6.6 Avoidance Concept

Summary: There is a need for a functional orchestration of previous concepts to achieve avoidance and navigation capabilities. The avoidance grid threat assessment done in (sec. ??) needs to be applied on the RSA of choice to produce a safe trajectory for one fixed time. This procedure is described in the avoidance grid run. There is a need to join output multiple avoidances runs over the time to achieve the required avoidance/navigation capabilities. This procedure is described in the navigation run. There is a need to assess the computational complexity of the approach to show implementation feasibility.

This section introduces *Platform Independent Avoidance Concept* core functionality (fig. ??) modules responsible for *pathfinding* and *navigation*. The sections are organized like follow:

- 1. Avoidance Grid Run (sec.6.6.1) (inner avoidance run) the best pathfinding in one Avoidance Grid with situation assessment done.
- 2. Mission Control Run (sec . 6.6.2) (outer navigation run) main navigation and decision making an algorithm for non-cooperative obstacle avoidance.
- 3. Computational Complexity (sec. 6.6.3) the computational feasibility study and weak point identification of our approach.

6.6.1 Avoidance Grid Run

Summary: Based on the provided threat assessment find the optimal trajectory in compliance with safety and given navigation goal.

Main Goal: The main goal of this section is to introduce the trajectory selection process, based on a *situation assessment*, originating from *Data Fusion Procedure* (sec. ??).

Note. The rating calculation is outlined in (sec. ??). Low-cost sensor fusion example usable to feed our data fusion procedure is given in [1]. Semi-optimal concatenation trajectory search like ours can be found in [2].

Note. The Sensor Fusion Procedure is solving all the following steps (sec. ??). The main purpose of Avoidance Run is finding the best path under certain conditions.

Space Assessment Principle: The *Avoidance Grid* is fed through *Data Fusion* (sec. ??). The process of *rating assessment* (tab. ??) is given in (fig. 6.1):

- 1. Obstacle detection (fig. 6.1a) assessment of detected obstacles (eq. ??). The red (O) cells have Detected obstacle set as true. The other threats: map obstacles (eq. ??), intruders (eq. ??), constraints (eq. ??) are false. The red (0) cells are representing $Occupied(t_i)$ (eq. ??) space in Avoidance Grid at decision time t_i .
- 2. Uncertainty assessment (fig. 6.1b) the uncertain cells are cells which status cannot be assessed. The Visibility (eq. ??) is low. The Uncertain cells (yellow (U) mark) are equal to Uncertain(t_i) (eq. ??) in Avoidance Grid in decision time t_i . The Constrained(t_i) (eq. ??) space is equal to \varnothing in this example.
- 3. Trajectory reachability evaluation (fig. 6.1c) the Reach Set given as Trajectory Set (eq. ??). is then projected through Avoidance Grid and pruned according to (def. ??). Reachable Trajectories (eq. ??) are only those contained in Free(t_i) space (eq. ??). The Reachable Trajectories are denoted as green lines. The Unreachable trajectory segments are denoted as red lines.
- 4. Cell reachability evaluation (fig. 6.1d) the evaluation of cells reachability is going according to (eq. ??). The Reachable cells are those which contains at least one Reachable Trajectory Segment.

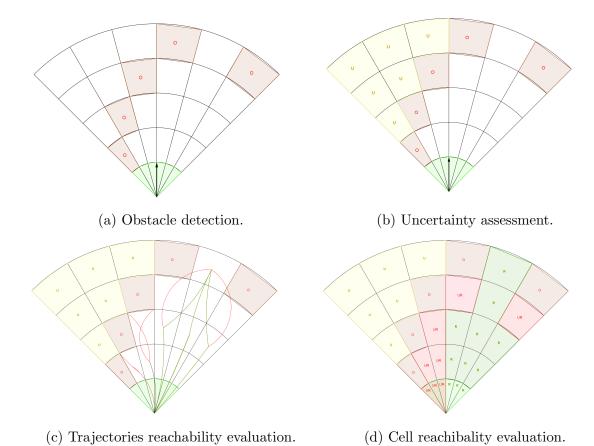


Figure 6.1: Significant steps of Avoidance grid run (inner loop).

Finding Best Path: ¹ Each $cell_{i,j,k}$ in Avoidance Grid at decision time t_i has assessed ratings according to data fusion procedure (tab. ??). The following properties are known prior the trajectory selection:

- 1. Reachability for each $cell_{i,j,k}$ (eq. ??).
- 2. Reachability for each $Trajectory(\circ)$ (eq. ??).
- 3. Free Space as non-empty set of cells in Avoidance Grid (eq. ??), with Reachable Space (eq. ??).
- 4. Goal Waypoint WP_G from Mission Control Run (sec. 6.6.2).

¹Avoidance Run Function Implementation: RuleEngine/MissionControl/MissionControl.m:: findBestPath(avoidanceGrid)

end

 $message = \emptyset;$

return [avoidancePath, message]

Algorithm 6.1: Find best *Path* in *Avoidance Grid* Input : Cell[] reachable (eq. ??), Waypoint goal, AvoidanceGrid (t_i) grid Output: Trajectory avoidancePath, Error message # Initialization & Reachability test; avoidancePath = \emptyset ; if $reachable == \emptyset$ then return [avoidancePath,"No path available, empty Reach Set"] end avoidanceCell = GetRandomCell(reachable); # Look for for goal cell; if $goal \in grid$ then # Goal is inside Avoidance Grid, Check if reachable; avoidanceCell = grid.selectCellXYZ(goal); if avoidanceCell.Reachable != true then return [avoidancePath," Waypoint not Reachable"] end else # Goal is outside Avoidance Grid, look for closest reachable $\text{cell}_{i,j,k}$; minimalDistance = distance(avoidanceCell,goal); for $cell_{i,j,k} \in reachable$ do if $distance(cell_{i,j,k},goal) < minimal Distance$ then if $isOuterCell(cell_{i,j,k})$ then avoidanceCell = $\operatorname{cell}_{i,j,k}$; end end endend # Reachable cell was found, Look for cheapest reachable trajectory; avoidancePath = GetRandomTrajectory(avoidanceCell); for $trajectory \in avoidance\ Cell\ \mathcal{EE}\ trajectory.Reachable == true\ \mathbf{do}$ if trajectory.Cost < avoidancePath.cost then avoidancePath = trajectory; end

The Algorithm (alg. 6.1) is based on shortest path search. Navigation is trying to reach goal waypoint; therefore it tries to shorten the distance between final trajectory cell

and goal waypoint. If there is reachable space two situations can occur:

- 1. Goal waypoint is inside the Avoidance Grid the avoidance cell is $\operatorname{cell}_{i,j,k}$ containing goal waypoint if reachable.
- 2. Goal waypoint is outside the Avoidance Grid the avoidance cell is the closest cell considered as an outer cell to goal waypoint.

The Avoidance Path selection is simple lowest cost selection of $Trajectory \in cell_{i,j,k}$.

Note. Outer cell is a $\operatorname{cell}_{i,j,k}$ which has at least one wall directly neighbouring with outer space $(Universe - KnownWorld(t_i))$. The outer cell is selected to prevent navigation to the trap.

Space Assessment Example: For better understanding, there is the following example of *space assessment* and *Best Path Selection*.

The *UAS* (blue plane) is following a *mission plan* in open space. Then there is a detection of a *collision situation* (fig. 6.2). The *Obstacle* is detected in the *top-right* Avoidance Grid corner.

The LiDAR hits are denoted as red filled circles. The Avoidance Grid space is constrained by the black dashed line. The Avoidance Grid is separated into five layers going from top to bottom. The Reach Set is projected as a set of Trajectories with colorization.

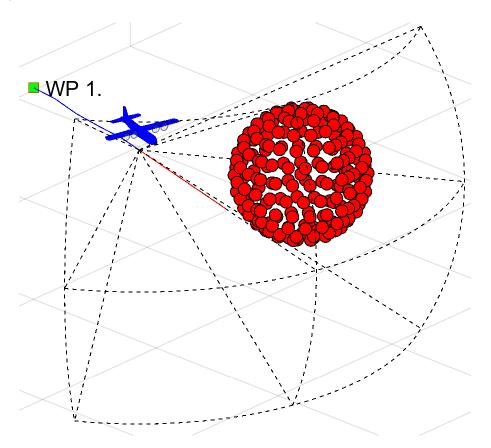


Figure 6.2: Example: The situation to be evaluated by Avoidance Run.

Visibility Assessment: The visibility assessment (fig. 6.3) divides the *Avoidance Grid* into two

- 1. Visible space (blue filled cells) is space through which LiDAR rays roamed freely until they hit an Obstacle.
- 2. *Uncertain space* (black filled cells) is space where no *LiDAR ray* passed nor hit. Therefore its status is uncertain.

Note. The detected obstacle cells are part of visible space because there is certainty about its containment.

The *Reach Set* trajectories are colored based on their visibility, blue for *uncertain* trajectories and *green* for visible trajectories.

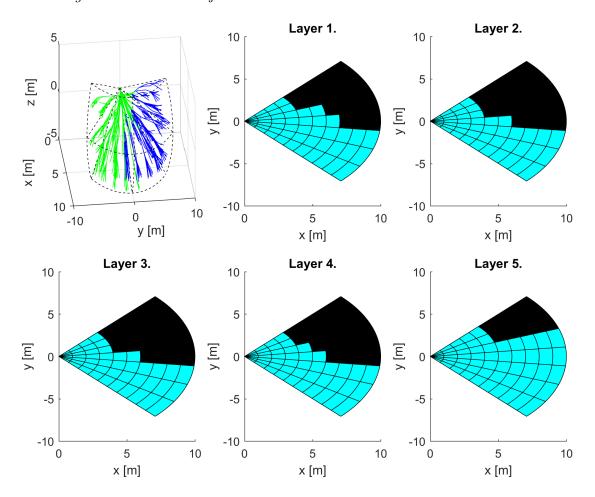


Figure 6.3: Example: The *Visibility* evaluation by *Avoidance Run*.

Reachability Assessment: For Each trajectory, the *Reachability* is assessed (fig. 6.4). The *Obstacle Space* and *Uncertain Space* are rendering *reachability*, effectively separating *trajectories* into two categories:

- 1. *Unreachable Trajectories* (red lines) there is at least one trajectory segment leading through *Obstacle* or *Uncertain* space.
- 2. Reachable Trajectories (green lines) all trajectory segments are lying in Free space.

Cells in Avoidance grid are divided in a similar matter, depending on the count of reachable trajectories passing through them:

- 1. Unreachable Cells (red fill) there is no trajectory through free space or the cell is not in free space.
- 2. Reachable cells (green fill) there is at least one feasible trajectory reaching free cell.

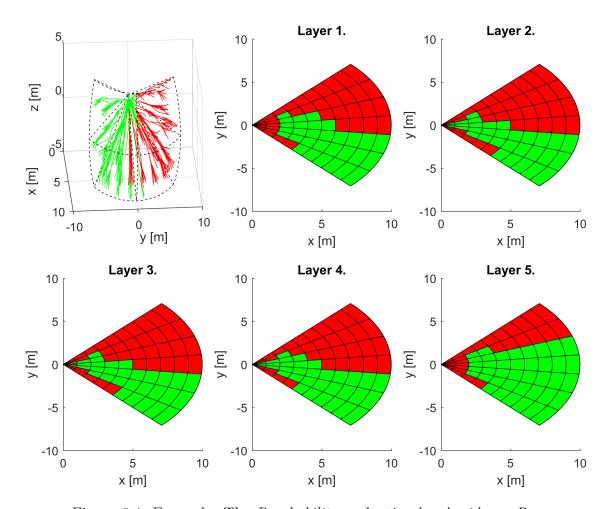


Figure 6.4: Example: The Reachability evaluation by Avoidance Run.

Note. The best avoidance path is selected form reachable outer cells (green fill in fig. 6.4), depending on goal waypoint according to (alg. 6.1).

6.6.2 Mission Control Run

Summary: Event-based navigation algorithm connecting results of the multiple Avoidance Grid Runs over time to generate a trajectory satisfying the mission. The concept of discrete future events is introduced to support the processing of various threats and commands. The overview of process description and thread orchestration is provided.

Introduction and Motivation: This section will introduce Navigation Concept using Reach Set Approximation. The Avoidance Framework Concept (fig. ??) defines Navigation Module as a sub-system for long term trajectory tracking. The Avoidance Grid Run (sec. 6.6.1) is solving the Path Search problem inside operation space constrained by Avoidance Grid for time t_i .

There is a need to build a trajectory between Waypoints which are further away than the distance of one Avoidance Grid. The UAS is controlled via Movement Automaton. The Movements which are in Movement Buffer can be replaced with other movements. This feature of Movement Automaton is called Movement Chaining (eq. ??).

To join the multiple *Avoidance Grids* paths following terminology needs to be established (fig. 6.5a):

- 1. Goal (Selecting Goal of Navigation) the point where UAS want to get in the global coordinate frame. The selection needs to be defined.
- 2. Next Decision the point when the next Avoidance Grid Run is applied. The outline of events and triggers is required. The decision will be made in the next decision time t_{i+1} .

The Avoidance Grid from UAS viewpoint can be separated into following zones (fig. 6.5b):

- 1. Crash Area (last layers) there is no place for safe return and the border of Avoidance Grid is near. The Decision Point needs to lie before this zone.
- 2. Avoidance Area (middle layers) the area of Active Avoidance Maneuvering. The Reach Set Approximation performance (sec. ??) is important in this area.
- 3. Safe Zone (first layers) there is space for safe return or damage mitigation.

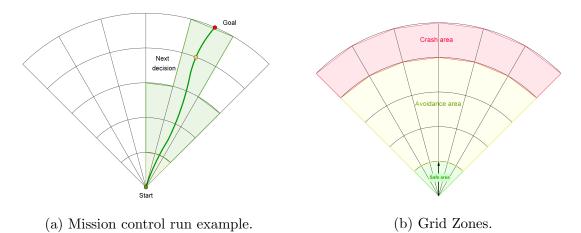


Figure 6.5: Definitions for *Mission Control Run* (outer loop).

Joining Avoidance Grid Runs (fig. 6.6) example portrays Avoidance Grid Runs invoked on various Decision Points to achieve Navigation functionality. The UAS (blue plane) is flying Mission (green numbered waypoints). The Avoidance Grid boundary (black dashed line) for each Decision Point (UAS position at time t_i). Following the example of Navigation (fig. 6.7) run is shown:

- 1. Mission Start (fig. 6.6a) UAS at the start of the mission have one Avoidance Grid at its position to determine the Navigation Path to Waypoint 2 (goal waypoint). The planned path (red line) is leading directly to Avoidance Grid boundary (black dashed line).
- 2. Mission End (fig. 6.6b) UAS have reached the last waypoint. All Avoidance Grid boundaries (black dashed line) for all runs are drawn along flown trajectory.
- 3. Waypoint Reach (fig. 6.6c) the waypoint is inside Avoidance Grid, the navigation path (red line) leads directly to goal waypoint. (Excessive Avoidance Grid boundaries are removed.)
- 4. Next Waypoint (fig. 6.6d) the new Goal Waypoint is selected, the UAS moves to new goal (invoking Avoidance Grid Runs when necessary).

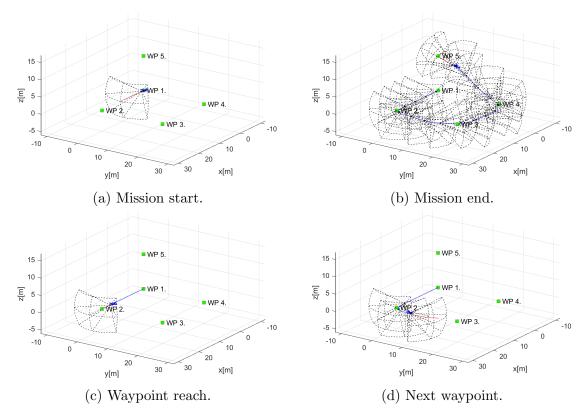


Figure 6.6: Joining multiple Avoidance Grid Runs to achieve Navigation.

General Concept: ² The *General Concept* is taken from [3, 4], consisting of following main modules:

- 1. Navigation Loop module responsible for Navigation providing Goal Waypoint.
- 2. Data Fusion (background in sec. ??) module responsible for Surveillance Data Feed.
- 3. Situation Assessment module responsible for UAS Safety Evaluation.
- 4. Avoidance Run (background in sec. 6.6.1) responsible for Avoidance Path selection.

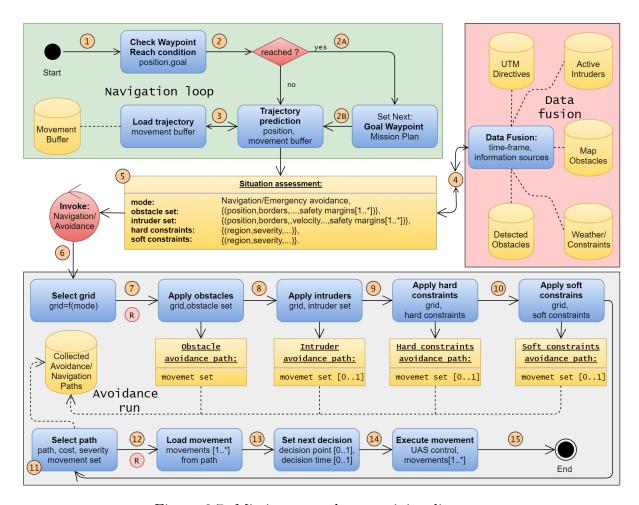


Figure 6.7: Mission control run activity diagram.

The main changes to *Navigation architecture* are given in *Mission Control Run* activity diagram (fig. 6.7):

- 1. Situation Assessment added event-based mode switching control.
- 2. Avoidance Run added hierarchical evaluation for Avoidance Path selection; This is responsible for prioritizing threat avoidance according to a type.

²Mission Control Run Function Implementation: RuleEngine/MissionControl/MissionControl.m::runOnce(.)

The Operation Mode is introduced, based on Situation assessment and Triggering Events one of the following modes are selected in Avoidance Run:

- 1. Navigation Mode the UAS is navigating through Airspace following cost-effective patterns and obeying Airspace Authority (UTM). The Navigation Grid is an instance of Avoidance Grid (sec. ??) with initialized Navigation Reach Set (ex. Turn-Minimizing Reach Set Approximation (sec. ??)).
- 2. Emergency Avoidance Mode the UAS is threatened by obstacle, intruder, hard constraint or soft constraint, the UAS is navigating through Airspace following safe avoidance patterns and minimizing the impact of possible damages. The Avoidance Grid is a term used for Emergency Avoidance Mode. The Avoidance Reach Set Approximation is initialized in Avoidance Grid (ex. Coverage-Maximizing Reach Set Approximation (sec. ??))

Note. Depending on Operation Mode the pair of Avoidance Grid and Reach Set is selected in Avoidance Run part.

The Navigation Grid and Avoidance Grid share the space portioning pattern; therefore the Data Fusion (sec. ??) needs to be evaluated only once for both grids.

Decision Time Frame ($[t_i, t_{i+1}]$): The Mission Control Run is executed for Decision Time Frame bounded to the period of the UAS executed movement (fig. ??).

The *UAS System* (sec. ??) controlled by *Movement Automaton Implementation* (sec. ??) *Planned Movements* can be changed at any time. The real impact on control is shown after the *actual movement* is executed.

Note. For our Movement Automaton Implementation movements, the average movement duration is 1/velocity second (tab. ??, ??).

The *Decisions* are made based on *system* state in *current* time-frame started at t_i for the *next* time frame starting at t_{i+1} .

Note. Because the Decision Delay is crucial in Avoidance System, it is beneficial to have short time movements. On the other hands, the length and duration of movements are impacting Reach Set Complexity. The proper construction of movement automaton is greatly impacting overall approach performance.

Initialization: The *UAS* is going to solve a problem for *Rules of the Air* (eq. ??). Using control scheme (fig. ??) with given *Sensors*:

$$Sensors = \{LiDAR, ADS - B\}$$

$$(6.1)$$

The sensors obstacle assessment into avoidance grid is outlined for static obstacles in (sec. ??) and for moving obstacles in (sec. ??.)

The Data Fusion Procedure is given as follow:

$$DataFusion = \{RatingBasedDataFusion \ (sec.??)\}$$
 (6.2)

Then the *UAS system* (sec. ??) with *Movement Automaton Implementation* (sec. ??) with empty movement buffer:

$$MovementBuffer = \{\}$$
 (6.3)

The Avoidance Grids for both Operation Modes are created with identical space segmentation. The Reach Set Approximations are loaded based on initial UAS State at decision time 0. The Reach Set Approximation is always selected based on UAS System State. The initial Operation Mode is set up as Navigation. The initialization is summarized like follow:

$$AvoidanceGrid(0) = \{UAS.position(0), AvoidanceReachSet(UAS.ReachSet)\}$$

$$NavigationGrid(0) = \{UAS.position(0), NavigationReachSet(UAS.ReachSet)\}$$

$$OperationMode = Navigation$$

$$(6.4)$$

The *Mission* is set up as a set of *ordered waypoints*. The *initial goal waypoint* is *first waypoint*. The initialization is summarized like follow:

$$Mission = \{Waypoint_1 \dots Waypoint_n\}$$

$$GoalWaypoint = Mission.waypoint_1$$

$$LastWaypoint = Mission.waypoint_n$$
(6.5)

The actual threats are set as empty sets for decision time $t_i = 0$:

$$obstacles = \{\}, intruders = \{\}, hardConstraints = \{\}, softConstraints = \{\} \quad (6.6)$$

Navigation Loop (1st-3rd step): The purpose of *Navigation Loop* is to select proper *Goal Waypoint* from *Mission* (sec. ??). If *last waypoint* have been reached the *Landing Procedure* will be initiated and *Mission Control Run* Ends.

First, start with the definition of waypoint reach condition (def. 1) and Unreachable waypoint (def. 2).

Definition 1. Waypoint Reach Condition for current decision time t_i for UAS position and current Goal Waypoint is satisfied only if:

$$distance(UAS.position(t_i), GoalWaypoint(t_i))$$

$$\leq \\ 2 \times \max \{length(movement) : \forall movement \in MovementSet \} \quad (6.7)$$

Note. The movements in our solution have a uniform length of 1 m (tab. ??, ??), therefore the waypoint reach condition is satisfied when the distance to goal waypoint is lesser than 2 m. The maximal movement length has an impact on navigation/avoidance precision.

Definition 2. Unreachable Waypoint. The Goal Waypoint evaluates as unreachable in decision time t_i when Avoidance Grid Run (alg. 6.1) cannot find the navigation/avoidance path leading to it.

Formally: The Avoidance/Navigation Grid has range defined as final layer distance. When the Goal Waypoint is in range of Grid:

$$Grid(t_i).range \ge distance(UAS.position(t_i), GoalWaypoint(t_i))$$
 (6.8)
and following condition is satisfied:

```
\forall cell_{i,j,k} \in Grid(t_i) \not\exists cell_{i,j,k}. Reachable == true \land \dots \\ \dots \land distance(cell_{i,j,k}, GoalWaypoint(t_i)) \leq \dots \\ \dots \leq 2 \times \max \{length(movement) : \forall movement \in MovementSet\}  (6.9)
```

The Goal Waypoint is unreachable.

Then the Navigation Loop is invoked every decision time t_i , Mission Control Run (fig. 6.7), it is described as a sequence of the following steps:

- 1st Check Waypoint Reach Condition the *UAS position* for given a *time frame* t_i is checked under condition (eq. 6.7). If the condition is met continue with 2nd step otherwise continue with 3rd step.
- 2nd Set Next Waypoint until the following condition is met:

$$GoalWaypoint == LastWaypoint$$

Set next goal waypoint like follow:

GoalWaypoint = Mission.getNextWaypoint()

Otherwise, enforce Landing sequence (Out of Scope).

3rd Trajectory Prediction - the *Movement Buffer* is loaded with planned movements from *Movement Automaton*. The *future trajectory* is predicted according to (eq. ??):

PredictedTrajectory =

$$Trajectory(state = UAS.state(t_i), buffer = futureMovements)$$

The Predicted Trajectory is used in 5th step Situation Assessment.

Data Fusion (4th step) The *Data Fusion* (sec. ??) in this context is *Threat Sets* preparation for *Avoidance Run*. It depends on the values of *Boolean values* defined in (tab. ??) for *threat* classification.

Note. Avoidance Grid's Data fusion (sec. ??) is run in the 7th- 10th step (fig. 6.7).

The static obstacles source is from LiDAR scan received at least at the beginning of current decision frame t_i :

$$obstacles = LiDAR.scan(UAS.position(t_i))$$

The intruder's source are valid active intruders notifications received from ADS-B In positioned to future expected positions at decision time t_{i+1} :

$$intruders = ADS - B.getActiveIntruders(t_{i+1})$$

Note. The Intruders needs to be predicted for the next decision time-frame starting at time t_{i+1} Due to their mobility.

The hard/soft constraints are obtained from Information Sources and the area of next decision time t_{i+1} Avoidance Frame is used as space parameter in the search. The sets of hard and soft constraints are obtained in the following manner:

 $hardConstraints = InformationSources.fuse(AvoidanceGrid(t_{i+1}))$

$$softConstraints = InformationSources.fuse(AvoidanceGrid(t_{i+1}))$$

The results of *Data Fusion* threats set preparation are used in the next step.

Invoke Navigation/Avoidance based on Situation Assessment (5th-6th step): The deciding events depending on Trajectory Prediction (3rd step) and Data Fusion (4th step) (fig. 6.7) are the following:

1. General Events are triggered regardless Operation Mode. They are considered after specific mode events are handled and Navigation/Avoidance Grid is selected:

- a. Empty Movement Buffer (MovementBuffer = \varnothing) if there is no movement in Movement buffer to be executed (from 3rd step: Load Trajectory), the Avoidance Run is enforced to run with Navigation/Avoidance Reach Set Approximation to generate the new path.
- b. Waypoint Reached (2nd step) the Navigation Loop run is forced to set goal Goal Waypoint. If the last waypoint from Mission (sec. ??) the Landing Procedure is enforced.
- c. Waypoint Unreachable this type of event is very situations based. The Waypoint Reachability (assumption. ??) has not been relaxed; therefore this event is not properly handled in approach. The implementation considers selecting next waypoint in the mission as a goal waypoint of the first waypoint if unreached/unreachable waypoints are exhausted.
- 2. Navigation Mode Events are triggered if Operation Mode is set as Navigation:
 - a. Empty Navigation Grid (|threats| = 0) if movement buffer contains at least one movement, the Avoidance Run is omitted. The Operation Mode stays in Navigation Mode.
 - b. Collision Case Resolution (|ActiveCollisionCases| > 0) there is new/active Collision Case (sec. ??), the Navigation Reach Set Approximation trajectories will be constrained according to active Collision Case(s) requirements. If there exists at least one Reachable avoidance path, the Operation Mode will remain Navigation. If there is no Reachable avoidance path, the Operation Mode switches to Emergency Avoidance.
 - c. Static Obstacle Detection (LiDAR.Hits > threshold) if static obstacle set contains at least one detected obstacle (eq. ??) intersecting with Navigation grid the Operation Mode will be switched to Emergency Avoidance Mode.
 - d. Intruder Detection (intruders > 0) if active intruders set contains at least one intruder which expected impact area (intersection models (app. ??)) Navigation grid the Operation Mode will be switched to Emergency Avoidance Mode.
 - e. Hard or Soft Constraint Occurrence ($|hardConstraints| > 0 \lor |softConstraints| > 0$) if hard/soft constraint set contains at least one constraints which intersects (static constraints (sec. ??), moving constraints (def. ??)) Navigation grid the Operation Mode will be switched to Emergency Avoidance Mode.
- 3. Emergency Avoidance Events are triggered if Operation Mode is set as Emergency Avoidance:
 - a. $Empty\ Avoidance\ Grid\ (|threats|=0)$ if there is no detectable threat, the remainder of $avoidance\ path$ is removed from $Movement\ Buffer$. The $Operation\ Mode$ is switched to Navigation, and new $navigation\ path$ is selected.

 ${f 5^{th}}$ Situation Assessment - if there is any flag raised by *Event Triggers*, there is an avoidance situation.

The Event Triggers describe complex Operation Mode switching. The simplified principle is the following: If UAS is in Emergency Avoidance Mode Always Invoke Avoidance Run. If UAS is in Navigation Mode Invoke Only if Necessary.

If there was event trigger continue with 7^{th} step, otherwise, wait for next decision time t_{i+1} , execute movement and continue with 1^{st} step.

6th Invoke Navigation/Avoidance depending on the Operation Mode the Reach Set/Grid pair is selected. The future $state(t_{i+1})$ in next decision frame t_{i+1} is necessary for Grid/Reach Set initialization. The next decision frame initial state is obtained by prediction:

$$state(t_{i+1}) = Trajectory(state(t_i), currentMovement)$$

The Reach Set Approximation is loaded based on mode and $state(t_{i+1})$. The Grid is initialized as $Free(t_{i+1})$ (eq. ??) for all cells.

Avoidance Run (7th-15th step): The Avoidance Run goal is to obtain Path represented as $Trajectory(state(t_{+1},MovementBuffer))$ (eq. ??) from Navigation/Avoidance Grid and associated Navigation/Avoidance Reach Set Approximation.

If the Operation Mode is set as Navigation Mode, the algorithm continues with the 11th step. Otherwise, the Avoidance Grid Space Assessment is run multiple times to obtain $Reachable(t_{i+1})$ (eq. ??). The Threat Data obtained from the 4th step are used.

7th Apply Obstacles - The *Space assessment* (tab. ??) for *Avoidance Grid* is calculated with following threat modification:

$$intruders = \varnothing, softConstraints = \varnothing, hardConstraints = \varnothing$$

The Find Best Path (alg. 6.1) is applied, the resulting avoidance path is labeled as Obstacle Avoidance Path.

8th Apply Intruders - The Space assessment (tab. ??) for Avoidance Grid is calculated with following threat modification:

$$softConstraints = \varnothing, hardConstraints = \varnothing$$

The Find Best Path (alg. 6.1) is applied, the resulting avoidance path is labeled as Intruders Avoidance Path.

9th Apply Hard Constraints - The Space assessment (tab. ??) for Avoidance Grid is calculated with following threat modification:

$hardConstraints = \emptyset$

The Find Best Path (alg. 6.1) is applied, the resulting avoidance path is labeled as Hard Constraint Avoidance Path.

10th Apply Soft Constraints - The *Space assessment* (tab. ??) for *Avoidance Grid* is calculated without any modification.

The Find Best Path (alg. 6.1) is applied, the resulting avoidance path is labeled as Soft Constraints Avoidance Path.

Note. The 7th to 10th steps are code-optimized for efficient calculation.

11th Select Path - based on Operation Mode the Navigation/Avoidance Path is selected.

The Navigation Path for Navigation Mode is selected by a standard Find Best Path (alg. 6.1) procedure. The Navigation Reach Set Approximation can be constrained by Rule Engine (fig. ??).

The Avoidance Path for Emergency Avoidance Mode is selected from Collected Avoidance Paths with the following priority:

- 1. Soft Constraints Avoidance Path if exists continue with 12th step, if does not exist try to select:
- 2. Hard Constraints Avoidance Path if exists continue with 12th step, if does not exist try to select:
- 3. Intruders Avoidance Path if exists continue with 12th step, if does not exist try to select:
- 4. Obstacle Avoidance Path continue with the 12th step.

Note. The Waypoint Reachability (assumption ??) is weakened to the point that it is necessary for the waypoint to be Reachable only in static obstacle environment. The Constrained and Occupied spaces are shrunk in the following matter to increase UAS survival chances. There are following relaxations with their conditions:

- 1. Soft Constraint Relaxation they are breakable by default. This kind of situation is allowed to happen under any circumstances.
- 2. Hard Constraints Relaxation they can be broken in case of emergency (airspace constraints) or UAS robust build (Weather Constraints). This kind of situation is allowed under very specific conditions depending on broken constraint severity.

- 3. Intruder Occupied Space Relaxation this can be broken if and only if there is guarantee the Intruder dynamic and navigation algorithm allows to avoid Collision with UAS. This relaxation should be used as the last resort.
- 12th Load Movements the Movement Buffer is flushed for future decision times t_{i+1}, \ldots, t_{i+k} . The Navigation/Avoidance Path movements are pushed into Movement Buffer instead. The executed movement for decision time t_i remains (because movement is executed at this time point).
- 13th Set Next Decision the next decision point is set depending on circumstances:
 - 1. Navigation Mode (no active collision cases) Decision Point is set as the point before UAS enters into Crash Zone (fig. 6.5b) in Navigation Grid.
 - 2. Navigation Mode (at least one active collision case) Decision Point is set after next movement execution. Current decision point $UAS.Position(t_i)$, next decision point $UAS.Position(t_{i+1})$.
 - 3. Emergency Avoidance Mode (any circumstances) Decision Point is set after the next movement execution. Current decision point $UAS.Position(t_i)$, next decision point $UAS.Position(t_{i+1})$.
- 14th Execute Movement the *First Movement* from *Movement Buffer* is loaded to be executed in decision time frame $[t_{i+1}, t_{i+2}]$.
- 15th Finish Avoidance Run if the *UAS* is flying, continue with 1st step.

Decision Frame: The mission control run (fig. 6.7) describes the overall process in sequence. The orchestration overview is given in (fig. 6.8).

The key idea is to explain what happens in one decision frame. The mission control run is implemented as multi-thread application which sends the signals between threads. Each thread is the semi-independent process with forced synchronization on decision frame switch.

The notable threads and their roles & responsibilities are summarized like follow:

- 1. Sensor Fusion responsible for processing real-time sensor array (sec. ??). The output is a partial known world assessment (sec. ??). Obstacle detection and intruder detection events can be risen by this thread.
- 2. Data Fusion responsible for enhancing data from sensor fusion by mixing data originating from information sources (sec. ??). The information sources used in this work contains constraints originating from geo-fencing, weather, airspace restrictions. This thread is delayed by sensor fusion. A data fusion procedure strongly depends on the operational space context (controlled/non-controlled airspace). The output of data fusion is full known world assessment (sec. ??, ??). The UTM-related and constraint related events can arise from data fusion.

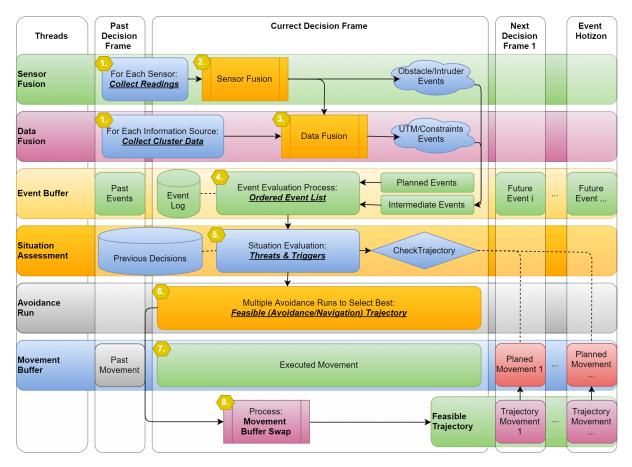


Figure 6.8: Mission control orchestration diagram.

3. Event Buffer - special data structure to store, raise, handle, prioritize events raised by other threads.

The *implemented events* are listed in the 5^{th} - 6^{th} step of *mission control run*. The events can be categorized like follow:

- a. *Planned events* raised in previous decision frames to be executed in actual or future *decision frame*.
- b. Intermediate events raised in actual decision frame by other threads to be solved intermediate.

The event buffer thread executes following event-related activities:

- a. Storing the events are stored in the event log. The trace is useful for process and rules fine-tuning.
- b. Raising the combination of events (multiple avoidance events) (example sec. ??) can trigger additional avoidance behavior in the form of combined-event.
- c. *Handling* the events are handled by invoking the *situation assessment* or by rule engine invocation (sec. ??).
- d. *Prioritizing* the multiple events can rise during one *decision frame*. Some events cannot be merged and need to have proper prioritization before handling, like the *obstacle detection* events before *intruder detection event*.

- 4. Situation Assessment invoked by event buffer to assess the situation, responsible for proper avoidance run (sec. 6.6.1) dataset preparation and invocation. The main responsibility is to check planned trajectory feasibility stored in movement buffer as planned movements.
- 5. Avoidance Run invoked by necessity to plan trajectory originating from event buffer or situation assessment threads. The avoidance run produces one or multiple avoidance/navigation feasible trajectories according to the 7th-11th step of mission control run.
- 6. Movement Buffer represents movement automaton implementation (sec. ??). The movement automaton consumes movement automaton buffer each decision frame contains exactly one movement. The movements can be viewed as:
 - a. Past movements already executed movements in past decision frames.
 - b. *Executed movement* actually executed movement in the current decision frame, this movement cannot be changed.
 - c. Future movements future planned movements to be executed after current decision frame expires. These movements outline planned trajectory (predictor mode sec. ??).
- 7. Feasible Trajectory consists of future planned movements taking place directly after the correct decision frame. If its necessary, the planned trajectory in movement buffer is no longer feasible, the planned movements will throw away and replaced by trajectory movements.

The roles & responsibilities of each thread have been explained to outline their orchestration and roles in mission control run (fig. 6.7). The numbered steps in (fig. 6.8) shows the threads orchestration in the following manner:

- 1. Sensor & Data fusion data set preparation/collection the sensor readings are collected through multiple past and over current decision frame. Each sensor reading is filtered and processed according to best practices.
 - The raw information from various data sources is loaded for relevant space clusters. The relevant space clusters are determined based on UAS expected position.
- 2. Sensor fusion the readings from sensors are preprocessed according to (sec. ??, ??).
- 3. Data fusion the information sources are preprocessed according to (sec. ??, ??).
- 4. Event evaluation process the events are evaluated, if there is any triggering event $(5^{\text{th}}-6^{\text{th}}$ mission control run steps) the situation evaluation process is called.

- 5. Situation evaluation process the situation is evaluated according to $5^{\rm th}$ - $6^{\rm th}$ mission control run steps.
- 6. Feasible trajectory selection process from collected navigation/avoidance trajectories (7th-10th mission control run steps). If there are more feasible trajectories (increasing threat) the one compliant with most of the threats is selected.
- 7. Movement execution the movement for the current decision frame is being executed.
- 8. Movement buffer swap if there is a new feasible trajectory the future movements for next decision frames are flushed away. The movement buffer is then filled with feasible trajectory movements.

Note. This step impacts the duration of future decision frames.

6.6.3 Computational Complexity

Summary: Brief approach computational complexity analysis considering navigation/control/data fusion in support of real-time application feasibility.

Introduction: The *Computational Complexity* one mission control run assessment is necessary to identify the strong and weak points of approach. Let us get through modules to assess notable calculations/algorithms complexity on high abstraction level.

Navigation Loop: On the navigation loop, the waypoint reach condition (eq. 6.7) is checked, this is a unitary operation with worst complexity O(1). The selection process of the next Goal Waypoint can get through all waypoints in the mission if they are all unreachable the complexity is O(|waypoints|).

The *notable steps* complexity is following:

Reach Condition: O(1)

Select Next Waypoint: O(|waypoints|)

Data Fusion: The data fusion is all about threat selection.

If UAS is in *controlled airspace*, it needs to iterate over received *collision Cases* to select *active ones*. The complexity of this step is linear; therefore boundary is given as O(|collisionCases|).

Thresholding Detected Obstacles is done by simple comparison of LiDAR ray hits in given $cell_{i,j,k}$ of Avoidance Grid.

Any loading of threats from information sources depends on clustering. The Airspace Clustering is considered as static for our setup. Therefore the count of active airspace clusters has the main impact on complexity. The count of information sources is static and not changing over mission time. Information sources usually implement Hash search function with complexity $O \ln |searchedItemSet|$.

The *computational complexity* boundaries for *Data fusion* in our setup are following:

Select Active Collision Cases: O(|collisionCases|)

Threshold Detected Obstacles: O(|cells|)

Load Map Obstacles: $O(\ln|activeClusters| \times |informationSources|)$ Load Hard Constraints: $O(\ln|activeClusters| \times |informationSources|)$ Load Soft Constraints: $O(\ln|activeClusters| \times |informationSources|)$

Note. The real-time clustering is a hard non-polynomial problem [5]. Usually, all information sources and sensor have polynomial complexity of processing. The controlled airspace clusters are usually set for a very long period. Therefore Obstacle Map, Airspace Constraints, and, Weather Constraints can be considered as preprocessed

Situation Assessment: The *Situation Assessment* is evaluating triggering events. The *evaluation* is usually simple existence question without further calculations. The *complexity* of *event evaluation* for our case is O(1). There are *eight* triggers. The count of *triggers* needs to be accounted in complexity boundary:

$$O(|triggers| \times eventEvaluationComplexity)$$

Note. The trigger calculation complexity needs to stay low because the triggers are verified every Mission Control Run. The Avoidance Run trigger frequency should be very low under normal conditions.

Avoidance Run: The *Avoidance run* is the most critical part of *Mission Control Run* because of *Avoidance Path* calculation. The *Navigation Path* calculation is less complex (Rule engine is not accounted); therefore *Emergency Avoidance Mode* is assumed.

The threat insertion is realized in 7^{th} to the 10^{th} step. The first is Avoidance Grid filled with Static Obstacles. The Avoidance Grid is designed to separate rotary LiDAR ray space into hit count even cells. Insertion of LiDAR scan into Avoidance Grid complexity depends on total cell count. The upper boundary for insert obstacles is given like follow:

Insert Obstacles:
$$O(|cells|)$$

The intruders intersection model type impact the insertion complexity. The linear intersection (app. ??) is going through the maximum of layers count cells.

The body volume intersection model (app. ??) can check the simple intersection condition overall Avoidance Grid in the worst case; therefore complexity for this check is bounded by a count of cells.

The Maneuverability Uncertainty Intersection (app. ??) can hit all cells in Avoidance Grid. The calculation complexity boundary is exponential depending on the horizon-tal/vertical spread in [rad]. The intersection implementation was done ad-hoc. The impact of intersection application is visible only when there are more than four concurrence intruders (fig. ??).

The *complexity boundary for* intruder insertion is given like follow:

Note. The intruder intersection is critical in non-controlled airspace. The main complexity gain in controlled airspace is from rule application. Our rule complexity is in the worst case depending on Reach Set node count, and Active Collision Cases count.

Apply Our Rules: $O(|activeCollisionCases| \times |nodes|)$

For *Hard/Soft Constraints* The algorithm used for intersection polygons was selected based on a study [6], the selected algorithm *Shamos-Hoey* [7]. The *calculation complexity* boundary is given like follow:

Hard Constraints Intersection:

$$O(|cells| \times |hardConstraints| \times \max |constraintPoints|^2)$$

Soft Constraints Intersection:

$$O(|cells| \times |softConstraints| \times \max |constraintPoints|^2)$$

Each threat category application in Mission Control Run is done after each intersection in 7th to the 10th step. All ratings (tab. ??) expect Reachability(cell_{ij,k}) and Reachability(Trajectory) are calculated. The calculation complexity boundary for one reachability rating is O(1). (eq. ??, ??). The Recalculate Reachability operation applied $4\times$ have maximal complexity boundary given as follow:

Recalculate Reachability:
$$O(4 \times (|nodes| + |cells|))$$

Each time at the end of in 7th to the 10th step the *Avoidance Path is Selected*. The *Worst Case* (expected) scenario is to *select* four paths for each *threat* application. The algorithm for *best path selection* (alg. 6.1) iterates overall *cells* in avoidance grid and over all *trajectories* passing through that cell. The complexity boundary for *path selection* is given as follow:

Select Path:
$$O\left(4 \times \left(|cells| + \frac{|nodes|}{|cells|}\right)\right)$$

Conclusion: Overall approach complexity is *low*. If proper *Information Sources* with efficient clustering and *intersection models for intruders* are used, the approach will stay within *non-polynomial complexity*. The average load time for *testing scenarios* is summarized in (tab. ??).

Note. The calculation of Reach Set is eliminated by pre-calculation for state range [8].

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