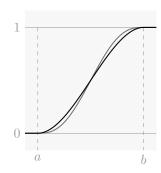
# The easing\* Library for PGF

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<sup>\*</sup>version 0.1, dated 2021/07/17. This version was tested with PGF version 3.1.9a <code>†loh.ka.tsun@gmail.com</code>

## 1 Introduction

This library adds easing functions to the PGF mathematical engine.

## 2 Installation

The easing library is a PGF library; it works both with IATEX and with plain TEX. Once the file pgflibraryeasing.code.tex is in a directory searched by TEX, the library can be loaded as follows:

with plain TeX:

```
\input pgf
\usepgflibrary{easing}
```

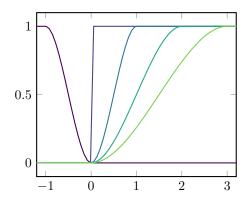
with LATEX:

\usepackage{pgf} \usepgflibrary{easing}

The easing library is compatible with, but does not depend on, the floating point unit library provided by PGF. To use both easing and the FPU, the FPU (or any packages/libraries which use the FPU, such as pgfplots) must be loaded before the easing library.

# 3 Usage

The routines implemented by the easing library are added to PGF's mathematical engine with  $\protect\$ 



```
\input pgfplots
\usepgflibrary{easing}
\tikzpicture
\axis[
   domain=-1.2:3.2, samples=64,
   xmin=-1.2, xmax=3.2,
   cycle list={
      [samples of colormap=6 of viridis]},
   no marks, thick]
\pgfplotsinvokeforeach{-1,...,3}{
   \addplot{smoothstep(0,#1,x)};}
\endaxis
\endtikzpicture
\end
```

(This example also demonstrates the behaviour of the easing functions in some special cases: when the endpoints  $b \leq a$ , and in particular the degenerate case where a = b, in which the library chooses to consider the function that is 1 for all  $x \geq 0$  and 0 otherwise.)

Like all functions declared in this way, the functions implemented by easing are also available as "public" macros, such as \pgfmathsmoothstep:

```
S_1(0) = 0.0
S_1(0.25) = 0.15625
S_1(0.5) = 0.5
S_1(0.75) = 0.84375
S_1(1) = 1.0
```

```
\input pgf
\usepgflibrary{easing}
\foreach\x in{0,0.25,...,1}{
  \pgfmathsmoothstep{0}{1}{\x}
  $$S_1(\x)=\pgfmathresult$\par
}
\end
```

See Part VIII of the PGF manual for more details on the mathematical engine.

#### 3.1 Naming conventions

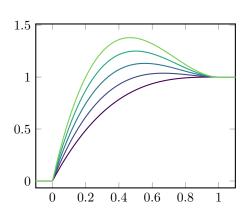
For each shape, three functions are declared, all of which take three arguments a, b, and x. Where a < b, all of these function take value 0 whenever  $x \le a$  and 1 whenever  $x \ge b$ . The names of the functions adhere to the following pattern:

- The ease-in form  $\langle shape \rangle$  easein(a,b,x) has easing applied near the endpoint a.
- The ease-out form  $\langle shape \rangle$  easeout (a,b,x) has easing applied near the endpoint b. Its graph is that of the ease-in form reflected about both axes.
- The step function form  $\langle shape \rangle$  step(a,b,x) has easing applied near both endpoints. Its graph is that of the ease-in and ease-out forms concatenated then appropriately scaled.

```
\input tikz
\usepgflibrary{easing}
\tikzpicture
\foreach\x in{0,...,12}{
    \draw[gray,dashed]
    (0,-1) -- (0,4) (5,-1) -- (5,4);
    \draw[thick]
    ({5*smootheasein(0,12,\x)},3)
    circle (0.25)
    ({5*smoothstep(0,12,\x)},1.5)
    circle (0.25)
    ({5*smootheaseout(0,12,\x)},0)
    circle (0.25);
}
\endtikzpicture
\end
```

### 3.2 Specifying parameters

Some of these shapes can be modified by adjusting one or more parameters, which is done through pgfkeys: the parameter  $\langle param \rangle$  for functions of shape  $\langle shape \rangle$  is specified by setting the PGF key /easing/ $\langle shape \rangle / \langle param \rangle$ :



```
\input pgfplots
\usepgflibrary{easing}
\tikzpicture
\axis[
  domain=-0.2:1.2, samples=64,
  xmin=0, xmax=1, enlarge x limits,
  cycle list={
    [samples of colormap=6 of viridis]},
  no marks, thick]
\pgfplotsinvokeforeach{0,...,4}{
  \pgfkeys{easing,back/overshoot=#1}
  \addplot{backeaseout(0,1,x)};
}
\endaxis
\endtikzpicture
\end
```

Setting a parameter affects the ease-in, step, and ease-out forms of the relevant function at once.

For detailed descriptions of the parameters admitted by each shape, see the following section.

# 4 List of easing function shapes

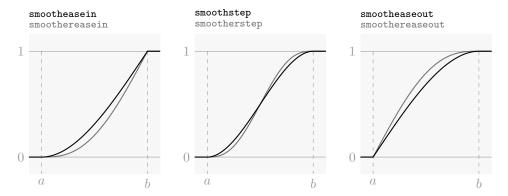
An exhaustive list follows of all the easing functions implemented by the easing library. For clarity, where mathematical expressions are given for functions, they are written in terms of a parameter t equal to  $\frac{x}{b-a}$ .

#### 4.1 Polynomials

#### 4.1.1 The smooth and smoother shapes

The step function form of the smooth shape is a third-order Hermite polynomial interpolation between 0 and 1, so that the first derivate at the endpoints are zero. It is defined  $3t^2 - 2t^3$  for 0 < t < 1.

The step function form of the **smoother** shape is a fifth-order Hermite polynomial interpolation between 0 and 1, so that the first and second derivatives at the endpoints are zero. It is defined  $10t^3 - 15t^4 + 6t^5$  for  $0 \le t \le 1$ .

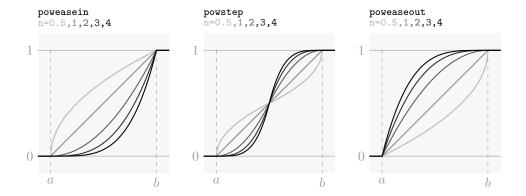


#### 4.1.2 The pow shape and friends (linear, quad, cubic, quart, and quint)

Polynomial easing. The ease-in form is defined as  $t^n$  for  $0 \le t \le 1$ , where the exponent n is set with the PGF key /easing/pow/exponent, and should be greater than 0. The parameter defaults to n = 2.4.

When n = 1, the function is linear between 0 and 1. For  $0 < n \le 1$ , the ease-in form has discontinuous derivative at 0.

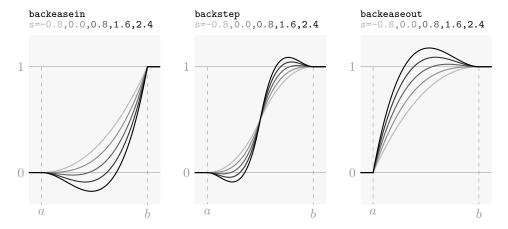
The shapes linear, quad, cubic, quart, and quint are the same functions as pow with n = 1, ..., 5, respectively. Computations for these shapes are implemented with TEX registers, which is a little faster and more accurate than setting the argument then evaluating the equivalent pow function.



### 4.1.3 The back shape

Anticipatory easing. The ease-in form is defined as  $t^2(1-t)s+t^3$  for  $0 \le t \le 1$ , where the parameter s is set with the PGF key /easing/back/overshoot. The parameter defaults to s=1.6.

When  $s \leq 0$ , there is no overshoot. When s = 0, the function is equivalent to pow with n = 3.

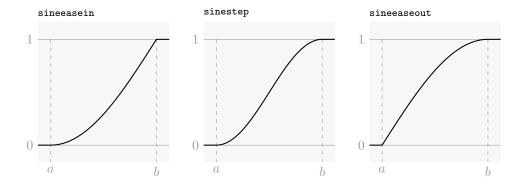


# 4.2 Trigonometric and exponential

### 4.2.1 The sine shape

An easing function that looks like a section of a sinusoid. The ease-out form is defined as  $\sin(\frac{\pi}{2}t)$  for  $0 \le t \le 1$ .

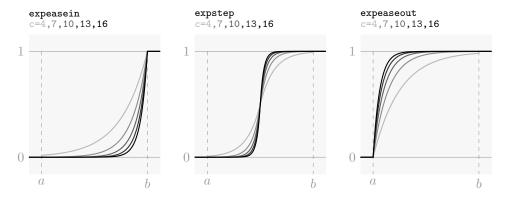
This shape admits no parameters.



### 4.2.2 The exp shape

An easing function that looks like an exponential function. The ease-in form is defined as  $e^{c(t-1)}$  for  $0 \le t \le 1$ , where the parameter c is set with the PGF key /easing/exp/speed, and should be greater than 0. The parameter defaults to c = 7.2.

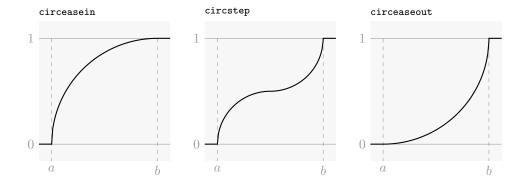
Because of the nature of the exponential function, this shape is only approximately continuous at the endpoints a and b. In practice, the discontinuity only becomes noticeable for small c, around  $c \le 4$ .



## 4.3 Other

#### 4.3.1 The circ shape

An easing function whose graph is part of an ellipse. This shape admits no parameters.

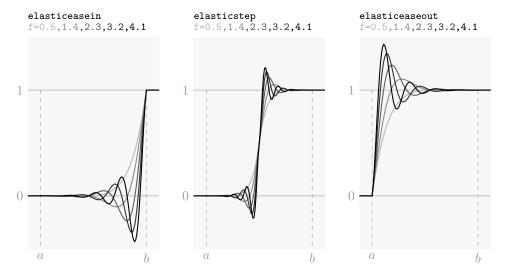


### 4.3.2 The elastic shape

Easing function that looks like a damped harmonic oscillator. The ease-out form is defined as  $e^c(t-1)\cos(2\pi f(1-t))$ . This shape admits two parameters:

- The frequency f is the number of oscillations between the endpoints. It is set with the PGF key /easing/elastic/frequency, and should be greater than 0. The frequency defaults to f = 3.
- The damping coefficient b affects the speed at which the amplitude decays. It is set with the PGF key /easing/elastic/damping, and should be greater than zero. The damping coefficient defaults to b=7.2.

The function overshoots the range [0,1] when f > 0.5. For  $0 < f \le 1$ , this function becomes a family of anticipatory easing curves that look slightly different from the back shape but are more expensive to compute.



# 5 Implementation

\ifeasing@withfpu \easing@divide This library uses TEX registers and PGF's mathematical engine for computations.

It is possible that the user is loading this library together with the floating point unit library. We save the basic routines from pgfmath, so that when this happens, the FPU doesn't break everything when it does a switcharoo with the pgfmath macros.

```
1 \newif\ifeasing@withfpu
2 \expandafter\ifx\csname pgflibraryfpuifactive\endcsname\relax
3 \easing@withfpufalse
4 \else
5 \easing@withfputrue
6 \fi
7 \ifeasing@withfpu
8 \let\easing@cos\pgfmath@basic@cos@
9 \let\easing@divide\pgfmath@basic@divide@
10 \let\easing@exp\pgfmath@basic@exp@
11 \let\easing@ln\pgfmath@basic@ln@
12 \let\easing@sqrt\pgfmath@basic@sqrt@
13 \else
14 \let\easing@cos\pgfmathcos@
15 \let\easing@divide\pgfmathdivide@
16 \let\easing@exp\pgfmathexp@
17 \let\easing@ln\pgfmathln@
18 \let\easing@sqrt\pgfmathsqrt@
19 \fi
```

\easing@linearstep@ne \easing@linearstep@fixed \easing@linearstep@float \easing@linearstep In absence of the FPU, the next section of code defines \easing@linearstep, which expects as arguments plain numbers (i.e. things that can be assigned to dimension registers). The net effect of \easing@linearstep{#1}{#2}{#3} is to set \pgfmathresult to  $\frac{\#3-\#1}{\#2-\#1}$ , clamped to between 0 and 1.

If the FPU is loaded, \easing@linearstep is instead named \easing@linearstep@fixed, and we additionally define \easing@linearstep@float, which expects FPU-format floats as arguments. We do not format the output as a float since the FPU is smart enough to do that conversion quietly on its own.

The \easing@linearstep routine is the first step in the definition of all other routines that compute easing functions.

```
20 \def\easing@linearstep@ne#1{%
21 \begingroup
22 \pgf@x#1pt
23 \ifdim1pt<\pgf@x\pgf@x 1pt\fi
24 \ifdim0pt>\pgf@x\pgf@x 0pt\fi
25 \pgfmathreturn\pgf@x
26 \endgroup
27 }%
```

```
28 \expandafter\def
\begingroup
30
    \pgf@xa#3pt
31
32
    \pgf@xb#2pt
33
    \pgf@xc#1pt
34
    \ifdim\pgf@xb=\pgf@xc
    \edef\pgfmathresult{\ifdim\pgf@xa>\pgf@xb 1\else 0\fi}%
35
36
    \advance\pgf@xa-\pgf@xc
37
    \advance\pgf@xb-\pgf@xc
38
    \easing@divide{\pgfmath@tonumber\pgf@xa}{\pgfmath@tonumber\pgf@xb}%
39
    \easing@linearstep@ne\pgfmathresult
40
41
    \pgfmathsmuggle\pgfmathresult
42
    \endgroup
43
44 }%
45 \ifeasing@withfpu
46 \def\easing@linearstep@float#1#2#3{%
47
    \begingroup
    \pgfmathfloatsubtract{#3}{#1}%
48
    \edef\pgf@tempa{\pgfmathresult}%
49
    \pgfmathfloatsubtract{#2}{#1}%
50
    \edef\pgf@tempb{\pgfmathresult}%
51
52
    \pgfmathfloatifflags{\pgf@tempb}{0}{%
53
      \pgfmathfloatifflags{\pgf@tempa}{-}{%
        \edef\pgfmathresult{0}%
54
55
        \ensuremath{\texttt{def}\pgfmathresult}{1}\%
56
      }%
57
    }{%
58
59
      \pgfmathfloatdivide\pgf@tempa\pgf@tempb
60
      \pgfmathfloattofixed{\pgfmathresult}%
      \easing@linearstep@ne\pgfmathresult
61
    }%
62
    \pgfmathsmuggle\pgfmathresult
63
    \endgroup
64
65 }%
66 \def\easing@linearstep#1#2#3{%
    \pgflibraryfpuifactive{%
67
68
      \easing@linearstep@float{#1}{#2}{#3}}{%
      \easing@linearstep@fixed{#1}{#2}{#3}}%
69
70 }%
71 \fi
```

\easing@linearstep@easein@ne \easing@linearstep@easeout@ne The linear ease-in and ease-out functions are identical to the linear step function. We define the respective macros so as not to surprise the user with their absence.

```
72 \let\easing@lineareasein\easing@linearstep
73 \pgfmathdeclarefunction{lineareasein}{3}{%
```

```
74 \easing@lineareasein{#1}{#2}{#3}}%
75 \let\easing@lineareaseout\easing@linearstep
76 \pgfmathdeclarefunction{lineareaseout}{3}{%
77 \easing@lineareasein{#1}{#2}{#3}}%
```

\easing@derive@easein@nefromstep@ne \easing@derive@easeout@nefromstep@ne \easing@derive@step@nefromeasein@ne \easing@derive@easeout@nefromeasein@ne The pattern in general is that, for each shape, we define the one-parameter version of the step, ease-in, and ease-out routines interpolating between values 0 at 1 at the ends of the unit interval. Then by composing with \easing@linearstep, we obtain the three-parameter versions that allow the user to specify the begin and end points of the interpolation.

Most of the time it suffices to define just one of the three one-parameter versions of a shape to be able to infer the form of all three. This is done with the \easing@derive-from- macros.

```
78 \def\easing@derive@easein@nefromstep@ne#1{%
    \expandafter\def\csname easing@#1easein@ne\endcsname##1{%
80
       \begingroup
81
       \pgf@x##1 pt
      \divide\pgf@x 2
82
      \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
83
84
       \pgf@x\pgfmathresult pt
       \multiply\pgf@x 2
85
       \pgfmathreturn\pgf@x
       \endgroup
87
    }%
88
89 }%
90 \def\easing@derive@easeout@nefromstep@ne#1{%
    \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
91
       \begingroup
92
       \pgf@x##1 pt
93
94
      \divide\pgf@x 2
      \advance\pgf@x 0.5pt
95
      96
       \pgf@x\pgfmathresult pt
97
       \multiply\pgf@x 2
98
       \advance\pgf@x -1pt
100
       \pgfmathreturn\pgf@x
       \endgroup
101
    }%
102
103 }%
104 \def\easing@derive@step@nefromeasein@ne#1{%
    \expandafter\def\csname easing@#1step@ne\endcsname##1{%
105
106
      \begingroup
      \pgf@x##1 pt
107
      \multiply\pgf@x 2
108
      \ifdim\pgf@x<1pt
109
      \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
110
111
       \pgf@x\pgfmathresult pt
112
       \divide\pgf@x 2
```

```
\else
113
        \multiply\pgf@x -1
114
        \advance\pgf@x 2pt
115
       \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
116
117
        \pgf@x\pgfmathresult pt
118
        \divide\pgf@x 2
119
        \multiply\pgf@x -1
        \advance\pgf@x 1pt
120
        \fi
121
        \pgfmathreturn\pgf@x
122
123
        \endgroup
     }%
124
125 }%
126 \def\easing@derive@easeout@nefromeasein@ne#1{%
     \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
127
        \begingroup
128
        \pgf@x##1pt
129
        \multiply\pgf@x -1
130
131
        \advance\pgf@x 1pt
132
        \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
133
        \pgf@x\pgfmathresult pt
        \multiply\pgf@x -1
134
        \advance\pgf@x 1pt
135
        \pgfmathreturn\pgf@x
136
137
        \endgroup
     }%
138
139 }%
```

\easing@pgfmathinstall

The three-parameter versions of each routine is installed into the mathematical engine, so that they are available in \pgfmathparse.

```
140 \def\easing@pgfmathinstall#1{%
     \pgfmathdeclarefunction{#1step}{3}{%
141
       142
       \csname easing@#1step@ne\endcsname\pgfmathresult
143
144
    }%
145
     \pgfmathdeclarefunction{#1easein}{3}{%
       \easing@linearstep{##1}{##2}{##3}%
146
       \csname easing@#1easein@ne\endcsname\pgfmathresult
147
148
     \pgfmathdeclarefunction{#1easeout}{3}{%
149
       \easing@linearstep{##1}{##2}{##3}%
150
       \csname easing@#1easeout@ne\endcsname\pgfmathresult
151
    }%
152
153 }%
```

\easing@smoothstep@ne \easing@smootheasein@ne \easing@smootheaseout@ne The smooth shape.

154 \def\easing@smoothstep@ne#1{% 155 \begingroup

```
\pgf@x#1pt
156
     \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
157
     \mathsf{multiply}\mathsf{pgf@x-2}
158
     \advance\pgf@x 3pt
159
160
     \pgf@x\pgf@temp\pgf@x
161
     \pgf@x\pgf@temp\pgf@x
162
     \pgfmathreturn\pgf@x
163
     \endgroup
164 }%
165 \easing@derive@easein@nefromstep@ne{smooth}%
166 \easing@derive@easeout@nefromstep@ne{smooth}%
167 \easing@pgfmathinstall{smooth}%
 The smoother shape.
168 \def\easing@smootherstep@ne#1{%
     \begingroup
     \pgf@x#1pt
170
     \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
171
     \multiply\pgf@x 6
172
     \advance\pgf@x -15pt
173
174
     \pgf@x\pgf@temp\pgf@x
175
     \advance\pgf@x 10pt
176
     \pgf@x\pgf@temp\pgf@x
177
     \pgf@x\pgf@temp\pgf@x
```

182 \easing@derive@easein@nefromstep@ne{smoother}%
183 \easing@derive@easeout@nefromstep@ne{smoother}%

\easing@powstep@ne \easing@poweasein@ne \easing@poweaseout@ne

\easing@smootherstep@ne

\easing@smoothereasein@ne

\easing@smoothereaseout@ne

The pow shape.

\endgroup

178

179

180 181 }%

\pgf@x\pgf@temp\pgf@x

184 \easing@pgfmathinstall{smoother}%

\pgfmathreturn\pgf@x

Because of some wonkiness in the FPU, \pgfmath@pow@basic@ actually doesn't work. Instead of invoking the pow function, we compute  $t^n$  approximately by computing  $e^{n \ln t}$  using ln and exp instead (which is what pgfmath does anyway when the exponent is not an integer.)

```
185 \pgfkeys{/easing/.is family}%
186 \pgfkeys{easing,
187  pow/exponent/.estore in=\easing@param@pow@exponent,
188  pow/exponent/.default=2.4,
189  pow/exponent}%
190 \def\easing@poweasein@ne#1{%
191  \begingroup
192  \pgf@x#1pt
193  \ifdim\pgf@x=0pt
194  \edef\pgfmathresult{0}%
```

```
\pgf@x\pgfmathresult pt
                              \pgf@x\easing@param@pow@exponent\pgf@x
                         198
                              \easing@exp{\pgfmath@tonumber\pgf@x}%
                         199
                         200
                         201
                              \pgfmathsmuggle\pgfmathresult
                         202
                              \endgroup
                         203 }%
                         204 \easing@derive@easeout@nefromeasein@ne{pow}%
                         205 \easing@derive@step@nefromeasein@ne{pow}%
                         206 \easing@pgfmathinstall{pow}%
    \easing@quadstep@ne
                          The quad-, cubic-, quart-, and quint- routines have explicit definitions.
  \easing@quadeasein@ne
                         207 \def\easing@quadeasein@ne#1{%
 \easing@quadeaseout@ne
                              \begingroup
   \easing@cubicstep@ne
                              \pgf@x#1pt
 \easing@cubiceasein@ne
                              \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
\easing@cubiceaseout@ne
                              \pgf@x\pgf@temp\pgf@x
   \easing@quartstep@ne 212
                              \pgfmathreturn\pgf@x
 \easing@quarteasein@ne 213
                              \endgroup
\easing@quarteaseout@ne 214 }%
   \easing@quintstep@ne 215 \easing@derive@step@nefromeasein@ne{quad}%
 \easing@quinteasein@ne 216 \easing@derive@easeout@nefromeasein@ne{quad}%
\verb|\easing@quinteaseout@ne|| 217 \verb|\easing@pgfmathinstall{quad}| % \\
                         218 %
                         219 \def\easing@cubiceasein@ne#1{%
                         220
                              \begingroup
                         221
                              \pgf@x#1pt
                              \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                         222
                         223
                              \pgf@x\pgf@temp\pgf@x
                              \pgf@x\pgf@temp\pgf@x
                         224
                         225
                              \pgfmathreturn\pgf@x
                         ^{226}
                              \endgroup
                         227 }%
                         228 \easing@derive@step@nefromeasein@ne{cubic}%
                         229 \easing@derive@easeout@nefromeasein@ne{cubic}%
                         230 \easing@pgfmathinstall{cubic}%
                         231 %
                         232 \def\easing@quarteasein@ne#1{%
                         233
                              \begingroup
                         234
                              \pgf@x#1pt
                              \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                         235
                              \pgf@x\pgf@temp\pgf@x
                         236
                              \pgf@x\pgf@temp\pgf@x
                         237
                              \pgf@x\pgf@temp\pgf@x
                         238
                              \pgfmathreturn\pgf@x
                         239
                         240
                              \endgroup
```

\else

\easing@ln{#1}%

195

196

197

241 }%

```
242 \easing@derive@step@nefromeasein@ne{quart}%
                        243 \easing@derive@easeout@nefromeasein@ne{quart}%
                        244 \easing@pgfmathinstall{quart}%
                        245 %
                        246 \def\easing@quinteasein@ne#1{%
                        247
                             \begingroup
                        248
                             \pgf@x#1pt
                             \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                        249
                             \pgf@x\pgf@temp\pgf@x
                        250
                             \pgf@x\pgf@temp\pgf@x
                        251
                             \pgf@x\pgf@temp\pgf@x
                        252
                        253
                              \pgf@x\pgf@temp\pgf@x
                             \pgfmathreturn\pgf@x
                        255
                             \endgroup
                        256 }%
                        257 \easing@derive@step@nefromeasein@ne{quint}%
                        258 \easing@derive@easeout@nefromeasein@ne{quint}%
                        259 \easing@pgfmathinstall{quint}%
   \easing@backstep@ne
                         The back shape.
 \easing@backeasein@ne
                        260 \pgfkeys{easing,
\easing@backeaseout@ne
                             back/overshoot/.estore in=\easing@param@back@overshoot,
                        ^{261}
                        262
                             back/overshoot/.default=1.6,
                             back/overshoot}%
                        263
                        264 \ensuremath{\mbox{\sc def}\mbox{\sc easein@ne\#1}}\%
                             \begingroup
                        265
                             \pgf@x#1pt
                        266
                             \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                        267
                             \advance\pgf@x -1pt
                        268
                             \pgf@x\easing@param@back@overshoot\pgf@x
                        269
                        270
                             \advance\pgf@x\pgf@temp pt
                             \pgf@x\pgf@temp\pgf@x
                        271
                        272
                             \pgf@x\pgf@temp\pgf@x
                             \pgfmathreturn\pgf@x
                        273
                        274
                             \endgroup
                        275 }%
                        276 \easing@derive@step@nefromeasein@ne{back}%
                        277 \easing@derive@easeout@nefromeasein@ne{back}%
                        278 \verb|\easing@pgfmathinstall{back}| %
   \easing@sinestep@ne
                         The sine shape.
 \easing@sineeasein@ne
                         We write down both the easein and step forms of this, since they are simple
\easing@sineeaseout@ne
                         compared to what would have been obtained by \easing@derive-.
                        279 \def\easing@sineeasein@ne#1{%
                        280
                             \begingroup
                             \pgf@x#1pt
                             \multiply\pgf@x 90
```

```
\easing@cos{\pgfmath@tonumber\pgf@x}%
                        283
                             \pgf@x\pgfmathresult pt
                        284
                             \multiply\pgf@x -1
                        285
                             \advance\pgf@x 1pt
                        286
                             \pgfmathreturn\pgf@x
                        287
                        288
                             \endgroup
                        289 }%
                        290 \def\easing@sinestep@ne#1{%
                             \begingroup
                        291
                             \pgf@x#1pt
                        292
                             \multiply\pgf@x 180
                        293
                             \easing@cos{\pgfmath@tonumber\pgf@x}%
                        294
                        295
                             \pgf@x\pgfmathresult pt
                             \divide\pgf@x 2
                        296
                        297
                             \multiply\pgf@x -1
                             \advance\pgf@x 0.5pt
                        298
                             \pgfmathreturn\pgf@x
                        299
                             \endgroup
                        300
                        301 }%
                        302 \easing@derive@easeout@nefromeasein@ne{sine}%
                        303 \easing@pgfmathinstall{sine}%
                        The exp shape.
    \easing@expstep@ne
  \easing@expeasein@ne
                        304 \pgfkeys{easing,
 \easing@expeaseout@ne
                             exp/speed/.estore in=\easing@param@exponent@speed,
                        306
                             exp/speed/.default=7.2,
                             exp/speed}%
                        307
                        308 \def\easing@expeasein@ne#1{%
                             \begingroup
                        309
                        310
                             \pgf@x#1pt
                             \advance\pgf@x -1pt
                        311
                        312
                             \pgf@x\easing@param@exponent@speed\pgf@x
                             \easing@exp{\pgfmath@tonumber\pgf@x}%
                        313
                             \pgfmathsmuggle\pgfmathresult
                        314
                        315
                             \endgroup
                        316 }%
                        317 \easing@derive@step@nefromeasein@ne{exp}%
                        318 \easing@derive@easeout@nefromeasein@ne{exp}%
                        319 \easing@pgfmathinstall{exp}%
   \easing@circstep@ne
                        The circ shape.
 \easing@circeasein@ne
                        320 \def\easing@circeasein@ne#1{%
\easing@circeaseout@ne
                        321
                             \begingroup
                             \pgf@x#1pt
                        322
                        323
                             \advance\pgf@x -1pt
                             \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
                        324
                        325
                             \pgf@x\pgf@temp\pgf@x
                        326
                             \multiply\pgf@x -1
```

```
327
                               \advance\pgf@x 1pt
                         328
                               \easing@sqrt{\pgfmath@tonumber\pgf@x}%
                               \pgfmathsmuggle\pgfmathresult
                         329
                              \endgroup
                         330
                         331 }%
                         332 \easing@derive@step@nefromeasein@ne{circ}%
                         333 \easing@derive@easeout@nefromeasein@ne{circ}%
                         334 \easing@pgfmathinstall{circ}%
                          The elastic shape.
   \easing@elasticstep@ne
\easing@elasticeasein@ne
                         335 \pgfkeys{easing,
\easing@elasticeaseout@ne
                              elastic/frequency/.estore in=\easing@param@elastic@frequency,
                         336
                              elastic/damping/.estore in=\easing@param@elastic@damping,
                         337
                              elastic/frequency/.default=3,
                         338
                              elastic/damping/.default=7.2,
                         339
                              elastic/frequency, elastic/damping}%
                         341 \def\easing@elasticeasein@ne#1{%
                              \begingroup
                         342
                              \pgf@xa#1pt
                         343
                              \advance\pgf@xa -1pt
                         344
                               \pgf@xb-\pgf@xa
                         345
                         346
                               \pgf@xa\easing@param@elastic@damping\pgf@xa
                         347
                               \easing@exp{\pgfmath@tonumber\pgf@xa}%
                               \pgf@xa\pgfmathresult pt
                         348
                               \pgf@xb 360\pgf@xb
                         349
                               \pgf@xb\easing@param@elastic@frequency\pgf@xb
                         350
                               \verb|\cos{\pgfmath@tonumber\pgf@xb}||
                         351
                               \pgf@xa\pgfmathresult\pgf@xa
                         352
                               \pgfmathreturn\pgf@xa
                               \endgroup
                         354
                         355 }%
                         356 \easing@derive@step@nefromeasein@ne{elastic}%
                         357 \easing@derive@easeout@nefromeasein@ne{elastic}%
                         Change History
```

0.1 General: Initial version . . . . . . . . 1