

## 7.3. Non-cooperative test cases

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The *main* goal of this section is to show operative capabilities for *non-cooperative avoidance mode* in *emergency* and *solo situations*.

Test avoidance capabilities against *static obstacles*, *non-cooperative intruders*, *moving hard constraints* are covered.

Coverage of the *soft constraints*, *map obstacles*, and *detected obstacles* are implicitly covered due to the properties of *safety* and *body margins* (tab. ??).

1. *Building Avoidance* (sec. 7.3.1) covers *static obstacles* explicitly and *map obstacles, hard constraints, ground avoidance* implicitly.
2. *Slalom* (sec. 7.3.2) covers *open space navigation capabilities*, showing the determinism of the *avoidance loop run*, in addition to *building avoidance*.
3. *Maze* (sec. 7.3.3) covers *closed space navigation capabilities*, showing the higher level navigation properties of primitive *right-side* 2D maze solver. The main point is to show the possibility to enrich the *Navigation loop algorithm* (fig. ??).
4. *Storm* (sec. 7.3.4) covers *hard moving constraints avoidance* explicitly and *hard static constraints, soft static constraints, soft moving constraints* implicitly.
5. *Emergency converging scenario* (sec. 7.3.5) covers *non-cooperative intruder with the right of way avoidance capability*.
6. *Emergency head-on scenario* covers (sec. 7.3.6) *non-cooperative intruder without right of way avoidance capability*
7. *Emergency mixed scenario* (sec. 7.3.7) covers *multiple intruders with/without right of the way avoidance capability*.

### 7.3.1. Building avoidance

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**Scenario:** The *UAS* is flying the mission given by (tab. 7.1) in the *open space environment*. There exists a map of obstacles with defined *safety and body margins*. *Reference trajectory* (direct interconnection of waypoints) is going through partially known space with some charted obstacles.

Position		Waypoints			
$[x, y, z]$	$[\theta, \varpi, \psi]$	$\mathcal{WP}_1$	$\mathcal{WP}_2$	$\mathcal{WP}_3$	$\mathcal{WP}_4$
$[0, 0, 0]^T$	$[0^\circ, 0^\circ, 0^\circ]^T$	$[100, 0, 0]^T$	$[100, 100, 0]^T$	$[0, 100, 0]^T$	$[0, 0, 0]^T$

Table 7.1: Mission setup for *Building avoidance* scenario.

**Obstacle set:** Obstacles are discovered during a flight by *UAS LiDAR sensor*, the set of obstacles is defined in (tab. 7.2).

Obstacle			Body Margin			Safety Margin
id	position	type	min.	max.	avg.	
1	$[50, 0, 0]^T$	polygonal	14	20	16	5
2	$[100, 50, 0]^T$	hospital	12	18	14	7
3	$[50, 100, 0]^T$	unusual	10	20	15	8
4	$[0, 50, 0]^T$	square	18	20	19	4

Table 7.2: *Obstacle set for Building avoidance scenario.*

**Main Goal:** Show *static obstacle avoidance capability* in an *open space environment*, using *LiDAR scanning* and *obstacle map* as the *information sources*.

#### Acceptance criteria:

1. Proper *algorithm mode switch*:
  - a *Avoidance mode* is active when the *UAS* is nearby to the obstacle (*distance* (*obstacleCenter*, *UASPosition*)  $\leq 20m$ ).
  - b *Navigation mode* is active when the *UAS* is further away from any obstacle (*UAS* is actively converging to *goal waypoint*).
2. *Minimal safety margin distance*  $\geq 0m$
3. *Reach each waypoint* (tab. 7.1) in the given order.

**Testing Setup:** The *standard test setup* defined in (tab. ??, ??, ??, ??, ??) is used with following parameter override:

1. *Avoidance grid - type - ACAS-like with horizontal enabled maneuvers*

*Note.* Enforced *safety margin* does not exceed the *avoidance grid range* (10 m). The concept of *Static obstacle avoidance* is in detail discussed in the *progress report* [1].

**Simulation Run:** Notable moments from the *simulation run* (fig. 7.1) are the following:

1. *1<sup>st</sup> building avoidance.* (fig. 7.1a) - UAS avoids the building from the left side because overall trajectory cost is cheaper. The first building is a convex obstacle.
2. *2<sup>nd</sup> building avoidance.* (fig. 7.1b) - UAS avoids the building from the right side while avoiding an active non-convex portion of the building.
3. *3<sup>rd</sup> building avoidance.* (fig. 7.1c) - UAS avoids the building from the right side, missing both traps from it.

4. 4<sup>th</sup> building avoidance. (fig. 7.1d) - UAS avoids the building from the right side. This building is also a convex obstacle.

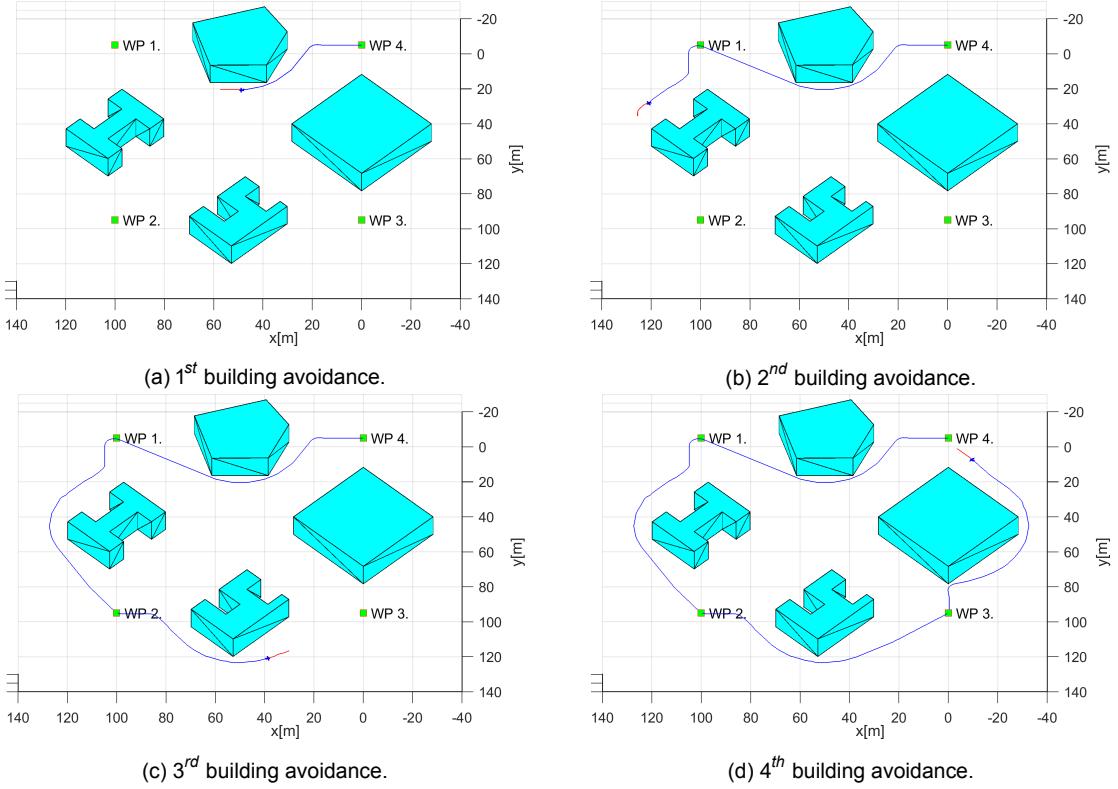


Figure 7.1: Test scenario for *Building avoidance* (static ground obstacles).

**Distance to Body/Safety Margin Evolution:** The distance of *UAS* center to the nearest obstacle (blue) does not break a *safety margin* (of the closest obstacle (yellow)) nor *body margin* of the closest obstacle (red) as it can be seen in (fig. 7.2). *Acceptance condition for algorithm mode switch* can be shown by *UAS active avoidance of obstacles*.

*Note.* The *body* and *safety margins* are changing depending on *UAS position and orientation*, is changing reflecting (tab. 7.2) margins.

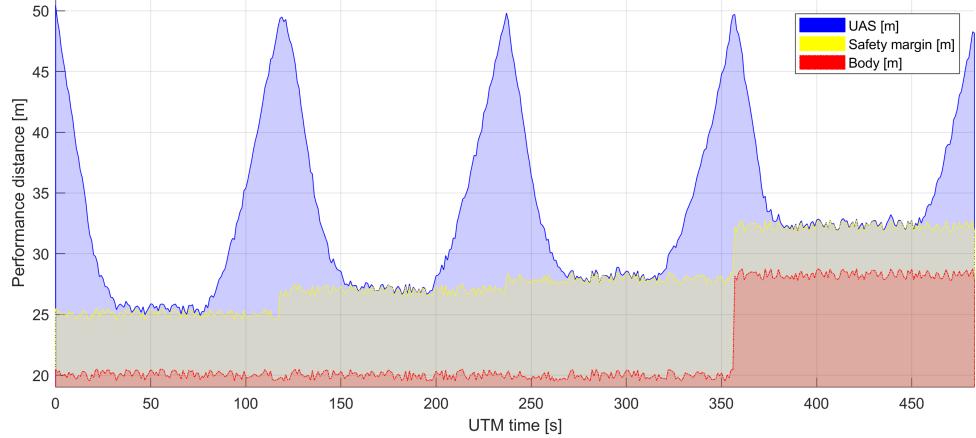


Figure 7.2: Distance to body/safety margin evolution for *Building avoidance scenario*.

**Distance to Body/Safety Margin Peaks:** Minimal distance to *safety margin* is 0.69 m. The *minimal distance to obstacle body* is 4.69 m which is more than sufficient for tested UAS type. *Safety margin acceptance criteria* have been achieved because the minimal distance is greater than zero. The minimal *body margin distance* is 4.69 m for obstacle no. 4 (tab. 7.2).

Parameter	UAS 1	
Distance to Safety Margin	min	0.69
	max	24.98
Distance to Body Margin	min	4.69
	max	29.98

Table 7.3: Distance to Body/Safety Margin Peaks for *Building avoidance scenario*.

**Path Tracking Performance:** Reference path (green dashed line) is given as direct interconnection between waypoints (green numbered square). The real trajectory (solid blue line) is split into its XYZ components. *All mission waypoints* (fig. 7.3) have been reached in the given order. There are some deviations on X – Y horizontal axes, while the UAS was in the *avoidance mode*.

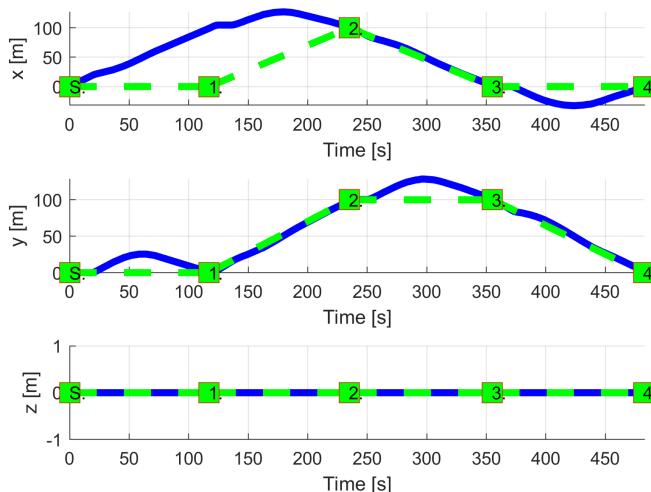


Figure 7.3: *Building avoidance path tracking*.

**Path Tracking Deviations:** Deviations (tab. 7.4) from the *reference trajectory* are in expected ranges considering the *mission plan* (tab. 7.1) and *obstacle properties* (tab. 7.2).

Param.	UAS 1			
	$\mathcal{WP}_1$	$\mathcal{WP}_2$	$\mathcal{WP}_3$	$\mathcal{WP}_4$
$\max x $	104	86	5.34	32.52
$\max y $	25.39	6.59	28.2	4.55
$\max z $	0	0	0	0
$\max dist.$	107.05	86.2	28.7	32.84

Table 7.4: Path tracking for properties *Building avoidance*.

**Computation Load:** The *computation load* for scenario (fig.7.4) shows used time (y-axis) over decision frame (x-axis).

There is a slight increase in *computation time* when UAS is in *Emergency Avoidance Mode*.

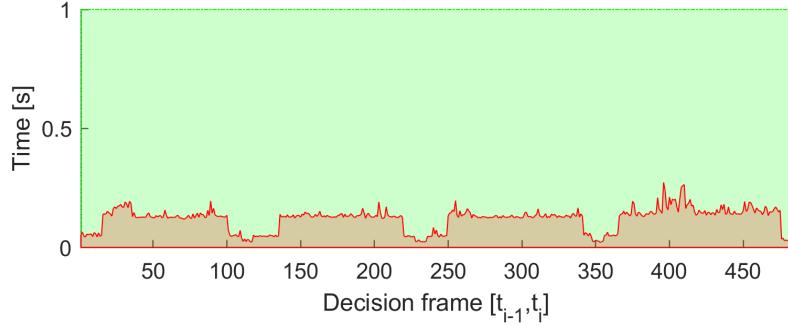


Figure 7.4: Computation time for *Building avoidance* scenario.

### 7.3.2. Slalom

**Scenario:** The *UAS* is flying the mission given by (tab. 7.5) in the *open-space environment*. An Operational space is more clustered than in the case of *Building Avoidance* (sec. 7.3.1). This map of notable *buildings* with defined *safety and body margins* imposing additional flight constraints. The *UAS* is flying through partially known space with some charted obstacles.

The *goal waypoint* is hidden behind the sensors line of sight. There are multiple cost equivalent trajectories to reach the goal.

Position			
$[x, y, z]$	$[\theta, \varpi, \psi]$		$WP_1$
$[25, 5, 0]^T$	$[0^\circ, 0^\circ, 90^\circ]^T$		$[35, 75, 0]^T$

Table 7.5: Mission setup for *Slalom* scenario.

**Obstacle set:** Obstacles are discovered during a flight by *UAS LiDAR Sensor*. The set of obstacles is defined in (tab. 7.6) Some obstacles does not have *Line of Sight* during a flight, which causes additional constraints during the *avoidance trajectory selection* process.

Obstacle	Body Margin			Safety Margin	
	position	type	min.	max.	avg.
multiple (4)	hospital	[0.5, 1]	[2.2, 3.1]	[1.5, 3]	[1, 3]
multiple (7)	unusual	[0.3, 1]	[2.3, 3.5]	[2, 3]	[1, 4]
multiple (3)	square	[3, 4]	[4, 5]	[4, 5]	[1, 4]

Table 7.6: *Obstacle set* for *Slalom* scenario.

**Main goal:** Show *static obstacle avoidance* in a *clustered environment* with *shorter decision frames* due to the obstacle density. Show *hidden waypoint navigation capability* and *Behind Line of Sight* impact on decision making.

**Acceptance Criteria** are given as follow:

1. *Hidden waypoint reach* - the UAS will safely reach *goal waypoint*.
2. *Minimal safety margin distance*  $\geq 0$ .
3. *Hindered space* is accounted into decision making (BLOS impact).

**Testing setup:** The *standard test setup* defined in (tab. ???. ???. ???. ???. ???. ???) is used with following parameter override:

1. *Avoidance grid - type - ACAS-like with horizontal enabled maneuvers*

*Note.* The *vertical separation* was disabled because *UAS* will increase its altitude to reach *goal waypoint*.

**Simulation run:** Notable moments from this *simulation run* (fig. 7.5) are the following:

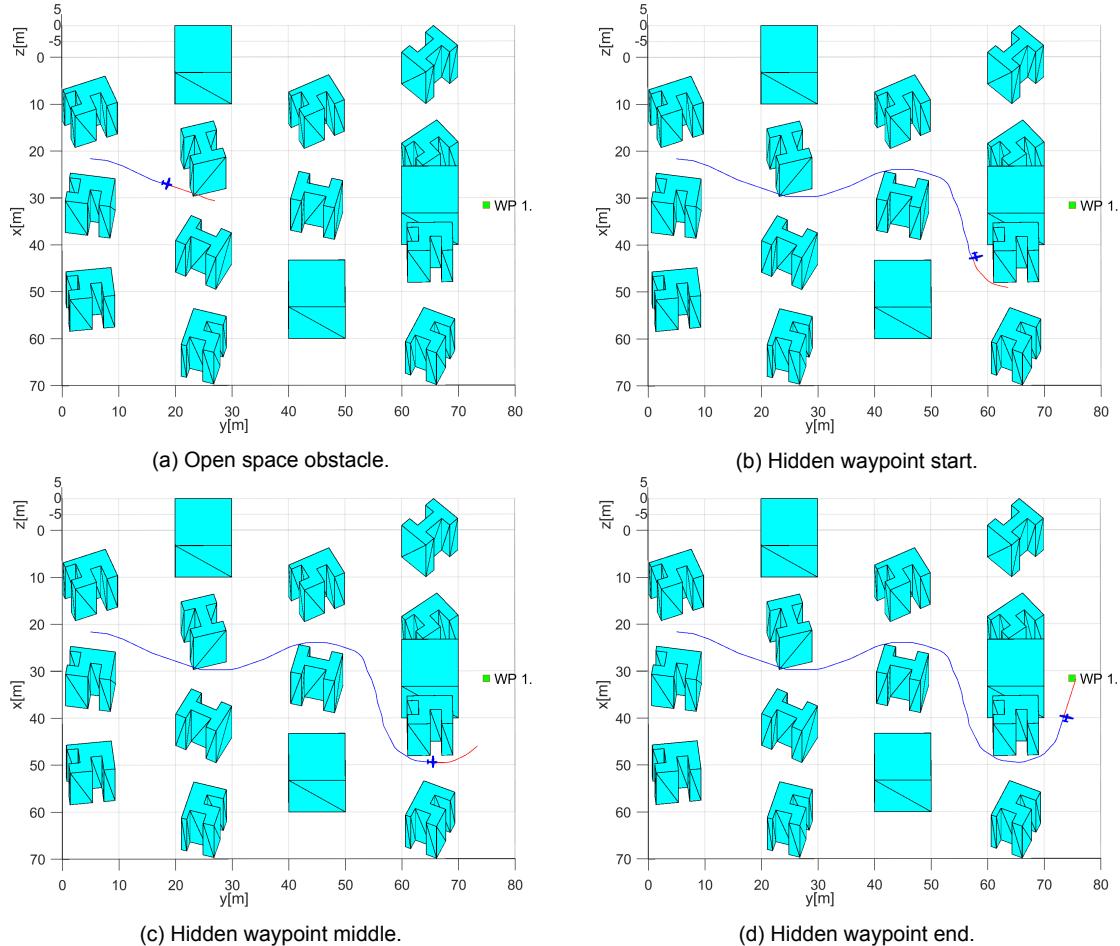


Figure 7.5: Test scenario for *Slalom* with a *hidden waypoint*.

1. *Open space obstacle* (fig. 7.5a) - avoidance of open space obstacle, while tracking *hidden waypoint*. This is standard navigation procedure, the middle building in front of *goal waypoint* is hidden by building in front of UAS.
2. *Hidden waypoint navigation* is shown in three stages start (fig. 7.5b), middle (fig. 7.5c), and end phase (fig. 7.5d). The *hidden goal waypoint* has been reached, and first acceptance criteria were fulfilled. The *Decision points* of the navigation loop are placed in

very high density around this area. The avoided building had following traps which were avoided:

- a. Trap (fig. 7.5b) on the left side of UAS was avoided because there was no turning point inside of space.
- b. Trap (fig. 7.5c) on the left side of UAS was avoided because it was not wide enough to be considered as trajectory space.

**Distance to Body/Safety Margin Evolution:** The *UAS* (blue fill) does not break a *safety margin* (yellow fill) nor *body margin* (red fill) as you can see in (fig. 7.6). Hindered space is accounted into decision making because the distance to closest obstacle will never breach *safety margin* (yellow fill). If it was not, the UAS would break *safety* or *body* margin.

*Body and Safety margin* is changing values depending on the *nearest obstacle* and *mutual position of obstacle and UAS*. The ranges of *body* and *safety margins* are reflected in (tab. 7.6).

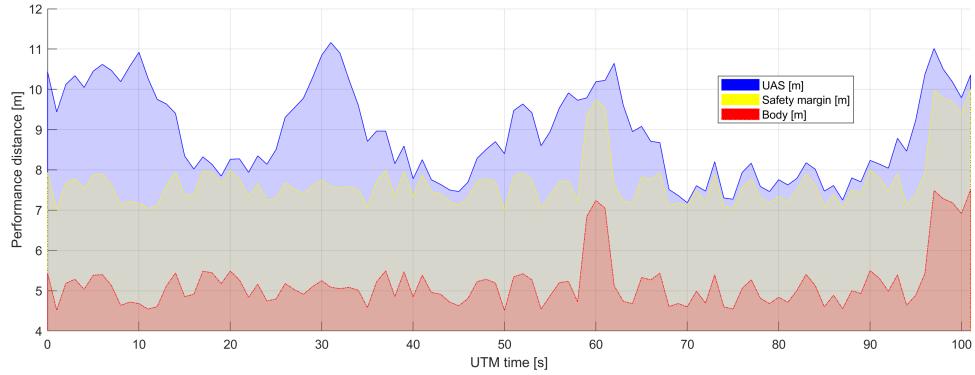


Figure 7.6: Distance to body/safety margin evolution for *Slalom scenario*.

**Distance to Body/Safety Margin Peaks:** The *UAS* distance to the boundary of *safety* and *body margin* is given in (tab. 7.7). The minimal distance of *UAS border*(blue line) to *safety margin boundary* (yellow line fig. 7.6) is 0.0856 m which can be considered as marginal 0. The minimal *body margin* distance is 2.5856 m; it takes into account *safety margin* of 2.5 m. The condition *safetyMarginDistance*  $\geq 0$  holds.

The difference between minimal and maximal *safety margin distance* is  $\sim 3$  m which indicate that the mission environment is tightly packed with obstacles.

Parameter	UAS 1	
Distance to Safety Margin	min	0.0856
	max	3.7391
Distance to Body Margin	min	2.5856
	max	6.2391

Table 7.7: Distance to body/safety margin peaks for *Slalom scenario*.

**Path tracking performance:** Path tracking is given in (fig. 7.7). The line between a Starting position (green square, marked S) and goal waypoint (green square marked 1) is reference trajectory (green dashed line). The flown trajectory (blue solid line) is showing evolution over

mission time (Time [s]) in global coordinate frame split into three axes ( $x[m]$ ,  $y[m]$ ,  $z[m]$ ). The UAS was all time in *Emergency Avoidance Mode* due to the vicinity of dangerous obstacles.

The UAS reached final navigation waypoint, which fulfills acceptance criteria. The UAS has taken a significant detour ( $x[m]$  evolution) due to the hidden *waypoint*.

The test has been run multiple times to check if *Right-Up* preference for avoidance is always selected. *Small noise* (0.5-1m) was added to obstacle positions. The algorithm always chose a similar deterministic path. The higher noise levels were not possible due to the obstacle original size (tab. 7.6).

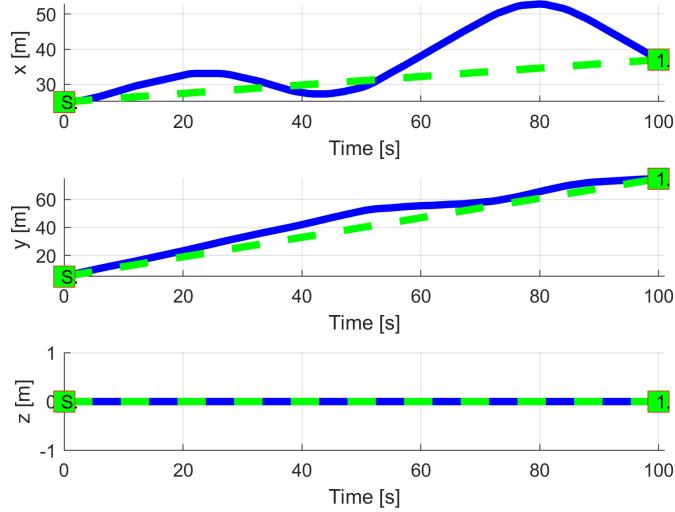


Figure 7.7: *Slalom* path tracking.

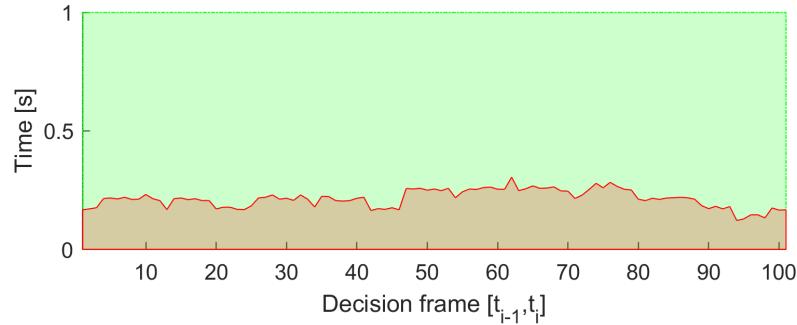
**Path Tracking Deviations:** Deviations given in (tab. 7.8) from *reference trajectory* (fig. 7.7) are in expected ranges considering the *mission plan* (tab. 7.5) and *obstacle properties* (7.6).

Param.	UAS 1
	$\mathcal{WP}_1$
$\max x $	17.90
$\max y $	12.41
$\max z $	0
$\max dist.$	20.06

Table 7.8: Path tracking properties for *Slalom* scenario.

**Computation Load:** The *computation load* for scenario (fig.7.8) shows used time (y-axis) over decision frame (x-axis).

The UAS is moving over *semi-clustered* environment the *computation load* is almost constant.

Figure 7.8: Computation time for *Slalom* scenario.

### 7.3.3. Maze

**Scenario:** The UAS is flying a mission given by (tab. 7.9) in *closed space* constrained by ground from the bottom, airspace constraint from top and building from sides. The maneuverable space is *maze-like* with *hidden goal waypoint*.

There exists an *Obstacle map* with defined *safety* and *body margins*. *Reference trajectories* (direct interconnection of the initial position and *goal waypoint*) is going through *partially known space* with some charted obstacles.

Position		$\mathcal{WP}_1$
$[x, y, z]$	$[\theta, \varpi, \psi]$	
$[15, 15, 0]^T$	$[0^\circ, 0^\circ, 0^\circ]^T$	$[15, 75, 0]^T$

Table 7.9: Mission setup for *Maze* scenario.

**Obstacle set:** *Obstacles* are discovered during a flight by *UAS LiDAR* sensor. The *Obstacle set* is defined in (tab. 7.10). The obstacles are placed in a *virtual grid* with *cell size*  $10 \times 10m$ . There are following obstacles:

1.  $5 \times$  *Hospital building* - H-shaped, with two open traps, with minimal body margin in the range  $0.5 - 1m$ , with maximal body margin in the range  $2.2 - 3.1m$  and variable *safety margin* in the range  $1 - 3m$ .
2.  $12 \times$  *Unusual trap building* - square-shaped building with two traps on the neighbouring side, with minimal body margin in the range  $0.3 - 1m$ , with maximal body margin in the range  $2.3 - 3.5m$  and variable *safety margin* in the range  $1 - 4m$ .
3.  $6 \times$  *Square building* - square-shaped building with minimal body margin in the range  $3 - 4m$ , with maximal body margin in the range  $4 - 5m$  and variable *safety margin* in the range  $1 - 4m$ .
4.  $7 \times$  *U-shaped Trap* - thin walled U shaped trap designed to catch incoming flying objects, with minimal body margin in the range  $2 - 4m$ , maximal body margin in the range  $3 - 5m$  and various *safety margin* in the range  $1 - 2m$ .

The purpose of these *Obstacles* except *Square building* type is to create false positive path diversions. These diversions are designed to take *UAS* into an unsolvable situation. *Avoidance*

of traps is possible due *Reach set properties* because many scenarios for avoidance can be evaluated at once.

Obstacle		Body Margin			Safety Margin
position	type	min.	max.	avg.	
multiple (5)	hospital	[0.5, 1]	[2.2, 3.1]	[1.5, 3]	[1, 3]
multiple (12)	unusual	[0.3, 1]	[2.3, 3.5]	[2, 3]	[1, 4]
multiple (6)	square	[3, 4]	[4, 5]	[4, 5]	[1, 4]
multiple (7)	trap	[2, 4]	[3, 5]	[2, 4]	[1, 2]

Table 7.10: Obstacle set for Maze scenario.

**Main Goal:** Demonstrate static obstacle avoidance in closed space navigation. Focus on determinism of *avoidance run*. Demonstrate the possibilities of primitives *right-hand* maze solver incorporated into *Navigation-loop*.

#### Acceptance Criteria:

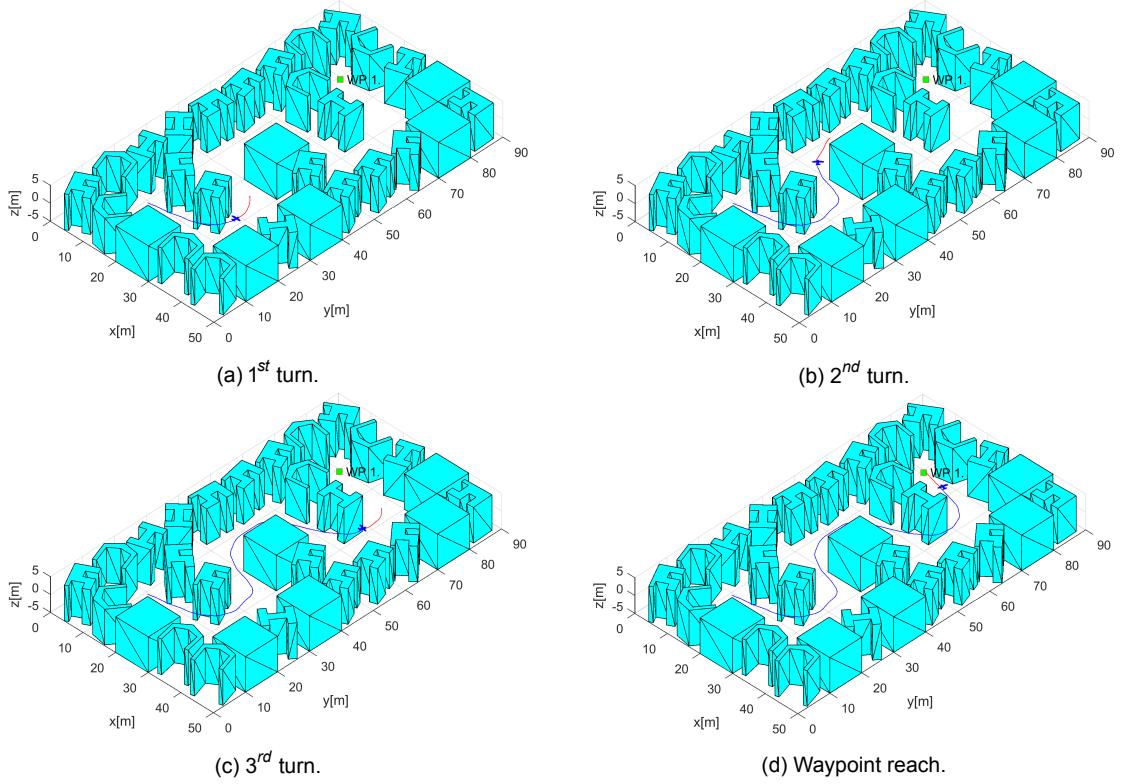
1. *Do not break top/bottom boundaries* - the UAS Z coordinate should not leave range  $-5$  to  $5m$ . The boundary break occurs when there is no feasible horizontal path, and UAS needs to climb up to resolve the situation.
2. Minimal safety margin distance  $\geq 0m$ .
3. *Reach hidden goal waypoint* by solving simple maze (tab. 7.9).

**Testing Setup:** The *standard test setup* defined in (tab. ??, ??, ??, ??, ??) is used with following parameter override:

1. *Avoidance grid - type - ACAS-like with horizontal enabled maneuvers*

**Simulation Run:** Notable moments from the simulation run (fig. 7.9) are the following:

1. *The Maze* consists from heavy constrained turns: 1<sup>st</sup> turn (fig. 7.9a), 2<sup>nd</sup> turn (fig. 7.9b), and 3<sup>rd</sup> turn (fig. 7.9c). The hidden waypoint reach is given by (fig. 7.9d).
2. UAS is constantly in *Emergency Avoidance mode* because there is always a presence of an obstacle.
3. *The Navigation path* is located in a slim corridor with width only 3-6 meters. Mutual distance of obstacles is 20 meters, and combined margins take 14-17 meters.
4. *Maze scenario* was very close to the urban environment concerning obstacle density and computational complexity.
5. *Avoidance run* computational complexity scaled linearly with a count of active obstacles in Field of View.
6. *Hidden Goal Waypoint* has been reached as shown in (fig. 7.9d). This satisfy *reach hidden waypoint* acceptance criterion.

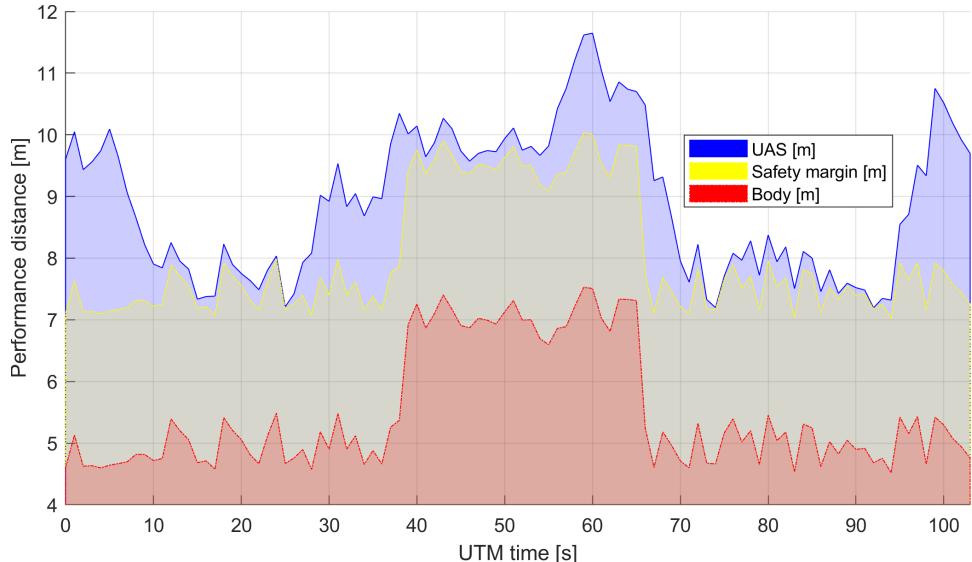
Figure 7.9: Test scenario for *Maze*.

**Distance to Body/Safety Margin Evolution:** The evolution of *body and safety margin* over time (x-axis, sec) given in meters distance (y-axis, m) is given in (fig. 7.10).

The *UAS* center distance to the nearest obstacle (blue line) does not break any *Safety Margin* (yellow line) of the closest obstacle. *Body Margin* of the closest obstacle (red line) has not been broken, because it always lies below *Safety Margin* (yellow).

For *UTM period* 37 to 68 s, there is a *margin spike* due to avoidance of bloated *Rectangle buildings* (fig. 7.9b) during the 2<sup>nd</sup> turn. The *acceptance criterion* for *Safety Margin* is satisfied.

*Note.* The *body and safety margin* is changing depending on *UAS position and orientation*. The changes are reflected in (tab. 7.11).

Figure 7.10: Distance to body/safety margin evolution for *Maze scenario*.

**Distance to Body/Safety Margin Peaks:** The minimal and maximal values for *UAS distance to safety margin* based on performance (fig. 7.10) is summarized in (tab. 7.11).

The *minimal distance to safety margin* is  $0.0131m$  which can be taken as  $\sim 0m$  due to the numerical error. The *maximal distance to safety margin* is  $2.9513m$  which is  $5 \times UAS\ radius$ . The safety margin distance is  $\leq 3m$  which means the scenario is tightly packed with obstacles. The *UAS* never left *Emergency Avoidance Mode* because of the condition:  $safetyMarginDistance \geq avoidanceGridLength$  was never satisfied.

The *minimal body distance* is  $5.0131m$ , while the *maximal body distance* is  $8.7117m$ . The difference between minimal and maximal body distance is  $\sim 4m$  which also indicates scenario packed with obstacles.

Parameter	UAS 1	
Distance to Safety Margin	min	0.0131
	max	2.9513
Distance to Body Margin	min	5.0131
	max	8.7117

Table 7.11: Distance to body/safety margin peaks for *Maze scenario*.

**Path Tracking Performance:** Reference path (green dashed) line is given as direct interconnection of *initial position* (green square with S marker) and *hidden waypoint* (green square with 1 marker). The *UTM Reference Time* is given on x-axis. The evolution of the real trajectory (solid blue line) for each axis is given as follow:

1. *X-axis path tracking* - reflects the maneuvering in the curves of the maze.
2. *Y-axis path tracking* - shows horizontal progress to the *hidden goal waypoint*. The expected linear tracking is not achievement due to the maneuvering delays on X-axis.
3. *Z-axis path tracking* - shows perfect linear tracking of the reference trajectory. The *altitude acceptance criterion*:  $-5m \leq altitude \leq 5m$  have been fulfilled.

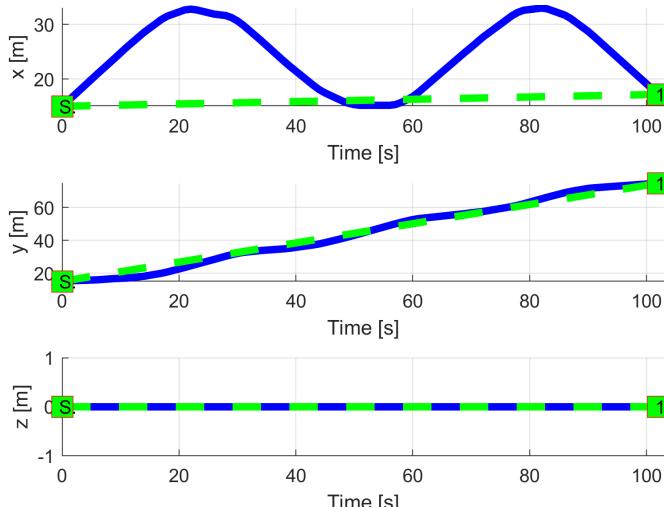


Figure 7.11: *Maze path tracking*.

**Path Tracking Deviations:** Deviations (tab. 7.12) from *reference trajectory* are in expected ranges considering the *mission plan* (tab. 7.9) and *obstacle properties* (tab. 7.10).

Param.	UAS 1
$\mathcal{WP}_1$	
$\max x $	27.32
$\max y $	2.41
$\max z $	0
$\max dist.$	28.06

Table 7.12: Path tracking properties for *Maze* scenario.

**Computation Load:** The *computation load* for scenario (fig.7.12) shows used time (y-axis) over decision frame (x-axis).

The UAS is constantly in *Emergency Avoidance Mode*; the *operational environment* is *cluttered* with obstacles. This causes very high *computation load*.

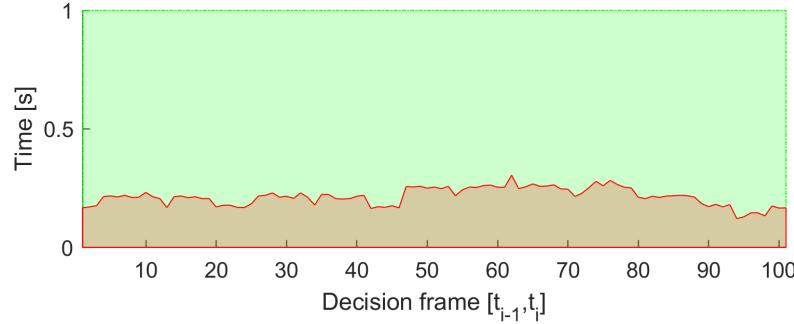


Figure 7.12: Computation time for *Maze* scenario.

### 7.3.4. Storm

**Scenario:** Small UAS is flying in open space in uncontrolled airspace ( $\leq 500$  feet AGL (Above Ground Level)). A *Weather Service* notices UAS about *Dangerous Weather zone* (virtual constraint s. ??) which is moving in UAS direction. The *UAS* is executing mission given by (tab. 7.13).

Position		$\mathcal{WP}_1$
$[x, y, z]$	$[\theta, \omega, \psi]$	
$[0, 0, 0]^T$	$[0^\circ, 0^\circ, 90^\circ]^T$	$[0, 60, 0]^T$

Table 7.13: Mission setup for *Storm* scenario.

**Constraints:** The *storm* is modeled as a *virtual constraint* with parameters given in (tab. 7.14). A constraint is modeled as a *convex polygon* for *horizontal boundary* and altitude for the *vertical boundary*.

The *Storm* is moving through an *operational region* with linear velocity  $0.5ms^{-1}$ . The *storm's center* was first detected at *decision frame* 0 at position  $[0, 50, 0]^T$ .

Constraint			Body Margin			Safety Margin
i. position	velocity	type	min.	max.	avg.	
$[0, 50, 0]^T$	$[0, -0.5, 0]$	polygon	9	10	9.5	5

Table 7.14: Constraint set for Storm scenario.

**Assumption:** Every *avoidable moving constraint* is usually slower than an *Approaching UAS*, or its radius is smaller than the turning radius of an *Approaching UAS*.

**Note.** *Manned aviation* receives a permit to operate in *controlled airspace* only if it has capability outmaneuver every known threat in requested airspace.

The *Constrained space portion* is usually very large, therefore in the majority of cases the assumption *uasSpeed >> constraintSpeed* holds.

**Main Goal:** Show dynamic moving constraint avoidance capability in *uncontrolled airspace*.

#### Acceptance criteria:

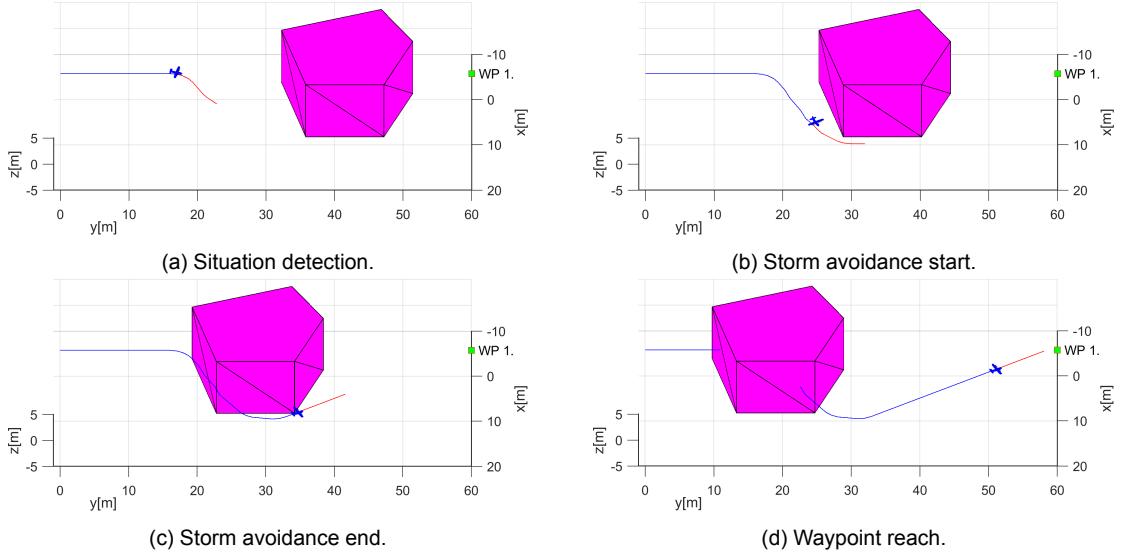
1. *Hard constraint avoidance* - the *UAS* must not cross the body margin:  $distance(stormCenter, UAS) \geq bodyMargin$ .
2. *Soft constraint avoidance* - the *UAS* cannot cross the safety margin to get into proximity of *Storms surrounding area*:  $distance(stormCenter, UAS) \geq safetyMargin$ .

**Testing setup:** The *standard test setup* defined in (tab. ??, ??, ??, ??, ??) is used with following parameter override:

1. *Avoidance grid - type - ACAS-like with horizontal enabled maneuvers*.

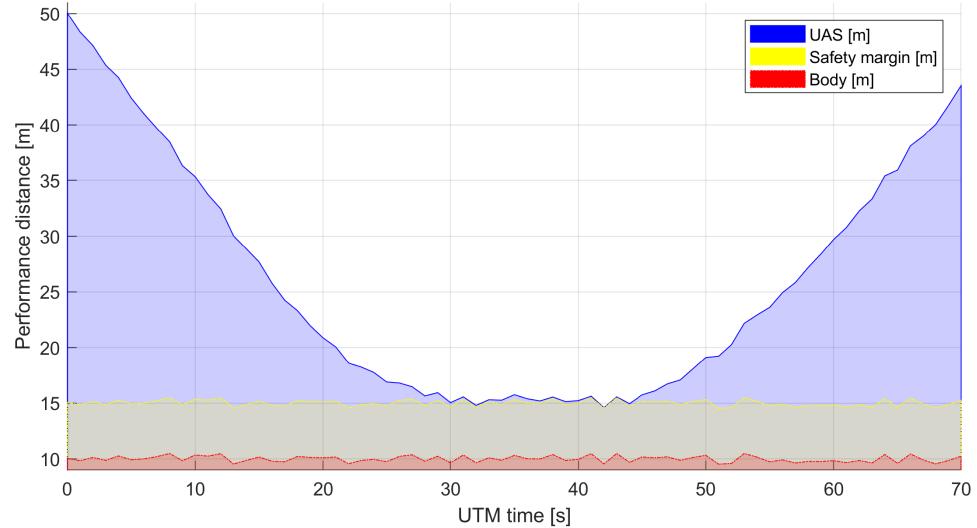
**Simulation run:** *Notable moments* from a *simulation run* (fig. 7.13) are the following:

1. *Detection* (fig. 7.13a) - the *Storm* (magenta polygon) is detected prior to the engagement (retrieved from associated weather service). The *UAS* (blue) stays in *Navigation mode*. *Trajectories in Navigation grid* are constrained by rule *Enforce safety margin* (tab. ??). The *Planned trajectory* (red) changes to avoid *Storm*.
2. *Avoidance start* (fig. 7.13b) - when UAS reaches optimal avoidance distance, the *navigation reach set* is constrained, forcing UAS to perform an evasive maneuver.
3. *Avoidance end* (fig. 7.13c) - navigation space is no longer constrained when the *minimal safe distance/heading* is achieved.
4. *Waypoint reached* (fig. 7.13d) - standard waypoint navigation procedure was used in this case.

Figure 7.13: Test scenario for *Storm* (Dynamic hard constraint).

**Distance to Body/Safety Margin Evolution:** The *body margin* (red line) and *safety margin* (yellow line) and *UAS distance to storm center* (blue line) evolution over *UTM time* (x-axis) are given in (fig. 7.14) The *body* and *safety margin* was changing according to the mutual position of the *storm* and the *UAS* (see tab. 7.14).

The acceptance criteria for the *hard constraint avoidance* and *soft constraint avoidance* have been fulfilled.

Figure 7.14: Distance to body/safety margin evolution for *Storm scenario*.

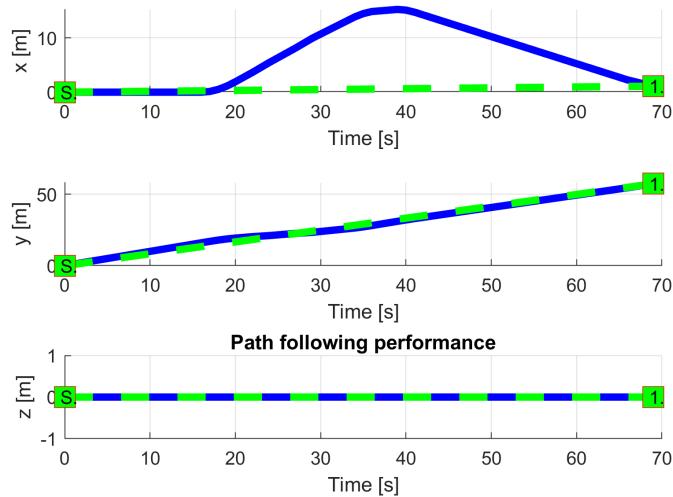
**Distance to Body/Safety Margin Peaks:** A *hard constraint* of *body margin* was not breached, because the  $distance(UAS(t), stormBody(t))$  was all time greater than 0. Thus the *UAS* stayed well clear from *Storm*. The summary (tab. 7.15) shows that the *minimal body margin distance* was 5.0335 m, which proves *avoidance of hard constraint*.

A *soft constraint* represented as a *safety margin* (protective coating around storm body) was not breached, because the  $distance(UAS(t), stormBody(t)) - safetyMargin(t)$  was all time greater than 0. The summary (tab. 7.15) show that the *minimal safety margin distance* was 0.0355 m, which proves *avoidance of soft constraints*.

Parameter		UAS 1
Distance to Safety Margin	min	0.0355
	max	34.9934
Distance to Body Margin	min	5.0355
	max	39.9934

Table 7.15: Distance to body/safety margin peaks for *Storm scenario*.

**Path Tracking Performance:** The *path tracking* (solid blue line) of *reference trajectory* (green dashed line) between *starting waypoint* (green square marked "S") and *final waypoint* (green square marked "1") is portrayed in (fig. 7.15). The UAS executes *horizontal right-side avoidance* of the *Storm* as is preferred.

Figure 7.15: *Storm avoidance scenario path tracking*.

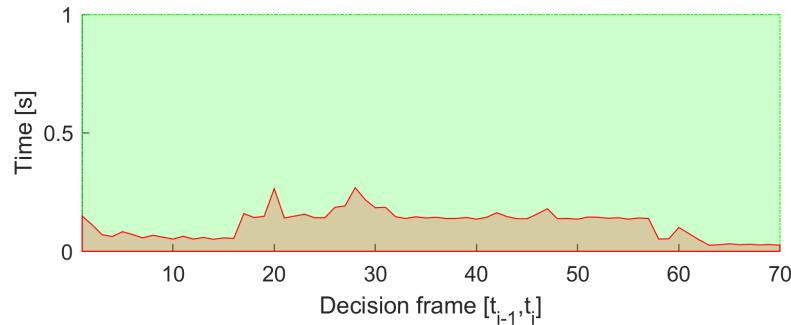
**Path Tracking Deviations:** *Deviations* (tab. 7.16) are in expected ranges considering the mission plan (tab. 7.13) and *body* and *safety* margins (tab. 7.14).

Param.	UAS 1
$\mathcal{WP}_1$	
$\max x $	15.26
$\max y $	1.32
$\max z $	0
$\max dist.$	15.76

Table 7.16: Path tracking properties for *Storm scenario*.

**Computation Load:** The *computation load* for *scenario* (fig.7.16) shows used time (y-axis) over decision frame (x-axis).

The *computation time* is low; it only increases slightly during avoidance maneuver.

Figure 7.16: Computation time for *Maze* scenario.

### 7.3.5. Emergency Converging

**Scenario:** Two *UAS* are flying in *uncontrolled airspace* (altitude  $\leq 500$  ft. Above the Ground Level) with missions defined in (tab. 7.17). Both *UAS* are in the *Navigation mode* with active *ADS-B-In/Out*, receiving position notification from each other. Cruising altitude is sufficient for horizontal separation (50-100 ft. Above the Ground Level). *Horizontal separation* is the preferred separation type for both *UAS*.

UAS	Position		$WP_1$
	$[x, y, z]$	$[\theta, \omega, \psi]$	
1	$[0, 20, 0]^T$	$[0^\circ, 0^\circ, 0^\circ]^T$	$[40, 20, 0]^T$
2	$[20, 0, 0]^T$	$[0^\circ, 0^\circ, 90^\circ]^T$	$[20, 40, 0]^T$

Table 7.17: Mission setup for *Emergency converging* scenario.

*Note.* *Collision point* is expected at  $C = [20, 20, 0]^T$ . The *angle of approach* is  $90^\circ$  which classifies the situation as *Converging maneuver* (fig. ??).

**Main Goal:** Show two *non-cooperative UAS* avoidance capability for *Converging maneuver* scenario in *uncontrolled airspace*.

#### Acceptance criteria:

1. *Proper mode invocation* - when an intruder intersects the UAS with *Right of the Way* navigation grid, both UAS will switch into *Emergency Avoidance Mode*.
2. *Minimal safety margin distance*  $\geq 0m$ .
3. *Each UAS* will reach own goal waypoint (tab. 7.17).

**Testing setup:** The *standard test setup* for each UAS defined in (tab ??, ??, ??, ??, ??) is used with the following without parameter override.

*Intruder intersection* model has been chosen depending on UAS (tab. 7.18). Each UAS is equipped with *ADS-B In/Out* sensor obtaining/distributing the following information:

1. *Position* - in operational section coordinate frame.
2. *Velocity* - vector representation in the given coordinate frame.

3. *Class size* - class body radius based on UAS propulsion and size.
4. *Safety margin set* - set of safety margins for different collision cases.

*Avoidance parameters* for the *Emergency converging scenario* are given in (tab. 7.18). Each UAS has the same speed set to  $1\text{ms}^{-1}$ . Second UAS has the *Right of Way*.

The *safety margin* is considered as sum of both participants *near miss margins*. In this case, the default safety margin is considered as  $1.2\text{ m}$ .

UAS	Parameters			Margins		Separation
	velocity	intruder model	ROW	body	safety	
1	1	body + spread	false	0.3	0.6	horizontal
2	1	body + spread	true	0.3	0.6	horizontal

Table 7.18: Avoidance parameters for *Emergency converging scenario*.

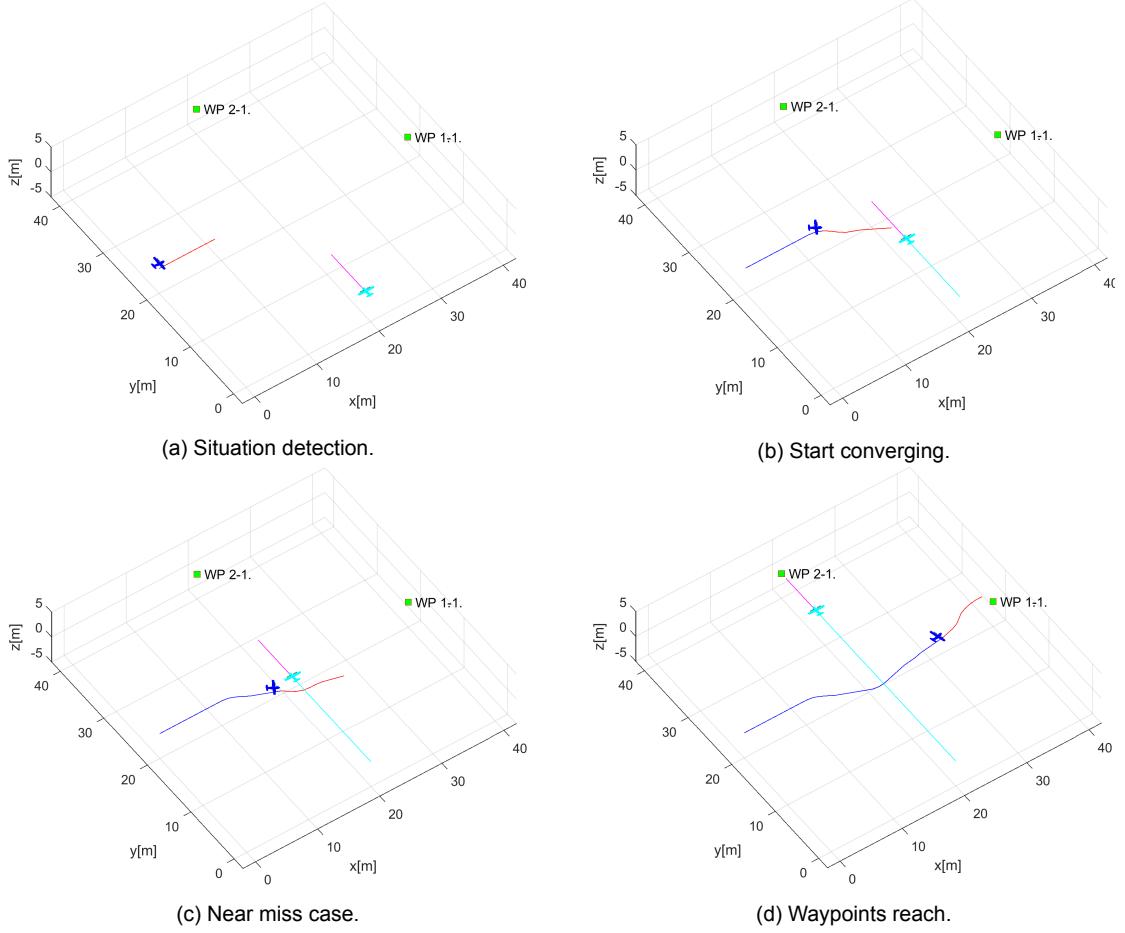
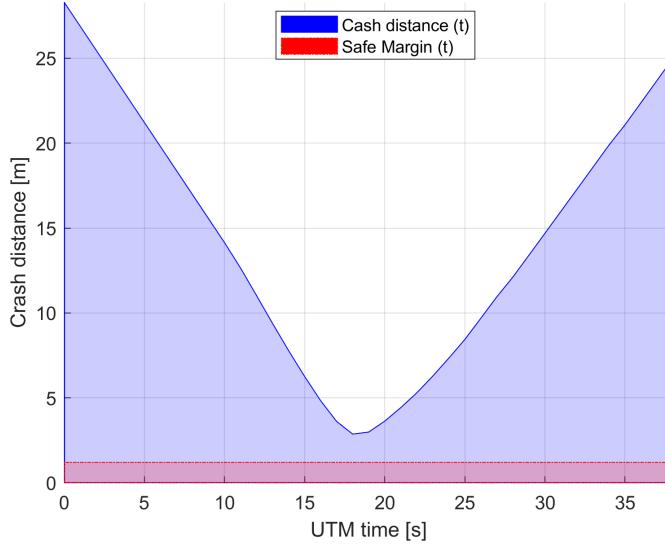
*Note.* Both UAS are using body (app. ??) and spread (app. ??) intersection models, reflecting both body volume and maneuverability of intruder. Both UAS have preferred separation mode as *horizontal*, typical for planes.

**Simulation Run:** Notable moments from the simulation run (fig. 7.17) are following

1. *Detection* (fig. 7.17a) - Intruder (UAS2 cyan) is approaching (UAS 1 blue) from the right side, Intruder (UAS2 cyan) has the right of way, because of  $70^\circ \leq \text{angleOfApproach} < 130^\circ$ . *Intruder intersection model* (for UAS 2) is created and propagated in *avoidance grid* (for UAS 1).
2. *Start Converging* (fig. 7.17b) - when *UAS 2 (cyan) parametric intruder intersection model* disables *trajectories*, converging maneuver for UAS 1 (blue) starts.
3. *Near miss case* (fig. 7.17c) - UAS 1 (blue) to UAS 2 (cyan) closest distance. The safety margin for *near miss* has not been breached. The safety margin for *well clear* in uncontrolled airspace is invalid.
4. *Waypoint reached* (fig. 7.17d) - the intruder intersection model for UAS 2 (cyan) is removed from UAS 1 (blue) *avoidance grid* after *converging maneuver competition*, standard navigation procedure is applied afterward.

*Note.* UAS 2 (cyan) has the *Right of way* in (tab. 7.18).

*Note.* UAS 1 (blue) used only horizontal separation (priority) in (fig. 7.19a).

Figure 7.17: Test scenario for *Emergency converging* (Intruder avoidance).Figure 7.18: Distance to safety margin evolution for *emergency converging* scenario.

**Distance to Safety Margin Evolution:** There is a need to compare the mutual distance between both UAS (y-axis [m]) and its evolution over UTM time (x-axis [s]). The *mutual* distance of *UAS 1 to UAS 2* is given by *blue line*. The *Safety margin* value is denoted by the red line at a *constant value* of 1.2 m.

The *Proper avoidance Invocation* is shown when UAS systems are getting closer to each other, and they enter (*Emergency Avoidance Mode*) to provide *active separation*. The *Mutual*

*distance evolution* (blue line) does not cross *safety margin* (red line).

**Distance to Safety Margin Peaks:** Minimal and Maximal mutual distance to safety margin is summarized in (tab. 7.19). The closest to the collision are UAS systems when the distance to safety margin is 1.6676m.

The *minimal distance to safety margin*  $\geq 0$  which means that the *safety acceptance criterion* is fulfilled.

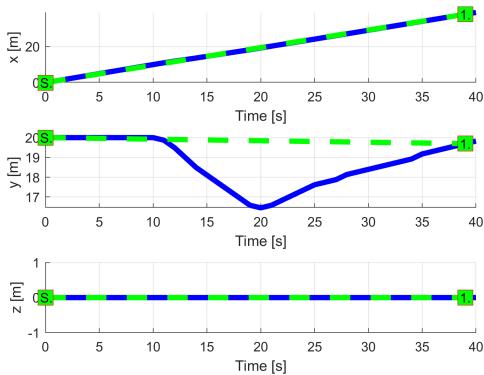
UAS:		1-2
Distance to Safety Margin	min	1.6676
	max	27.0843

Table 7.19: Distance to safety margin peaks for the *emergency converging scenario*.

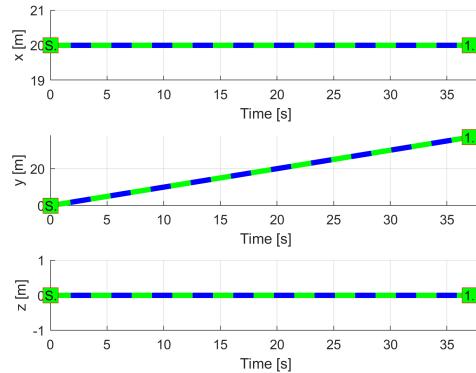
**Path Tracking Performance:** All waypoints (green numbered squares) for both UAS have been reached (fig. 7.19). *Reference trajectories* (green dashed lines), between the initial position (green square marked S) and goal waypoint (green square marked 1) are split into three XYZ values with respective figures. The tracked value is on y-axis [m] and time on x-axis [s]. The blue lines represent real parameter evolution over time.

Following observations can be made from path tracking (fig. 7.19) and preferred separations (tab. 7.18):

1. UAS 1 (fig. 7.19a) is using *horizontal separation* (y-axis). The UAS diverges from the reference trajectory to minimum necessary time.
2. UAS 2 (fig. 7.19b) has the right of way and is not using any active avoidance mechanism.



(a) UAS 1.



(b) UAS 2.

Figure 7.19: *Trajectory tracking for Emergency converging test case*.

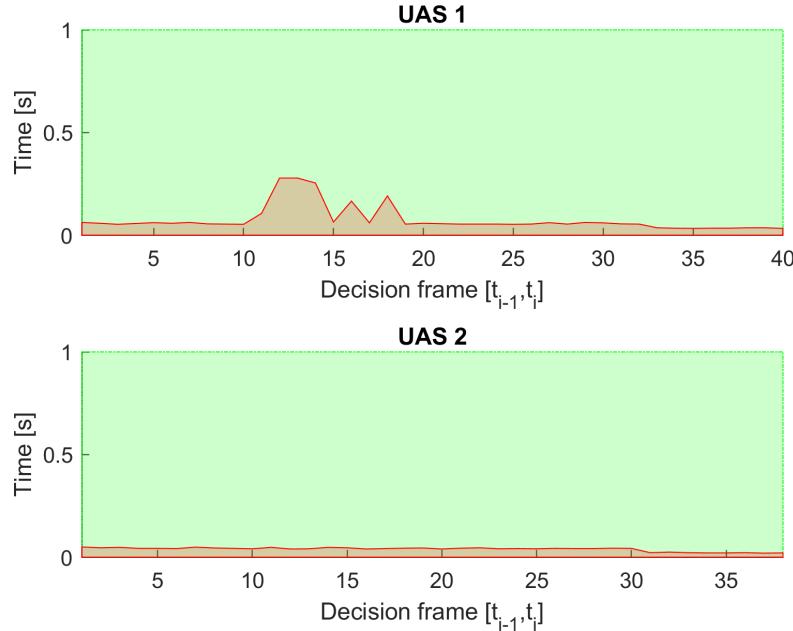
**Path Following Deviations:** *Deviations* (tab. 7.20) are in expected ranges considering the *mission plans* (tab. 7.17) and *separation safety margin* (tab. 7.18).

Param.	UAS 1	UAS 2
	$\mathcal{WP}_1$	$\mathcal{WP}_1$
$\max x $	0	0
$\max y $	3.25	0
$\max z $	0	0
$\max dist.$	3.25	0

Table 7.20: Path tracking properties for the *Emergency converging* scenario.

**Computation Load:** The *computation load* for scenario (fig.7.20) shows used time (y-axis) over decision frame (x-axis).

The *computation time* is increased only for UAS 1 during the avoidance period. The UAS 2 remains unaffected because it has the right of way.

Figure 7.20: Computation time for *Emergency converging* scenario.

### 7.3.6. Emergency Head-On

**Scenario:** Two *UAS* systems are flying in *uncontrolled airspace* (altitude  $\leq 500$  ft. Above the Ground Level) with missions defined in (tab. 7.21). Both *UAS* are in the *Navigation mode* with active *ADS-B-In/Out*, receiving position notifications from each other. Cruising altitude is sufficient for horizontal separation (50-100 ft. Above Ground Level). *Horizontal separation* is preferred mode for both *UAS*.

UAS	Position		$\mathcal{WP}_1$
	$[x, y, z]$	$[\theta, \omega, \psi]$	
1	$[0, 20, 0]^T$	$[0^\circ, 0^\circ, 0^\circ]^T$	$[40, 20, 0]^T$
2	$[40, 20, 0]^T$	$[0^\circ, 0^\circ, 180^\circ]^T$	$[0, 20, 0]^T$

Table 7.21: Mission setup for *Emergency head-on* scenario.

*Note.* Collision point is expected at  $C = [20, 20, 0]^T$ . The angle of approach is  $180^\circ$  which classifies the situation as *Head-on maneuver* (fig. ??).

**Main Goal:** Show two *non-cooperative* UAS avoidance for *Head-on approach scenario* in *uncontrolled* airspace.

**Acceptance criteria:**

1. *Proper mode invocation* - when an intruder intersects the opposing UAS Navigation grid, both intruder and UAS will switch to *Emergency Avoidance Mode*. None of the UAS have the *Right of Way*.
2. *Minimal Safety Margin distance*  $\geq 0m$ . That means the mutual distance of both UAS centers does not go below-given *safety margin*.
3. *Both UAS* will reach own goal waypoint (tab. 7.21).

**Testing setup:** The standard test setup for each UAS defined in (tab ??, ??, ??, ??, ??) is used with the following without parameter override.

*Intruder intersection model* has been chosen depending on UAS (tab. 7.22). Each UAS is equipped with *ADS-B In/Out* sensor obtaining/distributing the following information:

1. *Position* - in operational section coordinate frame.
2. *Velocity* - vector representation in the given coordinate frame.
3. *Class size* - class body radius based on UAS propulsion and size.
4. *Safety margin set* - set of safety margins for different collision cases.

*Avoidance parameters* for the *Emergency head-on scenario* are given in (tab. 7.22). Each UAS has the same speed set to  $1ms^{-1}$ . None of them have the *Right of Way*.

The *safety margin* is considered as a sum of both participants *near miss margins*. In this case, the default safety margin is considered as  $1.2 m$ .

UAS	Parameters			Margins		Separation
	velocity	intruder model	ROW	body	safety	
1	1	body (timed)	false	0.3	0.6	horizontal
2	1	body (timed)	false	0.3	0.6	horizontal

Table 7.22: Avoidance parameters for *Emergency head on* scenario.

*Note.* Both UAS are using body (app. ??) intersection model, reflecting both body volume along the expected trajectory. Both UAS have a preference for *horizontal* separation mode, typical for planes.

**Simulation Run:** Notable moments from the simulation run (fig. 7.21) are the following:

1. *Situation detection* (fig. 7.17a) - UAS 1 (blue) is approaching UAS 2 (cyan) with  $130^\circ \leq \text{angleOfApproach} \leq 180^\circ$ , this is considered head-on approach. Head-on approach gives the *right of the way* neither to UAS 1 nor UAS 2. An *intruder intersection model* for opposite UAS is created in respective avoidance grids. *Head on emergency avoidance* starts independently in each UAS without intruders coordination. First *avoidance maneuver* is invoked when the *intruder intersection model* constraints any trajectory in the *avoidance grid*. When this happens *Navigation mode* switch to the *Emergency avoidance mode*.

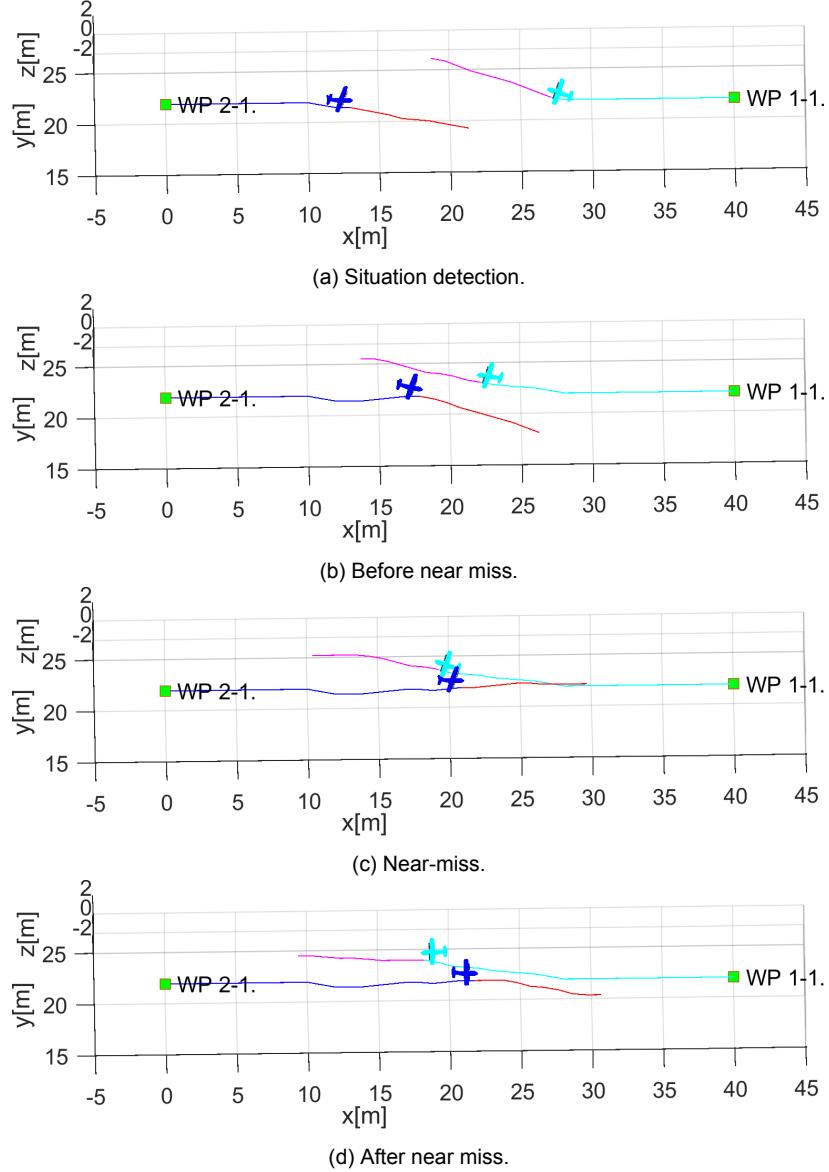


Figure 7.21: Test scenario for *Emergency head-on approach* (Intruder avoidance).

2. *Before near miss* (fig. 7.21b) - both UAS are in *emergency avoidance mode*, sticking to right side avoidance maneuver.
3. *Near miss case* (fig. 7.21c) - UAS 1 to UAS 2 closest distance. The safety margin for *near miss* has not been breached. The safety margin for *well clear* in uncontrolled airspace is invalid. Both UAS are using also *Horizontal separation* to avoid each other, *Emergency*

*avoidance mode* is switched to the *Navigation mode* when the risk of an *aerial clash* is voided.

4. After near-miss (fig. 7.21d) - both *UAS* are tracking back to respective waypoint, correcting *altitude* (Z-axis in (fig. 7.23)) first.

Note. *Collision point* was expected at  $C = [20, 20, 0]^T$ .

Note. Both *UAS* used *horizontal* (primary), *vertical* (secondary) separation (fig 7.23).

Note. Both *UAS* decision times were *synchronized*, this is not an assumption, but it shows critical performance. Usually, safety margin is bloated for (eq.??).

**Distance to Safety Margin Evolution:** There is a need to compare the mutual distance between both *UAS* (y-axis [m]) and its evolution over synchronized *UTM time* (x-axis [s].) The *mutual distance* between bodies of *UAS 1, UAS 2* (blue line) compared to *Safety Margin* (red line) is given in (fig. 7.22). The *Safety Margin* value was constant for all time at value 1.2 m which is double of *Near Miss Margin* for *UAS 1 UAS 2*.

The proper *Avoidance Invocation* is shown when *UAS* systems are getting closer to each other, and they start their *separation phase* (Emergency Avoidance Mode switch). The mutual distance (blue line) does not cross *safety margin* (red line).

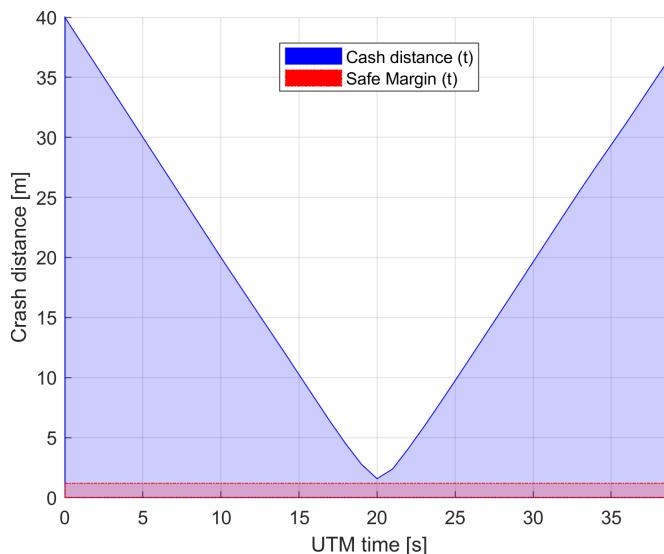


Figure 7.22: Distance to safety margin evolution for *emergency head-on scenario*.

**Distance to Safety Margin Peaks:** Minimal and Maximal mutual distance to safety margin is summarized in (tab. 7.23). The closest to the collision are *UAS* systems when the *distance to safety margin* is 0.3824m.

The *minimal distance to safety margin*  $\geq 0$  which means that the *safety acceptance criterion* is fulfilled.

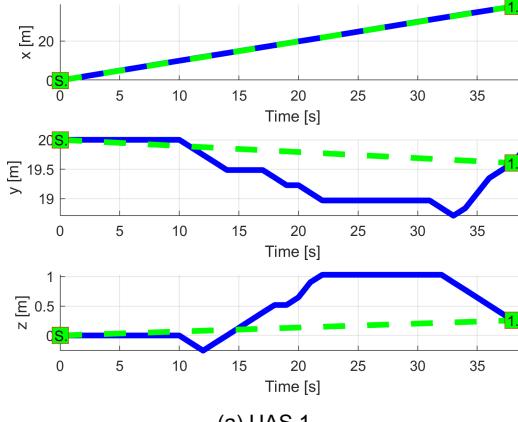
UAS:			1-2
Distance to Safety Margin	min	0.3824	
	max	38.8000	

Table 7.23: Distance to safety margin peaks for *Emergency head-on scenario*.

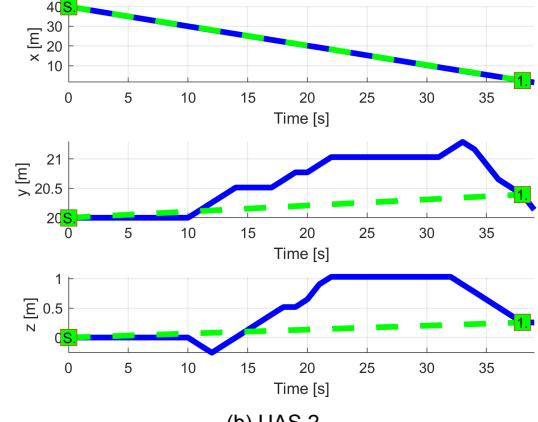
**Path Tracking Performance** All waypoints (green numbered squares) for both UAS have been reached (fig. 7.23). *Reference trajectories* (green dashed lines), between the initial position (green square marked S) and goal waypoint (green square marked 1) are split into three XYZ values with respective figures. The tracked value is on y-axis [m] and time on x-axis [s]. The blue lines represent real parameter evolution over time.

Following observations can be made from path tracking (fig. 7.23) and preferred separations (tab. 7.22):

1. UAS 1 (fig. 7.23a) is using horizontal separation going to the right (y-axis) and a little bit up (z-axis).
2. UAS 2 (fig. 7.23b) is using horizontal separation going to the right (left in GCS, y-axis) and a little bit up (z-axis).



(a) UAS 1.



(b) UAS 2.

Figure 7.23: *Trajectory tracking for Emergency head-on test case.*

**Path Following Deviations:** *Deviations* (tab. 7.24) are in expected ranges considering the *mission plans* (tab. 7.21) and *separation safety margins* (tab. 7.22).

Param.	UAS 1	UAS 2
	$\mathcal{WP}_1$	$\mathcal{WP}_1$
$\max x $	0.05	0.06
$\max y $	1.37	1.48
$\max z $	1.03	1.05
$\max dist.$	1.39	1.52

Table 7.24: Path tracking properties for *Emergency head-on* scenario.

**Computation Load:** The *computation load* for scenario (fig.7.20) shows used time (y-axis) over decision frame (x-axis).

The *computation time* is increased only during the *avoidance phase*. The *load* is symmetric for both UAS systems.

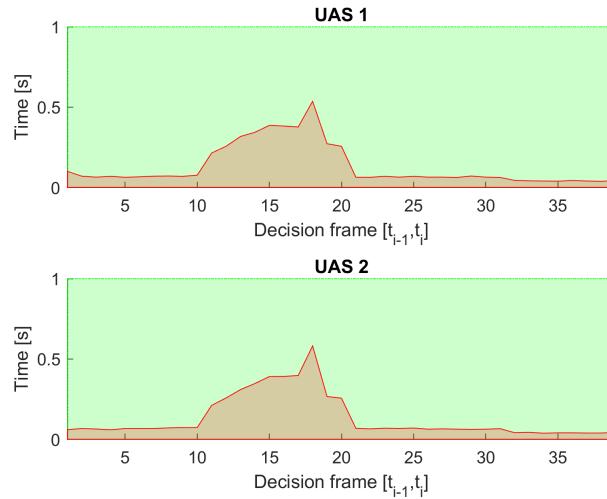


Figure 7.24: Computation time for *Emergency head-on* scenario.

### 7.3.7. Emergency Mixed Head-On with Converging

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**Scenario:** Four UAS are flying in *uncontrolled airspace* (altitude  $\leq 500$  ft. Above the Ground Level) missions defined in (tab. 7.25). All UAS are in the *Navigation mode* with active *ADS-B In*, receiving *position notifications* from each other. Cruising altitude is sufficient for *horizontal separation* (50-100 ft. Above the Ground Level).

UAS	Position		$\mathcal{WP}_1$
	$[x, y, z]$	$[\theta, \omega, \psi]$	
1	$[0, 20, 0]^T$	$[0^\circ, 0^\circ, 0^\circ]^T$	$[45, 20, 0]^T$
2	$[40, 20, 0]^T$	$[0^\circ, 0^\circ, 180^\circ]^T$	$[-5, 20, 0]^T$
3	$[20, 0, 0]^T$	$[0^\circ, 0^\circ, 90^\circ]^T$	$[20, 45, 0]^T$
4	$[20, 40, 0]^T$	$[0^\circ, 0^\circ, -90^\circ]^T$	$[45, 20, 0]^T$

Table 7.25: Mission setup for the *Emergency mixed* scenario.

*Note.* Collision point is expected at  $\mathcal{C} = [20, 20, 0]^T$

**Main Goal:** Show *multiple non-cooperative intruders avoidance capability* in *uncontrolled airspace*.

#### Acceptance criteria:

1. Proper avoidance mode invocation - when an *intruder intersection model* impact the *Avoidance Grid*, UAS system will switch to an *Emergency avoidance mode*.
2. Minimal safety margin distance  $\geq 0m$ .

3. Each UAS will reach own goal waypoint (tab. 7.25).

**Testing setup:** The *standard test setup* for each UAS defined in (tab ??, ??, ??, ??, ??) is used with the following without parameter override.

*Intruder intersection model* has been chosen depending on UAS (tab. 7.26). Each UAS is equipped with *ADS-B In/Out* sensor obtaining/distributing the following information:

1. *Position* - in operational section coordinate frame.
2. *Velocity* - vector representation in the given coordinate frame.
3. *Class size* - class body radius based on UAS propulsion and size.
4. *Safety margin set* - set of safety margins for different collision cases.

*Avoidance parameters* for the *Emergency mixed scenario* are given in (tab. 7.26). Each UAS has different *intruder model* and separation combination. Each UAS has same the speed set to  $1\text{ms}^{-1}$ . None of UAS has the *Right of Way*.

The *safety margin* is considered as the sum of both participants *near miss margins*. In this case, the default safety margin is considered as 1.2 m.

UAS	Parameters			Margins		Separation
	velocity	intruder model	ROW	body	safety	
1	1	body + spread	false	0.3	0.6	horizontal
2	1	body (timed)	false	0.3	0.6	vertical
3	1	body (timed)	false	0.3	0.6	horizontal
2	1	body + spread	false	0.3	0.6	vertical

Table 7.26: Avoidance parameters for *Emergency mixed scenario*.

**Note.** Each UAS use different intruder intersection models and primary *separations* (defined in the tab. 7.26). UAS reactions are based on primary *Separation mode*, intruders intersection models this is reflected on major axial deviations in (fig. 7.27) and summarized in *path tracking deviation* (tab. 7.28).

**Simulation Run:** Notable moments from the simulation run (fig. 7.25) are the following:

1. *Situation detection* (fig. 7.25a) - UAS 1 (blue) is detecting UAS 2 (cyan), UAS 3 (green), and UAS 4 (black) as possible intruders. There are multiple converging and head on approaches depending on mutual positions (UAS and *angle of approach*). There exist at least one *converging case* where each UAS has the *Right of way*. Each UAS creates intruder intersection models depending on the intruder configuration (tab. 7.26). Each UAS enters into the *Emergency avoidance mode* independently, when at least one trajectory is constrained in the *avoidance grid*.
2. *Before near-miss* (fig. 7.25b) - all UAS are in *emergency avoidance mode*, using various *separation modes* and *intruder intersection models*. Each UAS is performing its own avoidance maneuver, constantly checking other intruders. If the same separation and the same intruder model were used, there would be a virtual roundabout.

3. After near-miss (fig. 7.25c) - all UAS avoided each other which is covered in *safety margin performance* (fig. 7.26) and (tab. 7.27).
4. Situation resolution (fig. 7.25d) - all UAS returns to *Navigation mode* correcting *altitude* first and continuing to assigned waypoints.

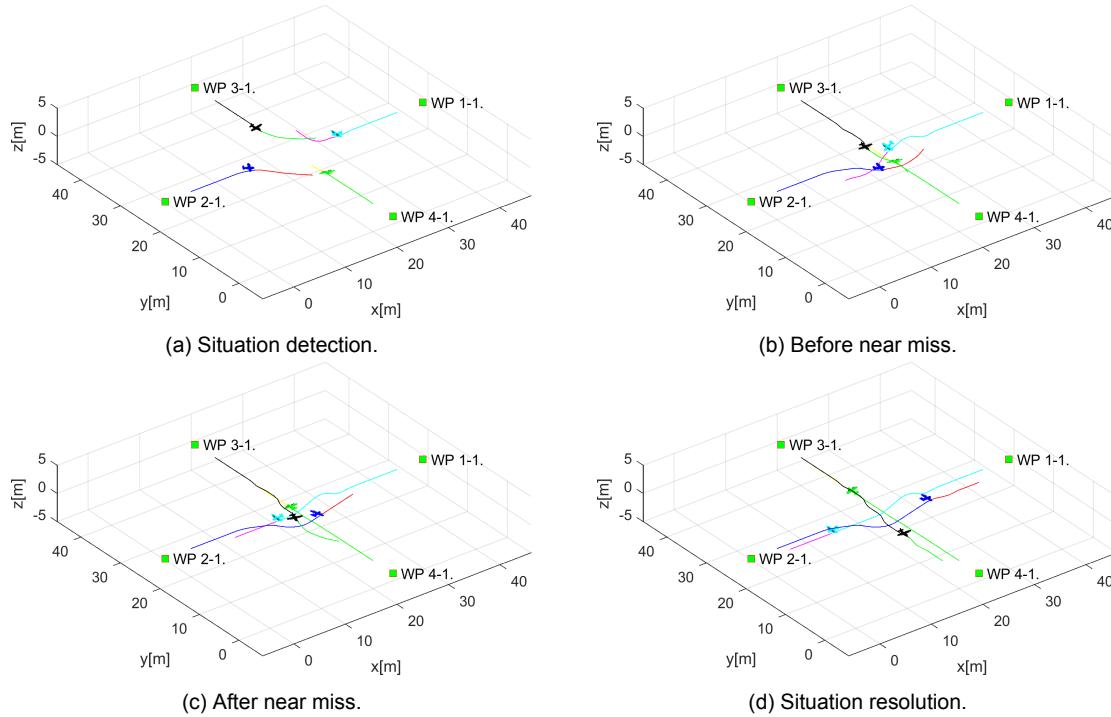


Figure 7.25: Test scenario for the *Emergency mixed* situation with the *self-separation mode*.

**Distance to Safety Margin Peaks:** Minimal and Maximal mutual distance to safety margin is summarized in (tab. 7.27). There is no detected breach for any combination.

The *closest to collision* is UAS pair 2 – 4 with mutual safety margin only 0.2019 m. On the other side is UAS pair 1 – 3 with mutual safety margin 4.3721 m.

The *minimal distance to safety margin*  $\geq 0$  which means that the *safety condition* is fulfilled.

UAS:	Distance to Safety Margin		
	min	max	breach
1-2	3.6231	44.0831	false
1-3	4.3721	30.7300	false
1-4	1.8959	30.7331	false
2-3	0.7331	32.0266	false
2-4	0.2019	31.7282	false
3-4	2.5171	45.4257	false

Table 7.27: Distance to safety margin peaks for the *emergency mixed scenario*.

**Distance to Safety Margin Evolution:** There is a need to compare the mutual distance between each UAS. The graph (fig. 7.26) shows six figures for each *UAS systems* mutual distance (blue line) in this scenario. The *Safety Margin* (red line) (1.2 m) was not breached for any pair (case).

The *Proper avoidance invocation* is shown when UAS systems are getting closer to each other, and then they start separation phase (Emergency avoidance mode).

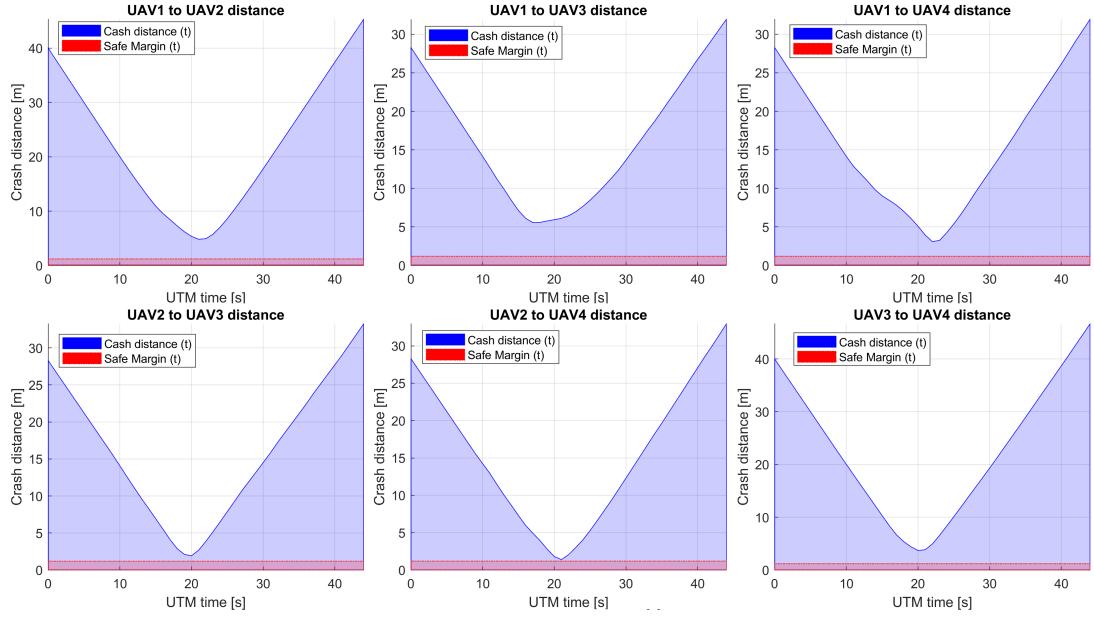


Figure 7.26: Distance to safety margin evolution for the *emergency mixed scenario*.

**Path Tracking Performance:** All waypoints (Green numbered squares) for all UAS have been reached (fig. 7.27). *Reference trajectories* (green dashed line) have been tracked by *UAS real path* (solid blue line) almost all time.

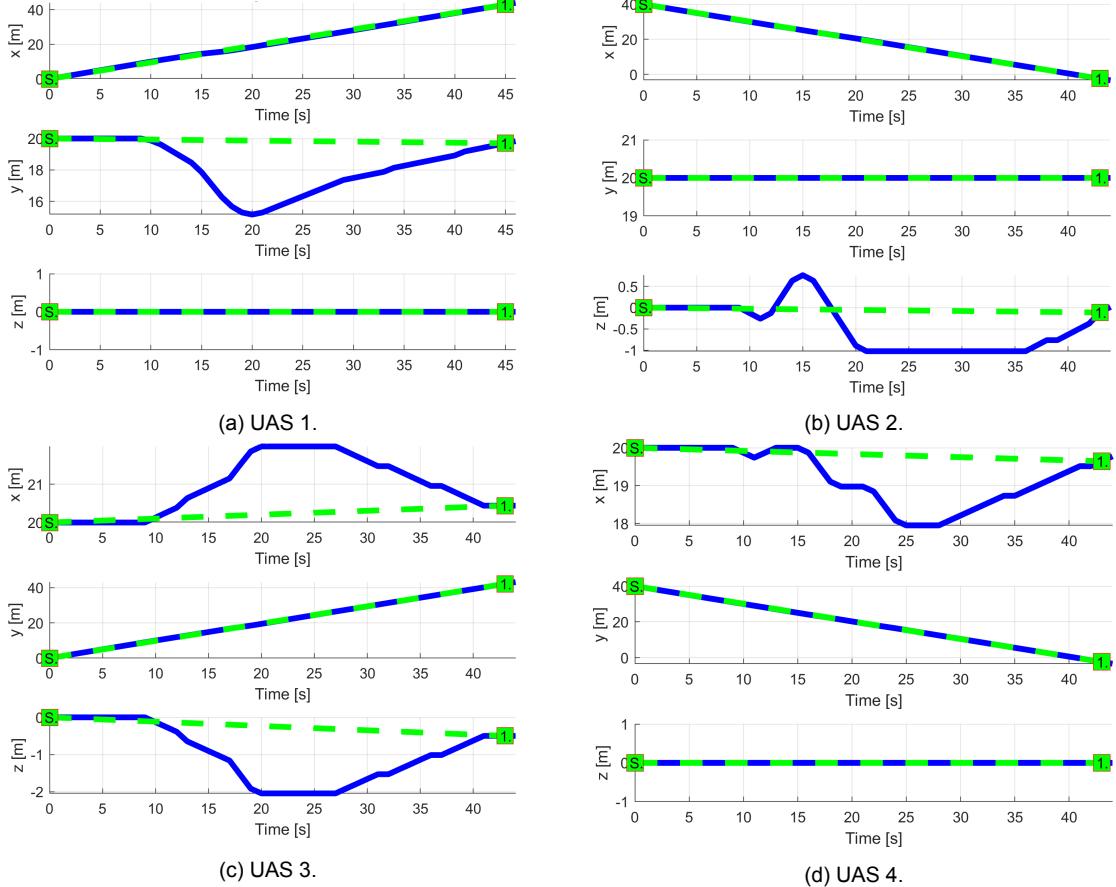


Figure 7.27: Trajectory tracking for the *Emergency mixed situation test case*.

Following observations can be made from *path tracking* (fig. 7.27) and *preferred separations* (tab. 7.26):

1. UAS 1 (fig. 7.27a) is using *horizontal separation* (y-axis right) having *preferred horizontal separation*.
2. UAS 2 (fig. 7.27b) is using vertical separation (z-axis up-down), having preferred vertical separation.
3. UAS 3 (fig. 7.27d) is using horizontal/vertical separation (x-right, z-down), having preferred horizontal separation. This UAS has used other than the preferred separation type.
4. UAS 4 (fig. 7.27c) is using horizontal separation (x-axis right/left), having preferred vertical separation. This UAS has used opposite separation type to preferred.

**Path Tracking Deviations:** *Deviations* (tab. 7.28) are in expected ranges considering the *mission plans* (tab. 7.25) and *separation safety margins* (tab. 7.26).

Param.	UAS 1	UAS 2	UAS 3	UAS 4
	$\mathcal{WP}_1$	$\mathcal{WP}_1$	$\mathcal{WP}_1$	$\mathcal{WP}_1$
$\max x $	0	0	1.98	2.05
$\max y $	4.84	0	0	0
$\max z $	0	1.23	2.43	0
$\max dist.$	4.84	1.23	3.45	2.05

Table 7.28: Path tracking properties for the *Emergency mixed* scenario.

**Computation Load:** The *computation load* for *scenario* (fig.7.28) shows used time (y-axis) over decision frame (x-axis).

The *computation time* increases during periods of *active avoidance*. The *shortest* period of avoidance has UAS 1 and the longest period of avoidance has UAS 4.

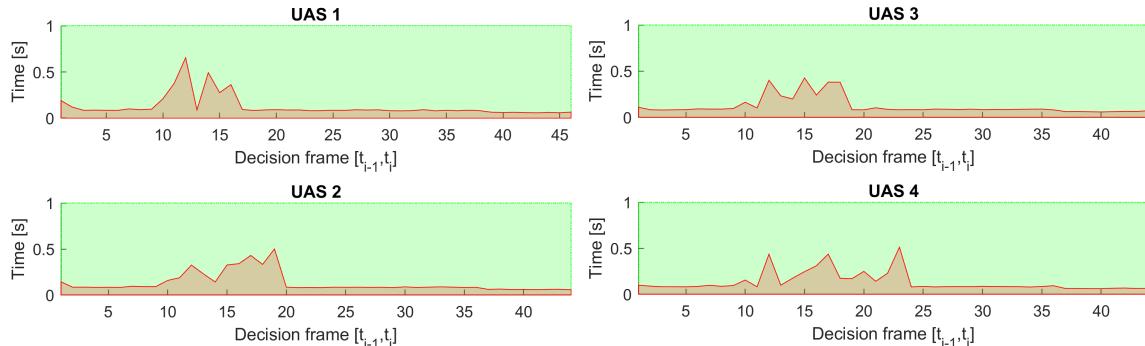


Figure 7.28: Computation time for *Emergency multiple* scenario.

# Bibliography

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- [1] Alojz Gomola, Pavel Klang, and Jan Ludvik. Probabilistic approach in data fusion for obstacle avoidance framework based on reach sets. In *Internal publication collection*, pages 1–93. Honeywell, 2017.