

Two general *strategies* to keep in mind:

**Note:** these are just general strategies *not* rules.

$l$	$\phi \vee \psi$
$m$	$\neg \phi$
	$\vdots$
$n$	$\psi$

$l$	$\phi \rightarrow \psi$
$m$	$\neg \psi$
	$\vdots$
$n$	$\neg \phi$

### Exercises

1. If I am asked to prove an argument of the following form ' $\dots \vdash \phi$ ', should I start my proof by assuming  $\phi$ ? Why?
2. Offer a proof of the following argument:

$$(a) \ (p \rightarrow q) \wedge r, \neg((p \wedge q) \wedge (r \wedge s)), p \vdash \neg s$$

### Practice Quiz

Offer a proof of the following arguments in 20 minutes:

1.  $(p \wedge r) \vee (r \wedge s) \vdash r$
2.  $\neg((s \vee p) \vee q) \vdash \neg s \wedge \neg q$
3.  $p \rightarrow s, \neg(r \wedge q) \rightarrow \neg s \vdash p \rightarrow (r \wedge q)$
4.  $s \rightarrow (p \rightarrow r), p \wedge \neg r \vdash \neg s$
5.  $(p \vee q) \rightarrow r, \neg r \vdash \neg q \vee r$