

Quantum sensing with superconducting qubits

Logan Bishop-Van Horn
QSQM Symposium
2021-09-10

Transmon Hamiltonian

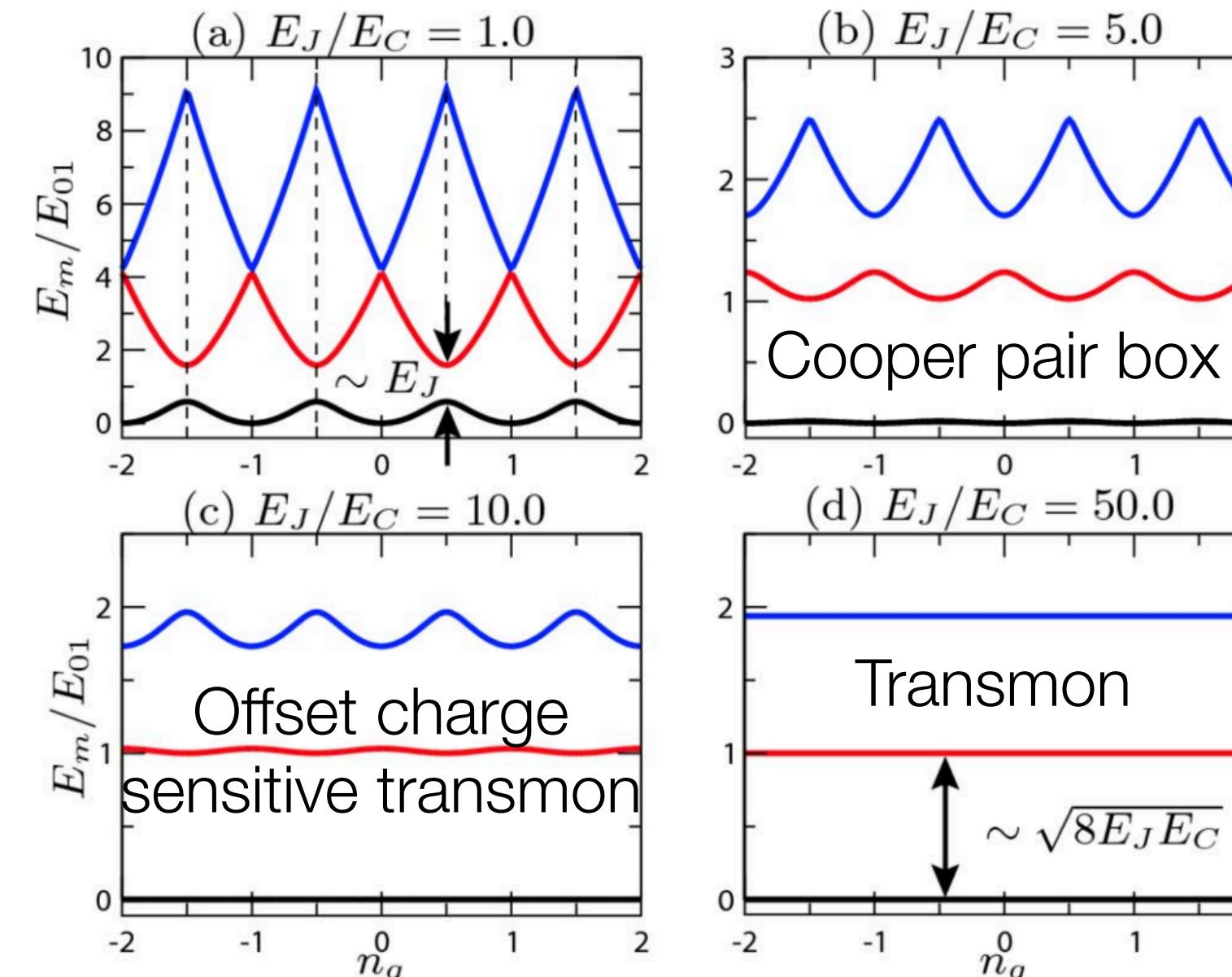
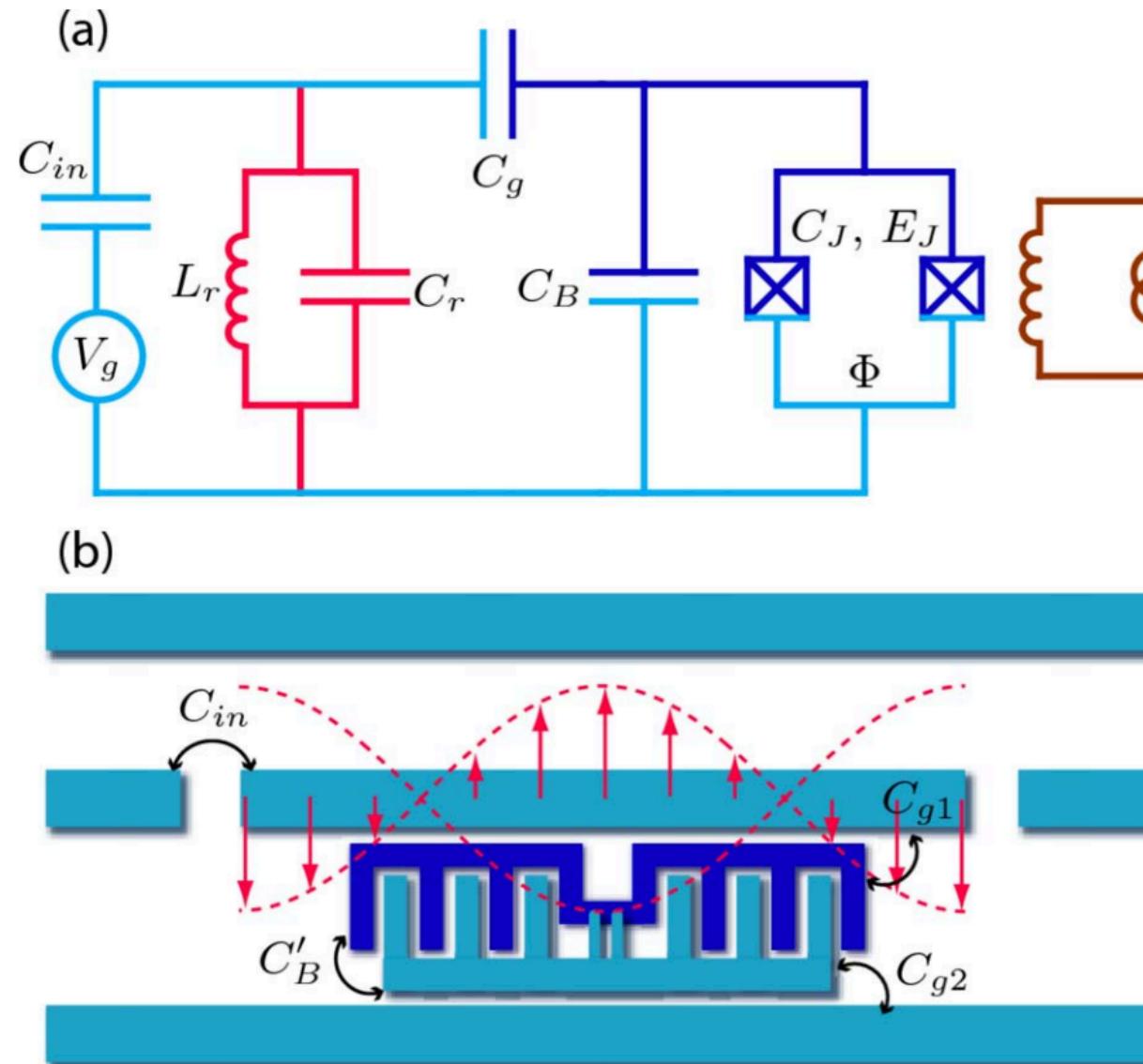
PHYSICAL REVIEW B 77, 180502(R) (2008)



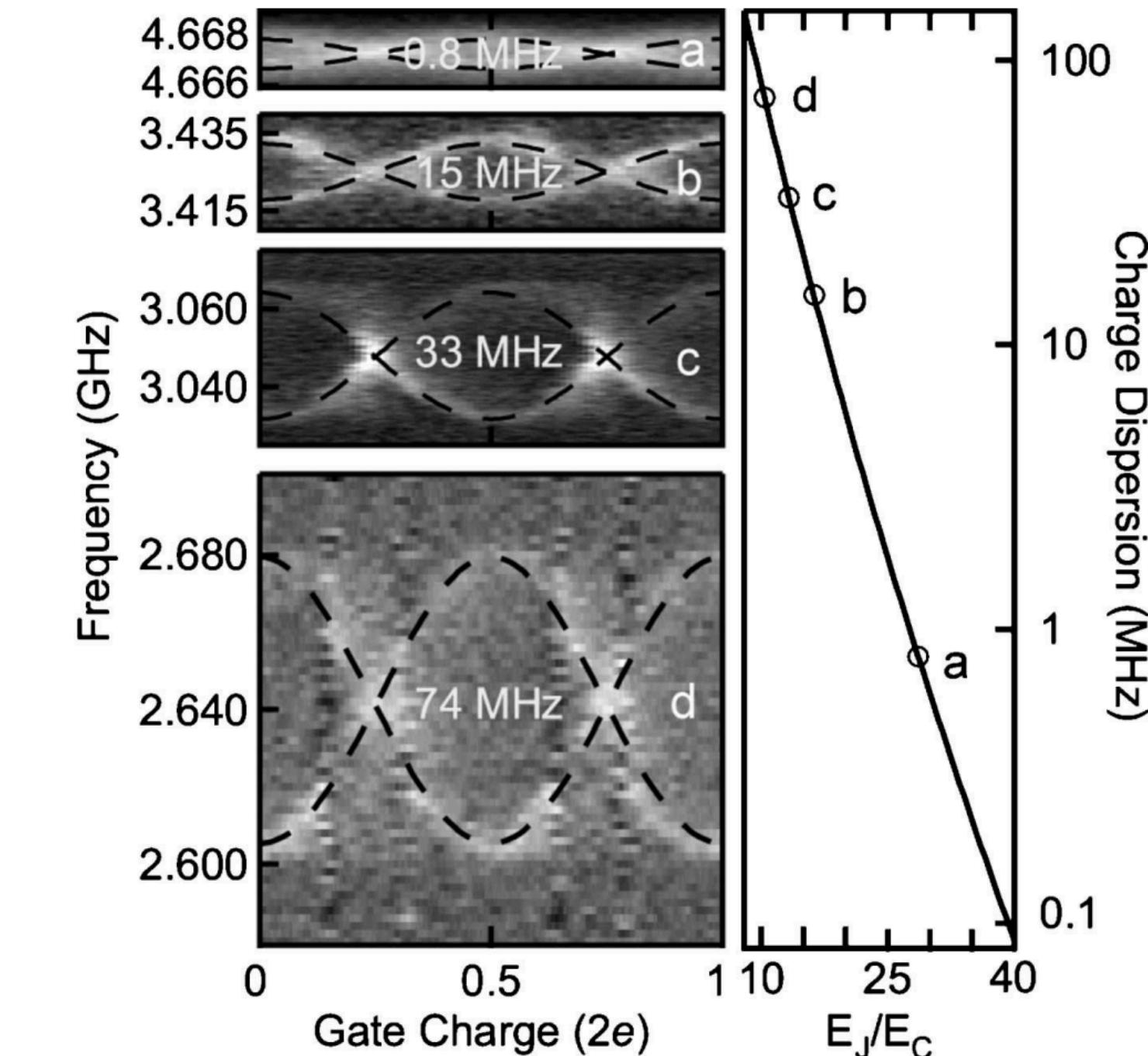
Suppressing charge noise decoherence in superconducting charge qubits

PHYSICAL REVIEW A 76, 042319 (2007)

Charge-insensitive qubit design derived from the Cooper pair box



$$\hat{H} = 4E_C(\hat{n} - n_g)^2 - E_J(\Phi)\cos \hat{\phi}$$

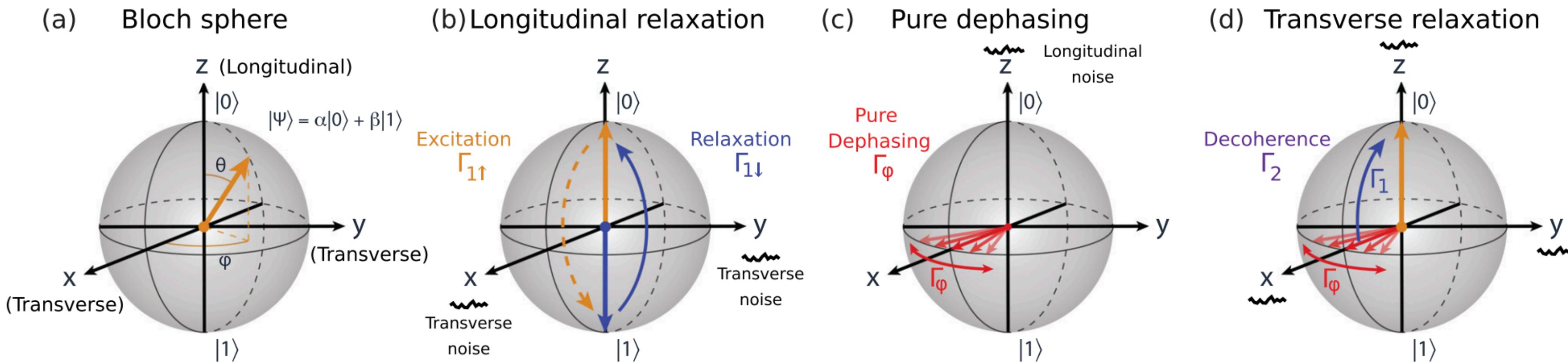


- Superconducting circuit with tunable charge and flux sensitivity
- Transition frequencies $\omega_{ij} = 2\pi f_{ij}$ are periodic in n_g and Φ
- E_J/E_C determines anharmonicity and charge sensitivity

Decoherence limits sensitivity

A quantum engineer's guide to superconducting qubits

Cite as: Appl. Phys. Rev. **6**, 021318 (2019); <https://doi.org/10.1063/1.5089550>



Goal: Measure qubit frequency $f_{01}(n_g, \Phi)$ to quantify electric potential (via n_g), magnetic field (via Φ), or fluctuations in those parameters (noise spectroscopy).

High frequency noise:
drives transitions
between states (T_1)

Control electronics
Lossy environment
Thermal radiation
Pair-breaking photons

Low frequency
(e.g. 1/f) noise:
stochastically shifts
qubit frequency (T_φ)

Control electronics
Two-level systems
Readout photons
???

$$|\langle 0 | \hat{O}_\lambda | 1 \rangle|^2, S_\lambda(f_{01})$$

$$\frac{\partial f_{01}}{\partial \lambda}, S_\lambda(f)$$

$$T_2 = \left(\frac{1}{T_\varphi} + \frac{1}{2T_1} \right)^{-1}$$
$$\delta n_g \sim \frac{1}{T_2 \left| \frac{\partial f_{01}}{\partial n_g} \right|} \quad \text{Uncertainty in offset charge}$$
$$\delta \Phi \sim \frac{1}{T_2 \left| \frac{\partial f_{01}}{\partial \Phi} \right|} \quad \text{Uncertainty in flux bias}$$

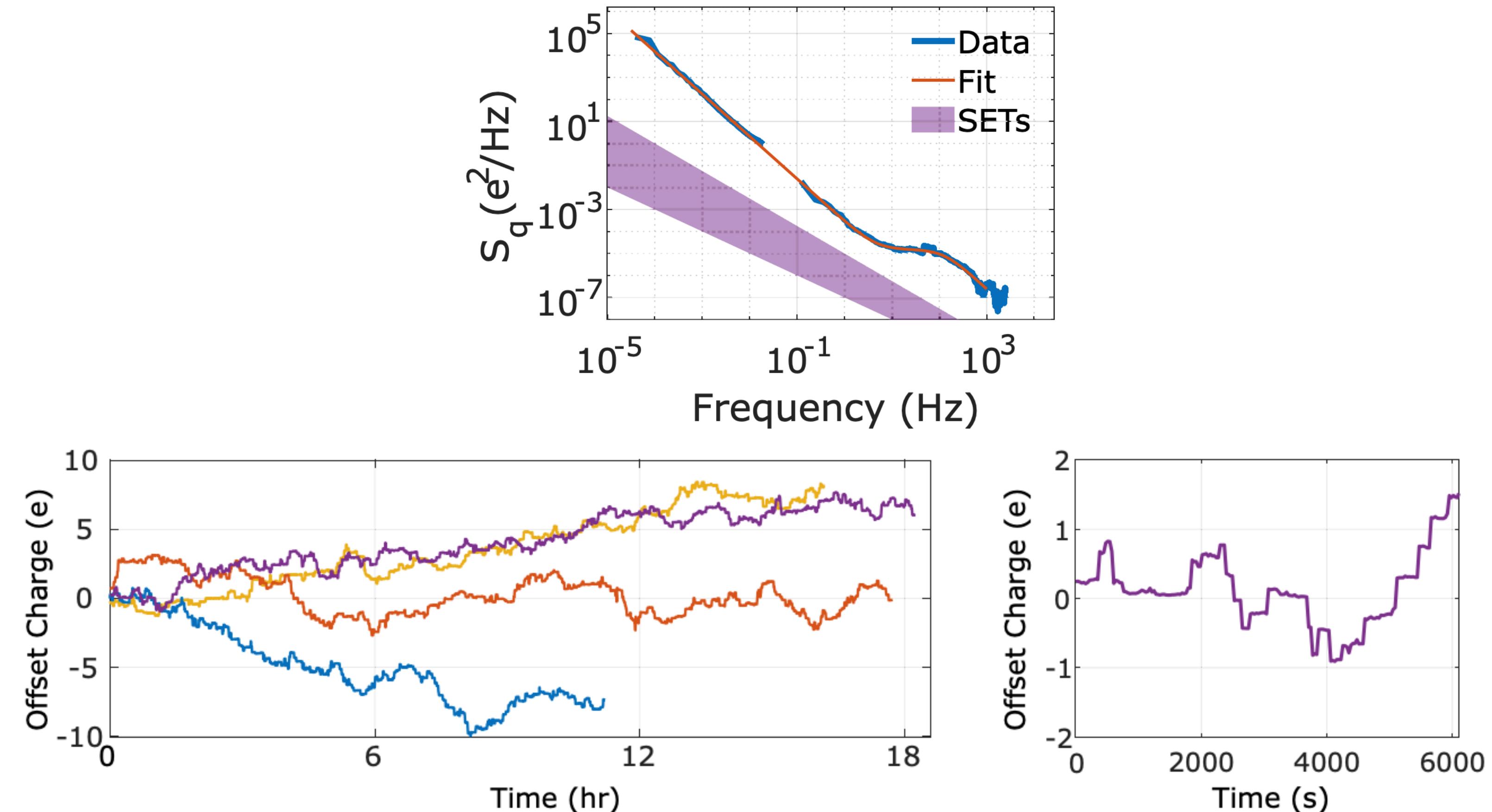
Low frequency charge noise

PHYSICAL REVIEW B 100, 140503(R) (2019)

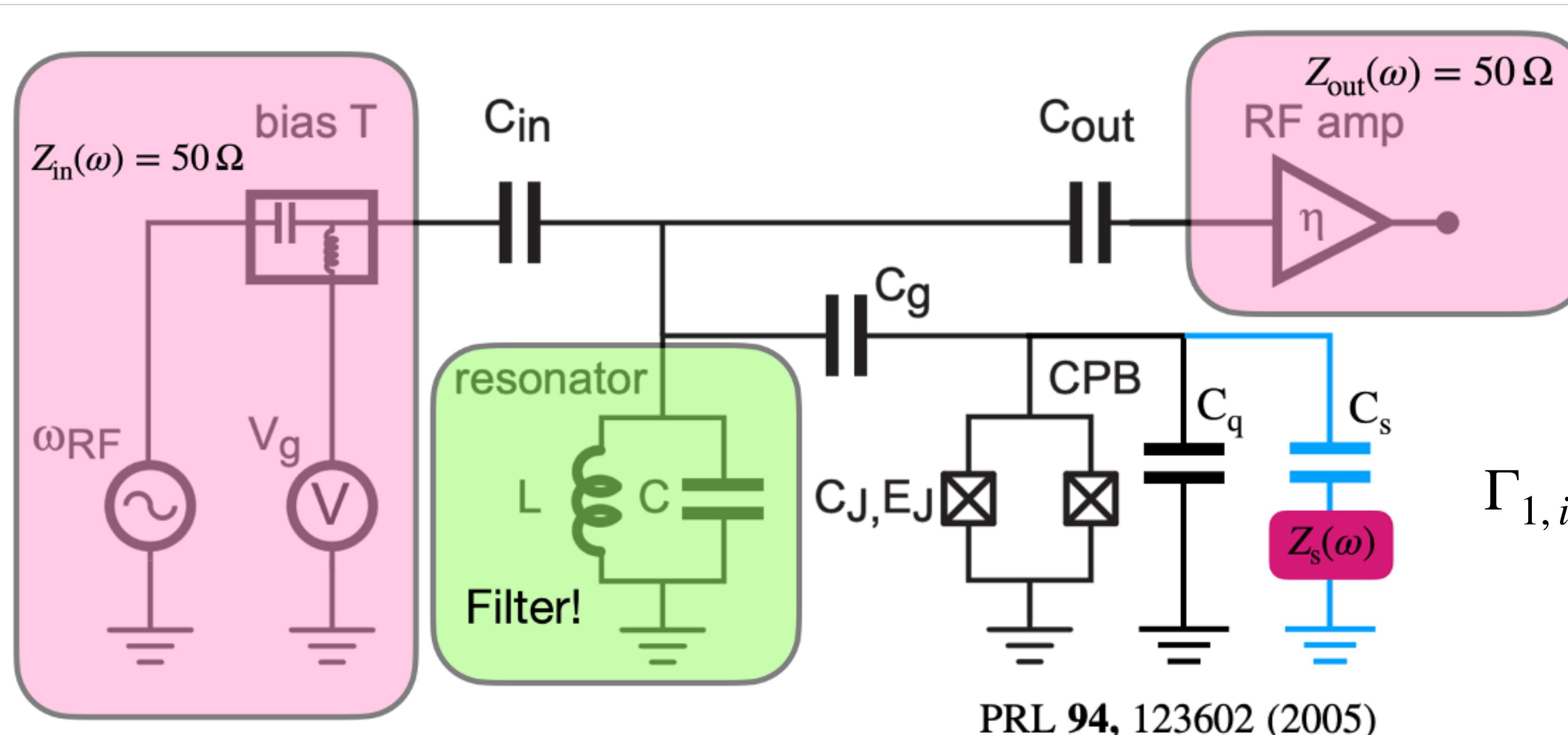
Anomalous charge noise in superconducting qubits

B. G. Christensen,¹ C. D. Wilen,² A. Opremcak,² J. Nelson,³ F. Schlenker,² C. H. Zimonick,² L. Faoro,^{2,4} L. B. Ioffe,^{2,4} Y. J. Rosen,⁵ J. L. DuBois,⁵ B. L. T. Plourde,³ and R. McDermott²

- 1/f-like charge noise in offset charge sensitive qubits is orders of magnitude worse than typically seen in SETs
- $\sim 0.1 - 1,000$ Hz: limits sensitivity via T_2
- $\lesssim 0.1$ Hz: frequency drift complicates data-taking and analysis



Coupling to sample with finite impedance



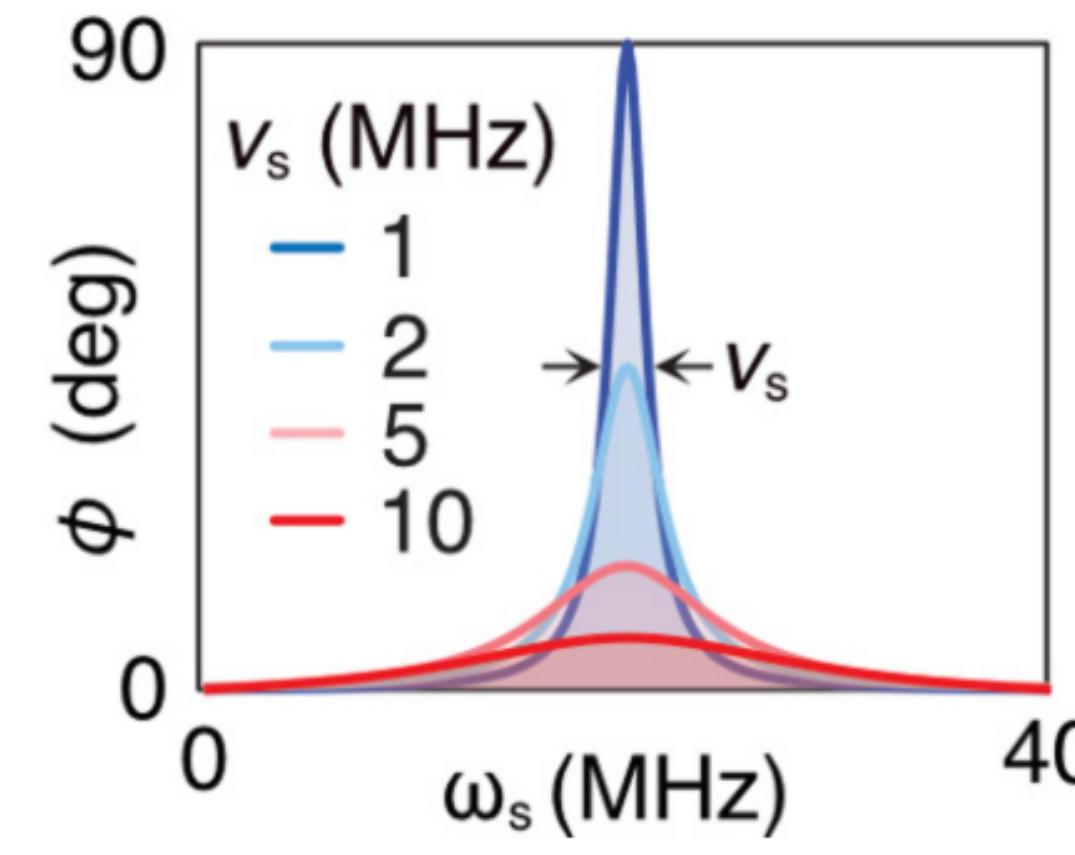
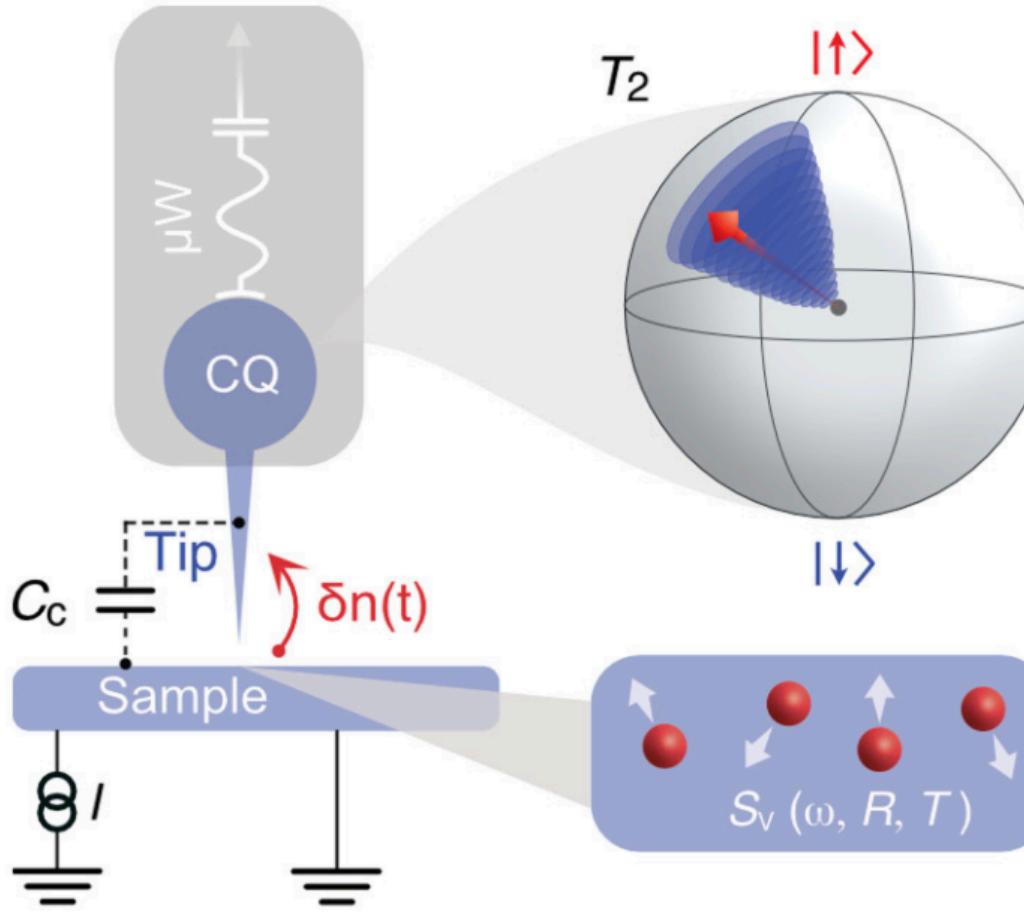
$$\Gamma_{1,i} \propto \left(\frac{C_i}{C_{tot}} \right)^2 \text{Re}[Z_i(\omega_{01})] |\langle 0 | \hat{n} | 1 \rangle|^2$$

- Want to maximize C_s/C_{tot} so that the sample gates the qubit island effectively
- But capacitive coupling to a lossy sample limits sensitivity via T_1
- Effect is small in CPB regime, but becomes significant as E_J/E_C is increased

Measurement methods

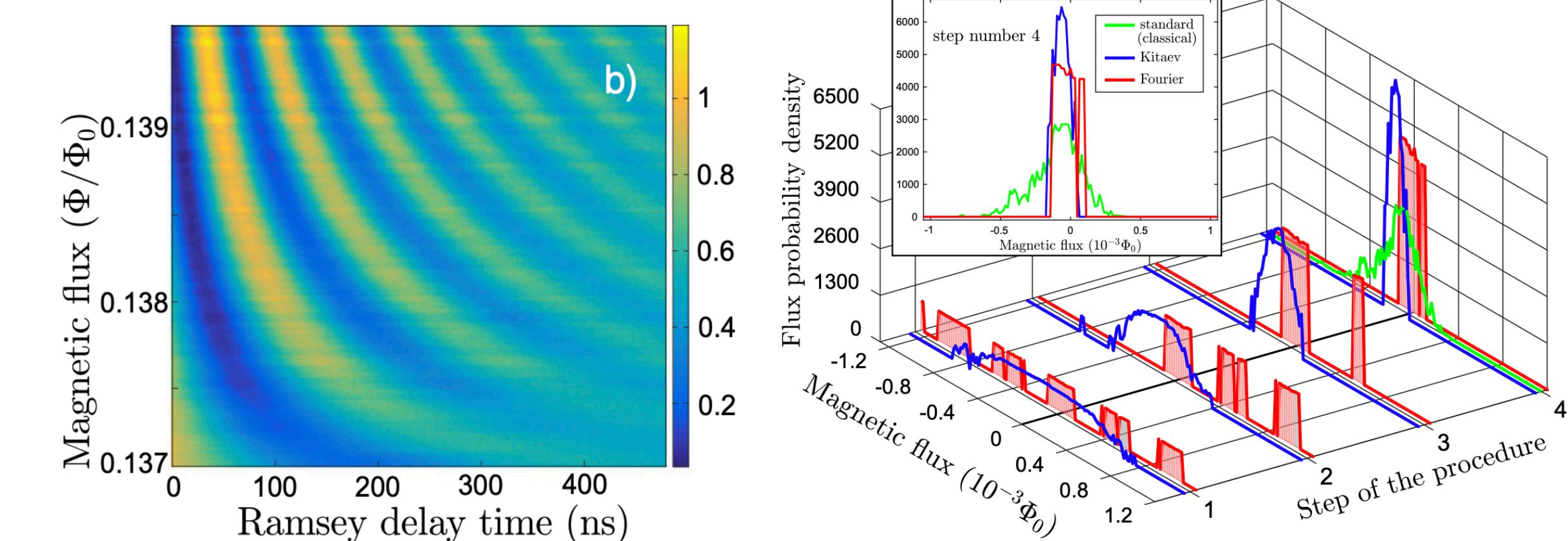
Spectroscopy

- Can be done with only CW microwave control
- Center frequency measures the mean value of n_g or Φ
- Linewidth measures T_2 but cannot easily be converted into a noise spectrum $S_{n_g}(\omega)$ or $S_\Phi(\omega)$
- Example: [Phys. Rev. Res. 2, 043031 \(2020\)](#)



Interferometry

- Enables noise spectroscopy via dynamical decoupling
- Requires time domain control and reasonably high-fidelity readout
- Limited dynamic range due to phase wrapping
- Limited measurement repetition rate:
 - At most 1 bit of information per measurement, then the qubit must be reset to ground state
- Example:
[npj Quant. Info. 4, 29 \(2018\)](#)



Can we borrow ideas from SC qubit research without inheriting qubit downsides?

Fast magnetic imaging/noise spectroscopy

- Requires mK temperatures
- Requires single-photon operation and few-photon readout
- Excess charge noise relative to SETs
- Limited measurement repetition rate
- Limited dynamic range

SQUID magnetometer with dispersive readout

- Noise spectroscopy: high BW measurement + FFT
- Compatible with parametric amplifiers
- Faster measurement repetition rate (no reset)
- See:
 - [doi:10.1103/PhysRevB.83.134501](https://doi.org/10.1103/PhysRevB.83.134501)
 - [doi:10.1088/0953-2048/26/5/055015](https://doi.org/10.1088/0953-2048/26/5/055015)
 - [doi:10.1063/1.5030489](https://doi.org/10.1063/1.5030489)

Fast potential imaging/noise spectroscopy

Radio-frequency SET

- Noise spectroscopy: high BW measurement + FFT
- Lower charge noise than charge-sensitive qubit
- See:
 - [doi:10.1126/science.280.5367.1238](https://doi.org/10.1126/science.280.5367.1238)

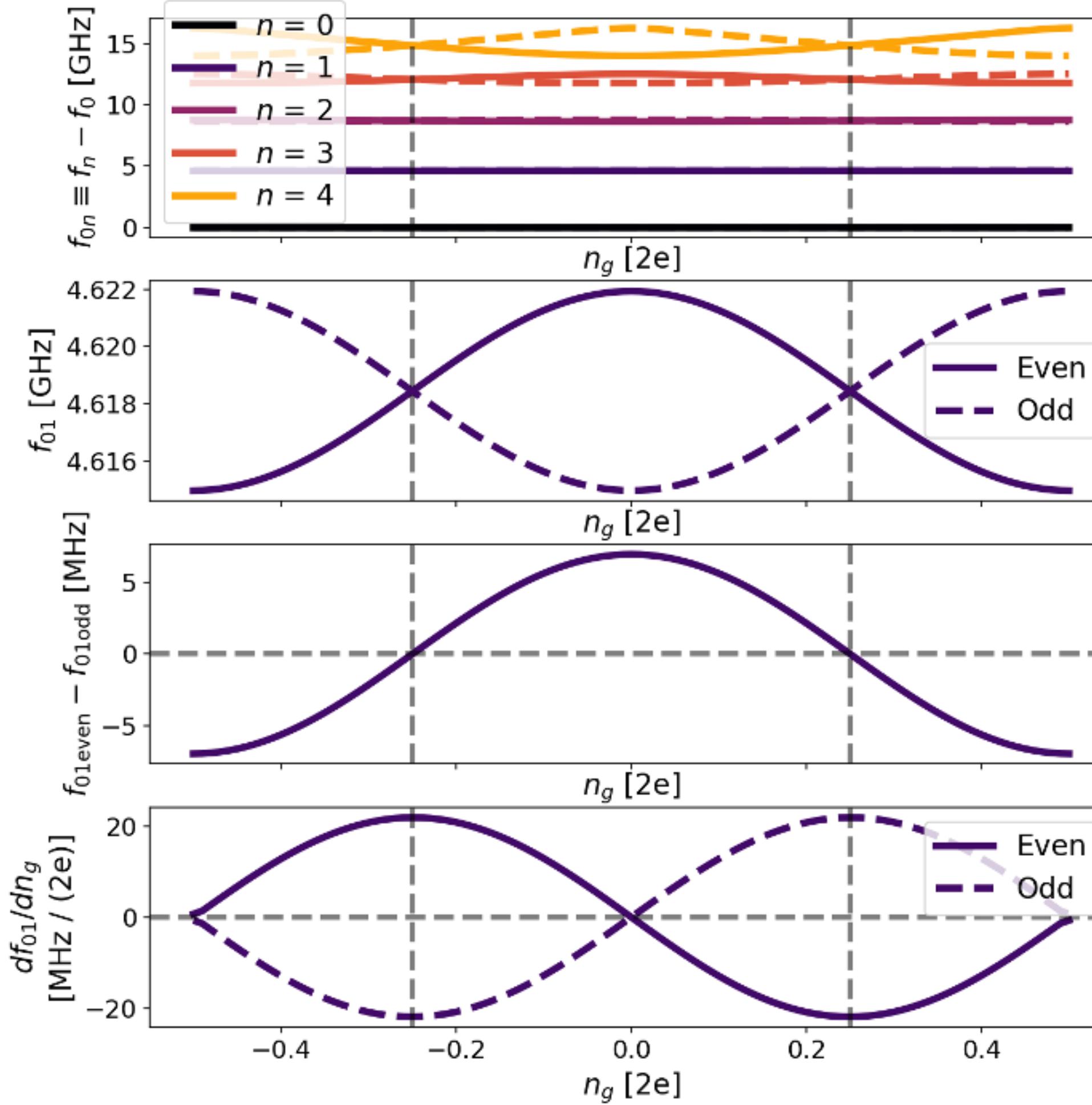
Imaging rf loss in SC circuits

Scanning high-Q SC resonator

- Measure Q vs. position
- Could be frequency-tunable with a SQUID
- See:
 - [doi:10.1063/1.4792381](https://doi.org/10.1063/1.4792381)
 - [doi:10.1103/PhysRevX.6.021044](https://doi.org/10.1103/PhysRevX.6.021044)

Goal: Measure qubit frequency $f_{01}(n_g, \Phi)$ to quantify electric potential (via n_g), magnetic field (via Φ), or fluctuations in those parameters (noise spectroscopy).

$$E_J = 8 \text{ GHz}, E_C = 0.4 \text{ GHz} (E_J/E_C = 20), \Phi_{\text{ext}} = 0$$



First-order insensitive to Φ

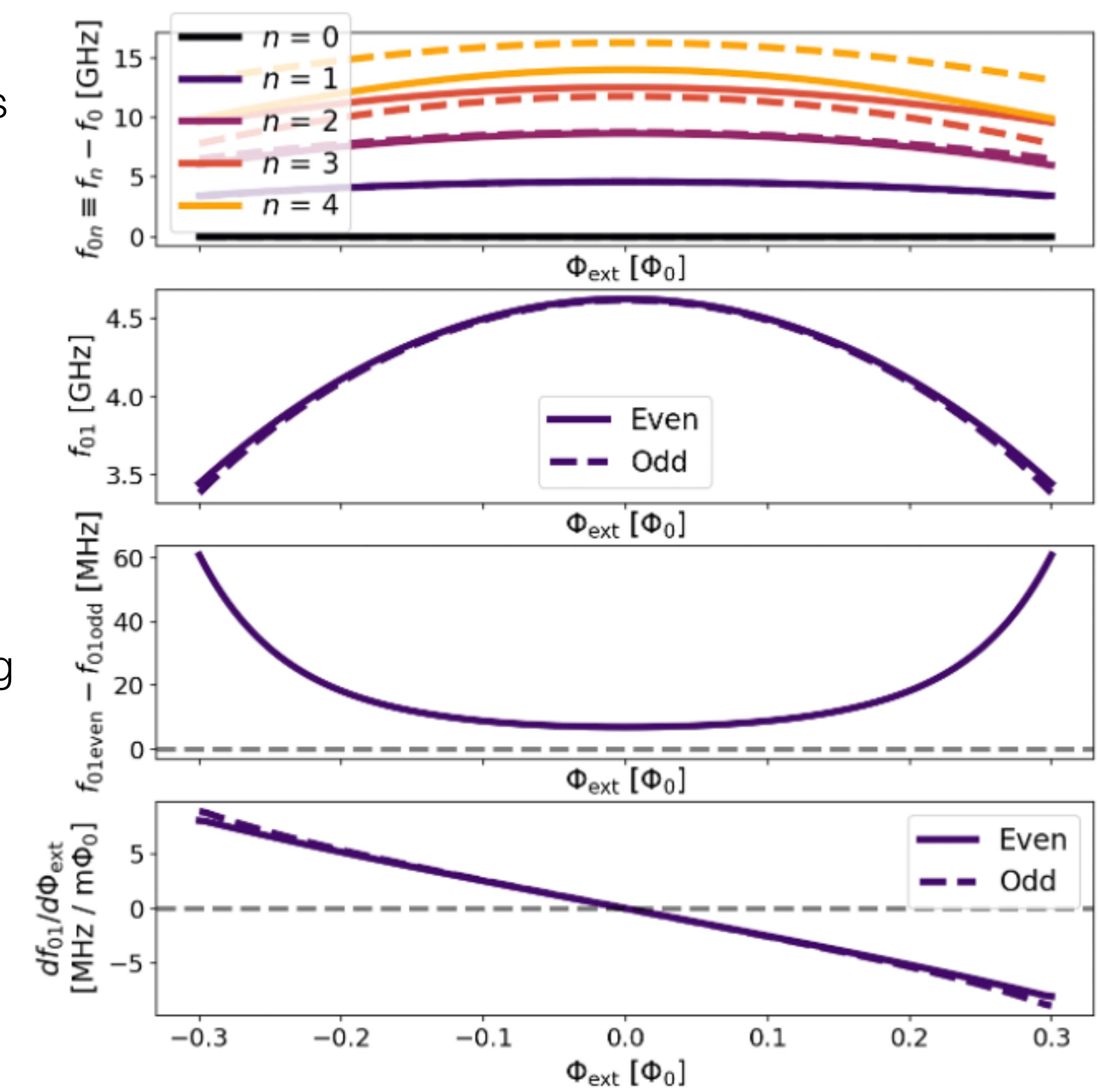
Transition frequencies

Qubit spectrum

Sensitivity to
quasiparticle tunneling

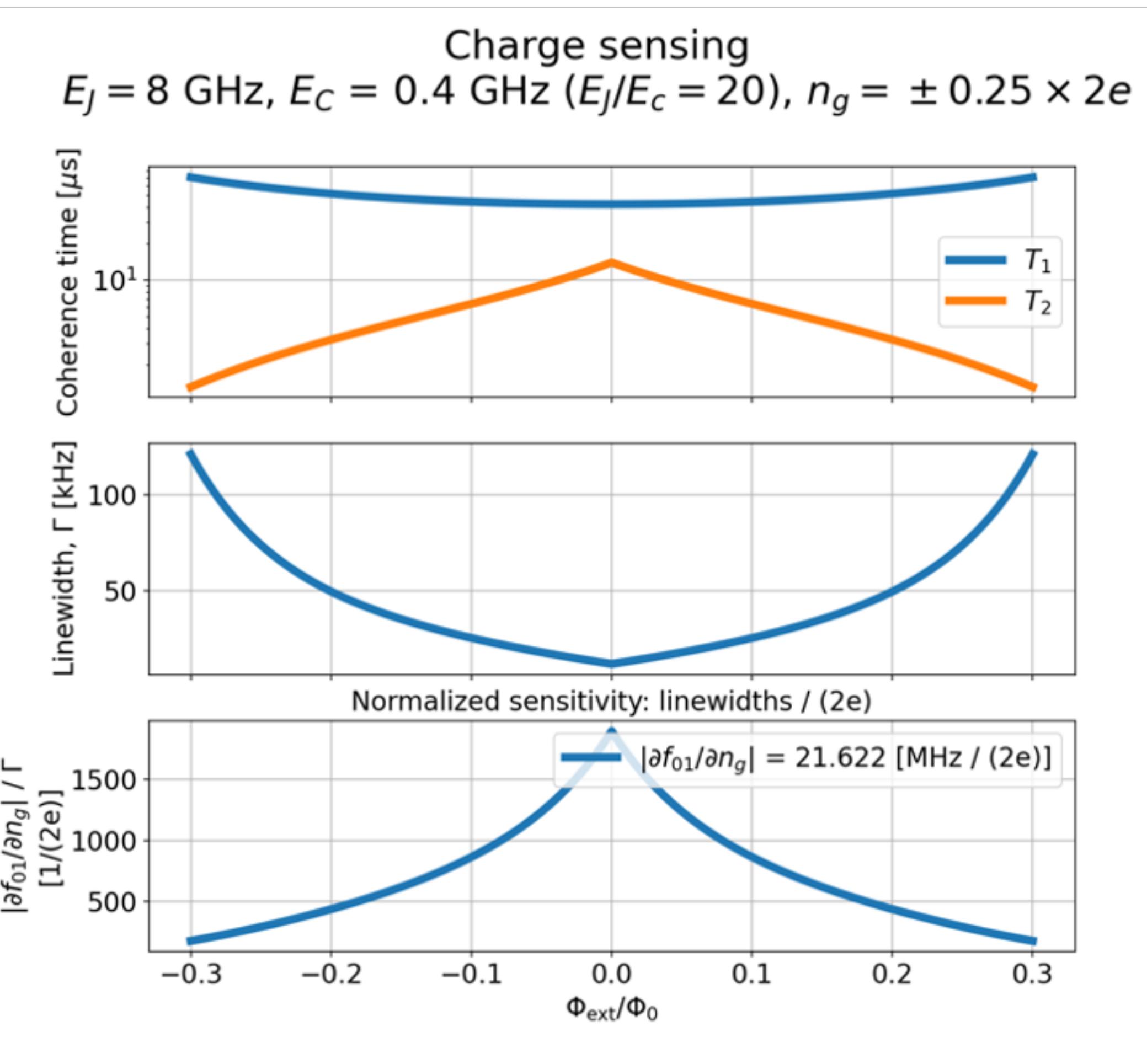
Sensitivity to n_g or Φ

$$E_J = 8 \text{ GHz}, E_C = 0.4 \text{ GHz} (E_J/E_C = 20), n_g = 0(\pm 0.5)$$

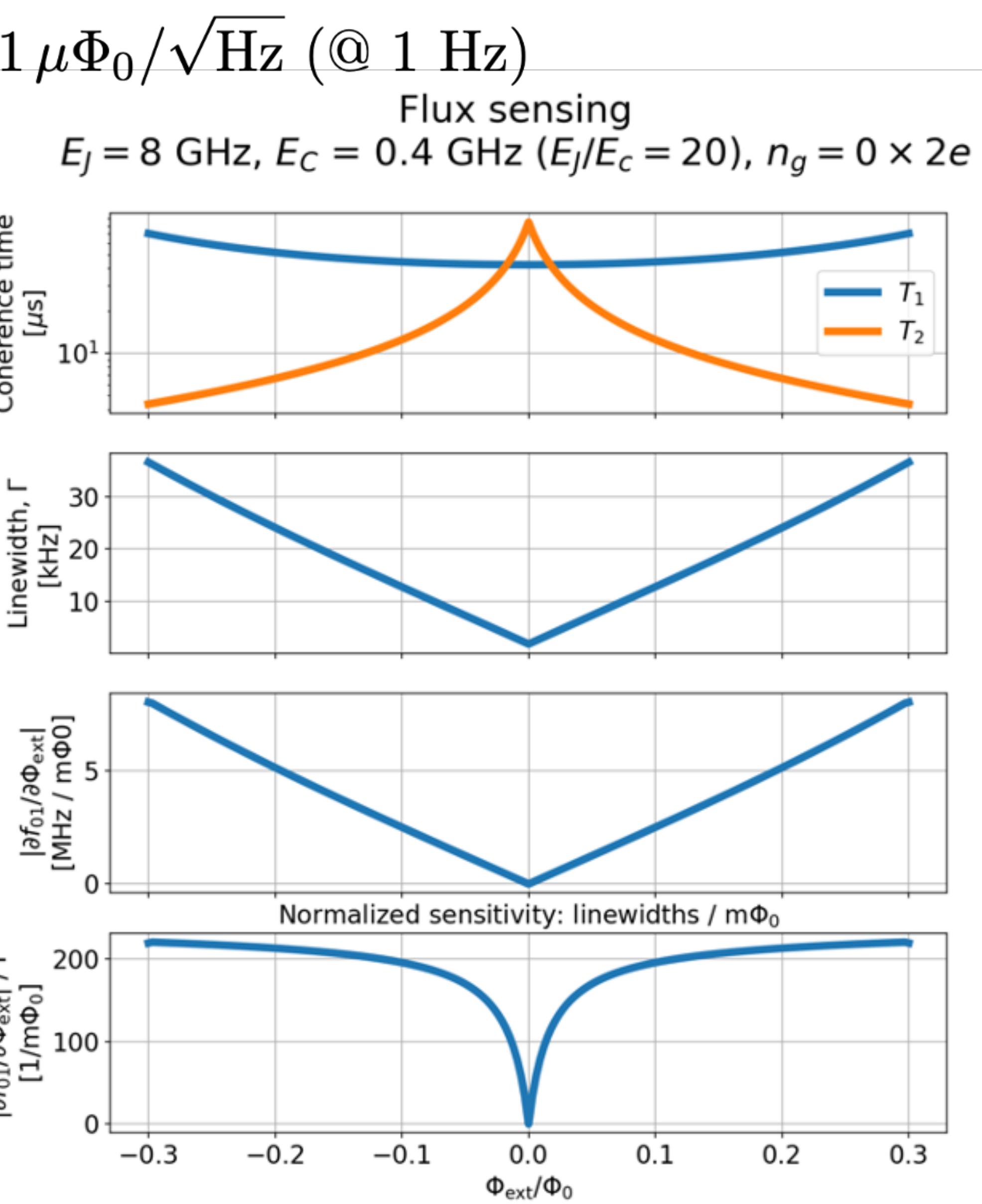


First-order insensitive to n_g

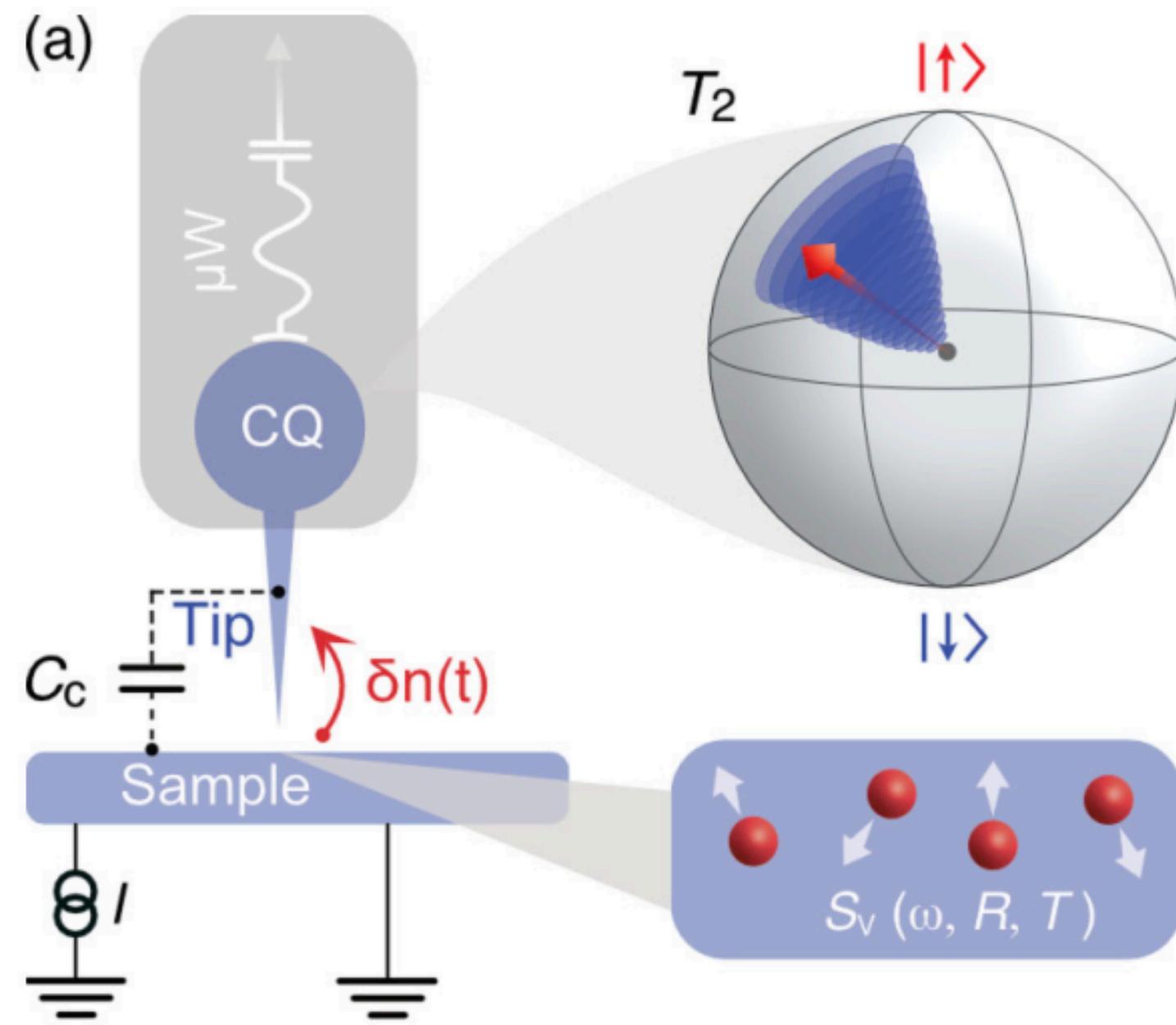
$$A_{n_g} = 10^{-4} e/\sqrt{\text{Hz}}, A_\Phi = 1 \mu\Phi_0/\sqrt{\text{Hz}} (\text{@ } 1 \text{ Hz})$$



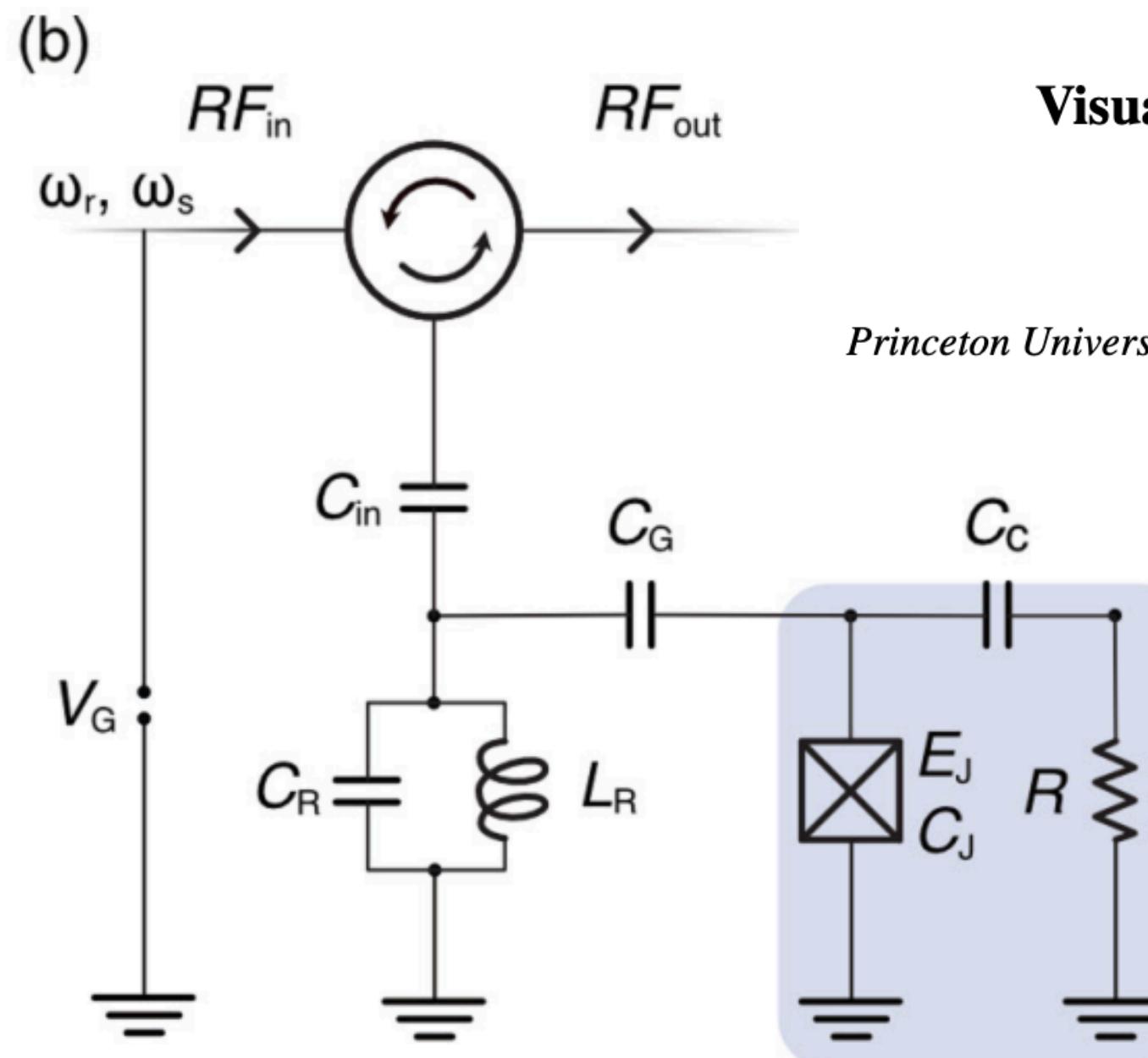
$$S_{n_g} = \frac{1}{\Gamma} \left| \frac{\partial f_{01}}{\partial n_g} \right| = 2\pi T_2 \left| \frac{\partial f_{01}}{\partial n_g} \right|$$



$$S_\Phi = \frac{1}{\Gamma} \left| \frac{\partial f_{01}}{\partial \Phi} \right| = 2\pi T_2 \left| \frac{\partial f_{01}}{\partial \Phi} \right|$$

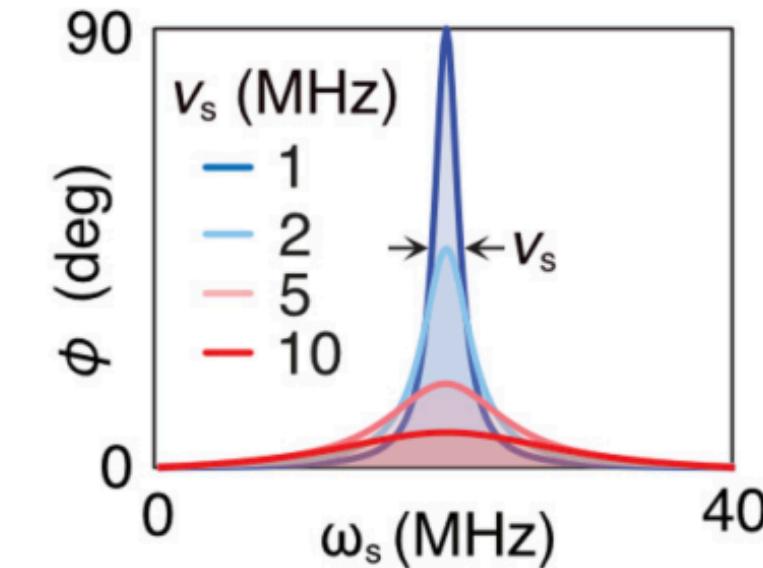
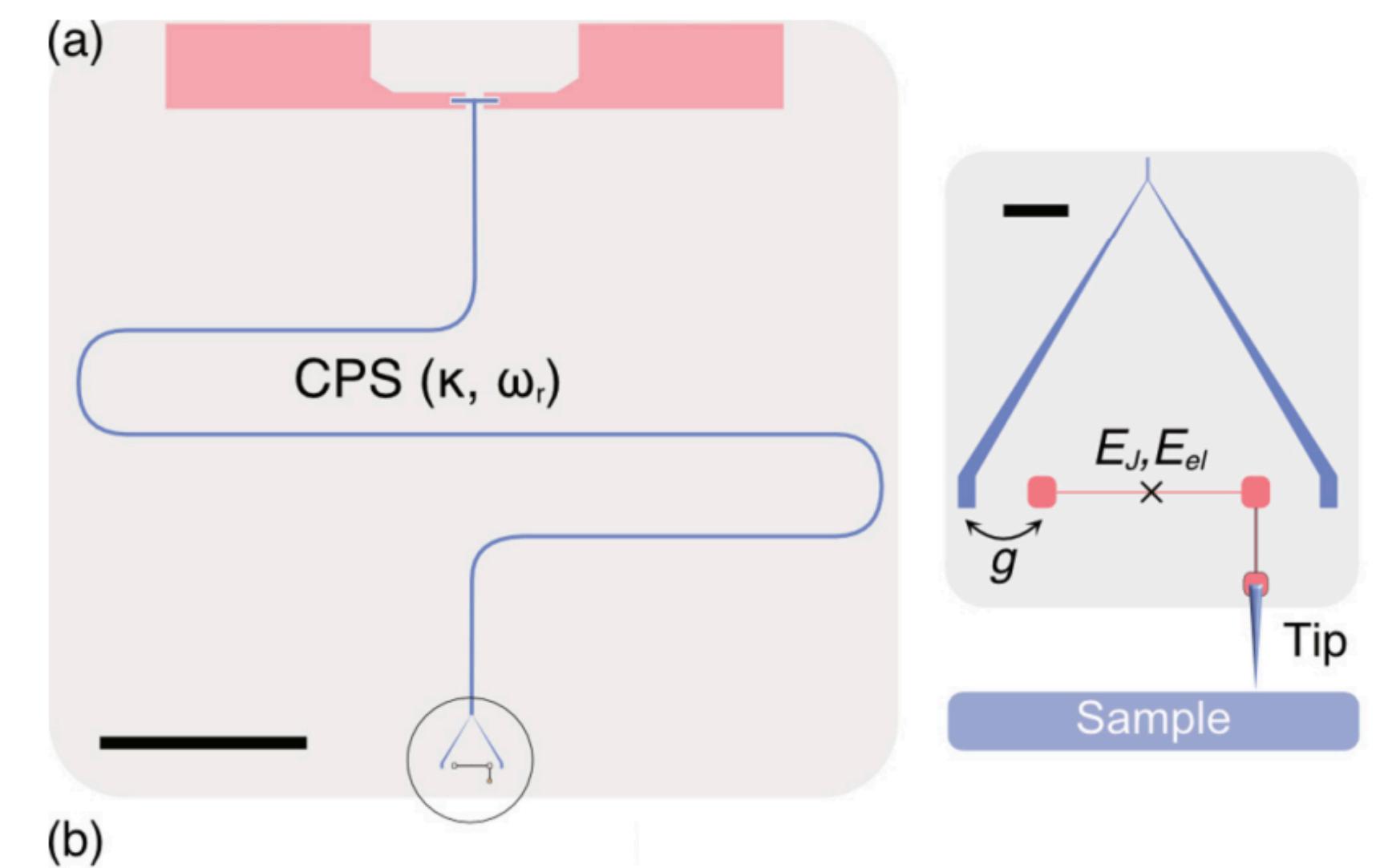


- Lossy sample capacitively coupled to a Cooper pair box
- Johnson noise from sample causes fluctuating n_g , reducing T_2
- Measure linewidth $1/T_2$ spectroscopically to infer local sample temperature, resistance



Visualizing dissipative charge-carrier dynamics at the nanoscale with superconducting-charge-qubit microscopy

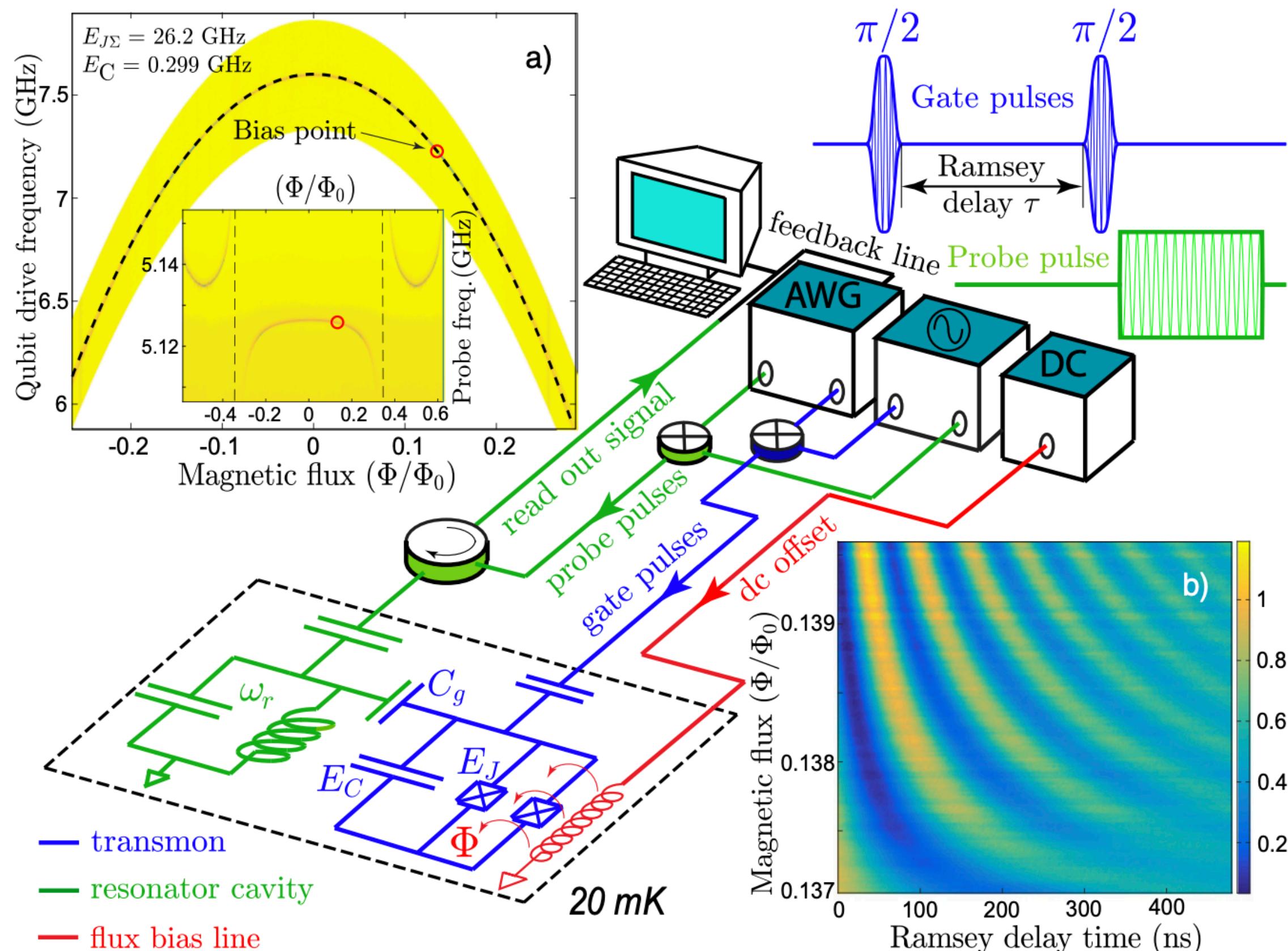
Berthold Jäck^{*}
Princeton University, Joseph Henry Laboratory at the Department of Physics, Princeton, New Jersey 08544, USA



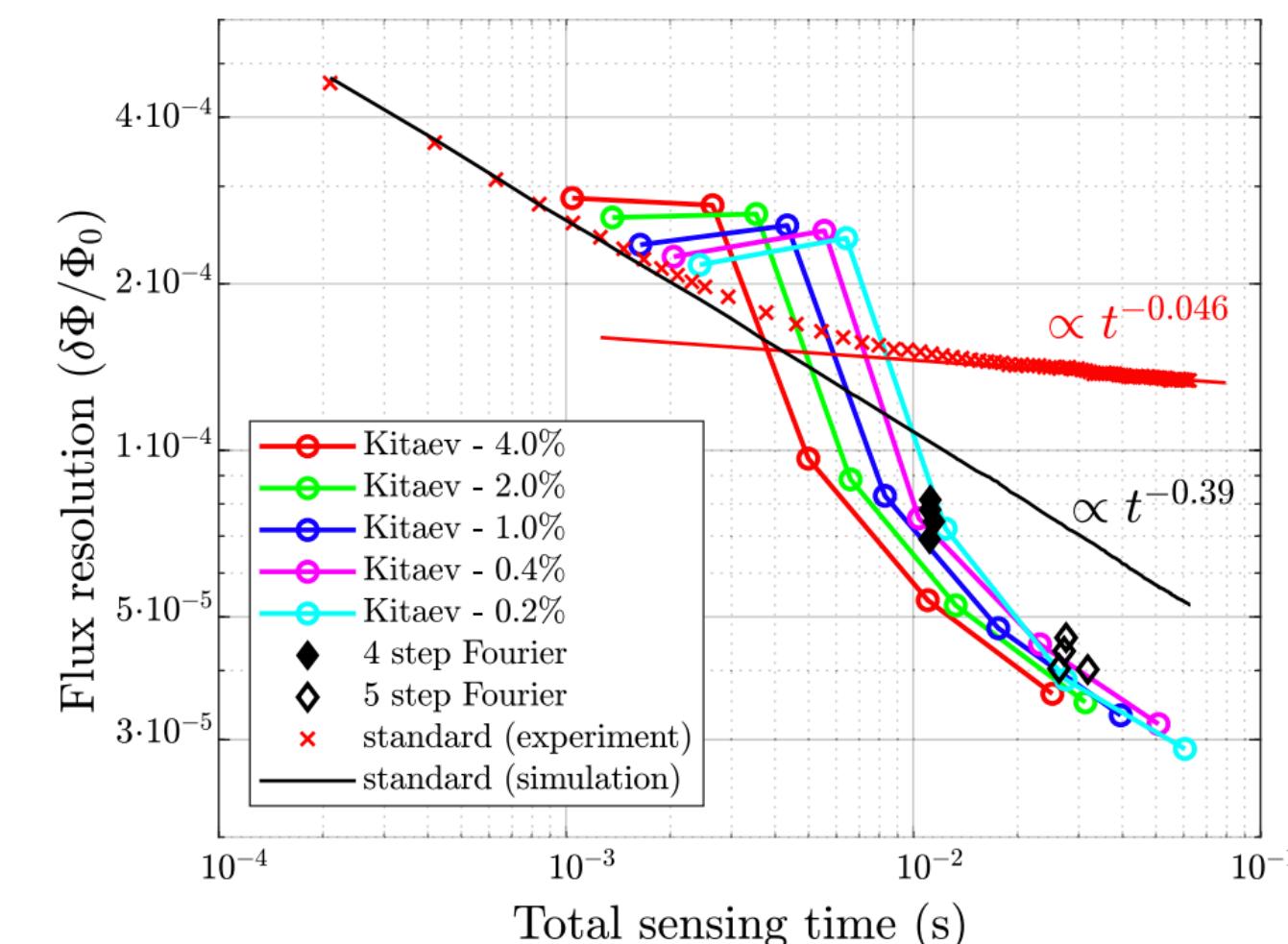
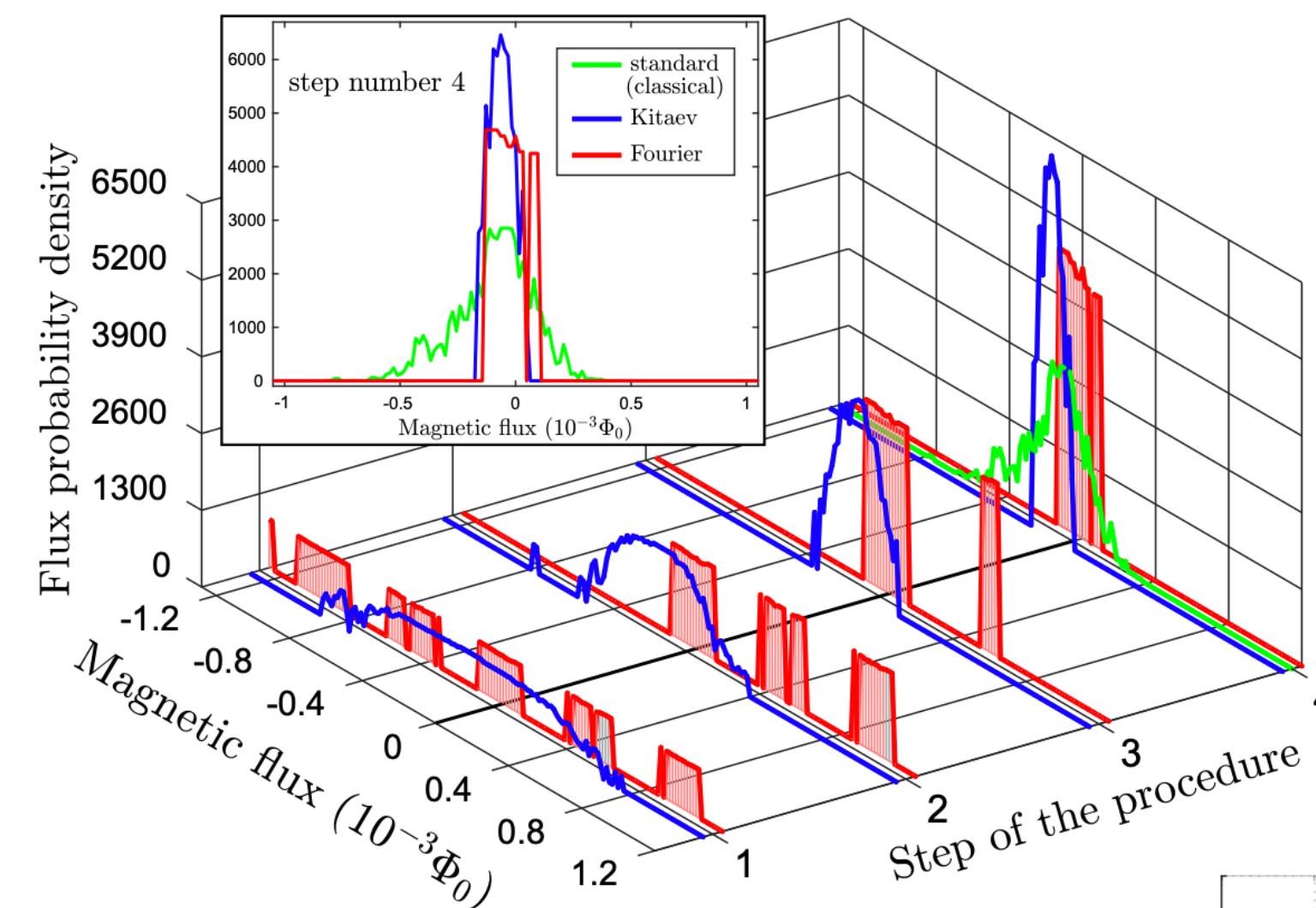
Quantum-enhanced magnetometry by phase estimation algorithms with a single artificial atom

S. Danilin, A. V. Lebedev , A. Vepsäläinen, G. B. Lesovik, G. Blatter & G. S. Paraoanu 

npj Quantum Information 4, Article number: 29 (2018) | Cite this article



- Tunable transmon, $E_J/E_C \approx 90$
- Measure qubit frequency with a Ramsey sequence
- Use phase estimation algorithm to overcome dynamic range issue (phase wrapping)
- Sensitivity still limited by T_2 , i.e. 1/f flux noise



Qubit type	DC sensing	T2 noise spectroscopy (dynamical decoupling)	Scanning geometry	Advantages over [X]
Single-junction CPB $E_J/E_C \sim 1$	Charge: Spectroscopy only, limited by 1/f Flux: No	Charge: Low T2 makes time domain control difficult Flux: No	Charge: Seems doable Flux: --	Charge (X = SET): I don't see any Flux: --
CPB with SQUID $E_J/E_C \sim 1$	Charge, flux: Spectroscopy only, limited by 1/f, impractical measurement	Charge, flux: Low T2 makes time domain control difficult	Charge + Flux: Seems pretty hard	Charge (X = SET): I don't see any Flux (X = SQUID): I don't see any Charge + Flux (X = SET + Hall): I don't know
Offset charge-sensitive transmon $E_J/E_C \sim 10-20$	Charge: Spectroscopy or interferometry, limited by sample impedance or 1/f Flux: --	Charge: Yes, possibly limited by sample impedance Flux: --	Charge: Seems doable Flux: --	Charge (X = SET): Noise spectroscopy, can measure SC samples Flux: --
Tunable transmon $E_J/E_C \sim 50$	Charge: No Flux: Spectroscopy or interferometry	Charge: No Flux: Yes, requires fast control and readout	Charge: -- Flux: Seems doable	Charge: -- Flux (X = SQUID): Noise spectroscopy (is this more useful than a fast SQUID?)
Flux qubit	Charge: No Flux: Spectroscopy or interferometry	Charge: No Flux: Yes, requires fast control and readout	Charge: -- Flux: I don't know	Charge: -- Flux (X = SQUID): Noise spectroscopy (is this more useful than a fast SQUID?)