do
   var s = "";
  nextch: while true do
   var c = read inp;
  if isalnum c do
```

```
s+=c;
else
   if s != "" call write (out,s);
   break nextch;
   done
   done // nextch
   done
}
```

Finally we need a sink to emit the result:

```
proc emit (inp:%<string) {
   while true do
    var word = read inp;
   println$ "Word = " + word;
   done
}</pre>
```

which you can use like this:

```
var text =
   "The quick, brown fox jumped "
   "over the lazy dog"
;
#(char_stream (text) |-> words |-> emit);
```

#### 3.4 Circuits

Circuits generalise the capabilities of pipelines. Two data sources:

```
open syntax chips;

chip w10
    connector pins
        pin outpin: %>int
{
    for i in 0..10 do
        write (pins.outpin,i);
    done
}

chip w100
```

```
connector pins pin outpin: %>int
{
  for i in 100..110 do
    write (pins.outpin,i);
  done
}
```

and a data sink:

```
chip conout
   connector pins pin inpin: %<int
{
   while true do
     var x = read pins.inpin;
     println$ "Read " + x.str;
   done
}</pre>
```

with a transducer:

```
chip doubler
  connector pins
    pin inpin: %<int
    pin outpin: %>int
{
    while true do
       var x = read pins.inpin;
       write (pins.outpin, 2 * x);
    done
}
```

can be combined like this:

```
circuit
  connect w10.outpin to doubler.inpin
  connect w100.outpin to doubler.inpin
  wire pins.inch to doubler.outpin
  endcircuit
}
```

to form a circuuit we can use like this:

```
var dummy_channel = mk_schannel[int]();

circuit
   wire dummy_channel to fred.inch
endcircuit

while true do
   var x = read dummy_channel;
   println$ "Read " + x.str;
done
```

## Chapter 4

## Variable Definitions

#### Syntax

A definition is a statement, clause, expression, phrase or other term which defines a name, but does not cause any observable behavior, or, a class statement, or, a var or val statement. The latter two exceptions define a name but may also have associated behaviour.

Felix provides two primary kinds of variables:

- 1. a var variable names mutable store, and.
- 2. a val variable names a functional expression

#### 4.1 The var binder

#### 4.1.1 The var statement

The var statement is used to introduce a variable name and potential executable behaviour. It has one of three basic forms:

```
var x : int = 1;
var y : int;
var z = 1;
```

- 1. The first form specifies the type and an initialising expression which must be of the specified type or a subtype thereof.
- 2. The second form specifies a variable of the given type without an explicit initialiser, however the variable will be initialised anyhow with the default contructor for the underlying C++ type, although that constructor may be trivial.

3. The third form does not specify the type, it will be deduced from the initialiser.

#### 4.1.2 Semantic rules

- 1. If the initialiser has observable behaviour it will be observed if at all, when control passes through the variable statement.
- 2. If the variable introduced by the var statement is not used, the variable and its initaliser will be elided and any observable behaviour will be lost.

To be used means to have its address taken in a used expression, to occur in a used expression. A used expression is one which initialises a used variable, or, is an argument to function or generator in a used expression, or an argument to a procedure through which control passes.

In other words, the variable is used if the behaviour of the program appears to depend on its value or its address.

3. The library procedure C\_hack::ignore ensures the compiler believes a variable is used:

```
var x = expr;
C_hack::ignore x;
```

so that any side effects of expr will be seen.

4. In general the argument to any primitive function, generator or procedure will be considered used if its containing entity is also considered used. In general this means there is a possible execution path from a root procedure of the program.

#### 4.1.3 Multiple variables

Multiple variables can be defined at once:

```
var m = 1,2;
var a,b = 1,2;
var c,d = m;
```

With this syntax, no type annotation may be given. The RHS of the statement must be an expression of tuple type, with the number of components of the tuple equal to the number of variables being defined.

#### 4.1.4 Var expressions

Variables can also be defined inside expressions:

```
var x = 1 + (2 as var y) + (var z = y+1);
println$ x,y,z;
```

The as var form has low precedence and usually requires parenthesis, in the assignment form parenthesis are mandatory.

Nested var definitions are evaluated before their containing expression, and for several expressions directly contained within the same expression, in left to right order. The order is therefore deterministic.

Unnamed one use temporary variables can also be specified in a var subexpression:

```
var x = 1 + (var rand());
println$ x;
```

The effect is to enforce eager, single evaluation of the subexpression prior to its containing expression.

#### 4.1.5 Addressing

A variable may have its address taken:

```
var x = 1;
var rwpx = &x; // read-write pointer
var rpx = &<x; // read-only pointer
var wpx = &>x; // write-only pointer
```

A variable may be assigned a value directly by an assignment statement:

```
x = 2;
```

or indirectly via a a call to the system intrinsic \_storeat procedure:

```
_storeat(rwpx,3);
_storeat(wpx,4);
```

If a variable stored no previous value and assignment sets the first value. Otherwise, if a variable previously stored a value, an assignment replaces it.

The standard grammar also provides the infix operator <- which invokes the standard library procedure storeat which by default invokes the procedure \_storeat:

```
storeat(rwpx,3);
wpx <- 4;</pre>
```

The standard library procedure **storeat** can be overloaded, which also changes the behaviour of the infix operator <-.

#### 4.1.6 Referencing

If a value is stored in a variable it can be referred to in an expression by using the name of the variable.

```
var x = 1;
println$ x; // prints 1
```

If a read-write or read only pointer to a variable is obtained, the stored value, if it exists, can be referred to by using the system intrinsic \_deref function:

```
println$ _deref &x; // prints 1
println$ _deref &<x; // prints 1</pre>
```

The standard grammar also provides the prefix operator \* which invokes the standard library function deref which by default invokes the system intrinsic \_deref:

```
println$ deref &x; // prints 1
println$ *(&x); // prints 1
```

The standard library function  $\mathtt{deref}$  can be overloaded, which also changes the behaviour of the prefix operator \*.

#### 4.1.7 Object Concept

A variable is said to name an object, not a value. This basically means it is associated with the address of a typed storage location.

#### 4.1.8 Hoisting and lookup

A variable can be assigned to, addressed, or otherwise used before the var statement or expression which introduces it. This is because Felix does setwise, not linear, lookup.

An initialising definition such as

```
var x = 1;
```

is split into an uninitialised variable definition and an assignment, and the definition is then hoisted to the top of the scope. For example:

```
x = 1;
var x = 2;
```

is converted to:

```
var x: int;
x = 1;
x = 2;
```

Javascript behaves the same way, and the phenomena is called *hoisting*.

Care should be taken because it is possible to refer to an uninitialised variable, a variable unexpectedly initialised by the underlying C++ default constructor, or the wrong variable entirely.

For example here:

the variable y is set to an indeterminate value because its initialiser x is the one which is subsequently set to 2 on line 4, not the one set to 1 on line 1. This also means this code is legitimate:

```
x = 1;
x = 2;
var x = 3;
```

because x is in fact defined as a variable on the third line.

#### 4.1.9 var parameters

A function or procedure may have a parameter marked var:

An argument bound to a var parameter will always be evaluated, if at all, before the main body of the function is entered; that is, it ensure eager evaluation.

A var parameter in a direct call or application may or may not be eliminated, unlike a local variable which will always be eliminated if not used.

If the function or procedure is inlined, it is likely but not assured that the parameter and its initialising argument will be eliminated, hence in the example the evaluation of rand() on line 3 could be eliminated because the parameter x is not ised in f.

On the other hand it is very unlikely that the argument to g will be eliminated, because parameters of a closure cannot be, without changing the closure's type. Therefore the rand() on line 4 will almost certainly be evaluated.

#### 4.2 The val binder

#### 4.2.1 The val statement

A val statement defines a name for an expression.

```
val x : int = 1;
val z = 1;
```

The value associated with a val symbol may be computed at any time between its definition and its use, and may differ between uses, if the initialising expression depends on variable state, such as a variable or call to a generator.

It is not an error to create such a dependence since either the value may, in fact, not change, or the change may not be significant.

Nevertheless the user must be warned to take care with the indeterminate evaluation time and use a var when there is any doubt.

Since a val simply names an expression, it is associated with a value not an object and cannot be addressed or assigned to.

However this does NOT mean its value cannot change:

```
for var i in 0 upto 9 do
  val x = i;
  println$ x;
done
```

In this example, x isn't mutable but it does take on all the values 0 to 9 in succession. This is just a most obvious case: a less obvious one:

```
var i = 0;
val x = i;
println$ x;
++i;
println$ x;
```

which is clearly just an expansion of the the first two iterations of the previously given for loop. However in this case there is no assurance x will change after i is incremented because the compiler is free to replace any val definition with a var definition.

#### 4.2.2 Multiple values

Multiple values can be defined at once:

```
val m = 1,2;
val a,b = 1,2;
val c,d = m;
```

With this syntax, no type annotation may be given.

#### 4.2.3 Val expressions

Values can also be defined inside expressions:

```
val x = 1 + (2 as val y) + (val z = y+1);
println$ x,y,z;
```

The as val form has low precedence and usually requires parenthesis, in the assignment form parenthesis are mandatory.

#### 4.2.4 Pattern variables

In a pattern match, pattern variables are implicitly val variables with their scope limited to the branch for which they're specified: For example the statement:

```
match 1,2 with
| (x,y) => println$ x +y;
endmatch;
```

the variables x and y act as if:

```
begin
  val x = 1;
  val y =2;
  println$ x + y;
end
```

had been written.

#### 4.2.5 let expressions

A let expression can be used to introduce a named value within an expression which has scope limited to the let expression:

```
var y = 42;
var x = let y = 1 in y + y;
println$ x,y; // 2,42
```

```
In fact, in a let expression, the phrase after let and before
    let pattern = expr1 in expr2

is syntactic sugar for
    match expr1 with
    | pattern => expr2
    endmatch
```

#### 4.2.6 val parameters

A function or procedure may have a parameter marked var:

```
fun f(val x: int, y: int) => x + y;
```

If a parameter is not explicitly marked var, then it is a val parameter. The explicit spelling of val is allowed but not required.

#### 4.2.7 val semantics

A name introduced by a val or let binder is assumed to bind to a purely functional expression. This means the expression depends only on explicitly visible terms of the expression, has no side-effects, and, has a value which is temporally invariant or referentially transparent.

The compiler may treat the val precisely as a var and allocate store to hold the value its initialiser designates. Alternatively, the compiler may replace occurences of the use of the defined name in an an expression with the initialising value, or, a combination of both. The compiler may also shift the position of the initialising assignment, in the case it choses to allocate store, to any point after the definition and before the first use. It may also evaluate the expression earlier, provided it does not impact the evaluation.

The kind of evaluation strategy described is a key feature of Felix and is called *indeterminate evaluation* strategy. It is one of the primary semantic design principles which provide high performance by allowing the compiler to choose whether to evaluate the val eagerly or lazily. In particular, val parameters of a closure are almost universally eagerly evaluated, which avoids the need to pass the closure a closure over the expression. On the other hand if a function is called directly and is inlined, the compiler is free to elide the parameter and substitute the expression for its occurrences, thus evaluating it lazily and saving a storage location as well.

#### 4.3 def statement

A special statement called a def statement can be used to introduce zero or more var variables, zero or more val variables, and perform simple assignments, simultaneously:

```
var x = 1;
def var a, (val b, x, _) = 2,(3,4,42);
```

The LHS pattern is called an *l-pattern* which consists of a list of *l-terms* each of which may be either a var binder introducing a new variable, a val binder introducing a new variable, a simple name referring to an existing var variable, an underscore, or a nested *l-pattern* enclosed in parens.

The components other than underscore, are assigned the corresponding values from the term on the RHS which must be of tuple type with the same number of components, recursively for nested l-patterns; underscore is a place holder for a component which is to be ignored.

A component matching an underscore may or may not be evaluated.

#### 4.3.1 Uniquely typed components

Uniqueness typing is provided to provide a way to implement move semantics instead of the usual copy and overwrite semantics of assignment; it allows the programmer to assert acquisition of exclusive ownership of an object, and transfer that ownership along with the objects value.

Felix provides an intrinsic type constructor \_uniq which maps a type T to its unique equivalent.

The programmer announces a value is acquired using the box intrinsic, which when applied to an object of type T returns an object of type \_uniq T. The programmer can then pass the object to a function which requires a uniquely typed parameter. The function can then pass the object on, or use the kill intrinsic to forget it, otherwise, to use the boxed object the unbox intrinsic is appled to return the boxed type T.

```
begin
  fun toupper (var s: uniq varray[char]) {
    var x = unbox s;
    for i in 0 ..< x.len.int perform
        set(x,i,toupper (get(x,i)));
    return box x;
}

var u = box (varray "hello");
    u = toupper u;
    println$ (unbox u);
end</pre>
```

Because a function acquiring a uniquely typed object is the exclusive owner, it is free to modify the object without compromising referential transparency, because by specification there can be no other observer.

In other words box/unbox together perform a move from the caller of a function to the function's implementation, using the uniquness typing of the interface to facilitate enforcement of the contract.

Variables which have a type which is <code>uniq</code>, or a product type with one or more component <code>uniq</code> are treated specially. Control flow analysis attempts to assign a consistent state to such variables or components, either <code>dead</code> or <code>live</code>.

The library provides a functor uniq: TYPE  $\rightarrow$  TYPE which maps a type T to uniq T.

1. Assignment to a live variable or component is not permitted and an error reported if detected.

- 2. Use of a dead variable or component in an expression is not permitted and an error reported if detected.
- 3. Using a live variable or component changes the state of the component from live to dead.
- 4. Assigning to a dead component changes the state from dead to live.
- 5. If the variable or component is a parameter or part of a parameter it is initially considered live, otherwise if it is a local variable it is considered dead.
- 6. A variable must be dead when control exits.
- 7. If a variable is used in one branch of a pattern match or conditional it must be used in all of them.
- 8. A uniquely typed component of an variable of a product type is treated as if it were a whole variable.

```
This rule is subtle! For example:

begin

var x = 1, uniq 2;

var y = x; // kills x.1

println$ y.0;
end // ERROR: y.1 unused!
```

9.  $\_$ uniq T is a subtype of T. Therefore, a variable of unique type can be passed as an argument to a function with the corresponding non-unique type, the argument will be implicitly unboxed.

Top level global variables are not analysed and should not be uniquely typed because they're not considered by the flow analyser.

Taking the address of a uniquely type variable is ignored by the flow analyser. For therefore the correctness of the analysis depends on the programmer not abusing pointers to unique variables or components.

The flow analyser will report an error if a consistent state cannot be assigned to a variable or component.

The flow analyser does first order static analysis only. It cannot cope with either indirect or dynamic access.

## Chapter 5

## **Assignment Statements**

Syntax

#### 5.1 Basic Assignment

In Felix, the core assignment operation is an instrinsic procedure

```
_storeat: &>T * T -> 0
```

which is wrapped by a library procedure:

```
proc storeat[T] (p: &>T, v:T) => _storeat(p, v);
```

so it can be overloaded. The parser, in turn, maps the statement

```
p <- v;
```

to call the library procedure. The type &>T denotes a write-only pointer to T, however the type &T of a read-write pointer to T is a subtype, so a pointer of that type can also be used for assignment:

```
var x = 1;
&x <- 2;</pre>
```

Felix provides a conventional assignment operator:

```
var x = 1;

x = 2; // means \mathcal{C}x \leftarrow 2;
```

The left hand side of such an assignment must be a variable, or a dereference of a pointer expression:

```
var px = new 1; // on the heap
*px = 2; // means px <- 2;</pre>
```

Initialisation of a variable in a var statement, or var l-term of a def statement is also an assignment.

# 5.2 Read-modify-write operations

The following read/modify/write operations are similar to those in C. Each of these dispatches to a *procedure* of the same name, taking two arguments, the first being a read-write pointer and the second a value. The parser automatically takes the address of the LHS of the assignment when calling the procedure. Therefore, the LHS must be a simple variable.

```
var x = 1u; var y=1u;

// from class Integer
    // all integers
x += y; // means +=(&x,y)
x -= y; // means -=(&x,y)
x *= y; // means *=(&x,y)
x /= y; // means /=(&x,y)
x %= y; // means %=(&x,y)
x %= y; // means <=(&x,y)
x >>= y; // means >>=(&x,y)
// from class Bits
// unsigned integers only
x ^= y; // means ^=(&b,y)
x != y; // means !=(&b,y)
x &= y; // means &=(&b,y)
```

Felix does not guarantee these operations are atomic.

# 5.3 Swap operator

Felix provides the \_swap intrinsic procedure to swap the contents of two variables.

```
var x,y = 1,2;
_swap (&x,&y); // now x=2, y=1
```

The variables must be of the same type. The parser maps the infix operator <-> to the procedure swap which is defined in the library to call \_swap by default.

```
var x = 1;
var y = 2;
x <-> y; // swap so x = 2, y = 1
```

# 5.4 Pre and post increment and decrement

Felix provides pre and post increment and decrement. These are procedures taking a pointer argument, not expressions. The procedures have special names as indicated:

```
var x = 1;
++x; // means pre_incr (&x);
--x; // means pre_decr (&x);
x++; // means post_incr (&x);
x--; // means post_decr (&x);
```

# Chapter 6

# **Control Flow Statements**

## 6.1 The goto statement and label prefix

Felix statements may be prefixed by a label to which control may be transfered by a goto statement:

```
alabel:>
  dosomething;
  goto alabel;
```

The label must be visible from the goto statement.

There are three kinds of gotos.

- 1. A *local goto* is a direct jump to a label in the same scope as the goto statement.
- 2. A non-local goto is a direct jump to any other label, visible in an ancestor scope.
- 3. An *indirect goto* is a goto with a non-constant expression of LABEL type as its operand.

### 6.1.1 Non-local gotos

Non-local transfers of control may cross procedure boundaries. They may not cross function or generator boundaries.

The procedure or function containing the label must be active at the time of the control transfer. A non-local goto may be wrapped in a procedure closure and passed to a procedure from which the goto target is not visible.

```
proc doit (err: 1 -> 0) { err; }

proc outer () {
  proc handler () { goto error; }
  doit (handler);
  return;

error:> println$ error;
}
```

This is a valid way to handle errors. the code is correct because outer is active at the time that handler performs the control transfer.

#### 6.1.2 Label values

Labels are first class values of the kind LABEL. They can be stored in variables, and targetted by a goto statement.

```
proc demo (selector:int) {
  var pos : LABEL =
    if selector == 1
    then lab1
    else lab2
    endif
  ;
  goto pos;
lab1:>
  println$ "Lab1"; return;
lab2:>
  println$ "Lab2"; return;
}
```

Used of saved label values may not be sound unless the procedure frame of the procedure containing the label at the time it is saved remains live at the time it is jumped to.

Label values are not merely code addresses, they are closures which capture the state of the containing procedure frame. This prevents the frame from being garbage collected, but it does not prevent control being returned from the frame. The effect of executing an already returned frame will cause the program to refer to local variables which have the values

they had when last modified. This is well defined!

In the current implementation, returning from a procedure resets the return address to NULL which means a return statement will actually return to the invoking scheduler terminating the fibre. Decoupling an exhausted frame from its caller is not done to make returning to a dead frame safe. This is a side effect of an optimisation which is intended to prevent a data pointer into the frame making the call chain reachable.

#### 6.1.3 Exchange of control

Built on top of label addressing and indirect gotos, the branch-and-link instruction is conceptually the most fundamental control instruction. The library implementation is

```
inline proc branch-and-link (target:LABEL, save:LABEL)
{
   save <- next;
   goto target;
   next:>
}
```

A good example is here, which shows an example of coroutines.

#### 6.2 Conditional Statements

#### 6.2.1 if/goto

If the condition is true, jump to the goto target, otherwise continue without jumping.

```
if c goto lab;
```

#### 6.2.2 if/return

If the condition is true, return from the current procedure, otherwise continue without returning.

```
if c return;
```

### 6.2.3 if/call

If the condition is true, call the specified procedure, otherwise continue without calling it.

```
if c call f x;
```

### 6.2.4 if/perform

If the condition is true, execute the specified statement, otherwise continue without executing it.

```
if c perform x = 1; // equivalent to
```

# 6.2.5 if/do/elif/else/done

The procedural conditional branch is used to select a control path based on a boolean expression.

The else and elif clauses are optional.

```
if c1 do
    stmt1;
    stmt2;
elif c2 do
    stmt3;
    stmt4;
else
    stmt5;
    stmt6;
done
```

The elif clause saves writing a nested conditional. The above is equivalent to:

```
if c1 do
    stmt1;
    stmt2;
else
    if c2 do
        stmt3;
        stmt4;
    else
        stmt5;
        stmt6;
        done
    done
```

One or more statements may be given in the selected control path. The bodies of the subclasses do not form a scope. Variables declared therein are visible in the containing context. Labels therein can be targetted by gotos.

#### 6.3 halt

Stops the program with a diagnostic.

```
halt "Program complete";
```

# 6.4 try/catch/endtry

The try/catch construction may only be used to wrap calls to C++ primitives, so as to catch exceptions.

```
proc mythrow 1 = "throw 0;";
try
   mythrow;
catch (x:int) =>
   println$ "Caughht integer " + x.str;
endtry
```

# 6.5 match/endmatch

The form:

```
match expr with
| pattern1 => stmts1
| pattern2 => stmts2
...
endmatch;
```

is an extension of the C switch statement. See chapter 9 Pattern Matching.

The match argument expression is compared in turn with each pattern. If a match is found, the pattern variables in the pattern are bound to the corresponding sub-expressions of the argument expression. Then the statements of that branch are executed with those variables in scope. The variables are val bound and so immutable. The branch statements form a scope.

# 6.6 chainmatch/ormatch

The form:

```
chainmatch expr1 with
| pattern1 => stmts1
| pattern2 => stmts2
```

```
ormatch expr2 with
| pattern3 => stmts3
| pattern4 => stmts4
ormatch expr3 with
| pattern5 => stmts5
| pattern6 => stmts6
| _ => stmts7
endmatch;
```

is sugar for:

```
match expr1 with
| pattern1 => stmts1
| pattern2 => stmts2
| _ =>
    match expr2 with
| pattern3 => stmts3
| pattern4 => stmts4
| _ =>
    match expr3 with
| pattern5 => stmts5
| pattern6 => stmts6
| _ => stmts7
    endmatch;
endmatch;
endmatch;
```

#### 6.7 call

The call statement is used to invoke a procedure.

```
proc p(x:int) { println$ x; }
call p 1;
```

The word call may be elided in a simple call:

```
p 1;
```

If the argument is of unit type; that is, it is the empty tuple, then the tuple may also be elided in a simple call:

```
proc f() { println$ "Hi"; }
call f (); // is equivalent to
f(); // is equivalent to
f;
```

# 6.8 procedure return

The procedural return is used to return control from a procedure to its caller.

A return is not required at the end of a procedure where control would otherwise appear to drop through, a return is assumed:

```
proc f() { println$ 1; }
// equivalent to
proc f() { println$ 1; return; }
```

### 6.9 return from

The return from statement allows control to be returned from an enclosing procedure, provided that procedure is active.

```
proc outer () {
    proc inner () {
        println$ "Inner";
        return from outer;
    }
    inner;
    println$ "Never executed";
}
```

# 6.10 jump

The procedural jump is an abbreviation for the more verbose sequence:

```
jump procedure arg; // is equivalent to
call procedure arg;
return;
```

#### 6.11 callcc

The callcc statement

```
callcc f a;
```

calls the function f passing the location of the next statement as its argument. The returned value is then called with a as its argument.

The location is represented as a value of LABEL type. If the procedure wishes to return to this point it should goto the parameter which received the argument.

```
proc f(cc:LABEL) (x:int) {
    println$ "F got " + x.str;
    goto cc;
}
callcc f 42;
println$ "Back";
```

```
The callcc statement above is equivalent to:

var tmo = f next;

call tmp 42;

next:>
```

#### 6.12 function return

The functional return statement returns a value from a function.

```
fun f () : int = {
    return 1;
}
```

Control may not fall through the end of a function.

# **6.13** yield

The yield statement returns a value from a generator whilst retaining the current location so that execution may be resumed at the point after the yield.

For this to work a closure of the generator must be stored in a variable which is subsequently applied.

```
gen counter () = {
  var x = 0;
next_integer:>
```

```
yield x;
++x;
goto next_integer;
}

var counter1 = counter;
var zero = counter1 ();
var one = counter1 ();
println$ zero, one;
```

# 6.14 call\_with\_trap and throw\_continuation

The call\_with\_trap statement calls a procedure, catching any uncaught thrown continuation, if there is one.

If control returns normally, it continues normally.

A procedure of type 1->0 may be thrown with a throw\_continuation statment. It will be caught by the closest dynamically enclosing call\_with\_trap statement or the top level scheduler.

Such a trapped continuation then replaces the currently running procedure and begins execution.

```
fun divide (error:1->0) (a:int, b:int) = {
  if b == 0 perform throw_continuation error;
  return a/b;
}
proc demo() {
 proc divide_by_zero () {
   println$ "Divide by zero";
   goto bad;
 var q = divide divide_by_zero (1,0);
 println$ "Quotient " + q.str;
 return;
bad:>
  println$ "Error Handled";
}
call_with_trap demo;
println$ "Done";
```

## **6.15** loops

#### Library Reference

Felix has two kinds of loops, low level loops and high level loops.

Felix loops consist of a control section and a body. The body must be a group statement. There are two kinds of group statements:

1. An basic group is a perform statement, a do/done group, an if/do/done statement, or a loop whose body is a basic group.

Basic groups do not constitute a scope.

2. A block A begin/end statement or a statement match statement is a block.

Block define an anonymous scope. Variables defined in a block do not escape, and you cannot jump to a label in a block.

#### 6.15.1 C like loop

This loop is similar to a C for loop except that the increment operation is a statement, not an expression, and so may need a semi-colon as a terminator. It is the fastest and most flexible loop, but it is hardest to optimise.

```
for(var i=0; i<20; ++i;)
  perform println$ i;
println$ "Final i " + i.str;</pre>
```

Note the control variable is defined in the containing scope and is not local to the loop.

#### 6.15.2 for/in/upto/downto

A basic loop with an inclusive range.

```
// up
for var ti:int in 0 upto 9 do println$ ti; done
for var i in 0 upto 9 do println$ i; done
for i in 0 upto 9 do println$ i; done

// down
for var tj:int in 9 downto 0 do println$ j; done
for var j in 9 downto 0 do println$ j; done
for j in 0 upto 9 do println$ j; done
```

The start and end expressions must be of the same type.

If the control variable is defined in the loop with a type annotation, that type must agree with the control variable.

The type must support comparison with the equality operator == the less than or equals operator <= and increment with the pre increment procedure pre\_incr

The loop logic takes care to ensure the control variable is not incremented (resp. decremented) past the end (resp. start) value.

Loops over unsigned integer types cannot handle the empty case. Loops over signed integer types cannot span the whole range of the type.

### 6.15.3 while loop

The while loop executes the body repeatedly whilst the control condition is true at the start of the loop body.

```
var i = 0;
while i < 10 do println$ i; ++i; done</pre>
```

#### 6.15.4 until loop

The until loop executes the loop body repeatedly until the control condition is false at the start of the loop, it is equivalent o a while loop with a negated condition.

```
var i = 0;
until i == 9 do println$ i; ++i; done
```

#### 6.15.5 Control Flow modifiers

Low level loops may be labelled with a loop label which is used to allow break, continue, and redo statements to modify the usual control flow.

```
outer:for var i in 0 upto 9 do
  inner: for var j in 0 upto 9 do
  println$ i,j;
  if i == j do break inner; done
  if i * j > 60 do break outer; done
  done
done
```

#### redo

The redo statement causes control to jump to the start of the specified loop without incrementing the control variable.

#### break

The break statement causes control to jump past the end of the specified loop, terminating iteration.

#### continue

The continue statement causes the control variable to be incremented and tests and the next iteration commenced or the loop terminated.

#### 6.15.6 Parallel for loop

The pfor loop is a high level loop which uses a thread pool to execute loops over subranges of the specified range in parallel.

```
proc copy(inp: varray[uinptr], out: varray[uintptr]) {
   pfor i in 0 upto 99 do
      set(out, i, f (get(inp,j));
   done
}
```

If the system thread pool is not created, it is constructed. The range of the control variable is divided into n subranges, where n is the number of threads. Then n procedures are created which run the loop over each subrange and are submitted to the thread pool. The statement after the **pfor** statement is executed after all the threads have completed.

Note the thread pool is not destroyed, even if it was created, the programmer must do this or the program will not terminate. [This is a design fault!]

The pfor statement requires that iterations of the loop be either uncoupled, or coupled appropriately, for example, by using atomic variables.

If pfor statements are nested, the result is undefined. It is always bad for performance and is likely to lead to a deadlock. A nested pfor is executed from a job running in the thread pool and will submit further jobs to the thread pool and then wait for them to complete. Unfortunately it is likely the won't start because the submitting job is still active, even though it is waiting.

# 6.16 Loops over iterators

The iterator based for loop takes sets a variable to each value stored in any data type with an iterator:

```
for i in (1,2,3) perform println$ i;
for i in 0..<10 perform println$ i;</pre>
```

An iterator is a generator taking the data type as an argument and returning an option type. The iterator over the data type constructs and iterator and then repeatedly calls it until it returns None, storing the argument v of the Some v otherwise returned in i and then executing the loop body.

The iterator is obtained generically, that is, by attempting to apply a function named iterator to the container.

The argument can also be any generator returning an option type, including any iterator.

This loop is wrapped in a block so that the control variable is *not* available at the end of the loop, definitions in the body do not leak into the surrounding context, and jumps into the loop body are not possible.

#### 6.16.1 Recursive for loop

The rfor loop is similar to the iterator based for loop, however it constructs a new data frame for each iteration. It does this by converting the loop into a procedure which self-tail calls itself to implement the iteration.

The compiler may optimise an **rfor** loop using self-tail-call optimisation, so it uses a single frame, as for a **for** loop. However, the optimisation is not performed unless it is safe, and in particular if a pointer to a local variable is exported from the body, it cannot be performed.

An rfor loop should be used when creating a closure that binds to the loop body, if you wish it to bind to the current values of that iteration. If a for loop is used instead the closure will bind to the sole data frame and containing the values of the last iteration, not the values current at the time the closure is formed. For example:

```
begin
    println$ "for loop -----";
    var v = varray[1->int] 4uz;
    for i in (0,1,2,3) perform push_back(v,{i});
    for j in 0..3 perform println$ #(v.j);
    // 3,3,3,3
end
begin
    println$ "rfor loop -----";
    var v = varray[1->int] 4uz;
    rfor i in (0,1,2,3) perform push_back (v,{i});
    for j in 0..3 perform println$ #(v.j);
    // 0,1,2,3
end
```

#### 6.16.2 match/in

This is an advanced iterator based loop which allows a single arbitrary pattern match to be applied to the values supplied by the iterator and present only those which match to the loop body.

```
match x,y when x < y in ((1,2),(4,3))
perform println$ x,y;</pre>
```

### 6.17 Assertions

Library Reference

#### 6.17.1 assert

Ad hoc assertion throws an assertion exception if its argument is false.

```
assert x > 0;
```

#### 6.17.2 axiom

An axiom is a relationship between functions, typically polymorphic, which is required to hold.

```
axiom squares (x:double) => x * x >= 0;
class addition[T]
{
   virtual add : T * T -> T;
```

```
virtual == : T * T -> bool;

axiom assoc (x:T, y:T, z:T) :
   add (add (x,y),z) == add (x, add (y,z))
;
}
```

In a class, an axiom is a specification constraining implementations of virtual function in instances.

Axioms are restricted to first order logic, that is, they may be polymorphic, but the universal quantification implied is always at the head.

Existential quantification can be provided in a constructive logic by actually constructing the requisite variable.

Second order logic, with quantifiers internal to the logic term, are not supported.

#### 6.17.3 lemma

A lemma is similar to an axiom, except that is it easily derivable from axioms; in particular, a reasonable automatic theorem prover should be able to derived it.

#### 6.17.4 theorem

A theorem is similar to a lemma, except that it is too hard to expect an automatic theorem prover to be able to derive it without hints or assistance.

There is currently no standard way to prove such hints.

#### 6.17.5 reduce

A reduce statement specifies a term reduction and is logically equivalent to an axiom, lemma, or theorem, however it acts as an instruction to the compiler to attempt to actually apply the axiom.

The compiler may apply the axiom, but it may miss opportunities for application.

The set of reductions must be coherent and terminal, that is, after a finite number of reductions the final term must be unique and irreducible.

Application of reduction is extremely expensive and they should be used lightly.

```
reduce revrev[T] (x: list[T]) : rev (rev x) => x;
```

#### 6.18 invariant

An invariant is an assertion which must hold on the state variables of an object, at the point after construction of the state is completed by the constructor function and just before the record of method closures is returned, and, at the start and end of every method invocation.

The invariant need not hold during execution of a method.

Felix inserts the a check on the invariant into the constructor function and into the post conditions of every procedure or generator method.

```
object f(var x:int, var y:int) =
{
   invariant y >= 0;
   method proc set_y (newy: int) => y = newy;
}
```

### 6.19 code

The code statement inserts C++ code literally into the current Felix code.

The code must be one or more C++ statements.

```
code 'cout << "hello";';</pre>
```

### 6.20 noreturn code

Similar to code, however noreturn code never returns.

```
noreturn code "throw 1;";
```

# 6.21 Service call

The service call statement calls the Felix system kernel to perform a specified operation.

It is equivalent to an OS kernel call.

The available operations include:

```
union svc_req_t =
/*0*/ | svc_yield
/*1*/ | svc_get_fthread of &fthread // CHANGED LAYOUT
/*2*/ | svc_read of address
```

```
/*3*/ | svc_general
                                of &address
                                               // CHANGED LAYOUT
/*4*/ | svc_reserved1
/*5*/ | svc_spawn_pthread
                                of fthread
/*6*/ | svc_spawn_detached
                                of fthread
/*7*/ | svc_sread
                                of _schannel * &gcaddress
/*8*/ | svc_swrite
                                of _schannel * &gcaddress
/*9*/ | svc_kill
                                of fthread
/*10*/ | svc_reserved2
/*11*/ | svc_multi_swrite
                                of _schannel * &gcaddress
/*12*/ | svc_schedule_detached of fthread
```

These operations are typically related to coroutine or thread scheduling. However svc\_general is an unspecified operation, which is typically used to invoke the asynchronous I/O subsystem.

Service calls can only be issued from flat code, that is, from procedures, since they call the system by returning control, the system must reside exactly one return address up the machine stack at the point a service call is executed.

# 6.22 with/do/done

The with/do/done statement is use to define temporary variables which are accessible only in the do/done body of the statement.

It is the statement equivalent of the let expression.

```
var x = 1;
with var x = 2; do println$ x; done
assert x == 1;
```

# 6.23 do/done

The do/done statement has no semantics and merely acts as a way to make a sequence of statements appear as a single statement to the parser.

Jumps into do/done groups are therefore allowed, and any labels defined in a do/done group are visible in the enclosing context.

Any variables, functions, or other symbols defined in a do/done group are visible in the enclosing context.

```
do something; done
```

# 6.24 begin/end

The begin/end statement creates an anonymous procedure and then calls it. It therefore appears as a single statement to the parser, but it simulates a block as would be used in C. It is exactly equivalent to a brace enclosed procedure called by a terminating semi-colon.

```
begin
   var x = 1;
end
// equivalent to
{
   var x = 1;
};
```

# Chapter 7

# Expressions

#### Syntax

Expressions are listed in approximate order of precedence, starting with the weakest binding.

We will often exhibit expressions in the form

```
var x = expr;
```

so as to present a complete statement. The  $\mathbf{x}$  is of no significance.

# 7.1 Priority levels

```
priority
   let_pri <
   slambda_pri <
   spipe_apply_pri <
   sdollar_apply_pri <
   stuple_cons_pri <
   stuple_pri <
   simplies_condition_pri <
   sor_condition_pri <
   sand_condition_pri <
   snot_condition_pri <
   stex_implies_condition_pri <
   stex_or_condition_pri <
   stex_or_condition_pri <
   stex_or_condition_pri <
   stex_and_condition_pri <
   stex_and_condition_pri <
   stex_and_condition_pri <
   stex_and_condition_pri <
   stex_not_condition_pri <</pre>
```

```
scomparison_pri <</pre>
sas_expr_pri <
ssetunion_pri <
ssetintersection_pri <
sarrow_pri <</pre>
scase_literal_pri <
sbor_pri <
sbxor_pri <
sband_pri <
sshift_pri <
ssum_pri <
ssubtraction_pri <
sproduct_pri <</pre>
s_term_pri <
sprefixed_pri <</pre>
spower_pri <
ssuperscript_pri <
srefr_pri <</pre>
sapplication_pri <</pre>
scoercion_pri <
sfactor_pri <
srcompose_pri <</pre>
sthename_pri <
satomic_pri
```

### 7.2 Chain forms

#### 7.2.1 Pattern let

The traditional let binding of ML. The syntax is

```
var x = let pattern = expr1 in expr2; // equivalent to
var x = match expr1 with pattern => expr2 endmatch;
```

```
var x = let a = 1 in a + 1; // equivalent to
var x = match 1 with a => a + 1 endmatch
```

#### 7.2.2 Function let

A let form which makes a function available in the expression

```
var x =
  let fun f(y:int)=> y + 1 in
  f 42
;
```

#### 7.2.3 Match chain

A variant on the terminated match which allows a second match to be chained onto the last branch without any endmatch.

#### 7.2.4 conditional chain

A variant on the terminated if/then/elif/else allowing chaining.

```
var x =
  if c1 then r1
  elif c2 then r2 else
  if c3 then r3 else
  r4
;
```

### 7.3 Alternate conditional chain

```
var x = n / d unless d == 0 then 0;
```

# 7.4 Dollar application

A right associative low precedence forward apply operator taken from Haskell.

```
var x = str$ rev$ list$ 1,2,3;
```

# 7.5 Pipe application

A left associative low precedence reverse apply operator taken from C#.

```
var x = 1,2,3 |> list |> rev |> str;
```

# 7.6 Tuple cons constructor

A right associative cons operator for tuples. Allows concatenating an element to the head/front/left end of a tuple. Can also be used in a pattern match to recursively decode a tuple like a list.

```
var x = 3,4;
var y = 1 ,, 2 ,, x; // 1,2,3,4
```

# 7.7 N-ary tuple constructor

The is a non-associative n-ary tuple constructor consists of a sequence of expressions separated by commas.

```
var x = 1,2,3,4;
```

# 7.8 Logical implication

An operator for function implies.

```
var x = false implies true;
```

# 7.9 Logical disjunction

A chaining operator for function lor.

```
var x = true or false;
```

A shortcut enabled disjunction is available too:

```
fun f(x:int, y:int) =>
    y == 0 or else x / y > 1
;
println$ f(1,0), f(10,1), f(1,10);
```

This operation is very expensive. The second argument is translated to a closure and the system orelse function is called:

```
noinline fun orelse (x: bool, y:1->bool) : bool =>
  if x then true else #y
;
```

The closure and conditional ensure the second argument is only evaluated if the first is false.

# 7.10 Logical conjunction

A chaining operator for function land.

```
var x = true and false;
```

A shortcut enable conjunction is available too:

```
fun g(x:int, y:int) =>
    y != 0 and then x / y <= 1
;
println$ g(1,0), g(10,1), g(1,10);</pre>
```

This operation is very expensive. The second argument is translated to a closure and the system andthen function is called:

```
noinline fun andthen (x: bool, y:1->bool) : bool =>
  if x then #y else false
;
```

The closure and conditional ensure the second argument is only evaluated if the first is true.

# 7.11 Logical negation

A bool operator for function lnot.

# 7.12 Comparisons

Non-associative.

```
var x =
    a < b or
    a > b or
    a <= b or
    a >= b or
    a == b or
    a!= b or
    1 in list(1,2,3)
    1 \in list (1,2,3);
;
```

# 7.13 Name temporary

Allows a subexpression to be named as a val by default or a var.

```
var x = a + (f y as z) + z; // equivalent to
val z = f y; var x = a + z + z;

var x = a + (f y as var k) + k; // equivalent to
var k = f y; var x = a + k + k;
```

Note that the var for ensures the subexpression is eagerly evaluated, before the containing expression.

# 7.14 Schannel pipe operators

Used to flow data through schannels from the source on the left to the sink on the right via processing units in between.

```
spawn_fthread$ source |-> filter |-> enhancer |-> sink;
```

This variant uses an iterator to stream data out of a data structure:

```
spawn_fthread$ list (1,2,3) >-> sink;
```

# 7.15 Right Arrows

Right associative arrow operators.

List cons operator.

```
var x = 1 ! 2 ! list (3,4);
```

Function types (type language only):

```
D -> C // Felix function
D --> C // C function pointer
```

#### 7.16 Case literals

The case tag is only used in pattern matches. The sum or union type isn't required because it can be deduced from the match argument.

```
var a = match a with Some v => v | #None => 0;
```

The case constructor with integer caseno has two uses.

It creates a value of a sum type with no arguments:

```
var x = case 1 of 2; // aka true
```

or it is a function for a sum type variant with an argument:

```
var x = (case 1 of int + double) 4.2;
```

A case literal with a name instead of an integer constructs a variant instead:

```
typedef maybe = union { No; Yes of int; };
var x = (case Yes of maybe) 42;
```

The tuple projection function names a tuple projection:

```
typedef triple = int * long * string;
var snd = proj 1 of triple;
var y: int = snd (1, 2L, "3");
```

# 7.17 Bitwise or

Left associative.

```
\operatorname{var} x = q | \mathbf{v} | b;
```

## 7.18 Bitwise exclusive or

Left associative.

```
\operatorname{var} x = q \sqrt{\hat{b}};
```

# 7.19 Bitwise and

Left associative.

### 7.20 Bitwise shifts

Left associative.

```
var x = a << b; // left shift
var x = a >> b; // right shift
```

### 7.21 Addition

Chain operator. Non-associative for types. Left associative for expressions.

```
var x = a + b + c;
```

## 7.22 Subtraction

Left associative.

```
var x = a - b;
```

# 7.23 Multiplication

Chain operator. Non-associative for types. Left associative for expressions.

```
var x = a * b;
```

# 7.24 Division operators

Left associative. Not carefully: higher precedence that multiplication, unlike C!!

```
var x = a * b / c * d; // means
var x = a * (b / c) * d;

var x = a * b % c * d; // means
var x = a * (b % c) * d;
```

## 7.25 Prefix operators

```
var x = !a;
var x = -a; // negation
var x = ~a; // bitwise complement
```

# 7.26 Fortran exponentiation

Infix \*\*} is special syntax for function @{pow. The left operand binds more tightly than \*\* but the right operand binds as for prefixed operators or more tightly. Observe than that:

```
var x = -a**-b; // means
var x = -(a**(-b));
```

preserving the usual mathematical syntax.

# 7.27 Felix exponentiation

Left associative. The right operand binds as deref operator or more tightly. Used for array notation in the type language.

```
var x = a ^ ix;
```

# 7.28 Function composition

Standard math notation. Left associative. Same precedence as exponentiation. Spelled  $\ensuremath{\mbox{\sc Square}}$ 

```
var x = f \circ g;
```

# 7.29 Dereference

For function deref.

```
var x = *p;
```

For builtin dereference operator:

```
var x = _deref p;
```

Note these usually have the same meaning however the function deref can be overloaded. If the overloaded definition is not to be circular it may use \_deref when dereferencing pointers.

#### 7.29.1 Operator new

Copies a value onto the heap and returns a pointer.

```
var px = new 42;
```

# 7.30 Whitespace application

Operator whitespace is used for applications.

#### **7.30.1** General

```
var x = sin y;
```

#### 7.30.2 Caseno operator

Returns the integer tag value of the value of an anonymous sum, union, or variant type.

```
var x = caseno true; // 1
var x = caseno (Some 43); // 1
```

#### 7.30.3 Likelyhood

Indicaties if a bool valued expression is likely or unlikely to be true. Used to generate the corresponding gcc optimisation hints, if available.

```
if likely (c) goto restart;
if unlikely (d) goto loopend;
```

## 7.31 Coercion operator

left associative. The right operand is a type.

```
var x = 1L :>> int; // cast
```

### 7.32 Suffixed name

The most general form of a name:

```
var x = qualified::name of int;
```

Used to name functions, with the right operand specifying the function argument type.

#### 7.33 Factors

#### 7.33.1 Subscript

Used for array and string subscripting. Calls function subscript. For strings, returns a character. If the subscript is out of range after adjustment of negative index, returns char 0 and thus cannot fail.

```
var x = a . [i]; // i'th element
```

### 7.33.2 Subsstring

Calls function **substring**. Negative indices may be used to offset from end, i.e. -1 is the index of the last element. Out of range indices (past the end or before the start, after adjustment of negative indices) are clipped back to the end or start respectively.

```
var x = a . [ first to past];
   // past is one past the last element refered to
```

### 7.33.3 Copyfrom

Calls function copyfrom. Copies from designated index to end. Supports negative indices and range clipping for strings.

```
var x = a . [to past]; // from the first
```

#### 7.33.4 Copyto

Calls function copyto. Supports negative indices and range clipping for strings.

```
var x = a . [to past]; // from the first
```

#### 7.33.5 Reverse application

Left associative.

```
var x = y .f; // means
var x = f y;
```

#### 7.33.6 Reverse application with deref

Left associative

```
var x = p *. k; // means
var x = (*p) . k;
```

#### 7.33.7 Reverse application with addressing

Left associative

```
var x = v \&. k; // means

var x = (&v) . k;
```

#### 7.33.8 Unit application

Prefix operator applies argument to empty tuple.

```
var x = #f; // means
var x = f ();
```

#### 7.33.9 Addressing

Finds the pointer address of a variable. Means pointer to in type language.

```
var x : int = 1;
var px : &int = &x;
  // address of x
  // type pointer to int
```

### 7.33.10 C pointer

Used in type language for pointer to type or NULL.

```
var px : @char = malloc (42);
```

Note that this symbol is also used in fdoc as a markup indicator. Please keep out of column 1, do not follow with a left brace.

#### 7.33.11 Macro freezer

Used to disable macro expansion of a symbol.

```
macro val fred = joe;
var x = fred + noexpand fred; // means
var x = joe + fred;
```

### 7.33.12 Pattern variable

Notation v Used in patterns to designate a val variable to be bound in the pattern matching.

```
var x =
   match y with
   | Some v => "Some " + v.str
   | #None => "None";
;
```

# 7.33.13 Parser argument

Notation n} for some integer  $\mathbb{Q}\{n$ . In user defined syntax designates the n'th term of a syntax production.

# 7.34 Qualified name

A name in Felix has the form:

```
class1 :: nested1 :: ... :: identifier [ type1, type2, ... ]
```

where the qualifiers and/or type list may be elided. This is the same as C++ except we use []} instead of  $Q{<>}$  for template argument types.

# Chapter 8

# Atoms

# 8.1 Record expression

```
var x = (name="Hello", age=42);
```

# 8.2 Alternate record expression

```
var x =
  struct {
    var name = "Hello";
    var age = 42;
  }
;
```

# 8.3 Variant type

Denotes a variant type.

```
var x :
   union {
    Cart of double * double;
    Polar of double * double;
}
;
```

# 8.4 Wildcard pattern

Used in a pattern match, matches anything.

```
var x = match a with _ => "anything";
```

# 8.5 Ellipsis

Used only in C bindings to denote varags.

```
fun f: int * ... -> int;
```

### 8.6 Truth constants

```
false // alias for case 0 of 2
true // alias for case 1 of 2
```

# 8.7 callback expression

??

```
callback [ x ]
```

# 8.8 Lazy expression

Function of unit.

```
var f = { expr };
var x = f ();
```

# 8.9 Sequencing

Function dependent on final expression.

```
var x = ( var y = 1; var z = y + y; z + 1 ); // equivalent to var x = #{ var y = 1; var z = y + y; return z + 1; };
```

## 8.10 Procedure of unit.

```
var p = { println$ "Hello"; } // procedure
p ();

var f = { var y = 1; return y + y; }; // function
var x = f ();
```

## 8.11 Grouping

Parentheses are used for grouping.

```
var x = (1 + 2) * 3;
```

# 8.12 Object extension

```
var x = extend a,b with c end;
```

# 8.13 Conditional expression

```
var x =
  if c1 then a elif c2 then b else c endif
;
```

# Chapter 9

# Pattern Matching

The patterns are composed of these forms:

```
pat | pat | pat ... // alternate matches
                        // tuple match
(v1, v2, ...)
h!t
                        // list match
h,,t
                        // tuple cons
                        // const union or variant match
Ctor
                        // nonconst union or variant match
Ctor v
(fld1=f1, fld2=f2, ...) // record match
pat as v
                       // assign variable to matched subexpression
                        // guarded match
pat when expr
                        // match either pattern
pat1 | pat2
999
                       // integer match
"str"
                        // string match
                        // range match
lit1 .. lit2
                        // wildcard match
```

The guarded match only matches the pattern if the guard expression is true.

```
match x with
| (x,y) when y != 0 => ...
endmatch
```

The tuple as list cons match is a form of row polymorphism where the first element of a tuple and the remaining elements considered as a tuple are matched.

A good example of this is found in the library here which allows printing a tuple of arbitrary number of components, indeed, this facility was implemented precisely to allow this definition in the library.

Record matches succeed with any record containing a superset of the specified fields.

As well as integer and string matches, a literal of any type with an equality and inequality operator can be matched. In addition, if there is a less than or equal operator <= an inclusive range match can be specified.

# Chapter 10

# **Definitions**

Syntax

### 10.1 Functions

A felix function definition takes one of three basic forms:

```
fun f (x:int) = { var y = x + x; return y + 1; }
fun g (x:int) => x + x + 1;
fun h : int -> int = | x => x + x + 1;
```

The first form is the most general, the body of the function contains executable statements and the result is returned by a return statement.

The second form is equivalent to a function in the first form whose body returns the RHS expression.

The third form specifies the function type then the body of a pattern match. It is equivalent to

```
fun h (a:int) = { return match a with | x => x + x + 1 endmatch; }
```

The first two forms also allow the return type to be specified:

```
fun f (x:int) : int = { var y = x + x; return y + 1; }
fun g (x:int) :int => x + x + 1;
```

Functions may not have side effects.

All these function have a type:

```
D -> C
```

where D is the domain and C is the codomain: both would be int in the examples.

A function can be applied by the normal forward notation using juxtaposition or what is whimsically known as operator whitespace, or in reverse notation using operator dot:

```
f x x.f
```

Such applications are equivalent. Both operators are left associative. Operator dot binds more tightly than whitespace so that

```
f x.g // means
f (g x)
```

A special notation is used for application to the unit tuple:

```
#zero // means
zero ()
```

The intention is intended to suggest a constant since a pure function with unit argument must always return the same value.

This hash operator binds more tightly than operator dot so

```
#a.b // means
(#a).b
```

# 10.2 Pre- and post-conditions

A function using one of the first two forms may have pre-conditions, post-conditions, or both:

```
fun f1 (x:int when x > 0) => x + x + 1;
fun f2 (x:int) expect result > 1 => x + x + 1;
fun f3 (x:int when x > 0) expect result > 1 => x + x + 1;
fun f4 (x:int when x > 0) : int expect result > 1 => x + x + 1;
```

Pre- and pos-conditions are usually treated as boolean assertions which are checked at run time. The compiler may occasionally be able to prove a pre- or post-condition must hold and elide it.

The special identifier result is used to indicate the return value of the function.

## 10.3 Higher order functions

A function may be written like

```
fun hof (x:int) (y:int) : int = { return x + y; }
fun hof (x:int) (y:int) => x + y;
```

These are called higher order functions of arity 2. They have the type

```
int -> int -> int // or equivalently
int -> (int -> int) //since -> is right associative.
```

They are equivalent to

```
fun hof (x:int) : int -> int =
{
  fun inner (y:int) : int => x + y;
  return inner;
}
```

that is, a function which returns another function.

Such a function can be applied like

```
hof 1 2 // or equivalently
(hof 1) 2
```

since whitespace application is left associative.

#### 10.4 Procedures

A function which returns control but no value is called a procedure. Procedures may have side effects.

```
fun show (x:int) : 0 = { println x; }
proc show (x:int) { println x; }
proc show (x:int) => println x;
```

The second form is a more convenient notation. The type 0 is also called **void** and denotes a type with no values.

A procedure may return with a simple return statement:

```
proc show (x:int) { println x; return; }
```

however one is assumed at the end of the procedure body.

Procedures can also have pre- and post-conditions.

A procedure may be called like an application, however it must be a whole statement since expressions of type void may not occur interior to an expression.

```
show 1;
1.show;
```

If a procedure accepts the unit argument, it may be elided:

```
proc f () => show 1;
f; // equivalent to
f ();
```

## 10.5 Generators

A generator is a special kind of function which is allowed to have side effects. It is defined similarly to a function, but using the binder gen instead of fun:

```
var seqno = 1;
gen seq () { var result = seqno; ++seqno; return result; }
```

When a generator is directly applied in an expression, the application is replaced by a fresh variable and the generator application is lifted out and assigned to the variable. For example:

```
fun twice (x:int) => x + x;
println$ twice #seq;
```

will always print an even number because it is equivalent to

```
var tmp = #seq;
println$ twice tmp;
```

Therefore even if twice is inlined we end up with the argument to println} being O{tmp+tmp} and not O{#se which would print an odd number.

#### 10.5.1 Yielding Generators

A generator may contain a yield statement:

```
gen fresh() {
  var x = 1;
  while x < 10 do
    yield x;
    ++x;
  done
  return x;
}</pre>
```

In order to use such a yielding generator, a closure of the generator must be stored in a variable. Then the generator may be called repeatedly.

```
var g = fresh;
for i in 1 upto 20 do
   println$ i,#g;
done
```

This will print pairs (1,1), (2,2) up to (10,10) then print (11,10), (12,10) up to (20,10).

The yield statement returns a value such that a subsequent call to a closure of the generator will resume execution after the yield statement. Therefore yield is a kind of cross between a return and a subroutine call.

If a generator executes a return statement, that is equivalent to yielding a value and setting the resume point back to the return statement, in other words return expr; is equivalent to

```
while true do yield expr; done
```

Yielding generators should not be called directly because they will always start at the beginning with a fresh copy of any local variables used to maintain state.

Function closures differ from generator closures in that the closures is cloned before every application to ensure that the initial state is fresh.

Yielding generators are primarily intended to implement iterators, that is, to provide lazy lists or streams.

## 10.6 Conversion Operators

Felix provides a special notation which allows an identifier naming a type to return a value of that type:

```
typedef cart = dcomplex;
typedef polar = dcomplex;
ctor cart (x:double, y:double) => dcomplex (x,y);
ctor polar (r: double, theta: double) =>
    dcomplex (r * sin theta, r * cos theta)
;
var z = cart (20.0,15.0) + polar (25.8, 0.7 * pi);
```

Such conversion operators are sometimes (incorrectly) called constructors. The constructions are equivalent to

```
fun _ctor_cart (x:double, y:double) : cart => dcomplex (x,y);
fun _ctor_polar (r: double, theta: double): polar =>
    dcomplex (r * sin theta, r * cos theta)
;
```

When a type with a simple name is applied to a value, Felix tries to find a function with that name prefixed by \_ctor\_ instead.

Note that Felix generates a constructor for struct and cstruct types automatically with argument type the product of the types of the structure fields.

# 10.7 Special function apply

When Felix finds and application

```
f a
```

where **f** is a value of type F which is not a function (or C function) type, Felix looks instead for a function named apply with argument of type:

```
F * A
```

where A is the type of a. For example

```
fun apply (x:string, y:string) => x + y; // concat
var x = "hello " "world"; // apply a string to a string
```

## 10.8 Dynanic Objects

Felix provides an object system with syntax based on Java, and technology based on CLOS.

An object is a record of function closures, closed over the local scope of a constructor function that returns the record.

```
interface person_t {
    get_name: 1 -> string;
    set_age: int -> 0;
    set_job : string -> 0;
    get_job : 1 -> string;
}

object person (name:string, var age:int) implements person_t =
{
    var job = "unknown";
    method fun get_name () => name;
    method proc set_age (x:int) { age = x; }
    method fun get_job () => job;
    method proc set_job (x:string) { job = x; }
}

var john = person ("John", 42);
println$ #(john.name) + " is " + #(john.age).str;
```

The entity person is a function which when called with its argument of name and age returns a record of type person\_t consisting of closures of the functions and procedures marked as method in its definition.

Since functions hide their local variables the object state is hidden and can only be accessed using the methods.

The implements clause is optional.

Objects provide an excellent way for a dynamically loaded shared library to export a set of functions, only the object function needs to be exported so it has a C name which can be linked to with dlopen.

# Part II Gross Structure

# Chapter 11

# Program structure

A Felix program consists of a nominated root parse unit and the transitive closure of units with respect to inclusion.

The behaviour of this system consists of the action of the initialisation code in each unit, performed in sequence within a given unit, with the order of action between units unspecified.

#### 11.1 Parse Unit

A parse unit is a file augmented by prefixing specified import files to the front. These consist of a suite of grammar files defining the syntax and other files defining macros.

By convention syntax files have the extension .fsyn, and other import files have the extension .flxh.

With this augmentation all parse units in a program are independently parsed to produce an list of statements represented as abstract syntax, denoted an AST (even though it is a list of trees, not a single tree).

#### 11.2 AST

The program consists of the concatenation of the ASTs of each parse unit, resulting in a single AST, which is then translated to a C++ translation unit by the compiler.

The ASTs to be concatenated are those parsed from the parse units specified by the transitive closure of include directives.

The order of concatenation is unspecified. Note that include directives do *not* cause an AST to be inserted at the point where the directive is written.

Parse units can be and are parsed independently. The contents of a parse unit cannot influence the parsing of another.

#### 11.3 Include Directive

#### 11.3.1 Syntax

An include directive has the syntax:

```
include "filename";
include "dirname/filename";
include "./filename";
```

where the filename is a Unix relative filename, may not have an extension, and may not begin with or contain . . (two dots).

If the filename begins with ./ then the balance of the name is relative, a sibling of the including file, otherwise the name is searched for on an include path.

In either case, a search succeeds when it finds a file with the appropriate base path in the search directory with extension .flx or .fdoc. If both files exist the most recently changed one is used. If the time stamps are the same the choice is unspecified.

#### 11.3.2 Effect

An include directive is included in the AST generated by the parser.

An extraction process extracts the set of directives and locates the files specified and adds them to a set of files which must be parsed.

Unparsed files are upgraded to parse units and parsed, and then the extraction process again applied.

When all the files have been processed the resulting ASTs are concatenated.

Felix uses a caching scheme to avoid parsing all the files every time.

#### 11.4 Grammar

The Felix grammar is part of the library. It is notionally prefixed to each file to be processed prior to any import files to specify the syntax with which the file is to be parsed and translated to an AST.

The grammar uses an augmented BNF like syntax with parse actions specified in R5RS Scheme.

The resulting S-expressions are translated to an intermediate form and then into an internal AST structure.

The parser is a scannerless GLR parser with significant extensions.

# Chapter 12

# **Parsing**

Felix has the most advanced parser of any production programming language. The parser is extensible, and Felix makes good use of this. The core, hardcoded grammar, called the *bootstrap grammar* does not provide the syntax for the Felix programming language the average production programmer is interested in.

Therefore, we recommended this chapter be lightly scanned or even skipped, until such time as a deeper understanding is required. Nevertheless we feel obligated to present some details now, since the ability to define Domain Specific Sub-Languages is one of the key advantages of the Felix system.

In Felix, the usual programming language is defined by a grammar in the library in user space. The compiler interprets the grammar to produce a parser for the scope in which the grammar is active. Grammar extension activations are properly scoped.

As with any modern programming language it is sometimes difficult to distinguish features present in the core language and those defined in the standard library. In particular the semantics of some features in the library could not be defined in the core language, but their syntactic representation can be. This is most evident in the C programming language where, for example, Posix defines semantics for multi-threading which are represented by library functions which could not possibly be defined in C.

However in Felix the situation is even more extreme, since the very language itself is defined in the library. What is more, most of the definitions are real Felix code: we are not just leveraging the library for syntactic modelling of semantics we could not otherwise define, but are actually presenting the definitions.

Naturally this is not possible without a core built-in parsing system and semantics, this called the bootstrap parser and the first stage abstract machine.

It reads the library syntax specifications to extend itself to the full blown Felix

language described in this document and maps the input syntax onto terms of the abstract machine.

## 12.1 Bootstrap Parser Grammar

#### Compiler Reference

The bootstrap parser is a hard coded parser which translates Felix EBNF like syntax specification into a parser automaton, which in turn translates Felix programs.

#### 12.1.1 Parser Processing

Felix use the Dypgen parsing system, which is a run time extensible GLR parsing engine with extensions.

When the parsing of the production of a non-terminal is complete, the associated action code is executed.

The action code is a string containing a procedure written in R5RS Scheme. The OCS Scheme language processor is used for the processing.

Using predefined variables representing the s-expressions associated with the evaluation of the actions associated with the symbols of the production, the client action code constructs a new s-expression representing the intended AST for parsing that production.

#### Example

Here is a complete, self contained, working example:

```
// define the DSSL Ceiling
syntax Ceiling {
   satom := "\lc" sexpr "\rc" =>#
        "`(ast_apply ,_sr (,(noi 'ceiling) (,_2)))"
   ;
}

// define the ceiling operation
fun ceiling (x:double) = "ceil($1)"
   requires '#include <math.h>'
;

// make the DSSL available for use
open syntax Ceiling;

// Use it
println$ \lc 42.3 \rc;
```

In the above example, a production for the satom non-terminal, recognises a the TeX like expression  $\c e \r c$ , where the e in the middle is any expression. The Scheme code returns an s-expression consisting of the ast\_apply symbol, followed by the value in the current source reference variable  $\c s r$ , then a pair consisting of the function name ceiling to be executed and its argument  $\c s r$  which is the s-expression returned from the second position in the prodiction.

The Scheme function noi converts a symbol into an s-expression which is the AST representation of a Felix name. The ast\_apply s-expression is the AST representation of a Felix application.

We then define the function ceiling in Felix by lifting it from the ISO C math library.

Finally we have to open the DSSL so the new grammar becomes active, and then when we write and expression like \lc 42.3 \rc the parser translates it into a function application.

The Felix standard library actually defines \lceil and \rceil and maps [e] to the function ceil so we couldn't use them in the example.

#### 12.1.2 Scheme Actions

Provided the returned AST is acceptable to subsequent processing steps, this mechanism is safe provided the executed Scheme code is purely functional.

If the Scheme actions have side effects, care must be taken. Dypgen parsers may parse the same text more than once. At any point in the parsing process the next symbol is used to determine a possible set of parses, and all these parses are then explored simultaneously.

Most of these parses will fail at some point in the future, and the AST constructed at that point is discarded. Except in special circumstances, if more than one parse succeeds, the Felix translator will fail with a parsing ambiguity.

The point, however, is that side effects from exploratory parses cannot be discarded, nor can the order in which the parses is performed be predicted. Although the parses are, in principle, simultaneous, Dypgen actually processes a single token for each parse in sequence, suspending the parsing of one thread until all parses have processed the token, then resuming with the next token, having discarded failed parses, but also possibly spawning a new set of parses. In other words, the parsing is performed using coroutines which ensure that the input is only consumed in a linear fashion without any backtracking.

If side effects are necessary, then they should usually be idempotent. For example setting a variable to a fixed value is an idempotent operation. Incrementing a variable is not.

There is, however, a special exception to this rule. Top level statements are guaranteed to be parsed exactly once. Although the start symbol is defined recursively, the recursion is optimised to a plain loop. This is not necessarily the case for nested statements!

#### 12.1.3 Spawning Choices

When presented with a non-terminal to parse, a GLR parser notionally processes all alternatives simultaneously. Many of these branches will fail, indeed, if the parse is to be ambiguous all but one should eventually fail. This method could be called purely speculative parsing.

However, Dypgen does not actually try all the alternatives. Some alternatives must start with a particular token or one of a set of tokens. Instead of starting the parse and failing after examining the next token, Dypgen uses an LALR1 predictive parser to narrow down the set of alternatives. The LALR1 automaton is a finite state machine which given the next token supplies a set of possible parse which might continue. Although LALR1 is not accurate, it is conservative, and only rejects alternatives that could not possibly work.

#### 12.1.4 No keywords

In most language, there is a severe lack of usable symbols. To compensate for this, certain identifiers called keywords are specified as symbols instead. The tokeniser checks if an identifier is a keyword and returns a suitable token if it is, otherwise it returns an identifier.

Unfortunately, because keywords encroach on user space, many languages such as C++ try to minimise the set used, and in the case of a language extension, introducing a new keyword may break existing code. So there is tendancy to reuse the keyword in a different context, leading to the nightmare that is evident in C++.

Felix also has keywords, but they are not global. The Felix parser is scannerless which means it does not require a separate tokeniser. Instead tokenisation is local to each parser state, and in particular the identifiers used as keywords are only recognised in this state. Felix also provides a consistent way to unkeyword with a special form of literal to force the parser to recognise an identifier instead of a keyword.

```
// var = 1;
  // Syntax error, variable init expected

var var = 1;
  // OK, declares identifier "var" as a variable
```

```
n"var" = 1;
  // allows assigning to identifier named "var".
```

#### 12.1.5 Predefined Variables

When scheme code is executed certain global variables are automatically predefined.

- The variable \_sr is set to contain the current location in the source file. It consists of a scheme list of the current original source filename as a string, then the starting line, starting column, ending line, and ending column of the text being parsed by the current production.
- The variables \_1, \_2 etc refer to the scheme s-expressions associated with the parse of the n'th symbol in a production.

Together these variables allow the scheme action code of a production to construct an scheme s-expression representing the AST desired for parsing the associated production.

#### 12.1.6 SCHEME statement

The keyword SCHEME followed by a string literal and semi-colon causes the embedded R5RS scheme interpreter to execute the text of the string literal as scheme code during parsing.

It is primarily intended to introduce global procedure definitions as helper functions to be used in the parser action codes.

However it may contain arbitrary Scheme code, including, for example diagnostic output, an interpreter, or anything else. The return value of the execution is discarded.

```
SCHEME """
  (display "Hello parsing world\n")
""";
```

The SCHEME statement may be used anywhere a statement is allowed, it results in a empty statement in the AST. At the top level, the side-effects will only be seen once. However if nested in a grouping statement, multiple explorations of the possible parses of that statement may occur, leading to multiple observations of the side-effects.

#### 12.1.7 STMT statement

The keyword STMT followed by a string literal and semi-colon causes the embedded R5RS scheme interpreter to execute the text of the string literal as scheme

code during parsing.

The result of the execution is returned and appended to the current list of statements being parsed.

It is primarily intended to provide an mechanism whereby arbitary Felix statements can be generated under program control, in other words it is a very sophisticated and properly structured macro processor. The client must have intimated knowledge of the which s-expressions are accepted by the subsequent compiler processing phases and what their semantics are.

Care must be taken if the result of the execution is not invariant. For example if the time, a file from the file system, or other such variable entity is used in the computation, the Felix dependency checking system will not recognise the external dependencies and the cached version of the current file's parse may be used.

```
for i in 0..10 do
    println "Stopping now";
    STMT '`(ast_halt ,_sr "STOPPED")';
done
```

#### 12.1.8 syntax statement

The syntax statement consists of the word syntax followed by an identifier and a list of syntax definition statements enclosed in curly braces { and }. The entity defined is called a *Domain Specific Sub-Language* or just *dssl*.

The given definitions are recorded as a set under the given name but are not activated. For example here is the DSSL for the Felix macros:

```
syntax macros {
  requires expressions, statements, list;

stmt := "macro" "val" snames "=" sexpr ";" =>#
    "`(ast_macro_val ,_sr ,_3 ,_5)";

stmt := "forall" sname "in" sexpr "do" stmt* "done" =>#
    "`(ast_macro_forall ,_sr (,_2) ,_4 ,_6)"
  ;
}
```

#### 12.1.9 requires statement

Within a dssl definition, the requires statement consists of the word requires followed by a comma separated list of identifiers, and terminated by a semi-colon.

The names in the list identify other dssls on which this dssl depends, so that subsequently activating the dssl will also cause the dependent dssls, recursively, to be activated.

#### 12.1.10 Priority statement

The priority statement introduces a set of priority names which can be used for indexed non-terminals, and specifies a total ordering between them, sometimes called a precedence. Here are the priorities used for non-terminal x representing expressions in the Felix grammar, lower priority means weaker binding:

```
priority
  let_pri <</pre>
  slambda_pri <
  spipe_apply_pri <
  sdollar_apply_pri <
  stuple_cons_pri <
  stuple_pri <
  simplies_condition_pri <</pre>
  sor_condition_pri <
  sand_condition_pri <</pre>
  snot_condition_pri <</pre>
  stex_implies_condition_pri <
  stex_or_condition_pri <
  stex_and_condition_pri <</pre>
  stex_not_condition_pri <
  scomparison_pri <</pre>
  sas_expr_pri <
  ssetunion_pri <
  ssetintersection_pri <
  sarrow_pri <</pre>
  scase_literal_pri <</pre>
  sbor_pri <
  sbxor_pri <
  sband_pri <
  sshift_pri <
  ssum_pri <
  ssubtraction_pri <
  sproduct_pri <
  s_term_pri <
  sprefixed_pri <
  spower_pri <
  ssuperscript_pri <
  srefr_pri <</pre>
  sapplication_pri <</pre>
  scoercion_pri <
```

```
sfactor_pri <
srcompose_pri <
sthename_pri <
satomic_pri
;</pre>
```

#### 12.1.11 Non-terminal definition

A nonterminal definition, in its most basic form, consists of the non-terminal name, followed by := followed by a list of alternatives separated by a  $\mid$  followed by a semi-colon ;.

An alternative is a sequence of grammar symbols followed by =># followed by a string. The sequence of symbols is called the rhs (right hand side) of the production, and the string is called the action. The string must encode an R5RS Scheme procedure which returns an s-expression representing the AST subtree desired to be inserted in the syntax tree.

The non-terminal name on the left is either an identifier, or, an identifier followed by [, an priority identifier, followed by ]. A priority identifier is an identifier appearing in a priority specification.

An grammar symbol is either a predefined atom, a string which is required to match the input stream, a non-terminal expression, or a grammar expression enclosed in parentheses ( and ), a macro invocation or a grammar symbol followed by one of \* representing 0 or more occurences, + representing one or more occurences, or ? representing 0 or 1 occurence.

A non-terminal expression is either a name, or a name followed by a priority indicator, or a macro invocation. A priority indicator is a priority name enclosed in either [ and ] which indicates a fixed non terminal, or [> and ] which indicates all the non-terminals with a greater priority than the specified one.

A macro invocation is a name optionally followed by :: and another name, followed by a sequence of macro arguments. A macro argument is a symbol enclosed in < and >.

#### 12.1.12 Preprocessing productions

Felix pre-proceses productions to reduce them to a sequence of basic symbols: either a terminal or non-terminal symbol.

- Expressions contained in parentheses are replaced by a generated non-terminal name and the non-terminal is defined by the enclosed sequence, its action is to return a list of the ASTs of each symbol.
- A non-terminal postfixed by \* or + is replaced by a generated non-terminal defined to recursively generate a list of the non-terminal, with either 0 or

more or 1 or more entries in the list, respectively.

- A non-terminal postfixed by ? returns the a list containing just the sexpression returned by the non-terminal if it is matched, otherwise an empty list.
- Macro calls are expanded. This done by replacing each occurrence of a macro parameter with the corresponding argument of the call.

#### 12.1.13 Grammar Macros

A grammar macro is defined by the same syntax as a non-terminal, except that a sequence of parameter names is added on the lhs after the first name. The first name may not be indexed.

On expansion due to an invocation of a macro, each parameter name in the production is replaced by the non-terminal argument.

As an example, suppose we wish to define a comma separated list of strings, a comma separated list of integers, and a comma separated list of names. By using a macro, the common structure of the productions can be captured: a macro is basically a grammar function. The following is actually found in the Felix library:

```
syntax list
{
    seplist1 sep a := a (sep a)* =># '(cons _1 (map second _2))';
    seplist0 sep a = seplist1<sep><a>;
    seplist0 sep a := sepsilon =># '()';
    commalist1 a = seplist1<","><a>;
    commalist0 a = seplist0<","><a>;
    snames = commalist1<sname>;
    sdeclnames = commalist1<sdeclname>;
}
```

Although grammar macros were primarily intended as basic boilerplate templates, macros can also be passed as arguments to another macro, thereby allowing higher order macros. Furthermore, since arguments are presented in a curried form, closures can also be created, that is, macros with some but not all parameters fixed.

In particular, a macro can actually be passed to itself! Although this seems weird it is in fact a very high power technique used in functional programming and type systems, known as *open recursion*.

Open recursion allows a recursive structure to be extended so that the extensions backport to the core, in other words, the extensions are covariant. This solves a

significant problem in grammar extension. Normally in a grammar extension is easily done by simply adding extra productions for a non-terminal.

The problem is that the nonterminal is then effectively a global variable and extensions from different sources can clash. However the use of a global automatically assures we have covariant extensions, since existing productions using the non-terminal will automatically parse the extensions since they're now alternatives of the non-terminal.

The problem with clashing is only a symptom of the deeper problem: the mechanism does not obey Meyer's Open/Closed principle.

Open recursion solves this problem. The recursions are replaced by parameters, flattening the term structure and allowing extenions in a tree like manner. The programmer then closes the loop at any desired point with a new definition formed by passing the flat term to itself.

More generally, a term structure with more details such as a language with statements, value expressions, type expressions, and patterns, allows any combination of the extensions to be used with nested (recursive) structures equal to the top level or constrained to some lower level as required.

This method obeys the Open/Closed principle because each closure is specific and cannot be further extended, yet the open part of the system remains open for extension.

#### 12.1.14 regdef statement

The regdef statement defines an alias for a regular expression. A regular expression may consist of:

- An atom, being
  - an alias for a regular expression,
  - a string, representing that string,
  - a string in square brackets [] representing one of the characters in the string.
  - an underscore \_ representing any character
  - a dot . representing any character except newline
  - a decimal integer representing the character with that ordinal
  - a range consisting of pair of decimal integers separated by a dash and enclosed in square brackets [ and ] representing one of the characters in the range, inclusive
  - a regular expression in parentheses ( )
- a repetition consisting of an atom optionally followed by

- a \* for zero or more occurences
- a + for one or more occurences
- a ? for zero or one
- a sequence of repetitions
- A list of alternatives separated by a vertical bar | each being a sequence

```
regdef octdigit = ['01234567'];
regdef linefeed = 10;
regdef hichar = [128-255];
regdef white = space | tab;
regdef bin_lit = '0' ('b' | 'B') (underscore? bindigit) +;
```

#### 12.1.15 literal statement

The literal statement associates a non-terminal with a regular expression.

The regular expression is formed by replacing all aliases with their regular definitions, recursively, until no aliases are left.

For example, from the library:

Assuming cstring\_literal is an alias for the regular definition for a C style string, we first create a final alias with the name of the desired non-terminal Cstring.

Then we define Cstring as a non-terminal with the literal statement, giving the required action code. The layout shown is the standard form for literals in the AST. the first field is the source reference \_sr, the second field ftype is the Felix type of the literal. The third field is the internal representation of the value. The last field is a string representing the value in C++.

#### 12.1.16 open syntax statement

The open syntax statement consists of the words open syntax followed by a comma separated list of names.

It simultaneously activates the transitive closure with respect to requires statements, of dssls previously recorded by syntax statements identified by the list of names.

# 12.2 Felix Grammar syntax

Library Package Grammar directory

# Chapter 13

# Modules

Every Felix program is encapsulated in a module with the name being a mangle of the basename of the root unit. The mangling replaces characters in the filename with other characters so that the module name is a valid ISO C identifier.

## 13.1 Special procedure flx\_main

A program module may contain at most one top level procedure with no arguments, exported as flx\_main. After initialisation code suspends or terminates, this procedure is invoked if it exists. It is the analogue of main in C++ however it is rarely used: side-effects of the root unit initialisation code are typically used instead.

A simple example:

```
println "Init";
var i,o = mk_ioschannel_pair[int]();
write (o,42);

export proc flx_main()
{
   println$ "main " + (read i).str;
   println$ "done ..";
}

println$ "Init done";
```

produces output:

```
Init
main 42
done ..
Init done
```

Note that  ${\tt flx\_main}$  must be exported to ensure that an extern "C" symbol is created by the linker.

## 13.2 Libraries

In Felix a library is a root unit together with its transitive closure with respect to inclusion, which does not contain a top level exported flx\_main.

A program unit can be augmented by a set of libraries which are then considered as if included, but without an include directive being present.

# Chapter 14

# Lexicology

All Felix files are considered to be UTF-8 encoded Unicode.

Felix uses a scannerless parser, there are no keywords.

#### 14.1 Comments

There are lexical commenting methods for \*.flx files. Comments are treated as white space separators. For example

```
println$ f/**/x; // parsed as f x not fx
```

The two forms of lexical comments are exclusive, once the parser is scanning one kind of comment the other is not recognised.

#### 14.1.1 C++ comments

 $\mathrm{C}++$  style comments consist of // followed by all the characters up to and including the next newline character.

#### 14.1.2 Nested C comments

C style comments consist of the lead in sequence /\* followed by all the characters up to and including the balancing exit sequence \*/. These comments can span multiple lines and can be nested. When scanning comments lead in and exit sequences are recognised as such even in strings.

## 14.2 Layout

Felix treats code points 0 through 32 (space) as whitespace which may be used freely between symbols. Whitespace is significant in strings, however, and newline is a terminator for C++ style comments.

#### 14.3 File inclusion

There is (deliberately) no support in the Felix language for lexical (physical) file inclusion. Inclusions are processed at the AST level instead, allowing files to be parsed independently of other files. However command line switches can be used to prepend files or sets of files to the command input file, in particular the grammar and some standard macros are notionally inserted.

#### 14.4 fdoc files

As well as \*.flx files, the Felix language processor can directly process \*.fdoc files using a limited subset of available fdoc commands.

fdoc files are processed slighly differently to \*.flx files. The translator begins treating the file in comment mode, so all text is ignored up to a Felix leadin code.

#### 14.4.1 Uncomments

A felix uncomment switches to processing lines as Felix program code. It consists of the line <code>@felix</code>, and is terminated by any line starting with <code>@.</code>

```
@title This is an fdoc.
@h1 Fdocs are documents.
They can contain code:
@felix
var x = 1;
@
Which defines a variable and
@felix
println$ x;
@
which prints it.
```

#### 14.4.2 #line directive

Felix provides support for programs that generate Felix code by allowing C style #line directives. Such a directive consists of the characters #line at the start of a line, followed by whitespace, a decimal number indicating the line number in

the original source, and optionally whitespace followed by a filename in double quotes.

If the filename is present the parser original source filename is set to it. The line number sets the line number, 1 origin, so that the next source line will be taken to be obtained from the original source file at that line number.

Felix provides two standard programs which make use of this facility: flx\_tangle and flx\_iscr both of which are literate programming tools which extract source code from mixed code and comments.

In the event of a compilation error, Felix will specify that the error occurred at a location in the original source file, as indicated by **#line** directives. An example:

```
#line 42 "anerror.fdoc"
var x = error;
```

If this program is processed by Felix the error on the second line will be reported as an error on line 42 of the file anerror.fdoc.

## 14.5 #! directive

If the first line of an \*.flx file starts with #! then the line is ignored. This allows a file on a Unix system marked executable to specify its natural translator so that the file may be run directly as a program. On Linux you should use:

```
#!env /usr/local/lib/felix/felix-latest/host/bin/flx
```

assuming you have a standard install and have linked felix-latest to a directory containing an installed version of Felix such as

```
%/usr/local/lib/felix/felix-2016.05.25%.
```

This is the standard way to refer to the most recent version of Felix installed on Unix systems. Note the path name to the translator on Unix systems must be an absolute path for security reasons.

#### 14.6 Identifiers

#### Library Reference

Felix has three kinds of basic identifiers, plain identifiers, which are an enhanced variant of standard C identifiers, TeX identifiers, which are encodings of mathematical symbols in the style of TeX, and some ascii-art character sequences normally use for punctuation or operators which are also recognised as names.

#### 14.6.1 Plain Identifiers

A plain identifier starts with a letter or underscore, then consists of a sequence of letters, digits, dash (-), apostrophy ('), has no more than one apostrophy or dash in a row, except at the end no dash is allowed, and any number of apostrophies.

```
Ab_cd1 a' b-x
```

Identifies starting with underscore are reserved for the implementation.

A letter may be any Unicode character designated for use in an identifier by the ISO C++ standard. In practice, all high bit set octets are allowed. Identifiers are uniquely identified by their sequence of ISO-10646 (Unicode) code points, alternate encodings of the same glyph are distinct.

#### 14.6.2 TeX Identifiers

A TeX identifier starts with a slosh and is followed by a sequence of letters.

Here is a partial table of TeX Symbols recognised by the grammar as identifiers with undefined semantics but pre-assigned kind and precedence.

## 14.7 Operator Identifiers

Felix allows some operators to be used as an identifier. For example you can write:

```
fun +: int * int -> int = "$1+$2";
```

to define addition on int in C. Symbols recognised by the parser such as + are usually mapped to functions with the same name as the operator.

These operators are recognised as identifiers by the parser in positions where an identifier is expected:

```
+ - * / % ^
\& \| \^ ~
= += -= *= /= %= ^= &= |= <<= >>=
< > == != <= >= << >>
```

#### 14.7.1 Special identifiers

The special string literal with a "n" or "N" prefix is a way to encode an arbitrary sequence of characters as an identifier in a context where the parser might interpret it otherwise. It can be used, for example, to define special characters as functions. For example:

```
typedef fun n"@" (T:TYPE) : TYPE => cptr[T];
```

#### 14.8 Boolean Literals

There are two literals of type bool, namely true and false.

## 14.9 Integer Literals

#### Library Reference

An plain integer literal consists of a sequence of digits, optionally separated by underscores. Each separating underscore must be between digits.

A prefixed integer literal is a plain integer literal or a plain integer literal prefixed by a radix specifier. The radix specifier is a zero followed by one of the letters bB for binary radix, oO for octal radix, optionally on may use dD for decimal radix, although this is the default, and xX for hexadecimal radix.

An underscore is permitted after the prefix.

The radix is the one specified by the prefix or decimal by default.

The digits of an integer consist of those permitted by the radix: 01 for binary, 01234567 for octal, 0123456789 for decimal, 0123456789abcdefABCDEF for hex.

Note there are no negative integer literals.

A type suffix may be added to the end of a prefixed integer to designate a literal of a particular integer type, it has the form of an upper or lower case letter or pair of letters usually combined with a prefix or suffix u or U to designate an unsigned variant of the type. The allowed lower case suffices are:

```
t s l ll
ut us u ul ull
tu su lu llu
i8 i16 i32 i64
u8 u16 u32 u64
p d j
zu pu du ju
uz up ud uj
```

In addition, one or more letters may be upper case, except that 1L and L1 are not permitted.

There is a table of the types Table 30.1 Felix Integer Types.

Note the suffices do not entirely agree with C.

## 14.10 Floating point literals

#### Library Reference

Floating point literals follow ISO C89, except that underscores are allowed between digits, and a digit is required both before and after the decimal point if it is present.

The mantissa may be decimal, or hex, a hex mantissa uses a leading 0x or 0X prefix optionally followed by an underscore.

The exponent may designate a power of 10 using E or e, or a power of 2, using P or p.

A suffix may be F,f,D,d, L or l, designating floating type, double precision floating type, or long double precision floating type.

```
123.4
123_456.78
12.6E-5L
0xAf.bE6f
12.7p35
```

There is a table of the operators Table 30.5 Floating Point Operators.

# 14.11 String like literals

Library Reference

#### 14.11.1 Standard string literals

Generaly we follow Python here. Felix allows strings to be delimited by; single quotes ', double quotes ", triped single quotes "' or tripled double quotes """.

The single quote forms must be on a single line.

The triple quoted forms may span lines, and include embedded newline characters.

The complete list of special escapes is shown in table Table 14.1 String Escapes.

#### 14.11.2 Raw strings

A prefix "r" or "R" on a double quoted string or triple double quoted string suppresses escape processing, This is called a raw string literal.

NOTE: single quoted string cannot be used, because this would clash with the use of single quotes/apostrophies in identifiers.

Basic		
Escape	Name	Decimal Code
\a	ASCII Bell	7
<b>\</b> b	ASCII Backspace	8
\t	ASCII Tab	9
\n	ASCII New Line	10
\r	ASCII Vertical Tab	11
\f	ASCII Form Feed	12
\r	ASCII Carriage Return	13
\'	ASCII Single Quote	39
\"	ASCII Double Quote	34
\\	ASCII Backslash	92
Numeric		
\d999	Decimal encoding	
\o777	Octal encoding	
\xFF	Hex encoding	
\uFFFF	UTF-8 encoding	
\UFFFFFFFF	UTF-8 encoding	

Table 14.1: String Escapes

#### 14.11.3 Null terminated strings

A prefix of "c" or "C" specifies a C NTBS (Nul terminated byte string) be generated instead of a C++ string. Such a string has type +char rather than string.

#### 14.11.4 Perl interpolation strings

A literal prefixed by "q" or "Q" is a Perl interpolation string. Such strings are actually functions. Each occurrence of \$(varname) in the string is replaced at run time by the value "str varname". The type of the variable must provide an overload of "str" which returns a C++ string for this to work.

```
var x = 1;
var y = 3.2;
println$ q"x=$(x), y=$(y)";
```

#### 14.11.5 C format strings

A literal prefixed by a "f" or "F" is a C format string.

Such strings are actually functions.

The string contains code such as "C format specifiers.

```
var x = 1;
var y = 3.2;
println$ f"x=%03d, y=%4.1f, s=%S" (x,y,"Hello");
```

Variable field width specifiers "\*" are not permitted.

The additional format specification is supported and requires a Felix string argument.

If vsnprintf is available on the local platform it is used to provide an implementation which cannot overrun. If it is not, vsprintf is used instead with a 1000 character buffer.

The argument types and code types are fully checked for type safety. There are some tables of accepted codes: Table 14.2 C format codes: integer, Table 14.3 C format codes: special integer, Table 14.4 C format codes: floating, Table 14.5 C format codes: other.

Please see a suitable reference to learn how to use C format codes.

Table 14.2: C format codes: integer

Code	Type	Radix	
hhd	$_{ m tiny}$	decimal	
hhi	$_{ m tiny}$	decimal	
hho	utiny	octal	
hhx	utiny	hex	
hhX	utiny	HEX	
hd	short	decimal	
hi	short	decimal	
hu	ushort	decimal	
ho	ushort	octal	
hx	ushort	hex	
hX	ushort	HEX	
d	int	decimal	
i	int	decimal	
u	uint	decimal	
O	uint	octal	
X	$\operatorname{uint}$	hex	
X	uint	HEX	
ld	long	decimal	
li	long	decimal	
lu	ulong	decimal	
lo	ulong	octal	
lx	ulong	hex	
lX	ulong	HEX	
lld	vlong	decimal	
lli	vlong	$\operatorname{decimal}$	
llu	uvlong	decimal	
llo	uvlong	octal	
llx	uvlong	hex	
llX	uvlong	HEX	

Table 14.3: C format codes: special integer

$\operatorname{Code}$	Type	Radix	
zd	ssize	decimal	
zi	ssize	decimal	
zu	size	decimal	
ZO	size	octal	
ZX	size	hex	
zX	size	HEX	
jd	intmax	decimal	
ji	intmax	decimal	
ju	uintmax	decimal	
jo	uintmax	octal	
jx	uintmax	hex	
jΧ	uintmax	HEX	
td	ptrdiff	decimal	
$_{ m ti}$	ptrdiff	decimal	
$\operatorname{tu}$	uptrdiff	decimal	
to	uptrdiff	octal	
tx	uptrdiff	hex	
tX	uptrdiff	HEX	

Table 14.4: C format codes: floating

$\operatorname{Code}$	Type	format
e	double	scientific
$\mathbf{E}$	double	SCIENTIFIC
f	double	fixed
$\mathbf{F}$	double	FIXED
g	double	general
G	double	GENERAL
a	double	hex
A	double	HEX
Le	ldouble	scientific
LE	ldouble	SCIENTIFIC
Lf	ldouble	fixed
$_{ m LF}$	ldouble	FIXED
$_{ m Lg}$	ldouble	general
LG	ldouble	GENERAL
La	ldouble	hex
LA	ldouble	HEX

Table 14.5: C format codes: other

Code	Type	
c	int (prints char)	
$\mathbf{S}$	string	
$\mathbf{s}$	&char	
p	address	hex
Р	address	HEX

# Chapter 15

# Macro processing

Library Syntax Reference Compiler Semantics Reference

#### 15.1 Macro val

The macro val statement is used to specify an identifier should be replaced by the defining expression wherever it occurs in an expression, type expression, or pattern.

```
macro val WIN32 = true;
macro val hitchhiker;
macro val a,b,c = 1,2,3;
```

#### 15.2 Macro for

This statement allows a list of statements to be repeated with a sequence of replacements.

```
forall name in 1,2,3 do
  println$ name;
done
```

## 15.3 Constant folding and conditional compilation

Compiler Semantics Reference

Felix provides two core kinds of constant folding: folding of arithmetic, boolean, and string values, and deletion of code, either statements or expressions, which would become unreachable due to certain value of conditionals.

Basic operations on integer literals, namely addition, subtraction, negation, multiplication, division, and remainder are folded.

Strings are concatenated.

Boolean and, or, exclusive or, and negation, are evaluated.

False branches of if/then/else/endif expression and match expressions are eliminated.

False branches of if/do/elif/else/done are also eliminated.

By this mechanism of constant folding and elimination, Felix provides conditional compilation without the need for special constructions.

Part III

Lookup

# Chapter 16

# Names

#### 16.1 Kinds of Names

Felix has several kinds of names which can find two kinds of entities.

#### 16.1.1 Simple Names

A *simple name* is just an identifier.

```
x
joe
```

#### 16.1.2 Simple Indexed Names

An *simple indexed name* is an identifier followed by an open square bracket [, a possibly empty comma separated list of type expressions, followed by a close square bracket ]. If the list is empty, the name is equivalent to a simple name.

```
x[] // equivalent to just x
joe[int]
fred[int,string]
```

#### 16.1.3 Unqualified Names

An unqualified name is a simple name or simple indexed name. Because indexed names with an empty index list are equivalent to simple unindexed names, all unqualified names are notionally simple indexed names.

#### 16.1.4 Qualified Names

A  $qualified\ name$  is sequence of at least two unqualified names separated by two colons ::.

```
A::B::f
A[int]::f[long]
root::B
```

#### 16.1.5 Special name root

The special name root is an alias for the top level module name and may be used to force qualified name lookup starting with the top level module.

#### 16.1.6 Unsuffixed Name

An unsuffixed name is a qualified or unqualified name.

#### 16.1.7 Suffixed Name

A  $suffixed\ name$  is an unsuffixed name followed by a suffix consisting of the word of followed either by a simple name, or a possibly empty comma separated list of type expressions enclosed in parentheses ( and ).

```
fun f (x:int) => x;
fun f (x:double, s:string) => x.str + s;
var closure = f of (double * string); // suffixed name
```

Suffixed names are used to disambiguate references to functions from an overloaded set.

## 16.2 Symbol Tables

Felix represents scopes using symbol tables. There are two kinds of symbol table.

#### 16.2.1 Symbol definition table

Every symbol defined is allocated a unique integer representative and the definition is stored in a hash table keyed by this integer, this is the *symbol definition table*. The definition includes a reference to the parent if any, and, a name lookup table if the defined entity contains a scope.

#### 16.2.2 Name lookup table

For each scope, another kind of hash table called a *name lookup table* is used which maps a string name to a single entry which is one of two kinds: either the entry is a non-function entry or a function entry. Non-function entries contain a single view of a symbol, whilst function entries contain a list of views.

Each scope is associated with two name lookup tables.

#### Private name lookup table

This table maps all the names defined in the scope to all the definitions in the scope. It is used for unqualified lookup within the scope or any children of the scope.

#### Public name lookup table

This table contains mappings of the names of all definitions in the scope which are not marked private to those definitions. It is used for qualified lookup into the scope from outside the scope.

#### 16.2.3 Views

A view of a symbol consists of the index of the definition in the symbol definition table together with a list of type variables and a list of type expressions using these type variables, this list of type expression must agree in number with the type variables in the entry in the symbol definition table.

The interpretation of a definition referred to by a view is as a polymorphic definition indexed by the view type variables, with each use of the definition's type variables in the body of the definition replaced by the corresponding type in the view's list of type expressions.

For example:

```
class A[T] { fun f:T * T -> T; }
open[U, V] A[U * V];
var x = f ( (1,2.0), (3, 4.0) );
```

This matches because the view of f available in the open has type

```
(U * V) * (U * V)
```

via the assignment  $T \leftarrow U * V$ , and the assignments  $U \leftarrow int$  and  $V \leftarrow long$  mean the function call is a specialisation of the view, which in turn is a specialisation of the original function. The view provided by the open may be described by a triple:

(index=A::f; vs=U,V; ts=U\*V)

where index is the integer index of f in the definition table.

Multiple views of a function, even if overlapping, never create an ambiguity: views are logically merged with non-discriminated setwise union.

This is effected as follows by overload resolution.

#### 16.2.4 Name lookup environments

A name lookup environment consists of a stack of pairs of name lookup tables. The top of the stack represents the current, innermost scope. This is where searching for an unqualified name or first component of a qualified name begins. Each layer represents an including or parent scope, up to the bottom of the stack, which represents the outermost or global scope, which has no parent.

The two name lookup tables at each level are the primary name lookup table and the shadow name lookup table.

#### Primary name lookup table

The primary name lookup table contains mappings for all the symbols defined in the scope or injected into the scope with a inherit or rename directives.

#### Shadow name lookup table

The shadow name lookup table contains mappings for all the symbols made available by an open directive or by the with clause of the type variable specification of a definition.

open directives make the public names defined in, or inherited into, a class available via a view.

The name lookup algorithms always search the primary lookup table first, if that fails they try the shadow table. This ensures any definitions in a scope can be used to hide names provided by an open, which ensures it is possible to resolve ambiguities or modify semantics for a particular name, whilst retaining the other names.

#### 16.3 Overload Resolution

Overload resolution proceeds as follows. We start with the result of a function lookup which returns a set of views called candidates. Our aim is to select a unique function, together with assignments to the type variables of the definition, which cause the signature of the call to equal the signature of the function, and any constraints specified for the function to be satisfied.

- During overload resolution, a subset of the candidates views is selected which match the supplied name and signatures.
- Constraints are now applied to eliminate candidates additional candidates. See section 26.1 Type Constraints for more details.
- The subset is then reduced by eliminating views which are strictly less specialised than another.
- If the result of this reduction consists of a set of more than one view of the same function, then they must map to the same specialisation of the function, and overload resolution has succeeded.

The algorithm is non trivial. Here is another example:

```
class A[T] { fun f (x:T) => x; }
open[U] A[U * int];
open[V] A[int * V];
println$ f (1,1);
```

Here, there are two views of f, both of which have T <-int as a specialisation. The first views is accepted because U <- int shows the call signature int \* int is a specialisation of signature U \* int, and the second because V <- int shows the call signatures is a specialisation of the signature int \* V.

Now, the first view provides the substitution  $T \leftarrow U * int$  and the second  $T \leftarrow int * V$ , and substituting the respective specialisations of the views by the call results in the same specialisation of the original function  $T \leftarrow int * int$ . Therefore this specialisation, being unique, allows the function f to be called directly with signature f int.

Not all calls match all views. For example a call on signature long \* int only matches the first view, and with int \* long only matches the second: the point is that if more than one view of the same function matches, it is never ambiguous because the views always lead to the same specialisation of the function.

This is not true if the views are views of distinct functions. Something like this can and does happen when the inverse of view lookup is performed when instantiating class virtual functions with distinct instances. In this case, if there are two instances which match, neither of which is most specialised, then Felix will report an ambiguity, even though semantically the behaviour is required to be the same: the semantic requirement is too sloppy to ensure this is meaninful.

Our conclusion is that the programmer is free to open overlapping views of the same function, and in particular duplicated opens do not cause a problem (the same consideration applies to non-functions). This is not the case when specifying type class instances, where overlaps are associated with distinct definitions, so that a single most specialised definition is required. This issue, however, does not occur in ordinary (phase 1) lookup of names. It occurs only during

instantiation by monomorphisation when a type class virtual must select from available instances. In this case, there is no overloading to consider since the particular function in each instance is already selected: we only need consider the specialisation lattice.

## 16.4 Lookup

Names refer either to a function set or single non-function entity. Finding the entity a particular use of a name refers to is called *name lookup* or *name binding*.

Note that unlike C++, Felix has no automatic type conversions. Matching of signatures in Felix must be exact. (However see subsection 21.2.7 Row Polymorphism).

#### 16.4.1 Unqualified name lookup

Unqualified name lookup is performed using one of two base general algorithms, depending on the kind of name required.

#### 16.4.2 Basic unqualified non-function lookup

When seeking a non-function, Felix first looks for the simple (non-indexed) part of the unqualified name in the current scope.

If the name is found but it is a function symbol the compiler aborts with a diagnostic message.

If the name is not found, it then looks in the special shadow scope of the current context which contains symbols inserted by open or rename directives.

If an open or rename directive introduces the same non-function name into the same shadow scope and it refers to the same non-function, with the equivalent indices, one entry is discarded to prevent an ambiguous name error, when in fact both insertions are equivalent and refer to the same entity.

The equivalent indices check works by testing for type equality after alpha conversion. For example

```
class Unique[T] { typedef A = B; }
open[U] Unique[U * U];
open[V] Unique[V * V];
var x: A[int]; // OK
```

If there are two occurrences of the name in the shadow scope, it aborts the compile with a diagnostic message. Note: this error occurs whilst creating the shadow scope, even if the symbol is not used.

If the name is still not found, Felix repeats the process in the parent scope, if any, or aborts the compile with a diagnostic if there is no parent.

```
var x = 1;
class A {
   var x = "hello";
   class C {
      fun f() => x; // A::x = hello
   }
}

begin
   fun f() => x; // root::x = 1
end

open A;
fun f() => x; // root::x = 1

begin
   open A;
fun f() => x; // A::x = hello
end
```

If the name is indexed, it then checks that the number and kind of indices matches the definition of the symbol discovered, if not it aborts the compile with a diagnostic.

#### 16.4.3 Basic unqualified function lookup

This is the same as non-function lookup, except that the result is expected to be a set of functions with exactly one member.

```
fun f() => 1;
var closure = f; // only one f, OK
```

#### 16.4.4 Lookup with signatures

Felix can find a list of signatures for a function lookup in two contexts.

If the name is a suffixed name, the suffix supplies the sole signature:

```
fun f (x:int) => x;
fun f (x:double) => x;
var closure = f of (double);
```

In an application or call the argument or arguments supply the signatures:

```
fun f (x:int) => x;
fun f (x:double) => x;
var xi = f 1; // f of (double);
var xd = f 1.0; // f of (double);

fun g(x:int) (y:int) => x + y;
fun g(x:int) (y:double) => x.double + y;

var yi = g 1 2; // signatures int,int
var ydi = g 1 2.0; // signatures int,double
// var closure = g 1; // ambiguous, error
```

Care must be taken designing functions to reduce possible ambiguities. Using curried arguments has advantages but one disadvantage is that eta-expansion may be required to select the right overload. A famous example from the Felix library:

```
class List {
   fun map[T,U] (f:T->U) (ls: list[T]) : list[U];
}
class Varray {
   fun map[T,U] (f:T->U) (ls: varray[T]) : varray[U];
}

open List;
open Array;
fun itod (x:int): double => x.double;
// var closure = map itod; // Error, which map?
```

#### 16.4.5 Unqualified function lookup with signatures

When seeking a function with signatures, felix follows similar rules to nonfunctions, except as follows.

When a function symbol is found, it consists of a set of functions, not a single function. Felix then performs overload resolution to determine if any of the candidates matches.

If there is no match at all, it proceeds with the next step. If there is more than one match, and no match is most specialised, it aborts with a diagnostic message.

Lookup in the shadow scope is performed similarly. Function names introduced from multiple opens are merged prior to the shadow scope lookup. This merger ensures that if the same name is present in two opens, refers to the same original symbol, and has the same type indicies, one is discarded. Note: this merge of equivalent names is not done when constructing the shadow scope, but during overload resolution. Therefore it is not an error to introduce the same name with the same signature for distinct functions, it is only an error if there is an attempt to use such a name. This is different from non-function lookup.

```
fun f(x:int) => x; // signature int
class A {
  fun f(x:double) => x; // signature double
  fun g() {
    return f 1; // signature int: finds root::f of (int)
  }
}
begin
  open A;
  fun f(x:string) => x; // signature string;
  var x = f 1.1; // signature int: finds A::f of (double)
end
```

For the first lookup, there is no f in g. There is no shadow scope. The f in A has signature double which doesn't match. The f in root has signature int which matches.

For the second lookup we want an f with signature double. The f in the begin/end scope does not match. The f in the begin/end shadow scope introduced by the open does match so A::f of (double) is found.

Note that this algorithms is not the same as C++. Felix has fixed the design fault.

#### 16.4.6 Qualified non-funtion name lookup

Qualified name lookup for a non-function proceeds by first performing an unqualified name lookup on the first component of the qualified name, ignoring indices.

If the name is not found the compile aborts and a diagnostic is issued. If the name is not a class name, the compiler aborts and a diagnostic is issued.

Now, the next component is searched for in the specified class scope. If the name is not found, the compile aborts and a diagnostic is issued. The search ignores shadow scopes, and it does not proceed into the context of the classes parent. However it does take inherited names into account. All names except the final one must resolve to class names.

The search a non-ultimate name requires a class to be found in the previously found class. Qualified name lookup, therefore, drills down into a class heirarchy

from the root.

The final name is sought similarly and must be of the kind sought.

Finally the complete sequence of type index parameters is checked for length against the entity's definition.

#### 16.4.7 Qualified function name lookup

Searching for a qualified name of a function is the same as for a non-function, except that a set of overloaded functions may be returned.

If a unique symbol is required, then the set must contain only one function name.

#### 16.4.8 Qualified lookup for function with signatures

A standard qualified name lookup is performed so that the last component returns a function set.

Overload resolution is then performed on the function set. The result is final.

# Chapter 17

## Libraries

The library statement may be used to form extensible groups of named definitions.

```
library A {
    proc f(x:int) => println$ "A::f " + x.str;
}
library B {
    proc f(x:int) => println$ "B::f " + x.str;
}
library A {
    proc g(x:int) => println$ "A::g ";
}

open A;
f 1;
B::f 1;
```

Unlike classes and modules, libraries are extensible and so may span multiple files (however the library statement may not!).

Libraries cannot be polymorphic, and may not contain virtual functions or procedures directly.

Libraries must be at the top level or nested in other libraries.

Statements within a library statement are executed in order. Statements in multiple library statements for the same library in the same file are executed in order.

Statements in a library statement nested in a library statement are executed before any statements in the enclosing library statement.

Top level code not enclosed in a library statement is treated as if enclosed in an anonymous library.

Otherwise the order of execution is unspecified.

# Chapter 18

# Abstract Types

An abstract type is a type for which a specific implementation is given, but which can only be accessed by specified methods.

#### 18.0.1 Syntax

An abstract type is created like this, taken from the standard library. First define the type in terms of another type:

```
open class Darray {
  private struct darray_ctl[T]
  {
    a: varray[T];
    resize: size * size --> size;
  }
  type darray[T] = new &darray_ctl[T];
```

Now, we provide a constructor for the abstract type:

```
//f Make an empty darray, give it 20 slots
//f for no particular reason.
ctor[[T] darray[T] () =>
    _make_darray[T]$ new darray_ctl[T](
    varray[T] 20uz , dflt_resize
);
```

We use the special name <code>\_make\_darray</code> for the constructor. It constructs a value of the abstraction implementation secretly and casts it to the abstract type.

Now we need some methods defined on the abstract type:

```
// resize
proc do_resize[T] (pd: darray[T], new_size: size)
{
    var old = (_repr_ pd)*.a;
    (_repr_ pd).a <-
        varray[T] (new_size, (len old), (fun(i:size)=>old.i));
}

// pop head
proc pop[t](a:darray[t]) {
    pop (_repr_ a)*.a;
    newsize := (_repr_ a)*.resize
        (maxlen (_repr_ a)*.a, len (_repr_ a)*.a)
    ;
    if newsize != maxlen (_repr_ a)*.a
        call do_resize (a,newsize)
    ;
}
// end Darray class
```

These methods use the special name <code>\_repr\_</code> to cast the abstract type to its implementation.

So, the statement

```
type darray[T] = new &darray_ctl[T];
```

defines a new, abstract, polymorphic type, darray[T] implemented as a pointer to a struct containing an bounded array varray and a resize function.

In order to construct a darray, we first create pointer to a darray\_ctl objects, and then cast it to the abstract type using special name \_make\_darray. The cast from the representation to the abstract type is the name of the abstract type constructor prefixed by \_make\_.

To access the implementation, which is needed to define methods on the abstract type, we use the cast <code>\_repr\_</code>, which converts the abstract type back to its implementation.

Both these casts are private to the containing class Darray, so they can only be used in the class defining the abstract type, because private names of a class are only accessible within the class (and it descendants of course).

Therefore, the mechanism provides a way to rigorously protect the implementation of the abstract type. The privacy of the representation type in the example is not necessary, but is used to prevent name space pollution.

# Chapter 19

# Classes

Syntax

## 19.1 Class Statement

The top level Felix module can contain submodules which are specified by a non-polymorphic class statement:

```
class classname { ... }
```

#### 19.1.1 Qualified Names

The effect is to produce a qualified name to be used outside the class:

```
class classname { proc f () {} }
classname::f ();
```

#### 19.1.2 Nested Classes

Classes may be nested.

```
class A {
   class B {
     proc f () {}
     f();
   }
   B::f();
}
A::B::f ();
```

#### 19.1.3 Private definitions

A class may contain private definitions, if a symbol is marked private it is only visible in the scope class in which it is defined, including any nested classes:

```
class A {
  private proc f () {}
  class B {
    f(); // visible inside A
  }
  f(); // visible inside A
}
// A::f () fails, f is not visible outside A
```

#### 19.1.4 Single File Rule

A class must be specified within a single file.

#### 19.1.5 Completeness Rule

Classes are not extensible, a definition of a class with the same name in the same scope is not permitted.

#### 19.1.6 Setwise Lookup

The body of a class forms a nested scope. Within a class all symbols defined in the class are visible, along with all those visible in the enclosing context. This is called setwise lookup.

```
var x = "Hello";
class A {
   proc f() { g(); } // g visible before defined
   proc g() { x = x + 1; }
   var y = f(); // calls g which uses x uninitialised!
   var x = 1;
}
```

Beware using uninitialised variables! The procedure g above uses A::x before it is initialised.

#### 19.1.7 Top level module alias

The reserved name root may be used as a prefix for the top level module:

```
var x = 1;
class A { var x = root::x; }
```

## 19.2 Polymorphic Classes

#### 19.2.1 Parametric Polymorphism

A class may be specified with one or more type variables. Such a class is said to be a polymorphic class.

```
class MakePair[T,U] {
  fun fwd_pair (x:T) (y:U) => x,y;
  fun rev_pair (x:T) (y:U) => x,y;
}
```

#### 19.2.2 No Variables

Polymorphic classes may not directly contain variables, all members must be function or type definitions.

#### 19.2.3 Indexed Names

Entities from a class can be specified from outside using a qualified name in which the class name is followed a square bracketted list of types instantiating the corresponding type variables, this is an *indexed name*:

```
var f = MakePair[int,string]::fwd_pair 42 "Hello";
var r = MakePair[int,string]::rev_pair 42 "Hello";
```

#### 19.2.4 Deduced indices

However one or more or even all the types can be omitted from the right end of the list if they can be deduced by overload resolution.

#### 19.2.5 Elision of indices

The square brackets are optional if they enclose an empty list.

```
f = MakePair[int,string]::fwd_pair 42 "Hello";
f = MakePair[int]::fwd_pair 42 "Hello";
f = MakePair[]::fwd_pair 42 "Hello";
f = MakePair::fwd_pair 42 "Hello";
```

Note that all symbols in Felix are considered to be indexed. So for example this is correct:

```
var x = 1;
println$ x[];
```

#### 19.2.6 Sloppy indexing

It is also permitted to move the instance types across qualification boundaries:

```
f = MakePair[int]::fwd_pair[string] 42 "Hello";
```

although this practice is not recommended.

From the outside, class type variables are viewed as univeral quantification. From inside however, the variable names are fixed types which happen to be unknown, that is they're to be considered as existentials.

This means they cannot be specified explicitly or implicitly inside the class with unqualified access:

```
class A[T] {
  fun f(x:T) => x,x;
  fun g(y:T) => f y; // correct
  fun h(y:T) => A[T]::f y; // correct
  // fun h(y:T) => f[T] y; // wrong
}
```

From inside the class the function **f** above is monomorphic, not polymorphic. Although **T** is not known, it is a fixed, invariant type.

#### 19.2.7 Polymorphic Members

Functional members of a class may be polymorphic. This is independent of the class type parameters.

```
class A[T] {
  fun f[U] (x:T, y:U) => x,y;
  fun g(a:T) => f[T * T] (a,a);
```

In this case the function f has its own personal type variable U which is set in the call in g to T \* T because its argument is a pair of a which has that type.

#### 19.3 Virtuals and instances

A polymorphic class may contain functions or procedures marked virtual. In this case a definition is optional.

```
class A[T] {
    // non virtual function
    fun f(x:T) => x,x;

    // virtual function with definition
    virtual fun g (x:T) => f x;

    // virtual function without definition
    virtual function without definition
    virtual function h : T -> T * T;
}
```

If a virtual function without a definition from a class is used, it must be defined for the types for which it is used. This is done in an instance statement:

```
var a = 1; // int
var x = A[int]::h a; // h used for T=int

// instance defining h for int
instance A[int] {
  fun h(a:int) => a + 1, a - 1;
}
```

An instance can be defined anywhere in a non-functional scope provided the class being instantiated is visible.

In this case symbols in the instance definition are bound the context of the instance scope and its enclosing scope in the usual way.

It is not possible to directly access the definitions in an instance from outside the instance. Instead all access is diverted through the top level class being instantiated. Symbols are bound to the top level class member first to fix the type variables, then a matching instance is sought. This second lookup is called *phase 2 lookup*, it occurs during monormophisation.

If there is no matching instance, the program fails with a diagnostic.

If there is more than than one matching instance, the most specialised instance is used. If there is no most specialised instance, the use of the class member is ambiguous and the program fails with a diagnostic.

An instance must be not less specialised than the class it instantiates (that is, equally specialised or more specialised).

Instance specialisation is judged by the polymorphic subtyping rule which is implemented using a variant of the unification algorithm in which dependent and independent types are distinguished.

A polymorphic type S[T] parametrised by a type variable T is more specialised than a polymorphic type A[U] if U may be replaced by a type expression containing T the result of which equals S[T].

If S has more than one type variable, substitutions for each of them must be found. If A has more than one type variable, the substitutions involve all of these variables.

A specialisation S1 of A is strictly more specialised than a specialisation S2 of A if S1 is also strictly a specialisation of S2.

#### 19.3.1 Default Definition

If a virtual function has a definition, it is called a *default definition*. On a use of a function with a default definition, if no matching instance is found, the default definition is specialised and used instead. Note that default definitions do not resolve ambiguity from overlapping instances.

#### 19.3.2 Matching polymorphic functions

If a virtual function is polymorphic, the personal type variables of the function must not be specialised in an instance. The class type variables are resolved independently of the function type variables.

You may think of this as if the class type variables are resolved first by finding a uniquely matching instance, and then the function type variables are resolved in a second step (although in fact there is no coupling between the resolutions).

## 19.4 Classes as Categories

A class may thought of in a category theoretic sense.

A base category constists of objects which consists of a finite set of base types and all combinations thereof formed by the available set of type combinators such as tuples, records, function types, etc.

The arrows of this category consist of all the functions explicitly defined on these types, and all compositions thereof. This includes the identity functions implicitly defined by copying.

This is the category generated by the graph consisting of the defined functions, where paths in the graph are (reverse) function compositions. This is called the free category generated by the graph.

A class in the context of a base category generates an extension to that category by throwing in some additional types and arrows. The type variables are added to the set of base types, so that the set of combinations is extended. The functions are added to the set of digraph edges of the base generating graph, to add additional arrows.

This view of the role of a class is vital to understand semantic rules which correspond to the notion of a category generated by a graph with relations. The relations form a constraint. In category theory, the relations are generally equations relating the arrows which specify that certain function compositions are equal to others.

The freely generated category is sometimes called an initial algebra. When constraints are added a new category is formed by collapsing some sequences of arrows to a single arrow. There is a mapping called an epi-morphism which takes each arrow from the freely generated category to the target so that two distinct composites may map to the same arrow in the target.

Conversely, there is a reverse mapping from the arrows of the target category to sets of arrows of the freely generated one, forming another category called a quotient category. These two mappings are functions and together form an adjunction.

The purpose of this explanation is not merely for your entertainment. In most programming classes are intended to be constrained, that is, the instances are intended to have a certain behaviour.

Consider for example:

```
class Addable [T] {
  virtual fun add: T * T -> T;
}
```

Now consider the following instances:

```
instance Addable[uint] {
   fun add (x:uint, y:uint) => x + y;
}

instance Addable[int] {
   fun add (x:int, y:int) => x + y;
}

instance Addable[double] {
   fun add (x:double, y:double) => x + y;
}
```

These instances are good according to the specification, however the addition of int and double is unspecifed because we may have overflow. Furthermore one may get a big surprise adding floating point representations of reals: if you add a big float to a small one the small one may be so small that the result is equal to the big one.

Basic laws of arithmetic are not obeyed by floating representations, in particular addition of floats is not associative!

It is usual to specify requirements in comments and the programmer must carefully check that instances obey the constraints specified for the class in these comments.

Felix, however, can do a bit better.

## 19.5 Axioms, Lemmas and Theorems

Felix allows some semantic constraints on class instances to be specified with explicit axioms. For example:

```
class Addable [T] {
  virtual fun add: T * T -> T;
  axiom associative (x:T, y:T, z:T):
    add (add (x,y), z) == add (x, add (y, z))
  ;
}
```

The axiom documents in a formal language the requirement that the addition operator defined in an instance must be associative. An axiom is similar to an ordinary boolean function which tests whether some condition is met or not. By applying an axiom to particular values we can check for non-conformance of instances.

However, in a categorical sense, an equational axiom plays precisely the role of a relation in the formation of a category with generators and relations. It is a vital part of practical specification of semantics.

We should note that not all constraints can be expressed as axioms in Felix. In particular since Felix only provides first order polymorphism, only equational predicates in Horn form can be used, that is, all the quantifiers must be (implicitly or explicitly) on the left of the formula. Interior quantifiers require second order polymorphism.

Note also that like most programming languages we use constructive mathematics which constrains the role of existentials to calculations. That is, it is not acceptable to assert that something exists because if it did not a contradiction would be derived. Indirect proof is not allowed in constructive mathematics.

Instead, one must prove something exists by actually constructing one! So for example given a < b we know there exists a number x such that a < x < b. A proof of this by asserting that if no such x existed, then we would have a contradiction, is not allowed in constructive mathematics. Instead the proof is simply given by x = (a + b)/2. And of course .. the assertion is false for many types such as integers!

#### 19.5.1 Lemmas and Theorems

Lemmas and theorems play the same role as axioms. The idea, however, is that lemmas and theorems can be derived from the axioms. A lemma is a simple rule which a good automatic theorem prover could derive, and which seems obvious to a human.

A theorem is a more difficult rule which would require a proof assistant with hints to derive a proof.

#### 19.5.2 Reductions

A reduction is also an axiom, but it has an additional property. Instead of an equation, reductions use a directed equality:

```
reduce revrev[T] (x:list[T]):
   rev (rev x) => x
;
```

This reduction asserts that if you reverse a list twice you end up back where you started. But it does more: it give the compiler a hint that it is allowed to replace an expression which reverse a list twice with the list, removing the two reversing operations.

This is a particularly interesting example of the general rule that all theorems are nothing more than optimisations, in this case literally allowing the compiler to optimise a program. Note that it is only a hint!

## 19.6 Lookup control directives

#### 19.6.1 Open directive

The simple open directive may be used to make the symbols defined in a class visible in the scope containing the open directive.

```
class X { var x = 1; }
open X;
println$ x;
```

Names made visible by an open directive live in a weak scope under the current scope. Names in the weak scope may be hidden by definitions in the current scope without error.

```
class X { var x = 1; }
open X;
var x = 2;
println$ x; // prints 2
```

The open directive is not transitive. The names it makes visible are only visible in the scope in which the open directive is written.

#### 19.6.2 Inherit directive

The inherit directive allows all of the public symbols of a class to be included in another scope as if they were defined in that scope. This means such names inherited into a class can be accessed by qualification with the inheriting class name, and will be visible if that class is opened.

Inheriting is transtitive.

If a name is inherited it will clash with a local definition.

```
class A { var a = 1; }
class B { inherit A; }
println$ B::a;
```

#### 19.6.3 Rename directive

This directive is can be used to inherit a single symbol into a scope, possibly with a new name, and also to add an alias for a name in the current scope.

When applied to a function name all functions with that name are renamed.

```
class A {
   var a = 1;
   proc f() {}
   proc f(x:int) {}
}

class B {
   rename a = A::a;
   rename fun f = A::f;
}
```

The new name injected by a rename may be polymorphic:

```
class A { proc f[T] () {} }
class B { rename g[T] = A::f[T]; }
```

## 19.6.4 Use directive

This is a short form of the rename directive:

```
class A { var a = 1; }
class B { use A::a; use b = A::a; }
```

It cannot be applied to functions. The first form is equivalent to

```
use a = A::a;
```

Unlike the rename directive the new name cannot be polymorphic and is limited to a simple identifier.

# Part IV Type System

# Chapter 20

# typedef statement

#### Syntax

## 20.1 Type aliases

The plain typedef statement is used to define an alias for a type. It does not create a new type.

#### 20.1.1 Basic typedef

```
typedef Int = int;
```

#### 20.1.2 Polymorphic typedef

Typedef can also be polymorphic:

```
typedef Cplx[T] = {x:T,y:T};
```

## 20.2 Type Sets

A type set is a component of a type constraint expression which restricts a type variable one of a specified list of entities. Each entity may be either a type, a type predicate, or another type set. Syntax like:

```
typesetof (short, int, long, vlong)
```

is used for a typeset expression.

The typedef statement may be used to define an alias for a typeset:

```
typedef Integers = typesetof (short, int, long, vlong);
```

A typeset can be used with a membership test or kinding specification to form a constraint. For example:

```
fun f[T where T in Integers] (x:T) => x;
```

See also Table 30.3 Integer Typesets, subsection 26.1.2 Typeset membership constraints.

#### 20.2.1 basic type functions (functors)

Typedef can also be used to create a type functions, or *functors*. A basic definition is like this:

```
typedef fun pair0 (T:TYPE, U:TYPE) : TYPE => T * U;
var x0 : pair0 (int, long) = 1,2L;
println$ x0;
```

The kind TYPE is the meta-type or kind of all types. The return kind must be specified for functors.

#### 20.2.2 type functions with typematch

A more sophisticated defintion allows a typematch:

See also section 25.1 typematch expression.

#### 20.2.3 Higher order functors

You can also have curried type functions:

```
typedef fun pair2 (T:TYPE) (U:TYPE) : TYPE => T * U;

var x1 : pair2 int long = 1,2L;
println$ x1;

typedef pair3[T] = pair2 int T;
var x3 : pair3 [double] = 1,2.0;
println$ x3;
```

Type functions can be overloaded just like ordinary functions.

#### 20.2.4 Functors in classes

Note carefully there is a difference between an *indexed type* and a *type function*. In the above example, pair3 is not a functor, its an indexed type. Functors can be passed to type classes, for example:

The M above accepts a functor, Maybe in the instance. We can't use opt directly because it is an indexed type, not a functor.

# Chapter 21

# **Products**

# 21.1 Tuples

Tuple types are well known: a tuple is just a Cartesian Product with components identified by position, starting at 0. The n-ary type combinator is infix \* and the n-ary value constructor is infix ,:

```
val tup : int * string * double = 1, "Hello", 4.2;
```

#### **21.1.1** Unit Tuple

The 0-ary tuple type is denoted 1 or unit with sole value ():

```
val u : unit = ();
```

## 21.1.2 No 1-ary Tuple

The 1-ary tuple of type T component value v is identified with the type T and has value v.

## 21.1.3 Projections

The individual components of a tuple may be accessed by a projection function. Felix uses an integer literal to denote this function.

```
var x = 1,"Hello";
assert 0 x == 1; assert x.0 == 1;
assert 1 x == "Hello"; assert x.1 == "Hello";
```

A pointer to a tuple is also in itself a tuple, namely the tuple of pointers to the individual components. This means if a tuple is addressable, so are the components.

```
var x = 1, "Hello";
val px = &x;
val pi = px.0; pi <-42;
val ps = px.1; ps <-"World";
assert x.0 == 42;
assert x.1 == "World";</pre>
```

In particular note:

```
var x = 1, "Hello";
&x.0 <- 42;</pre>
```

because the precedences make the grouping (&x).0.

You cannot take the address of a tuple component because a projection of a value is a value.

Assignment to components of tuples stored in variables is supported but only to one level, for general access you must take a pointer and use the store-at-address operator <-.

#### 21.1.4 Standalone Tuple projections

The projections of a tuple can also be written in an expanded form so that they may stand alone as functions:

```
var first = proj 0 of (int * string);
var a = 1, "Hello";
var one = a . first;
var two = a . proj 1 of (int * string);
```

#### 21.1.5 Alternate Tuple Representation

Felix provides a second representation of tuples. Given a tuple of at least two components, another value may be prefixed to the head of the tuple with the , , operator:

```
var tail = 1,2L; // binary tuple
var triple = "head",,tail; // ternary tuple
assert triple == "head",1,2L;
```

Similarly, given a tuple type of at least two components, another type may be prefixed to the head of the type with the \*\* combinator:

```
typedef pair = int * long;
typedef triple = string ** pair;
// same type as string * int * long
```

### 21.1.6 Pattern matching tuples

The real value of the alternate notation lies in pattern matching. For example:

```
match "head",1,2L with
| head,,tail => println$ tail;
endmatch;
```

The real power comes with classes:

```
instance [T,U with Eq[T], Eq[U]] Eq[T ** U] {
  fun == : (T ** U) * (T ** U) -> bool =
    | (ah ,, at) , (bh ,, bt) => ah == bh and at == bt;
  ;
}

instance[t,u with Eq[t],Eq[u]] Eq[t*u] {
  fun == : (t * u) * (t * u) -> bool =
    | (x1,y1),(x2,y2) => x1==x2 and y1 == y2
  ;
}

instance[t with Eq[t]] Eq[t*t] {
  fun == : (t * t) * (t * t) -> bool =
    | (x1,y1),(x2,y2) => x1==x2 and y1 == y2
  ;
}
```

This mechanism allows recursive processing of heterogenous lists, that is, tuples. In the example we compute equality. The first instance provides heterogenous list recursion, the second case terminates the recursion. The third case is also a terminal which allows the recursion to work for arrays as well. Without this the library array recursion would be more specialised.

## 21.2 Records

A record is similar to a tuple except the components are named and considered unordered up to duplication.

#### 21.2.1 Plain Record

A plain record is one without duplicate fields. A plain record type is one without duplicate fields or a row variable. A record is constructed using a parenthesis enclosed list of comma separated field assignments. An empty record is equivalent to an empty tuple.

```
typedef xy = (x:int, y:int);
var r : xy = (x=1,y=2);
```

### 21.2.2 Record projections

A component of a record may be accessed with a function called a record value projection, it is denoted by the name of the field.

```
var r (x=1,y=2);
println$ x r, r.y;
```

Record value projections can also be used as stand-alone functions. For example:

```
var rl = list ((x=1,y=11),(x=2,y=22));
var xs = map (x of (x:int, y:int)) rl;
println$ xs; // list (1,2)
```

Records also have pointer projections, overloaded with the value projections: if the name of a field is applied to a pointer to a record, a pointer to the named component field is returned. This allows assignment and other mutators to be applied to record components.

```
var r =(x=1,y=2);
var px = &r.x; // means (&r).x
px <- 42;
r&.y <- 23;
println$ r.x, r.y; // (42,23)</pre>
```

Record pointer projects can also be used as stand-alone functions:

```
var prjx = x of (xy);
var prjpx = x of (&xy);
```

#### 21.2.3 General record

Records may have duplicate fields. In this case, reading from left to right in a record literal, a duplicate field is hidden by a previous field of the same name, in a push down stack like fashion.

```
var r = (x=1,y=2,x="Hello");
println$ r._strr, r.x;
// ((x=1,x='Hello',y=2), 1)
```

Note that the generic function \_strr displays the whole of the record including duplicate fields. However projections only find the left-most field.

### 21.2.4 Adding fields

Fields can be added to an existing record to construct a new record:

```
var r = (x=1,y=2);
var r2 = (a="one",b="two",x="newx" | r);
println$ r2._strr,r2,x;
// ((a='one',b='two',x='newx',x=1,y=2), newx)
```

Again, leftmost fields hide rightmost ones.

#### 21.2.5 Removing Fields

The without operator can be used to return a record with some fields removed. It works on values of record and polyrecord type. Note that because Felix uses scoped fields once a field is removed, the previous value of that field is exposed if it exists, and can also be removed. This means it is correct and sometimes necessary to list a field more than once when using the without operator.

```
var x = (a=1,b=2,c=3,c=4);
var y = (x \text{ without b c}); // (a=1,c=4)
```

#### 21.2.6 Adding records

You can also add two records with infix +:

```
var r = (a=1) + (b=2) + (a="hello");
println$ r._strr, r.a.str; // ((a=1,a='hello',b=2), 1)
```

The leftmost field with a given name dominates. Record addition by + is only applied if a user defined addition is not found for the argument types.

Currently, addition of fields of two records of the same type is not supported: it is likely the user intended to add corresponding field values rather than hide the fields in the right argument with those on the left.

#### 21.2.7 Row Polymorphism

Felix provides a special record type called a *polyrecord* which supports row polymorphism with scoped labels in the style of Daan Leijen. The article is here.

This allows a generic function to be written which accepts an argument which is or contains a value of a record type with more fields than required. Unlike subtyping, the extra fields, whilst inaccessible, are not lost and can be returned by the function. For example:

```
val circle = (x=0.0,y=0.0,r=1.0);
val square = (x=0.0,y=0.0,w=1.0,h=1.0);

fun move[T]
   (dx:double, dy:double)
   (shape: (x:double, y:double | T))
=>
   (x=shape.x+dx, y=shape.y+dx | (shape without x y))
;

var inc = 1.0,1.0;
println$ (move inc circle)._strr, (move inc square)._strr;
```

#### 21.2.8 Interfaces

An interface is a special notation for a record type all of whose fields are functions or procedures.

```
interface fred {
    f: int -> int;
    g: int -> 0; // procedure
}

// equivalent to
typedef fred = (f: int -> int, g: int -> 0);
```

The primary use is for specifying the type of a Java like objects. See section 10.8 Dynanic Objects

#### 21.3 Structs

A struct is a a nominally typed record, that is, it must be defined, and each definition specifies a distinct type.

```
struct S { x:int; y:int; };
var s1 : S = S (1,2);
var s2 : S = S (y=42,x=32);
println$ s1.x,s1.y,s2.x,s2.y;
```

### 21.3.1 Alternate Definition Syntax

As a special case, a struct can be defined with the field type before the field name:

```
struct S { int x; int y; };
```

Furthermore there is a special syntax:

```
typedef struct {
   int x;
   int y;
} S;
```

for defining structs. The purpose of this syntax is to allow a C struct to be copied directly into Felix code with minimal editing. Note the above form does not define an alias, it defines a struct called S.

#### 21.3.2 Struct constructor

A struct value can be constructued using the structure name as a function and passing a tuple of values corresponding by position to the fields of the struct, as shown above. A record with matching fields can also be used. Of course in both cases the types must also agree.

#### 21.3.3 Constructor as function

A struct constructor can be used a first class function. In this case the argument type is a tuple, not a record.

```
struct S { x:int; y:int; };

proc p (factory: int * int -> S) {
  var a = factory (1,2);
  println$ a.x,a.y;
}
p S;
```

## 21.3.4 Projections

The field names are projection functions and can be applied to a struct value to extract the nominated component.

They can also be applied to a pointer to a struct to find a pointer to the nominated component.

```
struct S {x:int, y:int; };
var a = S (1,2);
var px = &a.x;
px <- 11;
&a.y <- 22;</pre>
```

Projections can be used as first class functions with the notation:

```
var prjx = x of (S);
var prjpx = x of (&S);
```

can be used to refer to a projection in isolation, and a pointer projection in isolation, that is, as unapplied first class functions.

#### 21.3.5 Nested methods

A struct may also contain function and procedure definitions:

```
struct A {
    x:int;
    y:int;
    fun get2x => 2 * self.x;
    fun get2y () => 2 * self.y;
    proc diag (d:int) { self.x <- d; self.y <-d; }
};</pre>
```

These functions are precisely equivalent to:

```
fun get2x (self:A) => 2 * self.x;
proc diag (self: &A) (d:int) { self.x <-d; self.y <-d; }</pre>
```

Note that for a function self is a value, for a procedure self is a pointer.

#### 21.3.6 Method closures

Because of these definitions, we can form object closures over a struct:

```
var a = A(1,2);
var g2y = a. get2y;
var di = a . diag;
```

Note we can't form a closure for  $\mathtt{get2x}$  without an explicit wrapper, i.e. eta-expansion.

# Chapter 22

# Sums

## 22.1 Anonymous Sum Types

Sum types are the dual of tuples. They represent a sequence of possible cases, potentially with arguments. For example the sum type:

## 22.1.1 Sum type

```
typedef num = int + long + double;
// dual to int * long * double
```

represents three cases and is dual to the tuple type shown.

#### 22.1.2 Sum values

The value of a sum represents one of the cases of the type. Case indicies are 0 origin as with tuples.

```
typedef num = int + long + double;
var c0 = (case 0 of num) 42;
var c1 = (case 1 of num) 53L;
var c2 = (case 2 of num) 66.0;
```

The parenthesised expressions above are called *type constructors*.

#### 22.1.3 caseno operator

The case number of a sum value can be extracted as an int:

```
println$ caseno c0, caseno c1, caseno c2;
// 0,1,2
```

#### 22.1.4 Switching on cases

Sum variables are decoded with a match which may also extract an argument value:

```
typedef num = int + long + double;
var x = (case 1 of num) 53L;
println$
  match x with
  | case 0 (i) => "int " + i.str
  | case 1 (l) => "long" + l.str
  | case 2 (d) => "double " + d.str
  endmatch
;
```

The match tags do not include the type of the sum, since it is known from the argument.

#### 22.1.5 Unit arguments

A sum component may have a unit argument.

```
typedef maybe_int = 1 + int;
var x = case 0 of maybe_int;
match x with
| case 0 () => println$ "Nothing";
| case 1 i => println$ "Integer " + i.str;
endmatch;
```

For the first case the () may be omitted:

```
typedef maybe_int = 1 + int;
var x = case 0 of maybe_int;
match x with
| case 0 => println$ "Nothing";
| case 1 i => println$ "Integer " + i.str;
endmatch;
```

or the unit application syntax can be used:

```
typedef maybe_int = 1 + int;
var x = case 0 of maybe_int;
match x with
| #case 0 => println$ "Nothing";
| case 1 i => println$ "Integer " + i.str;
endmatch;
```

If the argument is a unit, the constructor is sometimes called a *constant constructor*.

#### 22.1.6 Unit sum

There is a family of special sum types equivalent to:

```
2 = 1 + 1

3 = 1 + 1 + 1

4 = 1 + 1 + 1
```

Recall type 1, or unit, is the type of the empty tuple.

The type 2 is also known as bool, and represents two cases where false is an alias for case 0 of 2 and true is an alias for case 1 of 2.

The type 0 or void, is the type of no values.

These types are called  $unit\ sums$  because they're a sum of a certain number of units.

Note carefully that:

```
x + (y + z), (x + y) + z, x + y + z
```

are three distinct types because operator + is not associative.

#### 22.2 Unions

A union is the dual of a struct. It is a nominally typed version of a sum. Here for example is a list of integers:

```
union intlist {
   iEmpty ;
   iCons of int * intlist;
};
```

This alternative syntax is more commonly used and comes from ML family:

```
union intlist =
    | iEmpty
    | iCons of int * intlist
;
```

The fields of a union type are injections or type constructors. In effect they cast their argument to the type of the union, thus unifying heterogenous types into a single type.

Pattern matches are used to decode unions.

```
var x = iEmpty;
x = iCons (1, x);
x = iCons (2, x); // list of two integers

fun istr (x:intlist) =>
  match x with
  | #iEmpty => "end"
  | iCons (i, tail) => i.str + "," + istr tail
  endmatch
;
```

The first variant represents an empty list. The second variant says that a pair consisting of an int and a list can be considered as a list by applying the type constructor iCons to it.

Unlike product types, a sum may directly contain itself. This is because sum types are represented by pointers.

#### 22.2.1 enum

A restricted kind of union, being a nominally typed version of a unit sum.

```
enum colour { red, green, blue }; // same as
enum colour = red, green, blue; // same as
union colour = red | green | blue;
```

The tag value of an enum can be set:

```
enum wsize = w8=8, w16=16, w32=32, w64=64;
```

### 22.2.2 caseno operator

The caseno operator can find the tag value of any sum type, the anonymous sum, union, enum or variant as an integer.

```
assert caseno w16 == 16;
assert caseno (case 1 of 2) == 1;
```

## 22.3 Variants

Variants are the sum type which are the dual of records. They used named injections like unions but are structurally typed.

#### 22.3.1 Variant coercion

Variant values always have a singleton type, so to be used with a set of variants, a coercion must be used.

```
typedef vars = union { Int of int ; Float of float; };
var x = Int 32; // type union {Int of int}
var y = x :>> vars; // coerce to type vars
```

The type being coerced must be super type of the coercion type, this means it must have subset of the cases of the coercion type.

# Chapter 23

# **Exponentials**

## 23.1 Functions

Felix provides four core function types.

#### **23.1.1** Function

Functions use infix operator -> to denote a function, where the LHS is called the domain, and the RHS the codomain:

```
var f : int -> long = fun (x:int)=>x.long;
```

The operator is right associative so that

```
var f : int -> long -> string =
  fun (x:int) =>
    fun (y:long)=>
        (x.long + y).str
;
// equivalent to
var f : int -> (long -> string) =
  fun (x:int) (y:long) =>
        (x.long + y).str
;
```

If a function returns a function, it is a higher order functions. The number of -> symbols in the type is known as the *arity* of the function.

Function defined with fun binder may not have side effects.

Functions are slaves which accept data and control, perform a calculation, and return a result and control to the caller, which is the master. The master/slave relationship may also be expressed as a client/server relationship.

Felix uses the machine stack to save and retrieve the master return address for a function.

At run time a function closure is represented by a single machine address which is nominally a pointer to a heap allocated C++ object which retains the function local variables and provides an apply() method.

Functions which depend only on their arguments and any constants in their context are said to be *pure*, those which depend on external variables are *impure*. The kind can be noted with an adjectival descriptor on the definition:

```
pure fun sin: double -> double = "sin($1)";
var x = 1;
impure fun get_x() => x;
```

Impure functions are sometimes called observers or accessors.

#### 23.2 Generators

A generator is a function which is permitted to have side effects. It is defined with the gen binder instead of fun.

Generators have the same type as functions.

The exemplar generator is of course rand() which returns a different value each call, depending on some external state.

# 23.3 Yielding Generators

Generators may contain a yield statement which returns a value and control, but also records the current location in the local state, to allow the generator to be resumed where it left off.

To use a yielding generator a closure must be stored in a variable.

Yielding generators are a special case of coroutines, implemented in a special way.

```
gen integers () = {
  var i = 0;
next:>
  yield i;
++i;
```

```
goto next;
}

var counter = integers;
var zero = counter();
var one = counter();
```

#### 23.3.1 Procedure

A procedure is given the type of a function with the codomain set to 0 (aka void). Procedures are not functions, they return control but not a value. Technically a procedure is a delimited continuation.

Although procedures look like functions, in Felix they are utterly different because they do not use the machine stack to store the return address. Instead, procedures use a heap allocated data frame, with pointers to ancestral context and the caller continuation return address, and save the current location in a special variable in the data frame.

Thus procedures may cooperatively swap themselves out in favour of another procedure.

A procedure with its ancestral context, call chain, and current location is called a fibre. It represents an exchangeable locus of contol.

#### 23.3.2 C function

Felix can deal with C functions too. The infix operator --> is used to denote a C function type. C functions can be defined directly in Felix like:

```
cfun f(x:int) = x + x;
```

Felix will represent this function like:

```
int f(int x) { return x + x; }
```

which has a C function type. The Felix C function type is a C function closure, in C a pointer to the C function.

If a cfun uses the thread frame or garbage collector, it will fail to compile at C++ compile time because Felix always passes a pointer to the thread frame explicitly.

We provide cfun primarily to allow construction of C data types used by drivers as callback functions.

However they can also be used to define an interface to a C callable library written in Felix.

Note that Felix knows that C functions accept multiple arguments rather than tuples and automatically unpacks a tuple passed to a C function.

#### 23.3.3 C procedure

Felix can deal with C procedures too, the type is the same as a C function with the codomain set to void.

```
var y = 1;
cproc f(x:int) {y = x}
```

Felix will represent this like:

```
void f(int x) { y = x; }
```

which has a C function type. The Felix C function type is a C function closure, in C a pointer to the C function.

If a cfun uses the thread frame or garbage collector, it will fail to compile at C++ compile time because Felix always passes a pointer to the thread frame explicitly.

#### 23.3.4 Type indexed functions

Felix has an extension which allows function types to be indexed by types. For example:

```
struct IO {};
fun f(x:int) :[IO] int = {
   println$ x; return x;
}
var clos : int ->[IO] int = f;
```

The indexing type is known as the *effects* type of the function. For functions without effects annotations, the effects type defaults to unit.

By combining effects types, row polymorphism, and typematches, Felix provides tools to manage various effects. For example:

```
fun map[T,U] (f:T\rightarrow [G] U) (list[T]) : [G] list[U] => ...
```

says that the higher order function map, given a function f with effect G, will itself have effect G.

This is an experimental feature that is not yet utilised by the library.

## **23.4** Array

Felix has various kinds of array. The term is abused and sometimes refers to the abstract concept, and sometimes the statically typed fixed length array described here.

An array is nothing but a tuple all of whose elements have the same type. It is convenient to use an exponential operator with a unit sum index to provide a compact notation:

```
int ^ 3 // array of 3 integers equivalent to
int * int * int
```

Therefore the value:

```
var a3 = 1,2,3;
```

is, in fact, an array. As for tuples an integer literal applied to an array value returns a component, however for arrays, an expression may be used as well:

```
var i = 1;
var y = a3 . i;
var z = a3 . proj i of (int^3);
```

The last form is equivalent to

```
var z = a .
   match i with
   | 0 => proj 0 of (int^3)
   | 1 => proj 1 of (int^3)
   | 2 => proj 2 of (int^3)
   | _ => throw error
   endmatch
;
```

in other words there is a run time array bounds check equivalent to a match failure. Note that of course the actual generated code is optimised!

A run time check can be avoided by using the correct type of index:

```
var i = case 1 of 3;
var z = a . i; // no run time check
```

#### 23.4.1 Multi-arrays

Whilst we introduced the exponential notation

```
В ^ Ј
```

as a mere shorthand, where J is a unit sum, in fact Felix allows the index to be any compact linear type.

A compact linear type is any combination of sums, products, and exponentials of unit sums. The type

```
3 * 4 * 5
```

for example is compact linear, and therefore Felix allows the array type

```
typedef matrix = double \hat{\ } (3 * 4 * 5)
```

Although this looks like the type

```
typedef array3 = double ^ 3 ^ 4 ^ 5
```

as suggested by the usual index laws, the latter is an array size 5 of arrays size 4 of arrays size 3 which can be used like:

```
var a : array3;
var z = a . case 1 of 5 . case 1 of 4 . case 1 of 3;
```

where you will note that the projections are applied in the reverse order to the indices. On the other hand to use the first form we have instead:

```
var m : matrix;
var z = a . (case 1 of 3, case 1 of 4, case 1 of 5);
```

The exponent here is a value of a compact linear type. It is a single tuple value! It is called a multi-index when applied to an array.

The advantage of this type is that there is an obvious encoding of the values shown in this psuedo code:

```
i * 3 * 4 + j * 3 + k
```

which is nothing more than a positional number notation where the base varies with position. That encoding clearly associates with the compact linear value as integer in the range 0 to 59, or, alternatively, an value of type 60. In other words the type is linear and compact.

Since clearly, given an integer in range 0 through 59 and this type we can decode the integer into a tuple, being the positional representation of the integer in this weird coding scheme, the type is clearly isomorphic to the subrange of integer.

Therefore Felix allows you to coerce an integer to a compact linear type with a run time check, and convert a compact linear type to an integer or a unitsum:

```
var i : int = ((case 1 of 3, case 1 of 4, case 1 of 5) :>> int);
var j : 60 = ((case 1 of 3, case 1 of 4, case 1 of 5) :>> 60);
var clt : 3 * 4 * 5 = (16 :>> 3 * 4 * 5);
```

Because we can do this we can now write a loop over a matrix with a single iterator:

```
for i in 60 do
  println$ m . (i :>> 3 * 4 * 5);
done
```

This is an advanced topic which will require an extensive explanation beyond the scope of this summary. However we will not that this facility provides a very high level feature known as polyadic array programming. In short this means that one may write routines which work on matrices of arbitrary dimension. You can of course do this in C by doing your own index calculations at run time and using casts, however Felix does these calculations for you based on the type so they're always correct.

# Chapter 24

# Type Recursion

Felix provides two mechanisms to allow type recursion: implicit recursion by self reference, and explicit recursion using pointers.

## 24.1 The as combinator

We can express the type of a list without a definition using the as combinator:

```
typedef intlist = 1 + int * X as X;
```

The as combinator has low precedence and introduces a binding variable similar to a  $\mu$  binder in type theory, however the variable is visible outside the scope it controls as well. The inner use of the variable is known as a *fixoint* and is a place where whole term controlled by the binder may be substituted, resulting, if repeated, in an infinnite recursion. The use of the binder therefore allows infinite data types to be represented finitely.

In the list case above, a list is either a unit, or a pair consisting of an int and another list.

Type recursion in Felix may be written anywhere but will not work correctly unless a box intervenes. A box is either any sum type or a pointer.

#### 24.2 Pointers

Pointers provide another mechanism for implementing type recursion explicitly. Pointers are more powerful than fixpoints, which is not always an advantage.

The notation for a pointer to an object of type T is either

```
%T
ptr[T] // alias for &T
```

Values of pointer type can originate in two primary ways: from the address of a variable:

```
var x = 1;
var px : &int = &x;
```

or by constructing an object on the heap. The **new** operator copies a value to a heap object and returns its address as a pointer:

```
var px : &int = new 1;
```

The basic Felix pointer type cannot be NULL, cannot be incremented, and always points to a single object. It is therefore always safe to dereference to fetch the value stored at the pointer with the prefix dereference operator \*:

```
var px : &int = new 1;
var x = *px;
```

Objects located by pointers are intrinsically mutable. A new value can be stored with the store at operator:

```
var px : &int = new 1;
px <- 2;</pre>
```

Pointers to products have special properties. More precisely, for each value projection p which extracts a the value of a product component, there is a corresponding pointer projection which accepts a pointer to a product object and returns a pointer to the component;

```
var pair = 1,"Hello";
var s = pair . 1; // value projection
var ps = &pair . 1; // pointer projection
ps <- "Bye"; // pair is now 1,"Bye"</pre>
```

This machinery eliminates the need for the concept of addressable lvalues. Thus you cannot take the address of a product component:

```
var pair = 1,"Hello";

// var ps = &(pair.1); // ERROR
```

because pair.1 is a value, and values do not have public addresses. Instead Felix provides some sugar:

```
var pair = 1,"Hello";
var ps = pair&.1; // means (&pair).1
var &p = &pair;
var s = p*.1; // means (*p).1
```

# 24.3 Maybe NULL pointers

Felix also has a pointer type that could perhaps be NULL. It is defined in the library by:

```
union cptr[T] = | nullptr | Ptr of &T;
```

and the alias

```
@T
```

may also be used. Due to implementation magic, this type is compatible with C/C++ pointers, that is, Felix nullptr is C NULL. In particular, one should write, for example:

```
gen malloc: size -> @T = "malloc($1)";
```

because malloc could return NULL. Strict adherence to correctly typing C functions is necessary to ensure the guarrantee dereferencing Felix pointers is safe.

Note that dereferencing C pointers, even if not NULL, need not be safe because the pointed at object may not be live. Felix guarrantees to keep heap allocated objects to which Felix pointers exist live.

Note that a cptr[T] obtained from a ptr[T] has this guarrantee as well.

# 24.4 Incrementable Pointers

Felix also has C style incrementable pointers given the type <code>carray[T]</code> or alias <code>+T</code>. Pointers of this type are not intrinsically safe to use. They can be NULL.

The carray is provided as a model of C arrays so that they can be manipulated in Felix, even if such operations are risky.

# Chapter 25

# Meta-typing

Felix provides some facilities for meta-typing.

## 25.0.1 typedef fun

The notation

```
typedef fun diag (T:TYPE):TYPE=> T * T;
var x: diag int = 1,2;
```

defines a type function (or functor). Given a type T, this function returns the type for a pair of T's. The identifier TYPE denotes the kind which is a category of all types.

Applications of type functions must be resolved during binding, since the result may influence overloading.

# 25.1 typematch expression

Felix has a facility to inspect and decode types at compile time.

```
typedef T = int * long;
var x:
   typematch T with
   | A * B => A
   | _ => int
   endmatch
   = 1
;
```

As with type functions, type matches must be resolved during binding. If a type match fails, an error is issued a compilation halted. The wildcard type pattern \_ matches any type.

The real power of the type match comes when combined with a type function:

```
typedef fun promote (T:TYPE): TYPE =>
  typematch T with
  | #tiny => int
  | #short => int
  | #int => int
  | #long => long
  | #vlong => vlong
  endmatch
;
```

This functor does integral promotions of signed integer types corresponding to ISO C rules.

# 25.2 Type Sets

A type set is a component of a type constraint expression which restricts a type variable one of a specified list of entities. Each entity may be either a type, a type predicate, or another type set. Syntax like:

```
typesetof (short, int, long, vlong)
```

is used for a typeset expression.

The typedef statement may be used to define an alias for a typeset:

```
typedef Integers = typesetof (short, int, long, vlong);
```

#### 25.2.1 Union and Intersection

Two operators are provided for typesets, union and intersection which are spelled  $\c$ up and  $\c$ ap respectively and are printed as set theoretic union and intersection symbols  $\cup$  and  $\cap$ .

```
typedef sints = typesetof (int,long);
typedef uints = typesetof (uint,ulong);
typedef ints = sints \(\cup \) uints;
typedef shorts = typesetof (short,int,long);
typedef ssints = ints \(\cap \) shorts;
```

#### 25.2.2 Membership

The membership operator tests if a type is a member of a typeset, it is spelled in or  $\$ in, the latter being typeset as the set theoretic symbol  $\in$ . It serves to define the semantics of a typeset as a typematch.

```
typedef ints = typesetof(short,int,long);
typedef result = int ∈ ints;
```

The membership test above is precisely equivalent to

### 25.2.3 Typeset membership constraints

Typesets were introduced to Felix to simplify bindings to C functions. For example:

```
typedef someints = typesetof (int, long);
typedef someuints = typesetof (uint, ulong);
fun someadd[T in someints] : T * T -> T = "$1+$2";
fun someadd[T in someuints] : T * T -> T = "$1+$2";
println$ someadd (1,2); // OK, first function
println$ someadd (1u,2u); // OK, second function
// println$ someadd (1,2u); // fails
```

In this example, a call to someadd will only work if the arguments types are the same and both either int or long. Overload resolution first treats the functions as if there were no constraints. Then, any candidate which fails the constraint it thrown out of the set.

This method saves writing out all the cases individually, which may be exponential in the number of individual types involved, whilst at the same time preventing invalid cases which an unconstrained binding would allow.

If two candidates exist with the same signatures, and one has a constraint and the other does not (or has the constant constraint true), the constrained candidate is considered more specialised than the unconstrained one.

However in general, constraints cannot be compared to see which is most specialised. In particular if for all values of type variables constraint A implies

constraint B, A is more specialised, however there is no operational method for measuring this in general (halting problem!).

# Chapter 26

# Polymorphism

## 26.1 Type Constraints

Felix provides 4 kinds of type constraints.

### 26.1.1 Type class constraints

Class constraints have no impact on phase 1 overload resolution when selecting a binding.

However, when binding the definition of a symbol, specified class views are introduced in a shadow scope as if the class were opened.

During monomorphisation, any virtuals must be mapped to instance functions and this is done by a process similar to that used for overload resolution.

#### 26.1.2 Typeset membership constraints

Typesets were introduced to Felix to simplify bindings to C functions. For example:

```
typedef someints = typesetof (int, long);
typedef someuints = typesetof (uint, ulong);
fun someadd[T in someints] : T * T -> T = "$1+$2";
fun someadd[T in someuints] : T * T -> T = "$1+$2";
println$ someadd (1,2); // OK, first function
println$ someadd (1,2u); // OK, second function
// println$ someadd (1,2u); // fails
```

In this example, a call to someadd will only work if the arguments types are the same and both either int or long. Overload resolution first treats the functions

as if there were no constraints. Then, any candidate which fails the constraint it thrown out of the set.

This method saves writing out all the cases individually, which may be exponential in the number of individual types involved, whilst at the same time preventing invalid cases which an unconstrained binding would allow.

If two candidates exist with the same signatures, and one has a constraint and the other does not (or has the constant constraint true), the constrained candidate is considered more specialised than the unconstrained one.

However in general, constraints cannot be compared to see which is most specialised. In particular if for all values of type variables constraint A implies constraint B, A is more specialised, however there is no operational method for measuring this in general (halting problem!).

### 26.1.3 Equational Constraints

Felix allows a constraint to be For example:

```
fun f[T,U where T * int == int * U] (x:T * U) => x;
println$ f (1,2);
```

This example uses an equational constraint.

Here is another example using a typematch:

```
typedef fun ispair (x:TYPE) : TYPE =>
    typematch x with
    | _ * _ => 1
    | _ => 0
    endmatch
;
fun f[T where ispair T] (x:T)=>x;
println$ f (42,33L); // OK, signature ispair (int * long) true
```

# Chapter 27

# Generics

## 27.1 Generic Functions

Generic provide a way to do  $\it cut$  and  $\it paste$  polymorphism, similar to what C++ does. It is useful for one-off scripts, or times when parametric polymorphism and type classes are not enough.

# 27.1.1 Generic Syntax

The syntax is to just put the kind of a type variable as GENERIC:

```
fun accumulate [T:GENERIC] (container:T) = {
  var sum = 0;
  for elt in container do
    sum = sum + elt;
  done
  return sum;
}
```

#### 27.1.2 Using a generic

With the above example you can write:

```
println$ accumulate (1,2,3,4);
println$ accumulate (1,2,3,4).list;
println$ accumulate (1,2,3,4).varray;
```

#### 27.1.3 Operational Semantics

Felix handles generics as follows. The generic function is treated first, as if it were polymorphic, that is, the GENERIC kind replaced by the default TYPE. After overload resolution is complete, if a generic function is selected, Felix clones the function and all its descendants, creating a new function. In these clones, however, the generic type variable is removed and in the definition of the function and its descenants it is replaced by the actual type deduced by the overload resolution algorithm. The system then replaces the overload result with a reference to this new function.

Therefore, the call is dispatched to a non-generic function, specialised for the arguments.

This kind of operation is also done by the type class specialiser during monomorphisation, and inlining routines during optimisation, however with generics the specialisation is done *before* binding.

Unlike C++, the specialisation is done in the context of the definition. This is more reliable, but it means functions in the context of use cannot participate in overload resolution.

```
class X {
   proc f(x:int) => println$ "X::f " + x;
   proc g[T:GENERIC] (x:T) => f x;
   g 25;
}

class Y {
   proc f(x:int) => println$ "Y::f " + x;
   X::g 33;
}

X::g 99;
```

The output is:

```
X::f 25
X::f 33
X::f 99
```

# 27.2 The typecase expression

The typecase expression allows you to write expressions dependent on a type. Typecase expressions must be resolved before binding is complete.

```
fun f[T:GENERIC] (x:T) =>
  typecase T with
  | int => x + 1
  | double => x + 1.0
  endmatch
;
println$ f 1, f 4.2;
```

Although primarily of use in generic functions, typecases can also be useful for conditional compilation. For example:

```
if PLAT_WIN32
   type file = "HANDLE";
else
   type file = "int";
endif

fun read (f:file) =>
   typecase typeof f with
   | int => unix::read f
   | HANDLE => win32::read f
   endmatch
;
```

## 27.3 Builtin Generics

Felix has a number of builtin generic functions.

### 27.3.1 The strr function

The \_strr function converts any value into a string, with a syntax roughly approximating the syntax used in the program.

It was primarily intended to simplify output of records, the final  ${\tt r}$  from to record.

```
println$ (a=1,b="hello", c=(1,2,3), a=(1,2,3).list);
struct A {
    a:int;
    b:int;
}
println$ (A(1,2))._strr;
```

The output is:

```
(a=1,a=Snoc (Snoc (Snoc (Empty,3),2),1),b='hello',c=(1, 2, 3))
A {a=1,b=2}
```

The Snoc(tail,head) terms there are the native list constructors used by Felix, which are reversed Cons(head,tail) terms. Felix uses these because they generate a pointer followed by data in C++, which means list scanning is independent of the data type.

#### **Operational Semantics**

The converter works by calling the str function for primitives such as int, string, or float, so these must be in scope. The type class based str is injected into the global shadow scope so this will always be bound, however if there is no instance for a type an error will be generated during monomorphisation.

For structured types, \_strr exhibits the structure in some nice way, wrapping the child members of the structures, which are converted to strings recursively.

There is a limit on the recursion depth, and Felix will print ... when it hits that depth.

```
println$ (1,2,3,4,5,6,7,8,9).list._strr;
```

produces

```
Snoc (Snoc (Snoc (...,4),3),2),1)
```

## 27.3.2 The $\_$ eq function

Felix provides a builtin generic function \_eq which can be used to compare small acyclic values of arbitrary types:

```
var x = (1,(a=2,b=3,c=(1,2).list));
var y = x;
println$ _eq (x,y);
```

#### **Operational Semantics**

The comparator requires arguments of the same type. It operates by a recursive descent into the structure of the types. If the type of a subexpression is primitve, the function == is used. This function is defined in the typeclass Eq, and may also be defined in the context of the comparison.

Do not use this generic on a cyclic value, it will loop forever at run time.

The current implementation only expands tuples and records. It delegates to == for all other types. Therefore, lists will be handled correctly since == is already defined for lists in the library.

Technically \_eq is polyadic, not generic. However the implementation is generic.

### 27.3.3 The map function

The \_map operator maps an overloaded function set over a tuple. For example:

```
fun f(x:int)=> x + 1;
fun f(x:double)=> (x+42.0).str+ "!!";
fun f[T] (x:T)=>x;
println$ _map f (1,2.2,"Hello");
```

produces:

```
(2, 44.2!!, Hello)
```

Although many generic operations can better be defined using type classes, it is not possible to do this kind of operation other than with a generic.

All folds, for example, can be defined with type classes because folding mandates the return type be invariant, and we can use polymorphism on the argument type. However this is not possible with mapping because the return type is not dependent on the argument type in a predictable manner.

Technically, Felix can indeed express the return type of the individual functions. Consider:

```
typedef fun fret(argtype:TYPE):TYPE =>
  typematch argtype with
  | int => int
  | double => string
  | ?other => other
  endmatch
;

class U[T] {
  virtual fun ff: T -> fret T;
}

instance U[int] {
  fun ff(x:int)=> x + 1;
```

```
instance U[double] {
  fun ff(x:double)=> (x+42.0).str+ "!!";
}

instance[T] U[T] {
  fun ff[T] (x:T)=>x;
}

open[T] U[T];

println$ ff 22;
  println$ ff 3.0;
  println$ ff "Hello";
```

The first two prints actually work, but the last one fails:

The reason is, that the ff[T] in instance U[T] does not have the correct type to specialise the virtual. The virtual has type

```
T ->
  typematch argtype with
  | int => int
  | double => string
  | ?other => other
  endmatch
```

whereas the instance has type

```
T -> T
```

however matching T against int or because whether the match succeeds depends on the not yet performed replacement of T with a specific type.

Note that in theory if the double branch were removed, the typematch would always return T, since if it is int it returns int, and otherwise returns that. However the compiler is not able to reduce the typematch like that because it looks only at the top branch to begin, and continues only on definite failure.

# ${f Part\ V}$ Interfacing

# Chapter 28

# C bindings

Felix is specifically designed to provide almost seamless integration with  ${\bf C}$  and  ${\bf C}++.$ 

In particular, Felix and C++ can share types and functions, typically without executable glue.

However Felix has a stronger and stricter type system than C++ and a much better syntax, so binding specifications which lift C++ entities into Felix typically require some static glue.

# 28.1 Type bindings

In general, Felix requires all primitive types to be first class, that is, they must be default initialisable, copy constructible, assignable, and destructible. Assignment to a default initialised variable must have the same semantics as copy construction.

It is recommended C++ objects provide move constructors as Felix generated code uses pass by value extensively.

The Felix type system does not support C++ references in general, you should use pointers instead.

However, there is a special lvalue annotation for C++ functions returning lvalues that allows them to appear on the LHS of an assignment. Only primitives can be marked lvalue.

The Felix type system does not support either const or volatile. This has no impact when passing arguments to C++ functions. However it may be necessary to cast a pointer returned from a primitive function in order for the generated code to type check.

# 28.2 Basic type statement

The type statement is used to lift a C++ type into Felix.

The simplest example:

```
type metres = "double";
type Z = "long";
```

creates a Felix type metres based on C++ type double.

Polymorphic types can be created too:

```
type pair[T,U] = "::std::pair<?1,?2>";
```

The names of the type variables T and U are not used in the binding, but serve as placeholders. Instead the encoding ?1 and ?2 is used to refer to the first and second type variables. The Felix type pair[metres,Z] will become C++ type ::std::pair<double,long> in the generated code.

Please be sure to always fully qualify C++ names including leading :: since you do not know the namespace context in which the generated code will reside.

### 28.2.1 Semantics

Unless otherwise noted all types lifted into Felix with the type binding statement must be first class. This means that they must have a publically accessible default initialiser, copy constructor, copy assignment operator, and destructor.

To lift a type which is immobile, lift a pointer to the type instead. Please see below.

# 28.3 Adjectives

Felix needs to know some things about types to handle them properly, it uses a system of adjectives to provide some basic information.

# **28.3.1** pod types

A pod type is a *plain old data type* of the kind common in C. In Felix the annotation is used for optimisation: calls to the destructor are not made by the Felix garbage collector when an object of this type is finalised. This will have no impact provided the type has a trivial destuctor in C++.

Do not specify this adjective unless you are sure the destructor does no useful work.

```
pod type metres = "double";
```

# 28.3.2 \_gc\_pointer types

The \_gc\_pointer\_ adjective tells Felix that the type is a pointer which could be a pointer to an heap allocated object managed by the GC.

When a value of this type is included in a larger objects, the run time type description will include the offset of this subobject in the array of offsets which might contain managed pointers.

It is always safe to use this annotation if the C++ types is a pointer.

# 28.3.3 incomplete types

The adjective **incomplete** may be used to specify the type denoted may not be constructed. If the C++ type being bound is incomplete, for example void, or an incomplete C struct, this annotation will cause a type error in Felix if an attempt is made to construct values of the type.

The primary reason for introducing incomplete types is to permit a Felix pointer to be formed to it, in Felix. For example

```
incomplete type MyVoid = "void";
typedef MyVoidPointer = &MyVoid;
```

# 28.3.4 uncopyable types

This annotation may be used if a value of the type can be constructed but not copied. Since Felix always initialised variables with assignments, uncopyable type are useful only for heap construction yielding a pointer.

# 28.3.5 \_gc\_type T types

This adjective is for gurus only! In conjunction with \_gc\_pointer it is used to permit contruction of an immobile C++ type whilst at the same time ensuring that the type garbage collected.

The method is fraught with peril and use of C++ smart pointers is recommended instead.

```
private uncopyable type bQ_ =
    "::flx::pthread::bound_queue_t"
;
_gc_pointer _gc_type bQ_ type ts_bound_queue_t[T] =
    "::flx::pthread::bound_queue_t*"
```

```
requires
   package "flx_bound_queue",
   scanner "::flx::pthread::bound_queue_scanner"
;
ctor[T] ts_bound_queue_t[T]: !ints =
   """
   new (*PTF gcp, @0, false) ::flx::pthread::bound_queue_t(
   PTF gcp->collector->get_thread_control(), (size_t)$1)
   """ requires property "needs_ptf";
```

In this example from the library, we define the thread safe bound queue as type  $bQ_{-}$  and mark it private and uncopyable to protect it. The C++ type is defined the Felix run time library.

The type the user gets is a ponter, which is defined by a binding to C++ again, declared to be a pointer, and declared to point to  $bQ_-$ .

What this actually does is seen in the constructor which, in C++, constructs the object on the heap, passing the magic encoding **@O** to the second argument of the new expression.

This encoding *normally* denotes the pointer to the shape (RTTI) for the return type of the function. However that type, ts\_bound\_queue has the attribute \_gc\_type bQ\_ which tells Felix to use the shape object for that type instead. We need to do this because the heap value is represented by a pointer to the type, but we want the garbage collector to be able to map such a pointer to the type of the heap object at run time.

### 28.3.6 finaliser clause

A primitive type may have a finaliser clause with string argument which must specify a C++ function with type

```
typedef void finaliser_t (collector_t*, void*);
```

which is used to destroy objects of the type. If not specified the C++ destructor is used, unless the type is a pod in which case no finaliser is deployed. The finaliser is called by the collector after an object is determined to be unreachable, before the underlying storage is reclaimed.

### 28.3.7 scanner clause

A primitive type may have a scanner clause with string argument which must specify the name of a C++ function with type ::flx::gc::generic::scanner\_t given by the typedef

```
typedef void *scanner_t(
   collector_t*, gc_shape_t *, void *, size_t, int
);
```

This is a custom function respondible for finding all the pointers in a data type.

# 28.3.8 encoder clause

A primitive type may have an encoder clause with string argument which must specify the name of a C++ function with type ::flx::gc::generic::encoder\_t\_t given by the typedef

```
typedef ::std::string encoder_t (void *);
```

This is a custom function respondible for encoding the type in a string for serialisation.

### 28.3.9 decoder clause

A primitive type may have an decoder clause with string argument which must specify the name of a C++ function with type ::flx::gc::generic::decoder\_t given by the typedef

```
typedef ::std::size_t decoder_t(void *, char *, ::std::size_t);
```

This is a custom function respondible for decoding a string encoded by the corresponding encoder and building an object of the specified type on the heap.

# 28.4 Expression bindings

Felix has a simple method for introducing constants and expressions from C++ using the const statement:

```
type metres = "double";
const zero_metres: metres = "0.0";
const one_metre: metres = "1.0";
```

Const statements cannot be polymorphic.

# 28.5 Function bindings

In order to use types lifted from C++, Felix has a special form of function definition:

```
type metres = "double";
const zero_metres: metres = "0.0";
const one_metre: metres = "1.0";
fun +: metres * metres -> metres = "$1+$2";
fun *: metres * double-> metres = "$1*$2";
fun *: double * metres -> metres = "$1*$2";
fun todouble: metres -> double = "$1";
var len = one_metre * 3.7;
var len2 = len + len;
println$ "length " + len2.todouble.str;
```

Here the encodings \$1 and \$2 refer to the first and second components of the argument tuple type.

Felix instantiates such functions by substituting the C++ encoding of the argument component into the text string of the function at the position nominated location, possibly adding parentheses to ensure precedence rules do not interfere with the intended semantics.

There is a special set of strings for which Felix knows the precedence. You must use exactly these strings to trigger the rules. It is also possible to manually specify the precedence. If Felix does not understand the precedence then parentheses will be inserted. The purpose of the precedence controls is entirely to reduce the need for the generated C++ to be be littered with parentheses.

[Put table of special strings here] [Put list of precedence names here]

It is sometimes necessary to refer to other entities than the argument components.

[Put table of binding encodings here]

# 28.6 Conversion bindings

A special form is allowed for conversion function:

```
type metres = "double";
ctor metres: double = "$1";
ctor double: metres = "$1";
```

This is exactly the same as:

```
fun _ctor_metres: double -> metres = "$1";
fun _ctor_double: metres -> double = "$1";
```

so that the syntax makes it easier to see a conversion is being defined and what is being converted.

Conversion statements can be polymorphic, but the type variables must be introduced like this:

```
type vect[T] = "::std::vector<?1>"
    requires header '#include <vector>';
fun len[T]: vect[T]->size = "$1.size()";
ctor[T] vect[T]: size = "::std::vector<?1>($1)";
var x = vect[int] 42uz;
println$ x.len;
```

When Felix is seeking a function, if it finds a type name instead, it retries the lookup with \_ctor\_ prefixed to the type name. This only works with actual names! However the name may be the defined name of a type or a typedef alias.

Despite the spelling, a ctor is a conversion operator and not a type constructor.

# 28.7 Procedure bindings

Procedure bindings work the same as function bindings, by emitting the C++ string specified with substitutions.

The primary difference is that procedure bindings must generate one or more C++ statements.

# 28.8 cstruct bindings

A cstruct definition has the same syntax as a struct and provides the same facilities, except that the compiler does not actually emit a C++ structure definition.

Instead the statement is used to lift an existing C type into Felix. It can be used for structs or unions.

The compiler provides projection and pointer projections and a memberwise constructor.

Be warned against using the memberwise constructor if the definition is not complete, for example for certain standard C and Posix types which are incompletely specified.

[It is not currently possible to turn this off] [It currently is only possible to bind to names in the global namespace]

# 28.9 cenum bindings

Blah.

# 28.10 cflags bindings

Blah.

# 28.11 Floating insertions

Felix has a sophisticated system of *floating insertions* which are primarily designed to ensure that if a C++ binding is used, the appropriate C++ header files are included so the binding code is well defined. For example:

```
type vect[T] = "::std::vector<?1>"
  requires header '#include <vector>';
```

Floating insertions can be directly introduced as indicated for inclusion in either the C++ header file or body file Felix generates.

Floating insertions *float* to near the top of the relevant file. Insertions specified in a single file appear in order of writing, if they appear at all, and at most once. The actual insertion strings are checked to prevent duplication.

Insertions can be named:

```
header vector_h = '#include <vector>';
type vect[T] = "::std::vector<?1>"
    requires vector_h
;
```

so that a requires clause may specify the name of an insertion. Duplication of names is permitted:

```
header vector_h = '#include <vector>';
header vector_h = '#include <stdlib.h>';
type vect[T] = "::std::vector<?1>"
    requires vector_h
;
```

A floating insertion is included if, and only if, a C binding is actually used.

Floating insertions themselves may have dependencies expressed with requires clause:

```
header algo_h = '#include <algorithm>';
header vector_h = '#include <vector'
    requires algo_h
;</pre>
```

Insertions can also be polymorphic.

```
body sho[T] ='show<?1>();';
```

A module or non-polymorphic class may contain a naked requires statement:

```
class Vect {
  requires algo_h;
  type vect[T] = 'vector<?1>';
```

The effect is to apply the requirement to all C++ bindings in the class or module. Note: the specified insertion if only emitted if a C++ binding is used!

# 28.12 Property requirements

A requires clause may also specify properties:

```
fun f: int -> int = "f($1)"
   requires property "needs_ptf"
;
```

This provide a flexible tagging system in addition to the use of adjectives. [List of properties here]

# 28.13 Package requirements

A requires clause may specify a package requirement:

```
fun f: int -> int = "f($1)"
   requires packahe "mylib"
;
```

Packages are a collection of platform dependent resources which are configured so that the abstract requirement is used to locate the resource descriptors in a database managed by the flx\_pkgconfig system, mapping the abstract platform independent name to platform dependent names.

Packages can be used to add header files to compiler C++ output, and to find and link support libraries. In some cases, they can also help build the package.

The package system requires the user to supply a search path consisting of a list of directories which are searched to find the file with the package name and extension .fpc.

A typical file looks like this:

```
Name: SDL2
Description: Simple Direct Media Layer 2.0
cflags: -I/usr/local/include/SDL2
includes: '"SDL.h"'
provides_dlib: -L/usr/local/lib -lSDL2
provides_slib: -L/usr/local/lib -lSDL2
```

This description allows Felix to compile and link programs using the SDL2 library without any special switches on the flx command line.

The standard location for an installed Felix configuration is in the subdirectory host/config on Unix or host\config on Windows.

# Chapter 29

# **Embedding**

# 29.1 C Callable libraries

# 29.2 Export directives

The export directives make the exported symbol a root of the symbol graph.

The functional export and forces it to be place in the generated code as an extern "C" symbol with the given name:

```
export fun f of (int) as "myf";
export cfun f of (int) as "myf";
export proc f of (int) as "myf";
export cproc f of (int) as "myf";
```

Functions are exported by generating a wrapper around the Felix function. If the function is exported as fun or proc the C function generated requires a pointer to the thread frame as the first argument, if the cfun or cproc forms are used, the wrapper will not require the thread frame.

In the latter case, the Felix function must not require the thread frame.

A type may also be exported:

```
export type ( mystruct ) as "MyStruct";
```

This causes a C typedef to be emitted making the name MyStruct an alias to the Felix type. This is useful because Felix types can have unpredictable mangled names.

The word export optionally followed by a string may also be used as a prefix for any Felix function, generator, or procedure definition. If the string is omitted is taken as the symbol name. The effect is the same as if an export statement has been written.

Part VI

Library

# Chapter 30

# Core Primitive Types

# 30.1 Boolean type

The type bool which is also called 2 provides the usual boolean logic values false and true. The name bool is actually an alias for type unitsum of two cases. The name false is an alternate name of the value case 0 of 2 and the name true is an alternate name for the value case 1 of 2.

See ?? ?? for more information.

# 30.2 Integer types

### Library Reference

There is a table of the types Table 30.1 Felix Integer Types.

Note that all these types are distinct unlike C and C++. The types designated are not the complete set of available integer like types since not all have literal representations.

Signed integers are expected to be two's complement with one more negative value that positive value. Bitwise and, or, exclusive or, and complement operations do not apply with signed types.

The effect of overflow on signed types is unspecified.

Unsigned types use the standard representation. Bitwise operations may be applied to unsigned types. Basic arithmetic operations on unsigned types are all well defined as the result of the operation mathematically modulo the maximum value of the type plus one.

The maximum value of an unsigned type is one less than two raised to the power of the number of bits in the type. The number of bits is 8, 16, 32, or 64 or 128

Table 30.1: Felix Integer Types

Standard signed integers  tiny char t short short s int int long long long l vlong long long standard unsigned integers  utiny unsigned char ut ushort unsigned short us uint unsigned int u ulong unsigned long ul uvlong unsigned long ul exact signed integers  int8 int8_t i8 int16 int16_t i16 int32 int32_t i32 int64 int64_t i64 Exact unsigned integers  uint8 uint8_t us uint8 uint8_t us uint64 uint64_t u64 Exact unsigned integers  uint8 uint8_t us uint16 uint16_t u16 uint32 uint32_t u32 uint64 uint64_t u64  Weird ones  size size_t uz intptr uintptr_t up ptrdiff ptrdiff_t ud intmax intmax_t j uintmax uintmax_t j uintmax uintmax_t uj  Addressing  address void* byte unsigned char	Felix	С	Suffix
short         short         s           int         int         lnt           long         long         l           vlong         long         long           vlong         long         long           utiny         unsigned         thar           utiny         unsigned         thar           utiny         unsigned         thar           us         uint         u           usingned         long         ul           uvlong         unsigned         long         ul           Exact         signed         long         ul           Exact         signed         long         ul           uvlong         unsigned         long         ul           Exact         signed         long         ull           Exact         signed         long         ull           Exact         signed         long         ull           int8         int8_t         int         i8           int16_t         int6_t         i16         i16           int32_t         ii32_t         ii32           uint8_t         uint8_t         u8           uint4_	St	andard signed integers	
int         int           long         long           vlong         long long           vlong         long long           standard unsigned integers         ut           utiny         unsigned char         ut           ushort         unsigned short         us           uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ull           Exact signed integers         i16           int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         us           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         ud           intmax         intmax_t         uj           Addressing	tiny	char	t
long         long         l           vlong         long         l           Standard unsigned integers         ut           utiny         unsigned char         ut           ushort         unsigned short         us           uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ul           uvlong         unsigned long long         ul           Exact signed integers         i           int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         us           uint8         uint8_t         us           uint6         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         ud           intmax         intmax_t         uj           Addressing	short	short	$\mathbf{S}$
vlong         long         long           Standard unsigned integers           utiny         unsigned char         ut           ushort         unsigned short         us           uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ul           uvlong         unsigned long long         ul           Exact signed integers         it         it           int8         int8_t         it         it           int16         int16_t         it         it           int32         int32_t         it         it           uint8         uint8_t         us         unt           uint8         uint16_t         ut         ut           uint32         uint32_t         u32         uint64         ut           uint64_t         uint64_t         u64         ue           wird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         ud           intmax         intmax_t         uj           Addressing	int	int	
Standard unsigned integers           utiny         unsigned char         ut           ushort         unsigned short         us           uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ull           Exact signed integers         it           int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         u8           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         uj           Addressing         address         void*	long	long	1
utiny         unsigned char         ut           ushort         unsigned short         us           uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ull           Exact signed integers         it           int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         u64           Exact unsigned integers         unt8           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         uj           Addressing	vlong	long long	11
ushort         unsigned short         us           uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ull           Exact signed integers         it           int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         us           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	Sta	ndard unsigned integers	
uint         unsigned int         u           ulong         unsigned long         ul           uvlong         unsigned long long         ul           Exact signed integers         int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         i64           Exact unsigned integers         unt16           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         Weird ones         u64           Size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         void*	utiny	unsigned char	ut
ulong         unsigned long         ul           uvlong         unsigned long long         ull           Exact signed integers         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         i64           Exact unsigned integers         us           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	ushort	unsigned short	us
uvlong         unsigned long long long ints         ull is           int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         i64           Exact unsigned integers         us           uint8         uint8_t         us           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	uint	unsigned int	u
Exact signed integers   int8	ulong	unsigned long	ul
int8         int8_t         i8           int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         i64           Exact unsigned integers           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	uvlong	unsigned long long	ull
int16         int16_t         i16           int32         int32_t         i32           int64         int64_t         i64           Exact unsigned integers           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones           size         size_t         uz           intptr         uintptr_t         p           uintptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	-	Exact signed integers	
int32         int32_t         i32           int64         int64_t         i64           Exact unsigned integers           uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones           size         size_t         uz           intptr         uintptr_t         p           uintptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	int8	int8_t	i8
int64 int64_t i64  Exact unsigned integers  uint8 uint8_t u8 uint16 uint16_t u16 uint32 uint32_t u32 uint64 uint64_t u64  Weird ones  size size_t uz intptr uintptr_t up ptrdiff ptrdiff_t ud intmax intmax_t j uintmax uintmax_t uj Addressing  address void*	int16	int16_t	i16
Exact unsigned integers  uint8	int32	int32_t	i32
uint8         uint8_t         u8           uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones           size         size_t         uz           intptr         uintptr_t         p           uintptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing	int64	int64_t	i64
uint16         uint16_t         u16           uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones           size         size_t         uz           intptr         uintptr_t         p           uintptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing   address void*	$\mathbf{E}$	xact unsigned integers	
uint32         uint32_t         u32           uint64         uint64_t         u64           Weird ones         size         size_t         uz           intptr         uintptr_t         p           uintptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing           address         void*	uint8	uint8_t	u8
uint64 uint64_t u64  Weird ones  size size_t uz intptr uintptr_t p uintptr uintptr_t up ptrdiff ptrdiff_t d uptrdiff ptrdiff_t ud intmax intmax_t j uintmax uintmax_t uj Addressing  address void*	uint16	uint16_t	u16
Weird ones           size         size_t         uz           intptr         uintptr_t         p           uintptr         uintptr_t         up           ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing           address         void*	uint32	uint32_t	u32
size size_t uz  intptr uintptr_t p  uintptr uintptr_t up  ptrdiff ptrdiff_t d  uptrdiff ptrdiff_t ud  intmax intmax_t j  uintmax uintmax_t uj  Addressing  address void*	uint64	uint64_t	u64
intptr uintptr_t p uintptr uintptr_t up ptrdiff ptrdiff_t d uptrdiff ptrdiff_t ud intmax intmax_t j uintmax uintmax_t uj Addressing address void*		Weird ones	
uintptr     uintptr_t     up       ptrdiff     ptrdiff_t     d       uptrdiff     ptrdiff_t     ud       intmax     intmax_t     j       uintmax     uintmax_t     uj       Addressing       address     void*	size	size_t	uz
ptrdiff         ptrdiff_t         d           uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing           address         void*	intptr	uintptr_t	p
uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing           address         void*		uintptr_t	up
uptrdiff         ptrdiff_t         ud           intmax         intmax_t         j           uintmax         uintmax_t         uj           Addressing           address         void*	ptrdiff	ptrdiff_t	d
uintmaxuintmax_tujAddressingaddressvoid*		ptrdiff_t	ud
Addressing address void*	intmax	intmax_t	j
address void*	uintmax	uintmax_t	uj
		Addressing	
byte unsigned char	address	void*	
	byte	unsigned char	

for all unsigned types.

There is a table of the operators Table 30.2 Integer Operators.

# 30.2.1 Classification of integers

### Library Reference

Integer types can be grouped into sets. In Felix this can be done with a typeset construction. The defined typesets are show in Table 30.3 Integer Typesets.

Fast integers correspond to the usual C distinct integer types.

Exact integers are aliases to fast integers of specified sizes, in Felix these are distinct types.

The weird integers are special purposes aliases to fast integers which have special uses, again in Felix these are distinct types.

- The type ptrdiff is a signed type intended to represent the difference between two pointers.
- The size type is for measuring the sizes of objects and number of elements in an array.
- The intmax and uintmax types are the largest available signed and unsigned integer types, respectively.
- Finally the intptr and uintptr types are the same size as a pointer and can be used for low level numerical operations on pointers either by a conversion or reinterpret cast. They're typically used for to pack extra data into the low bits of a pointer to a type with an alignment which ensures the low bits of the pointer are zero.

Typesets can be used to simplify specification of C function bindings by leveraging constrained polymorphism.

```
fun add[T in ints]: T * T -> T = "$1+$2";

// or equivalently
fun add[T : ints]: T * T -> T = "$1+$2";
```

A special form which implies a quantifer for every use also exists, by specifying a! followed by a typeset name. For example,

```
fun intsum: !ints * !ints -> long = "(long)($1+$2)";

// or equivalently
fun intsum[T:ints, U:ints] : T * U -> long = "(long)($1+$2)";
```

Table 30.2: Integer Operators

symbol	kind	typo	semantics	
Symbol	KIIIQ	type		
		All Integers		
==	infix-nassoc	$T * T \rightarrow bool$	equality	
!=	infix-nassoc	$T * T \rightarrow bool$	inequality	
<	infix-nassoc	$T * T \rightarrow bool$	less	
<=	infix-nassoc	$T * T \rightarrow bool$	less or equal	
>	infix-nassoc	$T * T \rightarrow bool$	greater	
>=	infix-nassoc	$T * T \rightarrow bool$	greater or equal	
+	infix-lassoc	T * T -> T	addition	
-	infix-lassoc	T * T -> T	subtraction	
*	infix-lassoc	T * T -> T	multiplication	
/	infix-lassoc	T * T -> T	quotient	
%	infix-lassoc	T * T -> T	remainder	
<<	infix-lassoc	T * T -> T	multiplication by power of 2	
>>	infix-lassoc	T * T -> T	division by power of 2	
-	prefix	T -> T	negation	
+	prefix	T -> T	no op	
succ	func	T -> T	successor	
pred	$\operatorname{func}$	T -> T	predecessor	
	Signed Integers			
sgn	func	T -> T	sign	
abs	$\operatorname{func}$	T -> T	absolute value	
Unsigned Integers				
\&	infix-lassoc	T * T -> T	bitwise and	
\1	infix-lassoc	T * T -> T	bitwise or	
\^	infix-lassoc	T * T -> T	bitwise exclusive or	
~	prefix	T * T -> T	bitwise complement	
*********	non aggoriative	_		

nassoc: non-associative lassoc: left associative

func: function

note prefix - maps to function neg

Table 30.3: Integer Typesets

fast_sints	(tiny, short, int, long, vlong)
$exact\_sints$	(int8, int16, int32, int64)
$fast\_uints$	(utiny, ushort, uint, ulong, uvlong)
$exact\_uints$	(uint8, uint16, uint32, uint64)
$weird\_sints$	(ptrdiff, ssize, intmax, intptr)
$weird\_uints$	(size, uintmax, uintptr)
sints	$fast\_sints \cup exact\_sints \cup weird\_sints$
uints	$fast\_uints \cup exact\_uints \cup weird\_uints$
$fast\_ints$	$fast\_sints \cup fast\_uints$
$exact_{ints}$	$exact\_sints \cup exact\_uints$
ints	$sints \cup uints$

Note intsum can add any different kinds of integers, returning a long.

Polymorphism with typeset constraints is *only* useful for C bindings because the constraints are not propagated. It simply saves writing out all the finite combinations when genericity in the C or C++ target code means the C code would be the same in each case.

# 30.3 Floating point types

# Library Reference

There is a table of the operators Table 30.5 Floating Point Operators, we also have Table 30.4 Trig functions.

Felix also provides FINFINITY, DINFINITY and LINFINITY for positive infinity representation for float, double and ldouble types, respectively.

# 30.4 Complex types

There are three complex types, fcomplex, dcomplex and lcomplex corresponding to cartesian representation using a pair of float, double and ldouble values, respectively.

There is a table of the operators Table 30.6 Complex Operators, we also have Table 30.4 Trig functions.

# 30.5 Quaternion type

There is a table of the operators Table 30.7 Quaternion Operators.

Table 30.4: Trig functions

symbol	type	semantics
		circular
sin	T -> T	sine
cos	T -> T	cosine
tan	T -> T	tangent
asin	T -> T	arc (inverse) sine
acos	T -> T	arc (inverse) cosine
atan	T -> T	arc (inverse) tangent
		hyperbolic
sinh	T -> T	hyperbolic sine
cosh	T -> T	hyperbolc cosine
tanh	T -> T	hyperbolic tangent
asinh	T -> T	arc (inverse) hyperbolic sine
acosh	T -> T	arc (inverse) hyperbolic cosine
atanh	T -> T	arc (inverse) hyperbolic tangent
Note: In	verses ret	urn primary branch

Table 30.5: Floating Point Operators

symbol	kind	type	semantics
==	infix-nassoc	T * T -> bool	equality
! =	infix-nassoc	$T * T \rightarrow bool$	inequality
<	infix-nassoc	T * T -> bool	less
<=	infix-nassoc	$T * T \rightarrow bool$	less or equal
>	infix-nassoc	$T * T \rightarrow bool$	greater
>=	infix-nassoc	$T * T \rightarrow bool$	greater or equal
+	infix-nassoc	T * T -> T	addition
_	infix-nassoc	T * T -> T	subtraction
*	infix-nassoc	T * T -> T	multiplication
/	infix-nassoc	T * T -> T	quotient
_	prefix	T -> T	negation
abs	func	T->T	absolute value
log10	func	T->T	base 10 logarithm
sqrt	func	T->T	square root
ceil	func	T->T	ceiling
floor	func	T->T	floor
trunc	func	T->T	truncate
embed	func	int->T	embedding

nassoc: non-associative lassoc: left associative

func: function

note prefix – maps to function  ${\tt neg}$ 

Table 30.6: Complex Operators

symbol	kind	type	semantics
fcomplex	ctor	float * float -> fcomplex	cartesian
fcomplex	$\operatorname{ctor}$	<pre>float -&gt; fcomplex</pre>	from real
dcomplex	ctor	<pre>double * double -&gt; dcomplex</pre>	cartesian
dcomplex	$\operatorname{ctor}$	double -> dcomplex	from real
lcomplex	ctor	<pre>ldouble * ldouble -&gt; lcomplex</pre>	cartesian
lcomplex	ctor	<pre>ldouble -&gt; lcomplex</pre>	from real
==	infix-nassoc	T * T -> bool	equality
! =	infix-nassoc	T * T -> bool	inequality
+	infix-lassoc	T * T -> T	addition
_	infix-lassoc	T * T -> T	subtraction
*	infix-lassoc	T * T -> T	multiplication
/	infix-lassoc	T * T -> T	quotient
_	prefix	T -> T	negation
real	func	T->R	real part
imag	$\operatorname{func}$	T->R	imaginary part
abs	$\operatorname{func}$	T->R	norm
arg	func	T->R	argument

nassoc: non-associative lassoc: left associative

func: function ctor: constructor

note prefix – maps to function  ${\tt neg}$ 

Table 30.7: Quaternion Operators

symbol	kind	type	semantics
==	infix-nassoc	T * T -> bool	equality
! =	infix-nassoc	$T * T \rightarrow bool$	inequality
+	infix-lassoc	T * T -> T	addition
_	infix-lassoc	T * T -> T	subtraction
*	infix-lassoc	T * T -> T	multiplication
/	infix-lassoc	T * T -> T	quotient
	prefix	T -> T	negation

nassoc: non-associative lassoc: left associative

func: function

note prefix - maps to function neg

Table 30.8: ASCII charsets

symbol	definition
upper	ABCDEFGHIJKLMNOPQRSTUVWXYZ
lower	${\tt abcdefghijklmnopqrstuvwxyz}$
letters	upper + lower
digits	0123456789
alphanum	letters + digits
cidcont	alphanum+"_"
flxidcont	alphanum+"'"
camlidcont	alphanum+"_'"
numeric	digits + ".eEdD_"

# 30.6 Char Type

Felix has a type char corresponding to C's char. There are no literals of type char, instead there is a function, also called char to construct a char from a string literal. If the string at least length 1, the first character is returned, if the string is empty the NUL char \0x00 is returned.

An overload of the char function also accepts an int argument and constructs a char with the designated C code value which must be in the range 0 through 255.

The function ord extracts the C code value of a char as an int in the range 0 through 255.

We note that C code values were originally used for the ASCII character set. Strings of char may be used to represent ISO-10646 (Unicode) code points via the UTF-8 encoding method. ASCII characters in the range 0 through 127 agree with Unicode interpretation.

# 30.6.1 ASCII classification functions

There is a set of Table 30.9 ASCII classification functions used to test the ASCII class of char.

The library also provides character sets represents as strings, show in Table 30.8 ASCII charsets

Table 30.9: ASCII classification functions

1 1	1	· ·
symbol	type	semantics
ISO C functions		
isupper	char -> bool	A-Z
islower	char -> bool	a-z
isalnum	char -> bool	A-Za-z0-9
isalpha	char -> bool	A-Za-z
isdigit	char -> bool	0-9
isxdigit	char -> bool	0- $9$ A- $Z$ a- $z$
iscntrl	char -> bool	0x0-0x1F
isspace	char -> bool	0x20
isblank	char -> bool	0x20,0x09
isprint	char -> bool	0x20-0x7e
ispunct	char -> bool	punctuation
_	Lexing fur	nctions
isidstart	char -> bool	First char identifier
iscamlidcont	char -> bool	Ocaml, subsequent chars
iscidcont	char -> bool	C, subsequent chars
isflxidcont	char -> bool	Felix, subsequent chars
isnumeric	char -> bool	0-9+Ee
isalphanum	char -> bool	A-Za-z0-9
isletter	char -> bool	A- $Za$ - $z$
issq	char -> bool	1
isdq	char -> bool	п
isslosh	char -> bool	\
isnull	char -> bool	0x0
iseol	char -> bool	\n LF: Unix, CR: Windows
		,

# Chapter 31

# Algebraic Structure of numeric types

### Basic Algebra Package Number Package

The functionality identified in the previous chapter is not provided on a type by type basis, but instead leverages the mathematic structure of the types. This is modelled using Felix type classes.

In this section we display a subset of the definitions from the library. The real code also defines some other classes and also a rich set of alternate names for operators utilising the presence of LaTeX symbols: this allows for pleasant typesetting but usually doesn't provide essential semantic operations.

# 31.1 Equality

We start with class Eq which models equality based on the notion it is an equivalent relation:

```
class Eq[t] {
    virtual fun == : t * t -> bool;
    virtual fun != (x:t,y:t):bool => not (x == y);

    axiom reflex(x:t): x == x;
    axiom sym(x:t, y:t): (x == y) == (y == x);
    axiom trans(x:t, y:t, z:t): x == y and y == z implies x == z;
}
```

By providing an instance with ==, inequality != is automatically provided by the defaulty definition. An instance can also provide the inequality, as this is

sometimes more efficient.

Conformance to the axioms in instances is required, these axioms define the required semantics.

# 31.2 Total Ordering

Now we can define a total order:

```
class Tord[t]{
  inherit Eq[t];
  virtual fum < : t * t -> bool;
  fun >(x:t,y:t):bool => y < x;
  fun <= (x:t,y:t):bool => not (y < x);
  fun >= (x:t,y:t):bool => not (x < y);

fun max(x:t,y:t):t=> if x < y then y else x endif;
  fun min(x:t,y:t):t => if x < y then x else y endif;

axiom trans(x:t, y:t, z:t): x < y and y < z implies x < z;
  axiom antisym(x:t, y:t): x < y or y < x or x == y;
  axiom reflex(x:t, y:t): x < y and y <= x implies x == y;
  axiom totality(x:t, y:t): x <= y or y <= x;
}</pre>
```

To have a total order, we first have to have equality, this is effected by use of the inherit statement.

Next we define the less than function as virtual, instances must define this. The other functions are provided automatically.

The semantics are specified by the axioms which define a total ordering: reflexivity, anti-symmetry, transitivity, and finally totallity.

# 31.3 Addition

Now we define addition in two steps. First we define approximate addition

```
class FloatAddgrp[t] {
  inherit Eq[t];
  virtual fun zero: unit -> t;
  virtual fun + : t * t -> t;
  virtual fun neg : t -> t;
  virtual fun prefix_plus : t -> t = "$1";
  virtual fun - (x:t,y:t):t => x + -y;
```

```
virtual proc += (px:&t,y:t) { px <- *px + y; }
virtual proc -= (px:&t,y:t) { px <- *px - y; }

reduce id (x:t): x+zero() => x;
reduce id (x:t): zero()+x => x;
reduce inv(x:t): x - x => zero();
reduce inv(x:t): - (-x) => x;
axiom sym (x:t,y:t): x+y == y+x;

fun add(x:t,y:t)=> x + y;
fun plus(x:t)=> +x;
fun sub(x:t,y:t)=> x - y;
proc pluseq(px:&t, y:t) { += (px,y); }
proc minuseq(px:&t, y:t) { -= (px,y); }
}
```

Most the functions here are virtual without defaults. For the procedures we provide either virtual defaulted definitions or just the definitions.

The key requirement here is simply that some number added to zero returns the original number, as does negating a number twice. We also require subtracting a number from itself yields zero.

Normally addition has stronger requirements such as associativity, but this class is designed to support floating point numbers, and floating addition is not associative.

However since integer addition is, we provide another class:

```
class Addgrp[t] {
  inherit FloatAddgrp[t];
  axiom assoc (x:t,y:t,z:t): (x + y) + z == x + (y + z);
  reduce inv(x:t,y:t): x + y - y => x;
}
```

for an additive group, which just throws in the associative law. The semantic axiom requires cancellation.

Although technically signed integers in Felix do not obey these semantics due to overflow, the real axiom required cannot be modelled in Felix. The true axiom for computer signed integers is that the axioms are obeyed locally, that is, in a compact set close to zero.

This axiom would say, for example, that there exists some d such that if |a| < d and |b| < d and |c| < d then

$$(a+b) + c = a + (b+c)$$

where the restriction is there to ensure there is no overflow. However constructive mathematics cannot model existentials, and instead must provide an actual formula for calculating d. In this case, given the range of the integers, we can actually do that, however in general, even if it can be done, it is all too hard to bother.

Instead we just rely on the programmer understanding that the laws only apply locally and using calculations which they believe will not overflow. In practive many calculations with integers do not overflow, however there are a few very nasty cases.

# Chapter 32

# More core types

# 32.1 Slices

A basic slice is just a compact subset of the integers.

# 32.1.1 Slice Definition

```
union slice[T] =
    | Slice_all
    | Slice_from of T
    | Slice_from_counted of T * T /* second arg is count */
    | Slice_to_incl of T
    | Slice_to_excl of T
    | Slice_range_incl of T * T
    | Slice_range_excl of T * T
    | Slice_one of T
;
```

The \_incl suffix implies the second argument is included, whilst the \_excl suffix implies it is excluded.

All slices have a lower bound, if the initial value is not specified, the slice starts at 0.

# 32.1.2 Syntax

We provide a special syntax for slices as illustrated.

```
var i7up = 7..;  // from 7 up
var i7to11 = 7..11;  // 7 upto 11 inclusive
var i7lt12 = 7..<12;  // 7..11
var iall = ..;  // from 0 up
var ito11 = ..11;  // 0..11
var ilt12 = ..<12;  // 0..11</pre>
```

The syntax with <99 was stolen from Apple's Swift language.

### 32.1.3 Iterators

The slice type has an iterator method which allows you to enumerate the slice from its lower bound in increasing order. The iterator returns an option type and can be implicitly used in a for loop. The following program:

```
var it = iterator$ 7..8;
for i in 0..3 do
  println$ i,it ();
```

outputs:

```
(0, Some 7)
(1, Some 8)
(2, None)
(3, None)
```

# 32.1.4 String slices

Slices can be used with strings to extract substrings.

```
var x = "Hello World";
println$ x.[2..4];
```

Before the slice is applied it is clipped to the string dimensions by a special translation. First, negative values are considered to be relative to one past the end of the string going backwards, so the value -1 for example is the last character in the string, and -2 is the second last character.

After translation by adding the string length to negative values, the resulting start and end locations are clipped to the range 0...<n where n is the string length: the lower bound is the maximum of the calculated value and 0, the upper bound, exclusive, is the minimum of the calculated value and the string length. If the lower bound is greater than or equal to the upper bound exclusive

the result is an empty string, otherwise the substring from the lower bound to the upper bound exclusive is returned.

This sounds complicated but it is what Python does. Note that the substring slicing operation cannot fail.

[TODO: slices can be applied to arrays as well but this is not yet implemented]

# 32.1.5 Generalised Slices

A generalised slice is an arbitrary sequence of integers built by adding slices together. They also support mapping of slices.

```
union gslice[T] =
    | GSlice of slice[T]
    | GSSList of list[gslice[T]]
    | GSIList of list[T]
    | GSIter of 1 -> opt[T]
    | GSMap of (T -> T) * gslice[T]
;
```

A generalised slice can be built from an ordinary slice using GSlice.

It can also be built from a list of integers using GSIList, or a list of generalised slices using GSSList.

When an iterator of a gslice is used, it simply iterates over the underlying slices in order. The resulting stream of integers need not be either compact or ascending, and values can be repeated.

The form GSIter is a high power generalisation which allows any iterator over integers to form a gslice, without calling the iterator yet. So for example using a GSSList of two GSIter forms, when iterated over, will use the first iterator until it runs out of values, then move on to the second one.

The GSMap provides a way to take any sequence of integers from a gslice an translate them using a function.

Generalised slices are not supported by any high level mathematical concept, they're just a grab bag of convenient tools for generating sequences of integers.

### 32.1.6 Slice addition

Slices and generalised slices can be added to return a generalised slice.

# 32.1.7 Generalised String slicing

Strings can be mapped by generalised slices:

```
var yank = "11/23/16";
var oz = yank.[(3..5)+(0..2)+(6..7)];
var nip = yank.[(6..7)+(2..2)+(0..4)];
println$ yank,oz,nip;
```

[TODO: negative indices don't appear to work in generalised slices]

# 32.2 String Type

# 32.2.1 Equality and total ordering

```
fun == (s:string, c:string): bool
fun < (s:string, c:string): bool
fun <= (s:string, c:string): bool
fun > (s:string, c:string): bool
fun >= (s:string, c:string): bool
```

# 32.2.2 Equality of string and char

```
fun == (s:string, c:char): bool
fun == (c:char, s:string): bool
fun != (s:string, c:char): bool
fun != (c:char, s:string): bool
```

# 32.2.3 Append to string object

```
proc += : &string * string
proc += : &string * +char
proc += : &string * char
```

# 32.2.4 Length of string

```
fun len: string -> size
```

# 32.2.5 String concatenation

```
fun + : string * string -> string
fun + : string * carray[char] -> string
fun + : string * char -> string
fun + : char * string -> string
fun + ( x:string,  y: int):string
```

# 32.2.6 Repetition of string or char

```
fun * : string * int -> string
fun * : char * int -> string
```

# 32.2.7 Application of string to string or int is concatenation

```
fun apply (x:string, y:string):string
fun apply (x:string, y:int):string
```

# 32.2.8 Construct a char from first byte of a string

Returns nul char (code 0) if the string is empty.

```
ctor char (x:string)
```

# 32.2.9 Constructors for string

```
ctor string (c:char)
ctor string: +char
ctor string: +char * !ints
fun utf8: int -> string
```

# 32.2.10 Substrings

```
fun subscript: string * !ints -> char
fun copyfrom: string * !ints -> string
fun copyto: string * !ints -> string
fun substring: string * !ints * !ints -> string
fun subscript (x:string, gs:gslice[int]):string
proc store: &string * !ints * char
```

# 32.2.11 Map a string char by char

```
fun map (f:char->char) (var x:string): string = {
```

# 32.2.12 STL string functions

These come in two flavours: the standard C++ operations which return stl\_npos on failure, and a more Felix like variant which uses an @option type.

```
const stl_npos: size
fun stl_find: string * string -> size
fun stl_find: string * string * size -> size
fun stl_find: string * +char -> size
fun stl_find: string * +char * size -> size
fun stl_find: string * char -> size
fun stl_find: string * char * size -> size
fun find (s:string, e:string) : opt[size]
fun find (s:string, e:string, i:size) : opt[size]
fun find (s:string, e:+char) : opt[size]
fun find (s:string, e:+char, i:size) : opt[size]
fun find (s:string, e:char) : opt[size]
fun find (s:string, e:char, i:size) : opt[size]
fun stl_rfind: string * string -> size
fun stl_rfind: string * string * size -> size
fun stl_rfind: string * +char-> size
fun stl_rfind: string * +char * size
fun stl_rfind: string * char -> size
fun stl_rfind: string * char * size -> size
fun rfind (s:string, e:string) : opt[size]
fun rfind (s:string, e:string, i:size) : opt[size]
fun rfind (s:string, e:+char) : opt[size]
fun rfind (s:string, e:+char, i:size) : opt[size]
fun rfind (s:string, e:char) : opt[size]
fun rfind (s:string, e:char, i:size) : opt[size]
fun stl_find_first_of: string * string -> size
fun stl_find_first_of: string * string * size -> size
fun stl_find_first_of: string * +char -> size
fun stl_find_first_of: string * +char * size -> size
fun stl_find_first_of: string * char -> size
fun stl_find_first_of: string * char * size -> size
```

```
fun find_first_of (s:string, e:string) : opt[size]
fun find_first_of (s:string, e:string, i:size) : opt[size]
fun find_first_of (s:string, e:+char) : opt[size]
fun find_first_of (s:string, e:+char, i:size) : opt[size]
fun find_first_of (s:string, e:char) : opt[size]
fun find_first_of (s:string, e:char, i:size) : opt[size]
fun stl_find_first_not_of: string * string -> size
fun stl_find_first_not_of: string * string * size -> size
fun stl_find_first_not_of: string * +char -> size
fun stl_find_first_not_of: string * +char * size -> size
fun stl_find_first_not_of: string * char -> size
fun stl_find_first_not_of: string * char * size -> size
fun find_first_not_of (s:string, e:string) : opt[size]
fun find_first_not_of (s:string, e:string, i:size) : opt[size]
fun find_first_not_of (s:string, e:+char) : opt[size]
fun find_first_not_of (s:string, e:+char, i:size) : opt[size]
fun find_first_not_of (s:string, e:char) : opt[size]
fun find_first_not_of (s:string, e:char, i:size) : opt[size]
fun stl_find_last_of: string * string -> size
fun stl_find_last_of: string * string * size -> size
fun stl_find_last_of: string * +char -> size
fun stl_find_last_of: string * +char * size -> size
fun stl_find_last_of: string * char -> size
fun stl_find_last_of: string * char * size -> size
fun find_last_of (s:string, e:string) : opt[size]
fun find_last_of (s:string, e:string, i:size) : opt[size]
fun find_last_of (s:string, e:+char) : opt[size]
fun find_last_of (s:string, e:+char, i:size) : opt[size]
fun find_last_of (s:string, e:char) : opt[size]
fun find_last_of (s:string, e:char, i:size) : opt[size]
fun stl_find_last_not_of: string * string -> size
fun stl_find_last_not_of: string * string * size -> size
fun stl_find_last_not_of: string * +char -> size
fun stl_find_last_not_of: string * +char * size -> size
fun stl_find_last_not_of: string * char -> size
fun stl_find_last_not_of: string * char * size -> size
fun find_last_not_of (s:string, e:string) : opt[size]
fun find_last_not_of (s:string, e:string, i:size) : opt[size]
fun find_last_not_of (s:string, e:+char) : opt[size]
```

```
fun find_last_not_of (s:string, e:+char, i:size) : opt[size]
fun find_last_not_of (s:string, e:char) : opt[size]
fun find_last_not_of (s:string, e:char, i:size) : opt[size]
```

#### 32.2.13 Construe string as set of char

```
instance Set[string,char] {
  fun \in (c:char, s:string) => stl_find (s,c) != stl_npos;
}
```

#### 32.2.14 Construe string as stream of char

```
instance Iterable[string, char] {
   gen iterator(var x:string) () = {
    for var i in 0 upto x.len.int - 1 do yield Some (x.[i]); done
   return None[char];
   }
}
inherit Streamable[string,char];
```

#### 32.2.15 Test if a string has given prefix or suffix

```
fun prefix(arg:string,key:string)=
fun suffix (arg:string,key:string)
fun startswith (x:string) (e:string) : bool

// as above: slices are faster
fun endswith (x:string) (e:string) : bool

fun startswith (x:string) (e:char) : bool
fun endswith (x:string) (e:char) : bool
```

#### 32.2.16 h2 Trim off specified prefix or suffix or both

```
fun ltrim (x:string) (e:string) : string
fun rtrim (x:string) (e:string) : string
fun trim (x:string) (e:string) : string
```

# 32.2.17 Strip characters from left, right, or both end of a string.

```
fun lstrip (x:string, e:string) : string
fun rstrip (x:string, e:string) : string
fun strip (x:string, e:string) : string
fun lstrip (x:string) : string
fun rstrip (x:string) : string
fun strip (x:string) : string
```

#### 32.2.18 Justify string contents

```
fun ljust(x:string, width:int) : string
fun rjust(x:string, width:int) : string
```

#### 32.3 Regexps

Syntax

Combinators

Google Re2 Binding

Introspection

# Serialisation

Felix allows certain data structures to be serialised into a string, so that the data structure can be recovered from the string.

#### 34.1 Operation

#### 34.1.1 encode\_varray

This function accepts the address of a serialisable object, and returns a string containing the serialised contents of the object.

#### 34.1.2 deccode\_varray

This accepts a string previously serialised by encode\_varray, rebuilds a copy of the data structure it encoded, and returns the address of the object.

#### 34.1.3 Usage

The data structure to be serialised must reside entirely on the heap and satisfy other requirements. A pointer to the object is cast to type address. When deserialising, the address returned should be cast to a pointer to the same data type used in serialisation.

```
include "std/felix/serialise";
var px: &list[int] = (1,2,3,4).list.new;
var serialised_x : string = px.addresss.Serialise::encode_varray;
var px_copy = serialised_x.Serialise::decode_varray.&list[int];
println$ *px == *px_copy;
```

#### 34.1.4 Process Restrictions

Serialisation functions depend on the machine address of the Felix run time type information (RTTI) objects which also control garbage collection.

Therefore serialisation is only guaranteed to work within a single process. On some architectures with some linkage strategies it may be possible to save the string to disk, and reloaded it in a different process running the same program. In particular the core requirement must be met by the operating system: to load the process at the same virtual address. If you wish to try this, it is best to statically link your program since different orders of dynamic linkage may result in different addresses for shared library objects (DLLs).

If serialisation works across different processes, it should also work if the serialised data is transmitted to an remote machine running the same architecture, same operating system, and binary identical Felix program.

#### 34.1.5 Data Restrictions

All data to be serialised must either be a C data type bound to Felix with supporting serialisation and descrialisation functions provided in the binding, or, any Felix combination of such primitive data types effected by a tuple, array, struct, union, sum or unit sum type, or pointer type. Recursive data types are supported. Circular data structures do not present a problem.

Most Felix primitive types provided in the library are supported, except for data types derived from Judy arrays.

You cannot serialise function or procedure closures because these refer to the global thread frame object, which is the root for most of the rest of the program data: serialisation would then attempt to capture the whole program. Even if the thread frame were serialisable, deserialisation would create a copy of it which is not supported.

Pointers to C functions, however, are serialisable since they're just addresses. Pointers to an foreign objects remain invariant. Most simple data structures are serialised by simply using a blit operation, namely memcpy.

C++ strings are serialisable. Since serialisation produces a C++ string, data structures containing serialised data are also serialisable.

#### 34.1.6 How it works

Serialisation works by copying serialising primitives with user supplied serialisation functions. These currently must be written in C++. Non-primitives are serialised by copying the object and finding subobjects to also serialised using the same pointer location data the garbage collector uses from the types RTTI object.

Serialised data is tagged with the address of the RTTI object so that the deserialisation function and location of interior pointers can be found.

#### 34.1.7 Future Directions

A more portable method of locating RTTI than using the machine address would remove many of the restrictions, in particular the restriction that the exact same program must be used for deserialisation as for serialisation, as well as the restriction that deserialisation should be in the same processes.

In fact the primary difficulty here is finding a unique universal representation of a data type. Were such a kind available a search could be used to map universal type tokens to the RTTI address.

More portable representations of the data may also remove the restriction that the same processor must be run the processes with the same underlying binary ABI (so that, for example, an int has the same binary representation on both architectures).

## Fibres and Schannels

#### Library Package

Fibres (or f-threads) are coroutines which exchange control with other fibres by reading and writing synchronous channels (schannels).

#### 35.1 spawn\_fthread procedure

The spawn\_fthread procedure spawns a new fibre (fthread). The procedure being spawned must have type unit->void also written 1->0.

The new fibre begins execution immediately and continues until suspended by either an unmatched I/O request on an schannel, or a read operation matched by a write.

Fibres are similar to threads, however control exchange is synchronous, not pre-emptive. A communicating set of fibres runs in a pre-emptive single thread.

Fibres can also be suspended waiting for a synchronous events such as socket  ${\rm I/O}$  or a timer.

## 35.2 Schannel types

There is only one kind of schannel, however the type system provides three views:

ischannel[T] an input schannel for reading T values,

oschannel[T] an output put schannel for writing T values,

ioschannel[T] an input/output schannel for either reading or writing T values.

Each of these types is also a constructor for the corresponding type of schannel.

#### 35.3 mk\_ioschannel\_pair[T] function

This function creates a single schannel, returning a read end and a write end in a tuple:

```
var ins, outs = mk_ioschannel_pair[int]();
```

#### 35.4 ioschannel[T] constructor

A bidirectional channel can also be created:

```
var ios = ioschannel[int]();
```

#### 35.5 read generator and write procedure

The read and write operators on schannels are used for communication between fibres.

- When a read matches a write, the reader continues with the data, and the writer is placed by on the scheduler active list. If there is more than one writer, the writer chosen is unspecified.
- If a read has no matching write, the reading fibre joins a set of fibres waiting on the schannel for a write, and the scheduler begins execution of one fibre from its active list.
- A write will transfer control and data to one reader. The reader chosen is unspecified. The writer is then placed on the scheduler active list.
- If a write has no matching read, the writing fibres joins a set of fibres waiting for a read, and the scheduler begins execution of one fibre from its active list.

Thus, an schannel is, in effect, a localised scheduler, queueing either writers or readers until matching operations are performed.

## 35.6 Cross thread I/O

Schannel read and write operations are not thread safe. Schannels should usually not be shared between pthreads to ensure I/O cannot be performed between pthreads using schannel I/O. Pthreads can use pchannels to communicate instead. On the other hand fibres must not use pchannels to communicate within the same pthread since this would be an automatic deadlock.

#### 35.7 broadcast procedure

This procedure writes to all fibres waiting on an schannel, then returns. Unlike write it does not block.

broadcast can be used directly from C++. It is intended to permit custom C++ driver code to communicate with a suspended Felix system. The driver code must ensure the data sent with a broadcast remains live whilst target fthreads are processing it.

Felix broadcast is invoked by the member function external\_multi\_write of the object of type async\_sched with type shown below, passing the schannel to broadcast over, and a pointer to the data to broadcast.

```
void async_sched::external_multi_swrite(
    ::flx::rtl::schannel_t *chan,
    void *data
)
```

Felix can be embedded in C++ code, in particular it can run in framework loop idle function as a callback. It runs until there are no active fibres. The external\_multi\_write is used to schedule more active fibres so the next resumption via the idle loop callback has work to do.

#### 35.7.1 Fibre States

Fibres may be in one of five states:

Running Only one fibre can be running at a time in a given pthread.

Waiting to Run A fibre is active if it is on the scheduler active list but not running.

Waiting on Schannel A fibre may be waiting for either input or to output.

Waiting for Asynchrons Event Fibres may also wait for asynchronous events.

A fibre which is running or waiting to run is said to be *active*. A fibre which is waiting on an schannel or asynchronous event is said to be suspended.

#### 35.7.2 Schannel States

An schannel may be in one of three states:

Empty The schannel has no fibres on its wait list.

Waiting for a reader The fibre has one or more writers on its wait list.

Waiting for a writer The fibre has one or more readers on its wait list.

#### 35.7.3 Abbreviated Type names

Felix provides short hand notation for input and output schannels as follows:

alias	full name	semantics
% <t< th=""><th>ischannel[T]</th><th>input schannel</th></t<>	ischannel[T]	input schannel
%>T	oschannel[T]	output schannel
%<>T	ioschannel[T]	bidirectional schannel

#### 35.7.4 Deadlock, Livelock, and Suicide

Both fibres and schannels are garbage collected. Thus they either be reachable or unreachable.

If a fibre is active it is a root, and is always reachable. If a fibre is waiting for an asynchronous event it is also always reachable.

An schannel may be also be reachable if it is stored in a variable in the global thread frame. This is the global data object which is shared between all preemptive threads.

Alternatively it may be reachable from a procedure reachable from an active fibre.

A fibre may terminate by returning. In this case it is unreachable and will be collected. This is known as normal termination.

A fibre which can only be reached from an unreachable schannel will be garbage collected. This is known as suicide and ensures fibres cannot deadlock: deadlocked fibres suicide and so aren't deadlocked because they no longer exist. For example consider:

```
begin
  var i1,o1 = ml_ioschannel_pair[int]();
  var i2,o2 = ml_ioschannel_pair[int]();
  spawn_fthread { write (o1,1); println$ read i2; };
  spawn_fthread { write (o2,2); println$ read i1; };
end
```

The first fthread suspends on channel 1, waiting to write, the second fthread suspends on channel 2, waiting to write. The fthreads are suspended and dead-locked. However the main fthread is active and now runs, and the begin/end block returns so its data frame, containg the two schannels, is no longer reachable. This means the two suspended fthreads are not reachable either. So the two fibres have suicided, they are no longer deadlocked because they no longer exist.

Suicide is not necessarily an error, it is, in fact, a common way to terminate fthreads. The problem above terminates correctly.

Now, consider the program above without the begin/end block. In this case, the fthreads will not be collected because they're reachable from global store (the so-called thread frame). So that program will not terminate, and is said to be *live-locked*.

It is a live-lock because the main fthread can read the channels and thus the suspended fibres and could unsuspend them with suitable I/O operations.

It is the responsibility of the holder of an schannel to ensure other holders I/O requests are satisfied. If a fibre does not intended to perform I/O on an schannel it should forget it. In the example the main thread forgets the schannels by forgetting the begin/end blocks data frame when it returns.

#### 35.7.5 Restrictions on use

Fibres can only be spawned with a basic **spawn\_fthread** by top level procedures or procedural desendants, or, from functions or generator which are inlined (eliminating the function).

This is because procedures spawned with a basic **spawn\_fthread** with a service call which requires the machine stack be empty, since the service calls are effected by *returning* control to the scheduler.

Similarly, the same restrictions apply to schannel I/O.

However these restrictions can be partly overcome with nested schedulers.

#### 35.8 Nested Scheduling

A nested scheduler of type fibre\_scheduler may be created a constructor accepting a unit argument. It is must be deleted when no longer required by the procedure delete\_fibre\_scheduler.

Fibres may be added to the scheduler using the advanced <code>spawn\_fthread</code> procedure, this procedure takes a <code>fibre\_scheduler</code> argument and returns a closure accepting procedure of type 1->0. Fibres starting with the procedure are added to the nested scheduler list, but are not yet run.

The run procedure takes a populated scheduler and runs the fibres on it.

Fibres on nested schedulers may communicate with each other using schannel operations.

The run procedure will not return until all the fibres on the nominated scheduler have completed. The fibres may not do asynchronous operations, or make service calls other than schannel I/O operations, however the scheduler handles schannel I/O properly.

The result of attempting to communicate with fibres on another scheduler such as the master scheduler are undefined.

```
fun foo () =
{
   var chin, chout = mk_ioschannel_pair[int]();
   var sched = fibre_scheduler();
   var res = 1;
   spawn_fthread sched { write (chout, 42); };
   spawn_fthread sched { res = read chin; };
   run sched;
   delete_fibre_scheduler sched;
   return res;
}
println$ foo();
```

#### 35.9 Synchronous pipelines

#### Library Reference lah.

A synchronous pipeline is a special case of fibres and channels in which data flow from one fibre to a series of others in sequence using a one schannel for each adjacent pair to connect them.

Special constructors are provided to make pipelines which ensure that only the fibres in the pipeline know the connecting schannels.

This ensures that the pipeline collapses when there is no more data to processes.

The starting point of a pipeline is known as a source, the ending point a sink, and the pieces in the middle are called transducers.

A transducer is a control inverted function. This means that instead of being called with data, it reads it, and instead of returning with a result it writes it.

Unlike functions, which form client/server relations, tranduces are all peers.

#### 35.10 Buffers

Synchronous I/O is unbuffered. This means the sequencing of reads and writes is critical. If a fibre writes channel A then B, and another reads B then A, the system is deadlocked and the fibres may suicide.

In order to read a set of inputs in an arbitrary order, buffers can be added to each input.

A buffer is simply an fibre running an infinite loop which reads from one channel and writes on another:

```
var Ain, Aout = mk_ioschannel_pair[int]();
var Bin, Bout = mk_ioschannel_pair[int]();
var Cin, Cout = mk_ioschannel_pair[int]();
var Din, Dout = mk_ioschannel_pair[int]();

proc buffer (r:%<int, w:%>int) () {
   while true perform write (w,read r);
}

spawn_fthread { write (Aout, 1); write (Bout,2); };
spawn_fthread { var d = read Din; c = read Cin; println$ c,d; };
spawn_fthread$ buffer (Ain, Cout);
spawn_fthread$ buffer (Bin, Dout);
```

Now, as you can see, the reader procedure reads the data from A in the reverse order to that in which it is written, but this works because of the buffers. Note that the first fthread can now proceed as soon as the buffer has read its output, before the second fthread gets it. In fact the second fthread gets what it wrote first.

Buffers are mandatory for a feedback.

# Circuits

Felix provides a high level general purpose *chips and wires* sublanguage which is designed to modularise use and deployment of safer iteracting fibre based processing systems.

#### 36.1 Chip definition

A chip is designated like:

```
open syntax chips;

chip filereader (filename:string)
  connector file
    pin outch: %>char
{
    var data = load filename;
    for ch in data do
        write (file.outch,ch);
    done
}
```

A chip is an ordinary procedure, which may have parameters such as filename in the example. The parser creates another argument for you: designated the connector, and named file in the example, has the type of a record whose fields are the connectors pins, in this case there is only one pin, outch, which has type %>char which is an abbreviation for oschannel[char] and is therefore a synchronous output channel of char.

Here is an output device which emits the characters of a string instead:

```
chip stringreader (s:string)
  connector file
    pin outch: %>char
{
  for ch in s do
    write (file.outch,ch);
  done
}
```

Such output devices are called *sources* or *suppliers*.

Now, we want to parse the data stream into words, so we will make a transducer chip.

```
chip parser
  connector pins
    pin inchar: %<char
    pin outword: %>string
    var ch = read inchar;
  while true do
    while isspace ch perform
      ch = read inchar
    var s = ""+ch;
    while not (isspace ch) do
      s += ch;
      ch = read inchar;
    done
    write (outword,s);
  done
}
```

Notice that if the input is exhausted in the middle of a word, the final word is not emitted. This transducer will process and character streams sent to it and then block waiting for data that is not coming. This is the correct way to design circuits. The absence is a explicit termination is the mark of a good design. Circuits should simply collapse when there is no work to do.

To complete the job, we will provide a simple sink or consumer chip:

```
chip printer
  connector pins
  pin inword: %<string
{</pre>
```

```
while true do
   var s = read inword;
   println s;
   end
}
```

Now, we have all the devices we need so lets wire them together:

```
device src = string_reader "Hello World\n";
circuit
  connect src.outch,parser.inchar
  connect parser.outch, printer.inword
endcircuit
```

#### Thats it!

[document wire clause and making a chip out of chips]

# **Asychronous Events**

Felix uses a synchronous I/O with fibres to provide access to a synchronous events. Currently two kinds of events are supported: a larm clock timeout events and socket I/O buffer and connection events.

Waiting for an event blocks the current fibre, but it does not block other fibres in the same pthread.

#### 37.1 Event Service demux

The event delivery service is called demux and runs in a separate premptive thread. It interfaces with the OS native event delivery services as shown in Table 37.1 Event Delivery Service Providers.

Felix automatically selects the best available service.

#### 37.2 Alarm Clock

The alarm clock service allows a fibre to block for a selected amout of time. A clock must be constructed first.

Table 37.1: Event Delivery Service Providers

Service	Availability	Notes
select	all	fallback
poll	Posix	better than select
epoll	Linux	better than poll
kqueue	BSD Unix, OSX	better than poll
Solaris iocompletion ports	Solaris	better than select
Windows iocompletion ports	Win32	better than select

Operation	Used By	Provider class			
	Platform Specific				
connect	Client	Faio_posix			
accept	Server	Faio_posix			
async_rw	Client and Server	Faio_posix			
async_read	Client and Server	Faio_posix			
async_write	Client and Server	Faio_posix			
Connect	Client	Faio_win32			
Accept	Server	Faio_win32			
WSARecv	Client and Server	Faio_win32			
WSASend	Client and Server	Faio_win32			
TransmitFile	Client and Server	Faio_win32			
Platform Independent					
connect	Client	Socket			
accept	Server	Socket			
read	Server	Socket			
write	Server	Socket			

Table 37.2: Asynchronous Socket Operations

```
fun mk_alarm_clock: 1 -> alarm_clock;

// delay in seconds
proc sleep(clock: alarm_clock, delta: double);
```

For example to delay 5 seconds use:

```
var clock = mk_alarm_clock();
sleep (clock, 5.0);
```

Note again this only causes the current active fibre to sleep. Clocks are reusable and may delays can be queued by any number of fibres within the same pthread.

#### 37.3 Sockets

Socket operations are covered more completely in ?? ??. Socket operations are synchronous unless shown in Table 37.2 Asynchronous Socket Operations.

## 37.4 How Async I/O works

Asynchronous I/O is performed as follows. First an fthread

Unfortunately shutdown and close requests are synchronous due to a design fault in sockets and TCP/IP protocol. Although Posix supports asynchronous shutdown, this may cause underlying socket buffers to be prematurely flushed. The only way to asychronously shutdown a socket would be to perform a synchronous shutdown in a dedicated pthread, defeating the purpose of using fibres.

# Preemptive Threading

Library Package Felix provides pre-emptive threading based on OS native threads called *pthreads*.

Felix pthreads are detached, there is no support for OS joinable threads. The primary synchronisation primitive is the *pchannel*.

#### 38.1 spawn\_pthread procedure

The spawn\_pthread procedure spawns a new pthread. The procedure being spawned must have type unit->void also written 1->0.

## 38.2 Pchannel types

There is only one kind of pchannel, however the type system provides three views:

ipchannel[T] an input pchannel for reading T values,

**opchannel**[T ] an outputput pchannel for writing T values,

 ${f iopchannel}[{f T}\ ]$  an input/output pchannel for either reading or writing T values.

Each of these types is also a constructor for the corresponding type of pchannel.

## 38.3 mk\_iopchannel\_pair[T] function

This function creates a single pchannel, returning a read end and a write end in a tuple:

```
var inp, outp = mk_iopchannel_pair[int]();
```

#### 38.4 iopchannel[T] constructor

A bidirectional channel can also be created:

```
var ios = iopchannel[int]();
```

#### 38.5 read generator and write procedure

The read and write operators on pchannels are used for communication between pthreads.

Pchannels are technically *monitors*. There is no buffering. Unmatched reads block until a matching write occurs on the same underlying pchannel. Unmatched writes block until a matching read occurs. Neither reader nor writer may proceed until data is exchanged.

Unlike fibres and schannels, pthread can be deadlock by out of order I/O.

#### 38.6 concurrently procedure

```
open class ForkJoin {
   proc concurrently_by_iterator (var it:1 -> opt[1->0])
   proc concurrently[T with Streamable[T,1->0]] (d:T)
}
```

Felix provides the procedure concurrently\_by\_iterator which uses an iterator returning procedures of type 1->0 to launch pthreads.

A more convenient procedure, concurrently, accepts any data structure with an iterator.

concurrently automatically joins the launched threads.

```
// using an array
concurrently (
    { println$ "Thread1"; },
    { println$ "Thread2"; },
    { println$ "Thread3"; }
);
```

#### 38.7 Atomics

Felix atomics utilise the C++11 standard library atomics. Atomic variables are not managed by the GC.

```
open class Atomic
{
   type atomic[T];
   ctor[T] atomic[T]: T;
   proc delete[T] : atomic[T;

   gen load[T] : atomic[T];
   proc store[T] : atomic[T];
   proc store[T] (a:atomic[T]) (v:T);

// integer types only
   proc pre_incr[T] : &atomic[T];
   proc pre_decr[T] : &atomic[T];
}
```

#### 38.8 Mutual Exclusion Lock

```
open class Mutex
{
   type mutex;
   ctor mutex: unit;
   proc lock: mutex;
   proc unlock: mutex;
   proc destroy: mutex;
}
```

Felix provides a garbage collector aware mutual exclusion lock mutex. It is a timed mutex which periodically checks for a GC world stop request.

Condition variables are not garbage collected.

#### 38.9 Condition Variables

Felix provides a GC aware condition variable based on C++11 condition variables. It uses a timed variant to periodically check for a GC world stop request.

```
open class Condition_Variable
{
   type condition_variable;
   ctor condition_variable: unit;
   proc destroy: condition_variable;

   //f lock/unlock associated mutex
   proc lock: condition_variable;
   proc unlock: condition_variable;

   proc wait: condition_variable;
   proc signal: condition_variable;

   proc broadcast: condition_variable;

   gen timedwait: condition_variable * double -> int;
}
```

Note that unlike Posix condition variables, the associated mutex is built-in to the condition variable.

#### 38.10 Bound Queue

Felix provides thread safe, GC aware, resizeble bound queue. The queue itself is garbage collected. The queue stores pointers to heap allocated copies of the queued objects, which are scanned by the GC.

```
open class TS_Bound_Queue
{
   ctor[T] ts_bound_queue_t[T]: !ints;
   proc enqueue[T] (Q:ts_bound_queue_t[T]) (elt:T);
   gen dequeue[T] (Q:ts_bound_queue_t[T]): T;
   proc wait[T]: ts_bound_queue_t[T]; // until Q empty
   proc resize[T]: ts_bound_queue_t[T] * !ints;
}
```

The constructor creates a queue with the specified maximum capacity or bound.

The enqueue operation may wait until there is space in the queue before depositing its payload and returning.

The dequeue operation may wait whilst the queue is empty until it can acquire a payload before returning.

The wait procedure blocks until the queue is empty.

The resize procedure changes the queue bound.

Note: When threads are enqueing and dequeing from the queue, there is no defined method for closing down the use of the queue. Neither enqueue nor dequeue can fail, nor can they be cancelled.

#### 38.11 Thread Pool

```
class ThreadPool
{
   typedef job_t = 1 -> 0;
   fun get_nthreads () => nthreads;

proc barrier();
proc start ();
proc start (n:int);
proc queue_job (job:job_t);
proc stop ();
proc post_barrier();
proc notify (chan:opchannel[int]) ();
proc join ();

proc pfor_segment (first:int, last:int) (lbody: int * int -> 1 -> 0)
   inline proc forloop (lbody: int -> 0) (first:int, last:int) ()
}
```

Felix provides a global thread pool which consists of a thread safe job queue and a set of running Felix pthreads. The number of threads is determined from the architecture if possible, otherwise set to a reasonable value such as 8.

The job queue is bound to 1024 jobs.

The queue\_job procedure accepts a unit procedure of type 1->0 and adds it to the job queue. It may block whilst the job queue is full. Queing a job automatically starts up the thread pool.

Threads in the pool dequeue jobs from the queue and run them. When finished, a thread fetches another job if there is one, and runs it. If there are no jobs, the thread waits until a job is available.

The start procedure can be used to manually start the thread pool.

The post\_barrier procedure posts n barrier jobs, where n is the number of threads in the pool. A barrier job causes a thread to stop acquiring jobs and wait until all threads are waiting on a barrier.

The join procedure posts n barriers, where n is the number of threads in the pool. This causes each thread to suspend on a barrier until all threads have suspended. Then all threads may continue processing jobs.

The stop procedure attempts to stop the pool by posting a n special ThreadStop jobs, where n is the number of threads in the pool. A ThreadStop job causes the thread executing it to suicide.

#### 38.11.1 Restrictions

Jobs submitted to the thread pool should be either be entirely independent or transiently coupled. In general, jobs should not communicate with each other or other threads using condition variables or pchannels. It is counter productive for jobs to spawn new threads although it is not disallowed, because the thread pool is designed to saturate multi-core CPUs (that is, keep all the cores busy).

Transient coupling, however, is permitted. For example if jobs are used to calculate some value which is then added to a single variable, a mutex can be used to serialise access to the variable, because the lock will only be held transiently.

#### 38.12 Parallel For Loop

#### 38.12.1 Syntax

```
loop_stmt :=
    "pfor" sname "in" sexpr "upto" sexpr block
;
```

#### 38.12.2 Operation

The parallel for loop constructs n subjobs which are submitted to the thread pool, where n is approximately the number of threads in the thread pool. Each job runs a loop over a subrange of the loop range so that all the indices in the range are covered.

The thread pool is automatically started if it wasn't running. Note: it is not automatically stopped. You must manually call ThreadPool::stop() if you use a pfor statement otherwise Felix will not terminate.

#### 38.12.3 Example

The pfor loop was specifically designed for matrix multiplication. The following code multiplies a by  $b^T$  where the latter is the transpose of b, and puts the result in r. The matrices are square of dimension N. The inner product is captured in a function and returns a single value.

```
pfor i in 0 upto (N-1) do for (\text{var } j=0; \ j< N; \ ++j;) perform &r . i . j <- inner_product (&a.i, &b.j); done
```

#### 38.12.4 Restrictions

It is essential the body of the pfor loop behaves independently for each value of the control index, or uses lock free coupling such as adding to a shared atomic variable.

pfor loops must not be nested. It would be counter productive, but it will also most likely cause a deadlock.

# Part VII Platform Support

# Platform Modelling

The Felix language processor is a translator which outputs C++. Because of this, the translator can produce code intended to run on one platform on an unrelated platform. For example, Windows native programs can be generated on Linux, although there may not be a suitable compiler and library available to produce a binary, or an emulator to run it.

So for platform related libraries, Felix provides three kind of code:

- platform specific code
- platform independent code
- platform adaptive code

Platform specific code consists of functions which are specific to the platform.

Platform independent code uses a type class to represent a common subset of functions with the same interface. The type parameter is used to represent the platform variable.

Class instances then bind the virtuals of the class for each supported platform.

By convention the class name ends in \_class.

Platform adaptive code is the simplest to use, and simply provides the platform dependent code for the host platform. The host is specified by macro file which is included with parse units, and conditional compilation is used for the selection.

Note that in addition to the above Felix level modelling, similar modelling methods can be used in C++ libraries to which Felix binds. Therefore a call to a function like Shell::system() can be mapped in Felix in a platform independent way to the underlying call in the ISO C library.

The client may write platform independent code, accepting the restrictions of common functionality, but the code must reside in a class with OS control parameter which can be passed on to the platform mapping virtual functions.

Note that Felix with the C++ backend is a cross-cross compiler, not just a cross compiler! There do exist C++ compilers that run on Linux but produce Windows binaries. Felix front end such a compiler, and produce Windows C++ for it.

# Processes

Blah.

# **Programs**

#### 41.1 Basic Program interface

```
class System
 const argc:int;
 fun argv:int -> string;
 fun argv_dflt (x:int) (y:string) : string;
 fun args () : list[string];
 gen system (cmd:string) : int => Shell::system(cmd);
 gen exit: int -> any;
 gen abort: 1 -> any;
 const ptf:ptf_t;
 //f pexit examines the return code from a system call.
 //£ If the code is 0 it exists with 0.
 //£ On Windows:
 //£ if the code is -1, it exits with errno.
 //£ otherwise code 3
 //£ On Unix:
 //f if the code is non-zero then
 //f if the callout aborted, return its abort code.
 //f if the callout died due to a signal, exit with code 2
 //f otherwise exit with code 3
 //f In both these cases a non-zero return causes a message
 //f to be printed on stderr.
 proc pexit(e:int)
 gen get_stdout(x:string) : int * string => Shell::get_stdout x;
```

```
}
```

#### 41.2 Environment Variables

```
class Env_class[os]
{
    //f Separator for filename lists
    virtual fun pathsep: 1 -> string;

    //f Get the value of a given variable.
    //f Returns empty string if the variable doesn't exist.
    fun getenv:string -> string =
        "::flx::rtl::strutil::atostr(std::getenv($1.c_str()))"
        requires package "flx_strutil", Cxx_headers::cstdlib;

    //f Get the value of a given variable.
    //f Returns specified default if the variable doesn't exist.
    fun getenv(name:string,dflt:string):string=>let result = getenv(name) in
        if String::len result != Ouz then result else dflt endif
    ;

    fun getenvlist (name:string) : list[string] =>
        split (getenv name, #pathsep)
    ;
}
```

#### 41.3 Shell callouts

```
// system() function
//£ System command is ISO C and C++ standard.
gen raw_system: string -> int = "::std::system($1.c_str())"
 requires Cxx_headers::cstdlib
//f basic command with line quoting.
gen basic_system (cmd: string) :int =>
  cmd.quote_line_for_system.raw_system
// string argument
// responds to FLX_SHELL_ECHO environment variable
gen system (cmd:string) = {
  if Env::getenv "FLX_SHELL_ECHO" != "" do
    eprintln$ "[system] " + cmd;
 done
 return basic_system cmd;
// list of string argument
gen system (args:list[string]) : int =>
 args.quote_args.system
gen system[T with Iterable[T,string]] (args:T) : int =
 var lst = Empty[string];
 for arg in args do
   lst = lst + arg;
 done
 return system 1st;
virtual fun quote_line_for_popen: string -> string;
//f get_stdout is a synchronous version of popen_in/pclose pair.
virtual gen raw_get_stdout : string -> int * string;
gen basic_get_stdout (cmd: string) : int * string =>
  cmd.quote_line_for_popen.raw_get_stdout
gen get_stdout (cmd:string) : int * string = {
  if Env::getenv "FLX_SHELL_ECHO" != "" do
```

```
eprintln$ "[get_stdout] " + cmd;
done
  return basic_get_stdout cmd;
}

// arbitrary Streamable argument
gen get_stdout (args:list[string]) : int * string =>
  args.quote_args.get_stdout
;

gen get_stdout[T with Iterable[T,string]] (args:T) : int * string;
}
```

## 41.4 Signals

File System

# Dynamic Linkage

- 43.1 Basic Library
- 43.2 Plugins

# Part VIII Data Structures

Chapter 44

**Iterators** 

## Chapter 45

## Lists

#### 45.1 Inductive lists

#### 45.1.1 Description

Lists are the core data structure for most functional programming languages. A list is an inductive data type: it is defined by a base term,  $\mathsf{Empty}[\mathsf{T}]$ , and an induction which says if x is a list of T, and v is a value of T, then  $\mathsf{Cons}(\mathsf{v},\mathsf{x})$  is a list.

The induction model of construction admits to a recursive model of destruction, for example:

```
fun str[T with Str[T]] (x:list[T]) : string =>
  match
  | Empty => "Empty"
  | Cons (head, tail) => head.str + ", " + str tail
  endmatch
;
```

In fact, Felix defines Snoc lists rather than Cons lists, using a Snoc(list,value) constructor based on a C++ implementation, instead of a Cons (value, list) constructor and then provides a translation with a user defined type constructor. The idea is to get the tail pointer first in the underlying data type, so that polymorphic visitors can be written without the offsets depending on the value type T.

```
open class List
{
  union list[T] = | Empty | Snoc of list[T] * T;
```

```
fun _match_ctor_Cons[T] : list[T] -> bool = "!!$1";
inline fun _ctor_arg_Cons[T]: list[T] -> T * list[T] =
    "flx::list::snoc2cons<?1>($1)"
    requires snoc2cons_h
;
inline fun Cons[T] (h:T, t:list[T]) => Snoc (t,h);
```

#### 45.1.2 Constructors

#### copy function

Make an entirely new copy of a list. Primarily a helper.

```
fun copy[T] (x:list[T]):list[T];
```

#### Copy and return last copy\_last

Yet another helper procedure.

```
proc copy_last[T] (inp:list[T], out:&list[T], last:&list[T]) {
  out <- rev inp;
  rev_last (out, last);
}</pre>
```

#### Named constructor for empty list

```
ctor[T] list[T] () => Empty[T];
```

#### Construct a singleton list

Does not work if the argument is an array or option iterator.

```
//f Make a list with one element.
//f NOTE: list (1,2) is a list of 2 ints.
//f To get a list of one pair use list[int*int] (1,2) instead!
ctor[[T] list[T] (x:T) => Snoc(Empty[T],x);
```

#### Construct a list from an array

```
//f Make a list from an array.
ctor[T,N] list[T] (x:array[T, N]) : list[T];
```

#### List comprehension.

Make a list from an option stream. Named variant.

```
//f List comprehension:
//f Make a list from a stream.
fun list_comprehension[T] (f: (1->opt[T])) = {
```

Constructor variant.

```
//£ List comprehension:
  //£ Make a list from a stream.
  ctor[T] list[T](f: (1->opt[T])) => list_comprehension f;
\end{miinted}
\subsection{Construe a list as an array value}
\begin{minted}
  //f Contrue a list as an array value
  instance[T] ArrayValue[list[T],T] {
    //£ Return umber of elements in a list.
   pure fun len (x:list[T]) = {
    //£ get n'th element
   pure fun unsafe_get: list[T] * size -> T =
    //£ Apply a procedure to each element of a list.
   proc iter (_f:T->void) (x:list[T]) {
    //£ Traditional left fold over list (tail rec).
    fun fold_left[U] (_f:U->T->U) (init:U) (x:list[T]):U =
    //£ Right fold over list (not tail rec!).
   fun fold_right[U] (_f:T->U->U) (x:list[T]) (init:U):U =
```

#### 45.1.3 Destructors

Test for empty list is\_empty

```
//f Test if a list is empty.
pure fun is_empty[T] : list[T] -> 2 =
```

Tail of a list tail

```
//£ Tail of a list, abort with match failure if list is empty.
pure fun tail[T] (x:list[T]) : list[T] = {
```

Head of a list head

```
//f Head of a list, abort with match failure if list is empty.
pure fun head[T] (x:list[T]) : T = {
```

#### 45.1.4 Maps

Reverse map a list rev\_map

Tail recursive.

```
//f map a list, return mapped list in reverse order (tail rec).
fun rev_map[T,U] (_f:T->U) (x:list[T]): list[U] = {
```

#### Map a list map

Tail recursive. Uses rev\_map and then inplace revseral. This is safe because we enforce linearity by abstraction.

```
//f map a list (tail-rec).
// tail rec due to in-place reversal of result.
fun map[T,U] (_f:T->U) (x:list[T]): list[U] =
```

Reverse a list rev.

Tail recursive.

```
//f reverse a list (tail rec).
pure fun rev[T] (x:list[T]):list[T]= {
```

#### Zip a pair of lists to a list of pairs zip2

Returns a list the length of the shortest argument.

```
//f Zip two lists into a list of pairs.
//f Zips to length of shortest list.
fun zip2[T1,T2] (l1: list[T1]) (l2: list[T2]) : list[T1 * T2] =
```

#### 45.1.5 Useful lists

A list of integers range.

From low to @high exclusive with given @step.

```
//f Generate an ordered list of ints between low and high with given step.
//f Low included, high not included.
fun range (low:int, high:int, step:int) =
```

#### Consecutive integers range

```
//f Range with step 1.
fun range (low:int, high:int) => range(low, high, 1);
```

Non-negative integers to limit range

num integers 0 to num-1.

```
//f Range from 0 to num (excluded).
fun range (num:int) => range(0, num, 1);
```

#### 45.1.6 Operators

Concatenate two lists join.

```
//f Concatenate two lists.
fun join[T] (x:list[T]) (y:list[T]):list[T] =

//f Concatenate two lists.
pure fun + [T] (x:list[T], y: list[T]):list[T] => join x y;
```

Cons an element onto a list.

```
//£ Prepend element to head of list.
pure fun + [T] (x:T, y:list[T]):list[T] => Snoc(y,x);
```

Append an element onto a list.

O(N) slow.

```
//f Append element to tail of list (slow!).
noinline fun + [T] (x:list[T], y:T):list[T] => rev$ Snoc (rev x,y);

//f Append element to tail of list (slow!).
proc += [T] (x:&list[T], y:T) { x <- *x + y; }</pre>
```

Concatenate a list of lists cat

```
//f Concatenate all the lists in a list of lists.
noinline fun cat[T] (x:list[list[T]]):list[T] =
```

#### 45.1.7 Lists and Strings

Pack list of strings into a string with separator cat

```
//f Concatenate all the strings in a list with given separator.
pure fun cat (sep:string) (x:list[string]):string =
```

Map a list to a list of strings and cat with separator catmap

```
fun catmap[T] (sep:string) (f:T -> string) (ls: list[T]) =>
fun strcat[T with Str[T]] (sep: string) (ls: list[T]) =>
fun strcat[T with Str[T]] (ls: list[T]) =>
```

#### 45.1.8 Searching

Value membership

```
//f Return true if one value in a list satisfies the predicate.
fun mem[T] (eq:T -> bool) (xs:list[T]) : bool =>

//f Return true if one value in the list satisfies the relation
//f in the left slot with
//f the given element on the right slot.
fun mem[T, U] (eq:T * U -> bool) (xs:list[T]) (e:U) : bool =>

//f Construe a list as a set, imbuing it with a membership
//f test, provided the element type has an equality operator.
```

```
instance[T with Eq[T]] Set[list[T],T] {
  fun \in (x:T, a:list[T]) => mem[T,T] eq of (T * T) a x;
}
```

#### Value Find by relation find

Returns option.

```
//f return option of the first element in a list satisfying the predicate.
fun find[T] (eq:T -> bool) (xs:list[T]) : opt[T] =>
//f Return option the first value in the list satisfies the relation
//f in the left slot with
//£ the given element on the right slot.
fun find[T, U] (eq:T * U -> bool) (xs:list[T]) (e:U) : opt[T] =>
//f Return a sub list with elements satisfying the given predicate.
noinline fun filter[T] (P:T -> bool) (x:list[T]) : list[T] =
//£ Push element onto front of list if there isn't one in the
//f list already satisfying the relation.
fun prepend_unique[T] (eq: T * T -> bool) (x:list[T]) (e:T) : list[T] =>
//£ Attach element to tail of list if there isn't one in the
//£ list already satisfying the relation.
fun insert_unique[T] (eq: T * T -> bool) (x:list[T]) (e:T) : list[T] =>
//£ Remove all elements from a list satisfying relation.
fun remove[T] (eq: T * T -> bool) (x:list[T]) (e:T) : list[T] =>
//£ Attach element to tail of list if there isn't one in the
//f list already satisfying the relation (tail-rec).
noinline fun append_unique[T] (eq: T * T -> bool) (x:list[T]) (e:T) : list[T] = {
//£ Take the first k elements from a list.
fun take[T] (k:int) (lst:list[T]) : list[T] =>
/\!/\!£ Drop the first k elements from a list.
fun drop[T] (k:int) (lst:list[T]) : list[T] =>
fun list_eq[T with Eq[T]] (a:list[T], b:list[T]): bool =>
instance[T with Eq[T]] Eq[list[T]] {
  fun ==(a:list[T], b:list[T])=> list_eq(a,b);
```

#### 45.1.9 Sort

```
//f Sort a list with given less than operator, which must be
//f total order. Uses varray sort (which uses STL sort).
fun sort[T] (lt:T*T->bool) (x:list[T])=

//f Sort a list with default total order.
//f Uses varray sort (which uses STL sort).
fun sort[T with Tord[T]](x:list[T])=> sort lt x;
```

#### 45.1.10 Streaming list

```
instance[T] Iterable[list[T],T] {
//f Convert a list to a stream.
gen iterator (var xs:list[T]) ()
```

#### 45.1.11 List syntax

```
syntax listexpr
{
    //f List cons, right associative.
    x[sarrow_pri] := x[>sarrow_pri] "!" x[sarrow_pri];
}
```

#### 45.2 Association List

A list of pairs

```
open class Assoc_list
{
   typedef assoc_list[A,B] = List::list[A*B];

   // check is the key (left element) of a pair
   // satisfies the predicate
   fun mem[A,B] (eq:A -> bool) (xs:assoc_list[A,B]) : bool =>

   // check is the key (left element) of a pair
   // satisfies the relation to given element
   fun mem[A,B,T] (eq:A * T -> bool) (xs:assoc_list[A,B]) (e:T) : bool =>

   instance[A,B] Set[assoc_list[A,B], A] {
```

```
fun mem[A,B with Eq[A]] (xs:assoc_list[A,B]) (e:A) : bool =>
}

// find optionally the first value whose associate key satisfies
// the given predicate
fun find[A,B] (eq:A -> bool) (xs:assoc_list[A,B]) : opt[B] =>

// find optionally the first value whose associate key (left slot)
// satisfies the given relation to the given element (right slot)
fun find[A,B,T] (eq:A * T -> bool) (xs:assoc_list[A,B]) (e:T) : opt[B] =>

fun find[A,B with Eq[A]] (xs:assoc_list[A,B]) (e:A) : opt[B] =>
}
```

#### 45.3 Purely Functional Random Access List.

#### 45.3.1 Definition

#### 45.3.2 Length

```
//f Length of an ralist.
fun ralist_length[a] : ralist[a] -> int =
```

#### 45.3.3 Cons

```
//f Cons: new list with extra value at the head.
fun ralist_cons[a] (x:a, xs: ralist[a]) =>
```

#### 45.3.4 Check if empty

```
//£ Check for an empty list.
fun ralist_empty[a]: ralist[a] -> bool =
```

#### 45.3.5 Split into head and tail

```
//f Proedure to split a non-empty ralist
//f into a head element and a tail.
proc ralist_uncons[a] (xs: ralist[a], phd: &a, ptl: &ralist[a])
```

#### 45.3.6 Pattern Matching Support

```
//f User define pattern matching support
fun _match_ctor_Cons[T] (x:ralist[T]) =>not ( ralist_empty x);
fun _match_ctor_Empty[T] (x:ralist[T]) => ralist_empty x;
fun _ctor_arg_Cons[T] (x:ralist[T]) : T * ralist[T] =
```

#### 45.3.7 Head

```
//f Head element of a non-empty ralist.
fun ralist_head[a] (xs: ralist[a]) : a =
```

#### 45.3.8 Tail

```
//£ Tail list of a non-empty ralist.
fun ralist_tail[a] (xs: ralist[a]) : ralist[a] =
```

#### 45.3.9 Random Access

```
//f Random access to an ralist. Unchecked.
fun ralist_lookup[a] (xs:ralist[a],i:int)=>
```

#### 45.3.10 Update

```
//f Return a list with the i'th element replaced by x0.
//f Index is unchecked.
fun ralist_update[a] (xs:ralist[a], i:int, x0:a) =>
```

#### 45.3.11 Iteration

```
//f Callback based iteration.
//f Apply procedure to each element of the ralist.
proc ralist_foreach[a]
(
    xs: ralist[a],
    f: a -> void
)
```

#### 45.3.12 Show

```
//f Convert ralist to a string.
instance[a with Str[a]] Str[ralist[a]]
{
   fun str (xx: ralist[a]):string = {
}
```

### 45.4 Doubly Linked Mutable List

A dlist\\_t is a doubly linked mutable list. It is suitable for use as non-thread-safe queue.

```
class DList[T]
{
  typedef dnode_t=
  (
   data: T,
```

```
next: cptr[dnode_t], // possibly NULL
prev: cptr[dnode_t] // possibly NULL
);
typedef dlist_t = (first:cptr[dnode_t], last:cptr[dnode_t]);
    // invariant: if first is null, so is last!

ctor dlist_t () => (first=nullptr[dnode_t], last=nullptr[dnode_t]);
```

#### 45.4.1 Length len

```
fun len (x:dlist_t) = {
```

#### 45.4.2 Inspection

```
fun peek_front (dl:dlist_t) : opt[T] =>
fun peek_back (dl:dlist_t) : opt[T] =>
```

#### 45.4.3 Insertion

```
proc push_front (dl:&dlist_t, v:T) {
proc push_back (dl:&dlist_t, v:T) {
```

#### 45.4.4 Deletion

```
gen pop_front (dl:&dlist_t): opt[T] = {
  gen pop_back (dl:&dlist_t): opt[T] = {
```

#### 45.4.5 Use as a queue

We can implement enqueue and dequeue at either end, we'll make enqueue push\_front and dequeue pop\_back for no particular reason.

```
typedef queue_t = dlist_t;
proc enqueue (q:&queue_t) (v:T) => push_front (q,v);
gen dequeue (q:&queue_t) :opt[T] => pop_back q;
ctor queue_t () => dlist_t ();
```

#### 45.4.6 Queue iterator

Fetch everything from a queue.

```
gen iterator (q:&queue_t) () => dequeue q;
```

#### 45.5 S-expressions

A scheme like data structure.

```
class S_expr
{
    union sexpr[T] = Leaf of T | Tree of list[sexpr[T]];

fun fold_left[T,U] (_f:U->T->U) (init:U) (x:sexpr[T]):U =>
    proc iter[T] (_f:T->void) (x:sexpr[T]) {

    fun map[T,U] (_f:T->U) (x:sexpr[T]):sexpr[U] =>

    instance[T with Eq[T]] Set[sexpr[T],T] {
        fun \in (elt:T, x:sexpr[T]) =>
    }

    instance[T with Str[T]] Str[sexpr[T]] {
        noinline fun str(x:sexpr[T])=>
    }
}
```

### 45.6 LS-expressions

A scheme like data structure, similar to sexpr, only in this variant the tree nodes also have labels.

```
class LS_expr
{
    union lsexpr[T,L] = | Leaf of T | Tree of L * list[lsexpr[T,L]];

    fun fold_left[T,L,U] (_f:U->T->U) (_g:U->L->U) (init:U) (x:lsexpr[T,L]):U =>

    proc iter[T,L] (_f:T->void) (_g:L->void) (x:lsexpr[T,L]) {
        fun map[T,L,U,V] (_f:T->U) (_g:L->V) (x:lsexpr[T,L]):lsexpr[U,V] =>
        instance[T,L with Str[T], Str[L]] Str[lsexpr[T,L]] {
            noinline fun str(x:lsexpr[T,L])=>
        }
}
```

}

## Chapter 46

# Arrays

- 46.1 Native Arrays
- 46.2 Varrays
- 46.3 Darrays
- 46.4 Sarrays
- 46.5 C arrays

# $\begin{array}{c} {\rm Part\ IX} \\ {\bf Appendices} \end{array}$

## Appendix A

## Special Names

- **\_make\_typename** Cast the representation of an abstract type to the abstract type.
- \_repr\_ Cast an abstract type to its representation.
- \_map Generic map.
- \_eq Generic equality.
- \_rev Tuple and tuple type reversal. Applied after monomorphisation. Works on arrays too using library function.
- map Tuple map and tuple type map. Applied after monomorphisation. Works on arrays too.
- \_rev\_map Reversing tuple map and tuple type map. Applied after monomorphisation. Works on arrays too using library function.
- \_strr Generic conversion to string. Supports records and tuples. Delegates primitives and arrays to library function str.
- \_tie Converts a pointer to a tuple, to a tuple of pointers to the components of the original tuple.
- ☐ Product of functions. Prefix quantifier over tuple.
- $\sum$  Sum of functions. Prefix quantifier over tuple.
- $\langle \cdot \rangle$  Mediating morphism of product of functions.
- [·] Mediating morphism of sum of functions.
- apply User defined application.
- typeof Denotes type of an expression. The expression is not eveluated.
- \_match\_ctor\_name User defined pattern match constructor check.

\_ctor\_arg\_name User defined pattern match extractor.

\_ctor\_arg\_typename User defined constructor/conversion function.

TYPE The kind of all types.

GENERIC A psuedo kind used to qualify a type variable in a definition which causes the compiler to generate a fresh definition for each instance type actually used on demand.

\_felix\_type\_name Trait reporting bound type name as string.

```
_felix_type_name[int * long] // "int * long"
```

\_scheme An application of the \_scheme psuedo function to a string causes the macro processor to execute the string as embedded Scheme code, resulting in an S-expression. The S-expression is then converted into Felix expression, in the same way the S-expressions generated by the parser are converted into expressions.

It can also be used as a procedure name in statement.

- \_str An application of \_str to any Felix expression causes the macro processor to translate the expression into a string representing the AST terms for the expression as would be presented in a compiler diagnostic. Useful to examine exactly how the parser translates a particular Felix expression.
- range\_check Applied to a tuple of three expressions, this psuedo function is translated by the macro processor into a system range check expression which checks that the middle term is greater than or equal to the first term and less than the third term. If the conditions are not met, an exception will be raised at run time.

# Glossary

 ${\bf coroutine}\,$  a programming unit which exchanges control with others on a neutral basis. 18

**polymorphism** a language feature which allows a function to process arguments of more than one type, and to behave differently depending on the argument type. 18

**setwise lookup** a method of lookup where a symbol may be used before or after it is defined. 130

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