

1. Consider the following translation key:

$p$ : Human beings will arrive to Mars.

$q$ : Human beings build a ship capable of interplanetary flight.

Now, say whether the following statements are true or false:

- (a) ' $p \rightarrow q$ ' is the correct translation of 'Human beings will arrive to Mars only if human beings build a ship capable of interplanetary flight.'
  - (b) ' $p \rightarrow q$ ' is the correct translation of 'If human beings build a ship capable of interplanetary flight, then human beings will arrive to Mars.'
  - (c) ' $p \rightarrow \neg q$ ' is the correct translation of 'Human beings will arrive to Mars unless human beings build a ship capable of interplanetary flight.'
2. Which steps should I follow in order to translate an argument into propositional logic and determine whether it is valid?
  3. Translate the following arguments into propositional logic and determine whether they are valid:
    - (a) If God is all powerful, then God can make the number 5 even. But no human can make the number 5 even, and even if no human can make the number 5 even, God can make the number 5 even. Therefore, God is all powerful.
    - (b) I see a stopped clock that says '2pm' at 2pm. If I see a stopped clock that says '2pm' at 2pm, then I have a justified belief that it is 2pm. If I see a stopped clock that says '2pm' at 2pm, it is 2pm. If I have a justified belief that it is 2pm and it is 2pm, then

I know that it is 2pm. In conclusion, I see a stopped clock that says '2pm' at 2pm only if I know that it is 2pm.

- (c) Harry Potter exists unless I can truthfully say 'Harry Potter does not exist'. But if I can truthfully say 'Harry Potter does not exist', then I can say of an object that it has the property of not existing. And I cannot say of an object that it has the property of not existing. Therefore, Harry Potter exists.