



heycoach

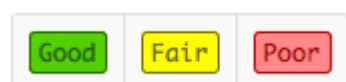
HeyCoach C++ DSA Cheat Sheet

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1.0 Data Structures

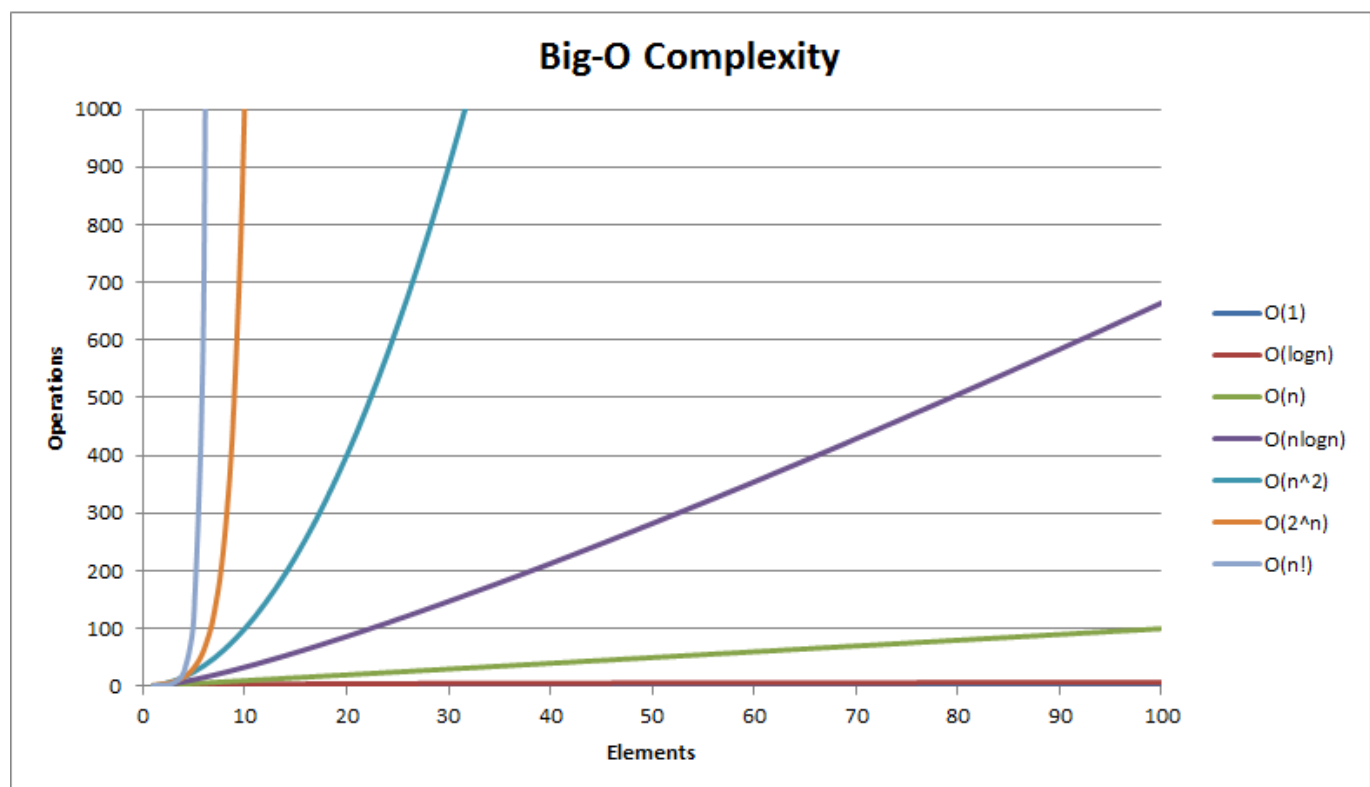
1.1 Overview

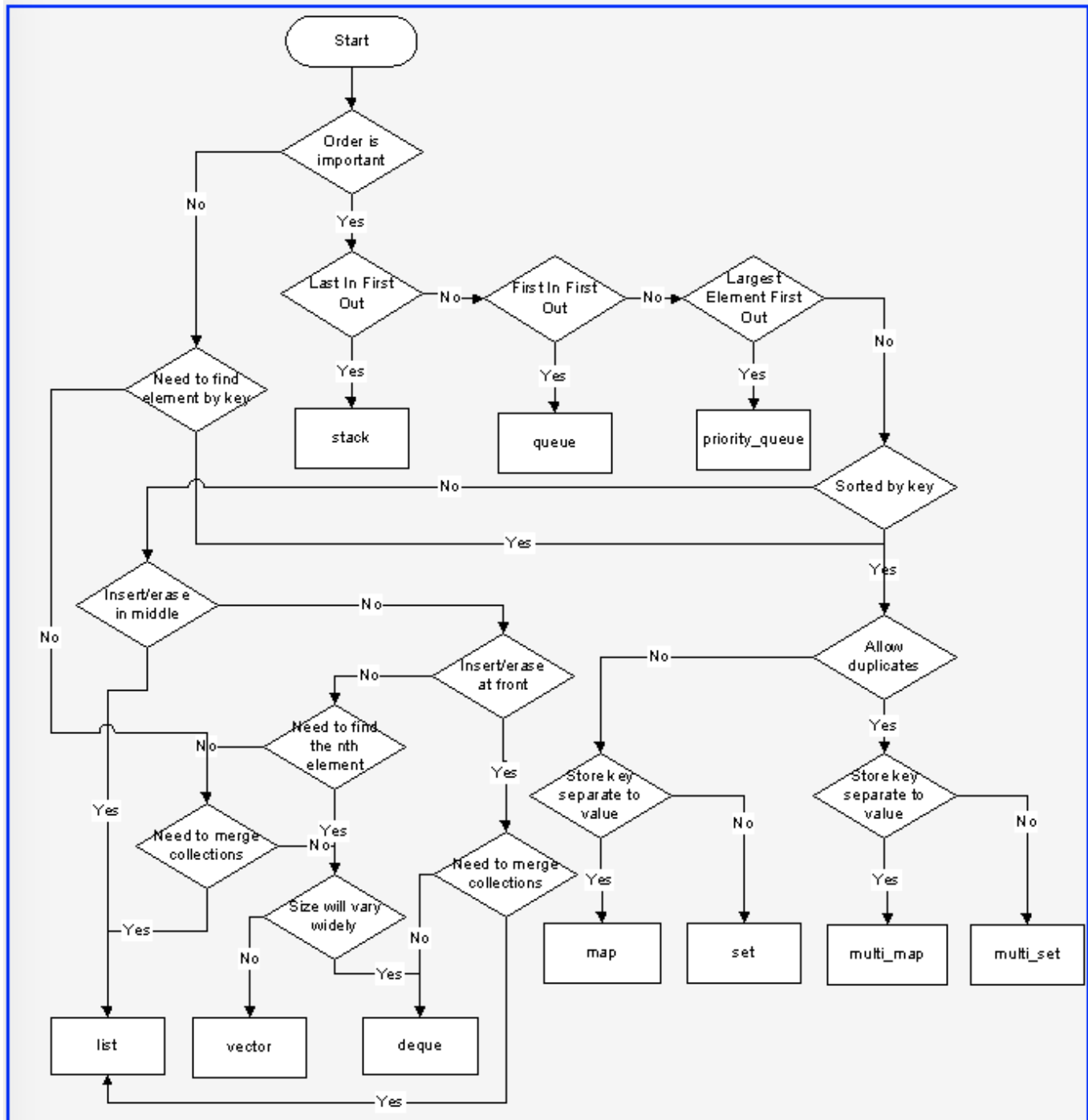


Data Structures

Data Structure	Time Complexity								Space Complexity
	Average				Worst				Worst
	Indexing	Search	Insertion	Deletion	Indexing	Search	Insertion	Deletion	
Basic Array	$O(1)$	$O(n)$	-	-	$O(1)$	$O(n)$	-	-	$O(n)$
Dynamic Array	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Singly-Linked List	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Doubly-Linked List	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Skip List	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n \log(n))$
Hash Table	-	$O(1)$	$O(1)$	$O(1)$	-	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Binary Search Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
Cartesian Tree	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	-	$O(n)$	$O(n)$	$O(n)$	$O(n)$
B-Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
Red-Black Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
Splay Tree	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
AVL Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$

Big-O Complexity Chart





1.2 Vector `std::vector`

Use for

- Simple storage
- Adding but not deleting
- Serialization
- Quick lookups by index
- Easy conversion to C-style arrays
- Efficient traversal (contiguous CPU caching)

Do not use for

- Insertion/deletion in the middle of the list
- Dynamically changing storage

- Non-integer indexing

Time Complexity

Operation	Time Complexity
Insert Head	$O(n)$
Insert Index	$O(n)$
Insert Tail	$O(1)$
Remove Head	$O(n)$
Remove Index	$O(n)$
Remove Tail	$O(1)$
Find Index	$O(1)$
Find Object	$O(n)$

Example Code

```
std::vector<int> v;

//-----
// General Operations
//-----

// Size
unsigned int size = v.size();

// Insert head, index, tail
v.insert(v.begin(), value);           // head
v.insert(v.begin() + index, value);   // index
v.push_back(value);                   // tail

// Access head, index, tail
int head = v.front();                 // head
head = v[0];                         // or using array style indexing

int value = v.at(index);              // index
value = v[index];                    // or using array style indexing

int tail = v.back();                  // tail
tail = v[v.size() - 1];              // or using array style indexing

// Iterate
for(std::vector<int>::iterator it = v.begin(); it != v.end(); it++) {
    std::cout << *it << std::endl;
}

// Remove head, index, tail
```

```

v.erase(v.begin());           // head
v.erase(v.begin() + index);   // index
v.pop_back();                 // tail

// Clear
v.clear();

```

1.3 Deque `std::deque`

Use for

- Similar purpose of `std::vector`
- Basically `std::vector` with efficient `push_front` and `pop_front`

Do not use for

- C-style contiguous storage (not guaranteed)

Notes

- Pronounced 'deck'
- Stands for **D**ouble **E**nded **Q**ueue

Time Complexity

Operation	Time Complexity
Insert Head	$O(1)$
Insert Index	$O(n)$ or $O(1)$
Insert Tail	$O(1)$
Remove Head	$O(1)$
Remove Index	$O(n)$
Remove Tail	$O(1)$
Find Index	$O(1)$
Find Object	$O(n)$

Example Code

```

std::deque<int> d;

//-----
// General Operations
//-----

// Insert head, index, tail
d.push_front(value);           // head

```

```

d.insert(d.begin() + index, value);    // index
d.push_back(value);                    // tail

// Access head, index, tail
int head = d.front();                  // head
int value = d.at(index);               // index
int tail = d.back();                  // tail

// Size
unsigned int size = d.size();

// Iterate
for(std::deque<int>::iterator it = d.begin(); it != d.end(); it++) {
    std::cout << *it << std::endl;
}

// Remove head, index, tail
d.pop_front();                         // head
d.erase(d.begin() + index);           // index
d.pop_back();                          // tail

// Clear
d.clear();

```

1.4 List `std::list` and `std::forward_list`

Use for

- Insertion into the middle/beginning of the list
- Efficient sorting (pointer swap vs. copying)

Do not use for

- Direct access

Time Complexity

Operation	Time Complexity
Insert Head	$O(1)$
Insert Index	$O(n)$
Insert Tail	$O(1)$
Remove Head	$O(1)$
Remove Index	$O(n)$
Remove Tail	$O(1)$
Find Index	$O(n)$

Operation	Time Complexity
Find Object	$O(n)$

Example Code

```

std::list<int> l;

//-----
// General Operations
//-----

// Insert head, index, tail
l.push_front(value);           // head
l.insert(l.begin() + index, value); // index
l.push_back(value);           // tail

// Access head, index, tail
int head = l.front();           // head
int value = std::next(l.begin(), index); // index
int tail = l.back();           // tail

// Size
unsigned int size = l.size();

// Iterate
for(std::list<int>::iterator it = l.begin(); it != l.end(); it++) {
    std::cout << *it << std::endl;
}

// Remove head, index, tail
l.pop_front();           // head
l.erase(l.begin() + index); // index
l.pop_back();           // tail

// Clear
l.clear();

//-----
// Container-Specific Operations
//-----

// Splice: Transfer elements from list to list
// splice(iterator pos, list &x)
// splice(iterator pos, list &x, iterator i)
// splice(iterator pos, list &x, iterator first, iterator last)
l.splice(l.begin() + index, list2);

// Remove: Remove an element by value
l.remove(value);

// Unique: Remove duplicates

```

```

l.unique();

// Merge: Merge two sorted lists
l.merge(list2);

// Sort: Sort the list
l.sort();

// Reverse: Reverse the list order
l.reverse();

```

1.5 Map `std::map` and `std::unordered_map`

Use for

- Key-value pairs
- Constant lookups by key
- Searching if key/value exists
- Removing duplicates
- `std::map`
 - Ordered map
- `std::unordered_map`
 - Hash table

Do not use for

- Sorting

Notes

- Typically ordered maps (`std::map`) are slower than unordered maps (`std::unordered_map`)
- Maps are typically implemented as *binary search trees*

Time Complexity

`std::map`

Operation	Time Complexity
Insert	$O(\log(n))$
Access by Key	$O(\log(n))$
Remove by Key	$O(\log(n))$
Find/Remove Value	$O(\log(n))$

`std::unordered_map`

Operation	Time Complexity
-----------	-----------------

Operation	Time Complexity
Insert	$O(1)$
Access by Key	$O(1)$
Remove by Key	$O(1)$
Find/Remove Value	--

Example Code

```
std::map<std::string, std::string> m;

//-----
// General Operations
//-----

// Insert
m.insert(std::pair<std::string, std::string>("key", "value"));

// Access by key
std::string value = m.at("key");

// Size
unsigned int size = m.size();

// Iterate
for(std::map<std::string, std::string>::iterator it = m.begin(); it != m.end();
it++) {
    std::cout << *it << std::endl;
}

// Remove by key
m.erase("key");

// Clear
m.clear();

//-----
// Container-Specific Operations
//-----

// Find if an element exists by key
bool exists = (m.find("key") != m.end());

// Count the number of elements with a certain key
unsigned int count = m.count("key");
```

1.6 Set `std::set`

Use for

- Removing duplicates
- Ordered dynamic storage

Do not use for

- Simple storage
- Direct access by index

Notes

- Sets are often implemented with binary search trees

Time Complexity

Operation	Time Complexity
Insert	$O(\log(n))$
Remove	$O(\log(n))$
Find	$O(\log(n))$

Example Code

```
std::set<int> s;

//-----
// General Operations
//-----

// Insert
s.insert(20);

// Size
unsigned int size = s.size();

// Iterate
for(std::set<int>::iterator it = s.begin(); it != s.end(); it++) {
    std::cout << *it << std::endl;
}

// Remove
s.erase(20);

// Clear
s.clear();

//-----
// Container-Specific Operations
//-----
```

```
// Find if an element exists
bool exists = (s.find(20) != s.end());

// Count the number of elements with a certain value
unsigned int count = s.count(20);
```

1.7 Stack `std::stack`

Use for

- First-In Last-Out operations
- Reversal of elements

Time Complexity

Operation	Time Complexity
Push	$O(1)$
Pop	$O(1)$
Top	$O(1)$

Example Code

```
std::stack<int> s;

//-----
// Container-Specific Operations
//-----

// Push
s.push(20);

// Size
unsigned int size = s.size();

// Pop
s.pop();

// Top
int top = s.top();
```

1.8 Queue `std::queue`

Use for

- First-In First-Out operations
- Ex: Simple online ordering system (first come first served)

- Ex: Semaphore queue handling
- Ex: CPU scheduling (FCFS)

Notes

- Often implemented as a `std::deque`

Example Code

```
std::queue<int> q;

//-----
// General Operations
//-----

// Insert
q.push(value);

// Access head, tail
int head = q.front();    // head
int tail = q.back();     // tail

// Size
unsigned int size = q.size();

// Remove
q.pop();
```

1.9 Priority Queue `std::priority_queue`

Use for

- First-In First-Out operations where **priority** overrides arrival time
- Ex: CPU scheduling (smallest job first, system/user priority)
- Ex: Medical emergencies (gunshot wound vs. broken arm)

Notes

- Often implemented as a `std::vector`

Example Code

```
std::priority_queue<int> p;

//-----
// General Operations
//-----

// Insert
p.push(value);
```

```
// Access
int top = p.top(); // 'Top' element

// Size
unsigned int size = p.size();

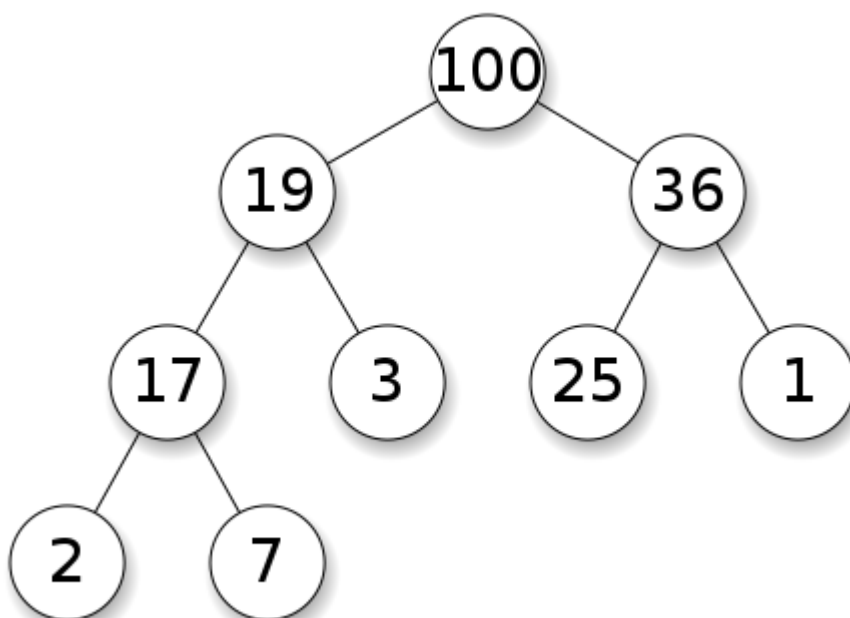
// Remove
p.pop();
```

1.10 Heap `std::priority_queue`

Notes

- A heap is essentially an instance of a priority queue
- A **min** heap is structured with the root node as the smallest and each child subsequently larger than its parent
- A **max** heap is structured with the root node as the largest and each child subsequently smaller than its parent
- A min heap could be used for *Smallest Job First* CPU Scheduling
- A max heap could be used for *Priority* CPU Scheduling

Max Heap Example (using a binary tree)



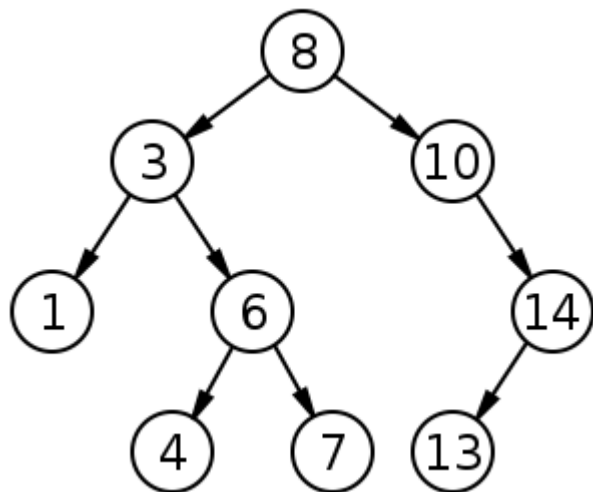
2.0 Trees

2.1 Binary Tree

- A binary tree is a tree with at most two (2) child nodes per parent

- Binary trees are commonly used for implementing $O(\log(n))$ operations for ordered maps, sets, heaps, and binary search trees
- Binary trees are **sorted** in that nodes with values greater than their parents are inserted to the **right**, while nodes with values less than their parents are inserted to the **left**

Binary Search Tree



2.2 Balanced Trees

- Balanced trees are a special type of tree which maintains its balance to ensure $O(\log(n))$ operations
 - When trees are not balanced the benefit of $\log(n)$ operations is lost due to the highly vertical structure
 - Examples of balanced trees:
 - AVL Trees
 - Red-Black Trees
-

2.3 Binary Search

Idea:

1. If current element, return
2. If less than current element, look left
3. If more than current element, look right
4. Repeat

Data Structures:

- Tree
- Sorted array

Space:

- $O(1)$

Best Case:

- $O(1)$

Worst Case:

- $O(\log n)$

Average:

- $O(\log n)$
-

2.4 Depth-First Search

Idea:

1. Start at root node
2. Recursively search all adjacent nodes and mark them as searched
3. Repeat

Data Structures:

- Tree
- Graph

Space:

- $O(V)$, V = number of vertices

Performance:

- $O(E)$, E = number of edges
-

2.5 Breadth-First Search

Idea:

1. Start at root node
2. Search neighboring nodes first before moving on to next level

Data Structures:

- Tree
- Graph

Space:

- $O(V)$, V = number of vertices

Performance:

- $O(E)$, E = number of edges
-

3.0 NP Complete Problems

3.1 NP Complete

- **NP Complete** means that a problem is unable to be solved in **polynomial time**
 - NP Complete problems can be *verified* in polynomial time, but not *solved*
-

3.2 Traveling Salesman Problem

3.3 Knapsack Problem

Implementation

4.0 Algorithms

4.1 Insertion Sort

Idea

1. Iterate over all elements
2. For each element:
 - Check if element is larger than largest value in sorted array
3. If larger: Move on
4. If smaller: Move item to correct position in sorted array

Details

- **Data structure:** Array
- **Space:** $O(1)$
- **Best Case:** Already sorted, $O(n)$
- **Worst Case:** Reverse sorted, $O(n^2)$
- **Average:** $O(n^2)$

Advantages

- Easy to code
- Intuitive
- Better than selection sort and bubble sort for small data sets
- Can sort in-place

Disadvantages

- Very inefficient for large datasets
-

4.2 Selection Sort

Idea

1. Iterate over all elements
2. For each element:
 - If smallest element of unsorted sublist, swap with left-most unsorted element

Details

- **Data structure:** Array
- **Space:** $O(1)$
- **Best Case:** Already sorted, $O(n^2)$
- **Worst Case:** Reverse sorted, $O(n^2)$
- **Average:** $O(n^2)$

Advantages

- Simple
- Can sort in-place
- Low memory usage for small datasets

Disadvantages

- Very inefficient for large datasets
-

4.3 Bubble Sort

Idea

1. Iterate over all elements
2. For each element:
 - Swap with next element if out of order
3. Repeat until no swaps needed

Details

- **Data structure:** Array
- **Space:** $O(1)$
- **Best Case:** Already sorted $O(n)$
- **Worst Case:** Reverse sorted, $O(n^2)$
- **Average:** $O(n^2)$

Advantages

- Easy to detect if list is sorted

Disadvantages

- Very inefficient for large datasets
 - Much worse than even insertion sort
-

4.4 Merge Sort

Idea

1. Divide list into smallest unit (1 element)
2. Compare each element with the adjacent list
3. Merge the two adjacent lists
4. Repeat

Details

- **Data structure:** Array
- **Space:** $O(n)$ auxiliary
- **Best Case:** $O(n \log(n))$
- **Worst Case:** Reverse sorted, $O(n \log(n))$
- **Average:** $O(n \log(n))$

Advantages

- High efficiency on large datasets
- Nearly always $O(n \log(n))$
- Can be parallelized
- Better space complexity than standard Quicksort

Disadvantages

- Still requires $O(n)$ extra space
 - Slightly worse than Quicksort in some instances
-

4.5 Quicksort

Idea

1. Choose a **pivot** from the array
2. Partition: Reorder the array so that all elements with values *less* than the pivot come before the pivot, and all values *greater* than the pivot come after
3. Recursively apply the above steps to the sub-arrays

Details

- **Data structure:** Array
- **Space:** $O(n)$
- **Best Case:** $O(n \log(n))$
- **Worst Case:** All elements equal, $O(n^2)$
- **Average:** $O(n \log(n))$

Advantages

- Can be modified to use $O(\log(n))$ space
- Very quick and efficient with large datasets
- Can be parallelized
- Divide and conquer algorithm

Disadvantages

- Not stable (could swap equal elements)
- Worst case is worse than Merge Sort

Optimizations

- Choice of pivot:
 - Choose median of the first, middle, and last elements as pivot
 - Counters worst-case complexity for already-sorted and reverse-sorted