

# The **easing** Library for PGF

Loh Ka-tsun

July 15, 2021

## 1 Introduction

This library provides easing functions for the PGF mathematical engine.

## 2 Usage

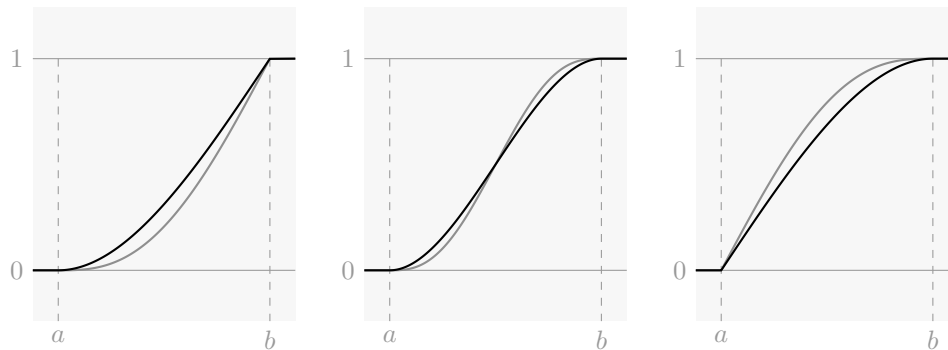
## 3 List of easing function shapes

### 3.1 Polynomial and trigonometric

#### 3.1.1 The smooth and smoother shapes

The step function form of the **smooth** shape is a third-order Hermite polynomial interpolation between 0 and 1, so that the first derivate at the endpoints are zero. It is defined  $3t^2 - 2t^3$  for  $0 \leq t \leq 1$ .

The step function form of the **smoother** shape is a fifth-order Hermite polynomial interpolation between 0 and 1, so that the first and second derivates at the endpoints are zero. It is defined  $10t^3 - 15t^4 + 6t^5$  for  $0 \leq t \leq 1$ .

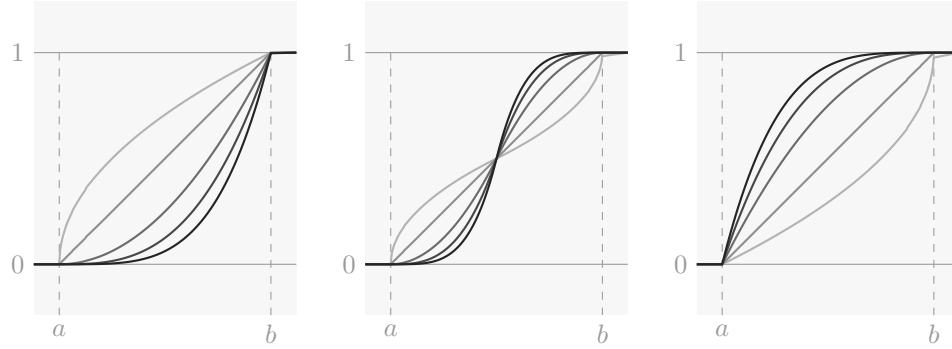


### 3.1.2 The pow shape and friends (linear, quad, cubic, quart, and quint)

Polynomial easing. The ease-in form is defined as  $t^n$  for  $0 \leq t \leq 1$ , where the exponent  $n$  is set by the PGF key `/easing/pow/exponent`, and should be greater than 0. The exponent defaults to 2.4.

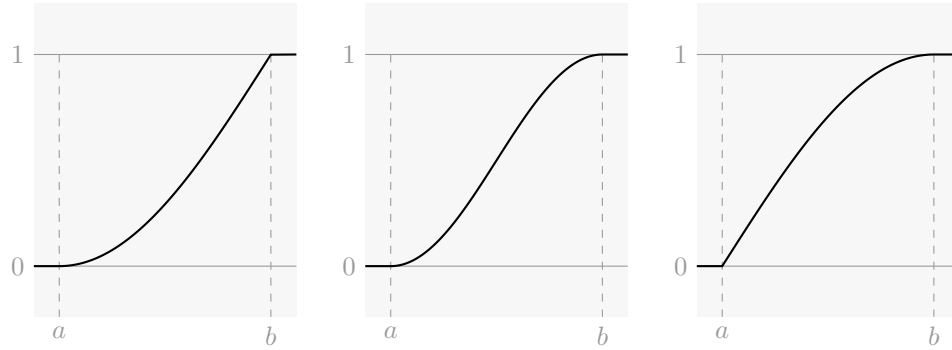
When  $n = 1$ , the function is linear between 0 and 1. For  $0 < n \leq 1$ , the ease-in form has discontinuous derivative at 0.

The shapes `linear`, `quad`, `cubic`, `quart`, and `quint` are the same functions as `pow` with  $n = 1, \dots, 5$ , respectively. Computations for these shapes are implemented with  $\text{\TeX}$  registers, which is a little faster and more accurate than setting the argument then evaluating the equivalent `pow` function.



### 3.1.3 The sine shape

An easing function that looks like a section of a sinusoid. The ease-out form is defined as  $\sin(\frac{\pi}{2}t)$  for  $0 \leq t \leq 1$ .



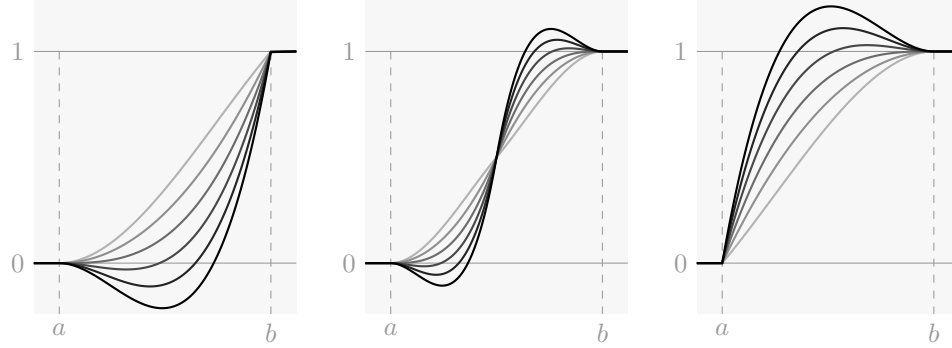
## 3.2 Other

### 3.2.1 The back shape

Anticipatory easing. The ease-in form is defined as  $t^2(1-t)s + t^3$  for  $0 \leq t \leq 1$ , where the parameter  $s$  is set by the PGF key `/easing/back/overshoot`. The

parameter  $n$  defaults to 1.6.

When  $s \leq 0$ , there is no overshoot. When  $s = 0$ , the function is equivalent to `pow` with  $n = 3$ .



## 4 Implementation

`\ifeasing@withfpu`  
`\easing@divide`

This library uses  $\text{\TeX}$  registers and PGF's mathematical engine for computations.

It is possible that the user is loading this library together with the floating point unit library. We save the basic routines from `pgfmath`, so that when this happens, the FPU doesn't break everything when it does a switcharoo with the `pgfmath` macros.

```

1 \newif\ifeasing@withfpu
2 \expandafter\ifx\csname pgflibraryfpuifactive\endcsname\relax
3 \easing@withfpufalse
4 \else
5 \easing@withfptrue
6 \fi
7 \ifeasing@withfpu
8 \let\easing@divide\pgfmath@basic@divide@
9 \let\easing@cos\pgfmath@basic@cos@
10 \let\easing@exp\pgfmath@basic@exp@
11 \let\easing@ln\pgfmath@basic@ln@
12 \else
13 \let\easing@divide\pgfmathdivide@
14 \let\easing@cos\pgfmathcos@
15 \let\easing@exp\pgfmathexp@
16 \let\easing@ln\pgfmathln@
17 \fi

```

`\easing@linearstep@ne`  
`\easing@linearstep@fixed`  
`\easing@linearstep@float`  
`\easing@linearstep`

In absence of the FPU, the next section of code defines `\easing@linearstep`, which expects as arguments plain numbers (i.e. things that can be assigned to dimension registers). The net effect of `\easing@linearstep{#1}{#2}{#3}` is to set `\pgfmathresult` to  $\frac{\#3-\#1}{\#2-\#1}$ , clamped to between 0 and 1.

If the FPU is loaded, `\easing@linearstep` is instead named `\easing@linearstep@fixed`, and we additionally define `\easing@linearstep@float`, which expects FPU-format floats as arguments. We do not format the output as a float since the FPU is smart enough to do that conversion quietly on its own.

The `\easing@linearstep` routine is the first step in the definition of all other routines that compute easing functions.

```

18 \def\easing@linearstep@one#1{%
19   \begingroup
20   \pgf@x#1pt
21   \ifdim1pt<\pgf@x\pgf@x 1pt\fi
22   \ifdim0pt>\pgf@x\pgf@x 0pt\fi
23   \pgfmathreturn\pgf@x
24   \endgroup
25 }%
26 \expandafter\def
27 \csname easing@linearstep\ifeasing@withfpu @fixed\fi\endcsname#1#2#3{%
28   \begingroup
29   \pgf@xa#3pt
30   \pgf@xb#2pt
31   \pgf@xc#1pt
32   \ifdim\pgf@xb=\pgf@xc
33   \edef\pgfmathresult{\ifdim\pgf@xa>\pgf@xb 1\else 0\fi}%
34   \else
35   \advance\pgf@xa-\pgf@xc
36   \advance\pgf@xb-\pgf@xc
37   \easing@divide{\pgfmath@tonumber\pgf@xa}{\pgfmath@tonumber\pgf@xb}%
38   \easing@linearstep@one\pgfmathresult
39   \fi
40   \pgfmathsmuggle\pgfmathresult
41   \endgroup
42 }%
43 \ifeasing@withfpu
44 \def\easing@linearstep@float#1#2#3{%
45   \begingroup
46   \pgfmathfloatsubtract{#3}{#1}%
47   \edef\pgf@tempa{\pgfmathresult}%
48   \pgfmathfloatsubtract{#2}{#1}%
49   \edef\pgf@tempb{\pgfmathresult}%
50   \pgfmathfloatifflags{\pgf@tempb}{0}{%
51     \pgfmathfloatifflags{\pgf@tempa}{-}{%
52       \edef\pgfmathresult{0}%
53     }{%
54       \edef\pgfmathresult{1}%
55     }%
56   }{%
57     \pgfmathfloatdivide\pgf@tempa\pgf@tempb
58     \pgfmathfloattofixed{\pgfmathresult}%
59     \easing@linearstep@one\pgfmathresult

```

```

60 }%
61 \pgfmathsmuggle\pgfmathresult
62 \endgroup
63 }%
64 \def\easing@linearstep#1#2#3{%
65 \pgflibraryfpuiactive{%
66 \easing@linearstep@float{#1}{#2}{#3}}{%
67 \easing@linearstep@fixed{#1}{#2}{#3}}%
68 }%
69 \fi

```

`\easing@linearstep@easein@ne` The linear ease-in and ease-out functions are identical to the linear step function.  
`\easing@linearstep@easeout@ne` We define the respective macros so as not to surprise the user with their absence.

```

70 \let\easing@lineareasein\easing@linearstep
71 \pgfmathdeclarefunction{lineareasein}{3}{%
72 \easing@lineareasein{#1}{#2}{#3}}%
73 \let\easing@lineareaseout\easing@linearstep
74 \pgfmathdeclarefunction{lineareaseout}{3}{%
75 \easing@lineareasein{#1}{#2}{#3}}%

```

`\easing@derive@easein@nefromstep@ne` The pattern in general is that, for each shape, we define the one-parameter version  
`\easing@derive@easeout@nefromstep@ne` of the step, ease-in, and ease-out routines interpolating between values 0 at 1 at  
`\easing@derive@step@nefromeasein@ne` the ends of the unit interval. Then by composing with `\easing@linearstep`, we  
`\easing@derive@easeout@nefromeasein@ne` obtain the three-parameter versions that allow the user to specify the begin and  
end points of the interpolation.

Most of the time it suffices to define just one of the three one-parameter versions of a shape to be able to infer the form of all three. This is done with the `\easing@derive-from-` macros.

```

76 \def\easing@derive@easein@nefromstep@ne#1{%
77 \expandafter\def\csname easing@#1easein@ne\endcsname##1{%
78 \begingroup
79 \pgf@x##1 pt
80 \divide\pgf@x 2
81 \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
82 \pgf@x\pgfmathresult pt
83 \multiply\pgf@x 2
84 \pgfmathreturn\pgf@x
85 \endgroup
86 }%
87 }%
88 \def\easing@derive@easeout@nefromstep@ne#1{%
89 \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
90 \begingroup
91 \pgf@x##1 pt
92 \divide\pgf@x 2
93 \advance\pgf@x 0.5pt

```

```

94     \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
95     \pgf@x\pgfmathresult pt
96     \multiply\pgf@x 2
97     \advance\pgf@x -1pt
98     \pgfmathreturn\pgf@x
99     \endgroup
100 }%
101 }%
102 \def\easing@derive@step@nefromeasein@ne#1{%
103   \expandafter\def\csname easing@#1step@ne\endcsname##1{%
104     \begingroup
105       \pgf@x##1 pt
106       \multiply\pgf@x 2
107       \ifdim\pgf@x<1pt
108         \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
109         \pgf@x\pgfmathresult pt
110         \divide\pgf@x 2
111       \else
112         \multiply\pgf@x -1
113         \advance\pgf@x 2pt
114         \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
115         \pgf@x\pgfmathresult pt
116         \divide\pgf@x 2
117         \multiply\pgf@x -1
118         \advance\pgf@x 1pt
119       \fi
120       \pgfmathreturn\pgf@x
121     \endgroup
122   }%
123 }%
124 \def\easing@derive@easeout@nefromeasein@ne#1{%
125   \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
126     \begingroup
127       \pgf@x##1pt
128       \multiply\pgf@x -1
129       \advance\pgf@x 1pt
130       \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
131       \pgf@x\pgfmathresult pt
132       \multiply\pgf@x -1
133       \advance\pgf@x 1pt
134       \pgfmathreturn\pgf@x
135     \endgroup
136   }%
137 }

```

`\easing@pgfmathinstall` The three-parameter versions of each routine is installed into the mathematical engine, so that they are available in `\pgfmathparse`.

```

138 \def\easing@pgfmathinstall#1{%
139   \pgfmathdeclarefunction{#1step}{3}{%

```

```

140 \easing@linearstep{##1}{##2}{##3}%
141 \csname easing@#1step@ne\endcsname\pgfmathresult
142 }%
143 \pgfmathdeclarefunction{#1easein}{3}{%
144 \easing@linearstep{##1}{##2}{##3}%
145 \csname easing@#1easein@ne\endcsname\pgfmathresult
146 }%
147 \pgfmathdeclarefunction{#1easeout}{3}{%
148 \easing@linearstep{##1}{##2}{##3}%
149 \csname easing@#1easeout@ne\endcsname\pgfmathresult
150 }%
151 }%

```

\easing@smoothstep@ne The smooth shape.

```

\easing@smootheasein@ne
\easing@smootheaseout@ne
152 \def\easing@smoothstep@ne#1{%
153 \beginpgfgroup
154 \pgf@x#1pt
155 \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
156 \multiply\pgf@x-2
157 \advance\pgf@x 3pt
158 \pgf@x\pgf@temp\pgf@x
159 \pgf@x\pgf@temp\pgf@x
160 \pgfmathreturn\pgf@x
161 \endpgfgroup
162 }%
163 \easing@derive@easein@nefromstep@ne{smooth}%
164 \easing@derive@easeout@nefromstep@ne{smooth}%
165 \easing@pgfmathinstall{smooth}%

```

\easing@smootherstep@ne The smoother shape.

```

\easing@smoothereasein@ne
\easing@smoothereaseout@ne
166 \def\easing@smootherstep@ne#1{%
167 \beginpgfgroup
168 \pgf@x#1pt
169 \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
170 \multiply\pgf@x 6
171 \advance\pgf@x -15pt
172 \pgf@x\pgf@temp\pgf@x
173 \advance\pgf@x 10pt
174 \pgf@x\pgf@temp\pgf@x
175 \pgf@x\pgf@temp\pgf@x
176 \pgf@x\pgf@temp\pgf@x
177 \pgfmathreturn\pgf@x
178 \endpgfgroup
179 }%
180 \easing@derive@easein@nefromstep@ne{smoother}%
181 \easing@derive@easeout@nefromstep@ne{smoother}%
182 \easing@pgfmathinstall{smoother}%

```

`\easing@sinestep@ne` The sine shape.  
`\easing@sineeasein@ne` We write down both the `easein` and `step` forms of this, since they are simple  
`\easing@sineeaseout@ne` compared to what would have been obtained by `\easing@derive-`.

```

183 \def\easing@sineeasein@ne#1{%
184   \begingroup
185   \pgf@x#1pt
186   \multiply\pgf@x 90
187   \easing@cos{\pgfmath@tonumber\pgf@x}%
188   \pgf@x\pgfmathresult pt
189   \multiply\pgf@x -1
190   \advance\pgf@x 1pt
191   \pgfmathreturn\pgf@x
192   \endgroup
193 }%
194 \def\easing@sinestep@ne#1{%
195   \begingroup
196   \pgf@x#1pt
197   \multiply\pgf@x 180
198   \easing@cos{\pgfmath@tonumber\pgf@x}%
199   \pgf@x\pgfmathresult pt
200   \divide\pgf@x 2
201   \multiply\pgf@x -1
202   \advance\pgf@x 0.5pt
203   \pgfmathreturn\pgf@x
204   \endgroup
205 }%
206 \easing@derive@easeout@nefromeasein@ne{sine}%
207 \easing@pgfmathinstall{sine}%

```

`\easing@powstep@ne` The pow shape.  
`\easing@poweasein@ne` Because of some wonkiness in the FPU, instead of invoking the `pow` function  
`\easing@poweaseout@ne` from `pgfmath`, we compute  $t^n$  approximately by computing  $e^{n \ln t}$  using `ln` and  
`exp` instead (which is what `pgfmath` does anyway when the exponent is not an  
integer.)

```

208 \pgfkeys{/easing/.is family}%
209 \pgfkeys{easing,
210   pow/exponent/.estore in=\easing@param@pow@exponent,
211   pow/exponent/.default=2.4,
212   pow/exponent}%
213 \def\easing@poweasein@ne#1{%
214   \begingroup
215   \pgf@x#1pt
216   \ifdim\pgf@x=0pt
217     \edef\pgfmathresult{0}%
218   \else
219     \easing@ln{#1}%

```



```

220 \pgf@x\pgfmathresult pt
221 \pgf@x\easing@param@pow@exponent\pgf@x
222 \easing@exp{\pgfmath@tonumber\pgf@x}%
223 \fi
224 \pgfmathsmuggle\pgfmathresult
225 \endgroup
226 }%
227 \easing@derive@easeout@nefromeasein@ne{pow}%
228 \easing@derive@step@nefromeasein@ne{pow}%
229 \easing@pgfmathinstall{pow}%

\easing@quadstep@ne The quad-, cubic-, quart-, and quint- routines have explicit definitions.
\easing@quadeasein@ne
\easing@quadeaseout@ne 230 \def\easing@quadeasein@ne#1{%
\easing@cubicstep@ne 231 \begin{group}
\easing@cubiceasein@ne 232 \pgf@x#1pt
233 \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
\easing@cubiceaseout@ne 234 \pgf@x\pgf@temp\pgf@x
235 \pgfmathreturn\pgf@x
\easing@quartstep@ne 236 \end{group}
\easing@quarteasein@ne 237 }%
\easing@quarteaseout@ne 238 \easing@derive@step@nefromeasein@ne{quad}%
239 \easing@derive@easeout@nefromeasein@ne{quad}%
240 \easing@pgfmathinstall{quad}%
241
242 \def\easing@cubiceasein@ne#1{%
243 \begin{group}
244 \pgf@x#1pt
245 \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
246 \pgf@x\pgf@temp\pgf@x
247 \pgf@x\pgf@temp\pgf@x
248 \pgfmathreturn\pgf@x
249 \end{group}
250 }%
251 \easing@derive@step@nefromeasein@ne{cubic}%
252 \easing@derive@easeout@nefromeasein@ne{cubic}%
253 \easing@pgfmathinstall{cubic}%
254
255 \def\easing@quarteasein@ne#1{%
256 \begin{group}
257 \pgf@x#1pt
258 \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
259 \pgf@x\pgf@temp\pgf@x
260 \pgf@x\pgf@temp\pgf@x
261 \pgf@x\pgf@temp\pgf@x
262 \pgfmathreturn\pgf@x
263 \end{group}
264 }%
265 \easing@derive@step@nefromeasein@ne{quart}%
266 \easing@derive@easeout@nefromeasein@ne{quart}%

```

```

267 \easing@pgfmathinstall{quart}%
268
269 \def\easing@quinteasein@ne#1{%
270   \beginpgfgroup
271   \pgf@x#1pt
272   \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
273   \pgf@x\pgf@temp\pgf@x
274   \pgf@x\pgf@temp\pgf@x
275   \pgf@x\pgf@temp\pgf@x
276   \pgf@x\pgf@temp\pgf@x
277   \pgfmathreturn\pgf@x
278   \endpgfgroup
279 }%
280 \easing@derive@step@nefromeasein@ne{quint}%
281 \easing@derive@easeout@nefromeasein@ne{quint}%
282 \easing@pgfmathinstall{quint}%

\easing@backstep@ne The back shape.
\easing@backeasein@ne
\easing@backeaseout@ne
283 \pgfkeys{easing,
284   back/overshoot/.estore in=\easing@param@back@overshoot,
285   back/overshoot/.default=1.6,
286   back/overshoot}%
287 \def\easing@backeasein@ne#1{%
288   \beginpgfgroup
289   \pgf@x#1pt
290   \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
291   \advance\pgf@x -1pt
292   \pgf@x\easing@param@back@overshoot\pgf@x
293   \advance\pgf@x\pgf@temp pt
294   \pgf@x\pgf@temp\pgf@x
295   \pgf@x\pgf@temp\pgf@x
296   \pgfmathreturn\pgf@x
297   \endpgfgroup
298 }%
299 \easing@derive@step@nefromeasein@ne{back}%
300 \easing@derive@easeout@nefromeasein@ne{back}%
301 \easing@pgfmathinstall{back}%

```