

The Oblique Throw

2022-03-20

What is the project about?

When we throw a ball (ignoring wind resistance) when the ball leaves our hand we know the only acceleration acting upon the ball is the gravitational constant.

The simulations

For the simulations I used the following equations to get the distance that the ball travelled

Using this I wrote the following python code to simulate the throws

```
import math
import sympy

def calc_dist(v, a, h = 10):
    """
    Take in an velocity, angle and a height and calculate the distance it will travel
    """
    g = 9.82 # Gravitational constant
    x = sympy.Symbol('x')

    # Left side of the equation
    c1 = -1 * h

    # Right side of the equation
    c2 = v * math.sin(math.radians(a)) * x - 1/2 * g * x**2

    # Solve it, we can discard the negative solution
    t = max(sympy.solve(sympy.Eq(c1, c2), (x,)))
    s = v * math.cos(math.radians(a)) * t

    return s
```

Here is an example

```
print(calc_dist(15, 10), # Velocity: 15 m/s, angle: 10 degree
      calc_dist(20, 15), # Velocity: 20 m/s, angle: 15 degree
      calc_dist(5, 25)) # Velocity: 5 m/s, angle: 25 degree
```

```
## 25.3608136859927 39.5736277406020 7.51523973272992
```

I wrote a script to run this 22860 times but I won't go over that in this document, it's linked as `main.py`

Visualising the data

Let's first take a look at what type of data we are working with here

```
summary(data)
```

```
##      vel      ang      dist
## Min.   : 0.2   Min.   : 0.0   Min.   : 0.00505
## 1st Qu.:12.8   1st Qu.:22.0   1st Qu.: 15.00609
## Median :25.5   Median :44.5   Median : 46.72623
## Mean   :25.5   Mean   :44.5   Mean   : 66.86415
## 3rd Qu.:38.2   3rd Qu.:67.0   3rd Qu.:101.62410
## Max.   :50.8   Max.   :89.0   Max.   :272.61055
```

From taking a look at the summary we can see that the highest distance we reached was 272 meters with an average of 66

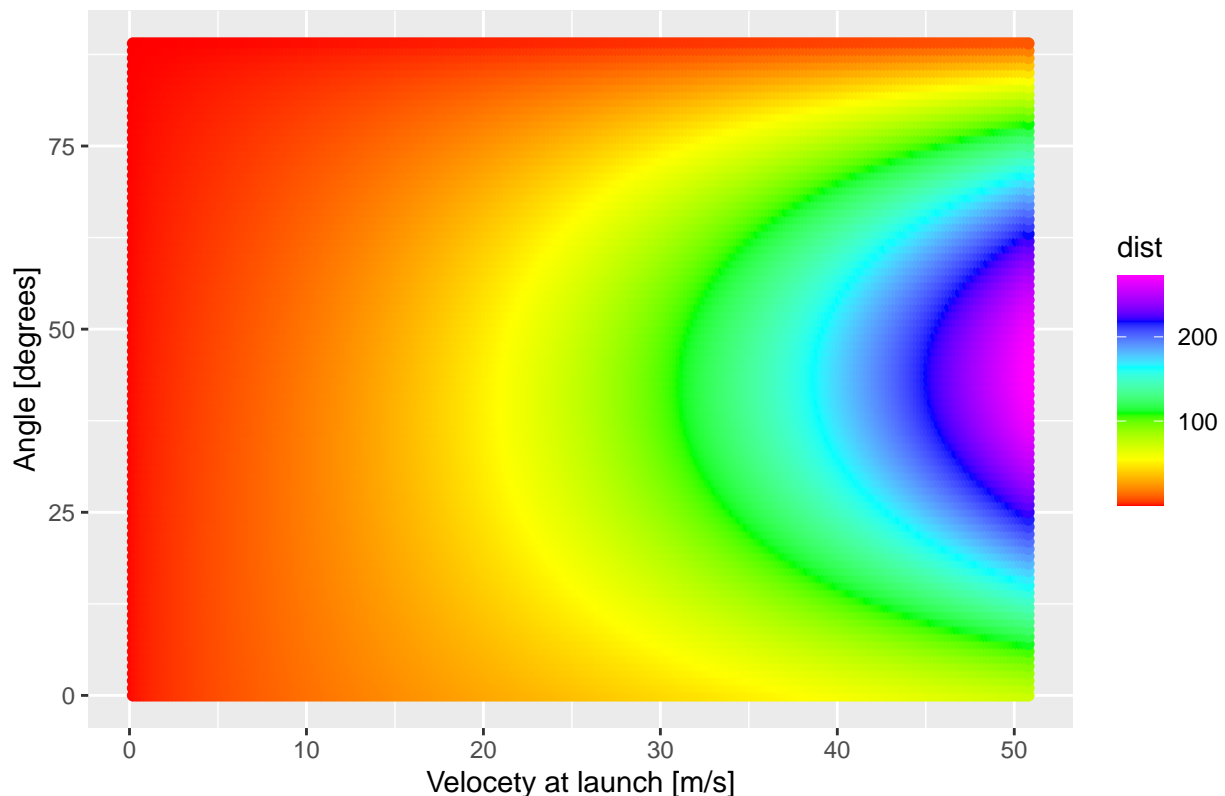
```
str(data)
```

```
## spec_tbl_df [22,860 x 3] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
## $ vel : num [1:22860] 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 ...
## $ ang : num [1:22860] 0 1 2 3 4 5 6 7 8 9 ...
## $ dist: num [1:22860] 0.285 0.285 0.285 0.285 0.285 ...
## - attr(*, "spec")=
## .. cols(
## ..   vel = col_double(),
## ..   ang = col_double(),
## ..   dist = col_double()
## .. )
## - attr(*, "problems")=<externalptr>
```

From the str function we get a preview of our data and we find that we have 22860 datapoints

Why not try and plot it?

The distance traveled corresponding to angle and velocity

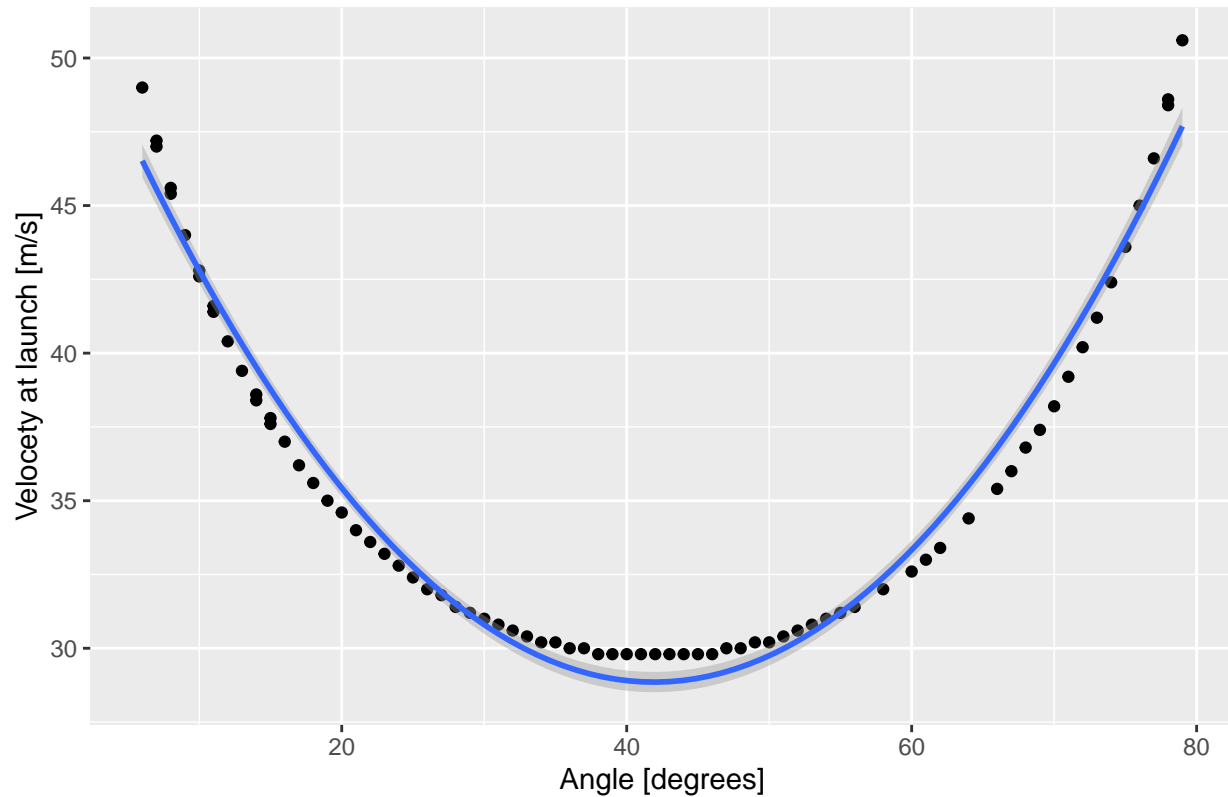


Now what can we do with this data?

Lets try to isolate a range of distances and with this range we can also try to use a regression

Here i got all the datapoints with a dist value between 99 and 100m

A slice of the above heatmap



From that parabola we find the formula to be $f(x) = 0.01369x^2 - 1.14801x + 52.91235$ with a r^2 value of 0.975, so quite a nice fit

My theory is that we can calculate the top of the parabola and find the optimal angle for all velocities when the height is 10

```
a <- 0.01369 # To get the point we are looking for we only need the a and b constants
b <- -1.14801
```

```
print((-1*b)/(2*a)) # -b/2a
```

```
## [1] 41.92878
```

So the optimal angle for the oblique throw when the height is 10m would be 41.93 degree