The easing Library for PGF

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July 15, 2021

1 Introduction

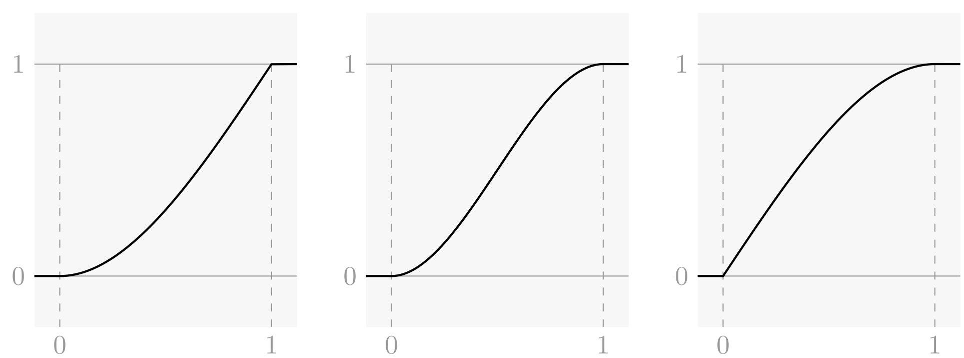
This library provides easing functions for the PGF mathematical engine.

2 Usage

3 List of easing function shapes

3.1 Polynomial and trigonometric

3.1.1 The smooth and smoother shapes

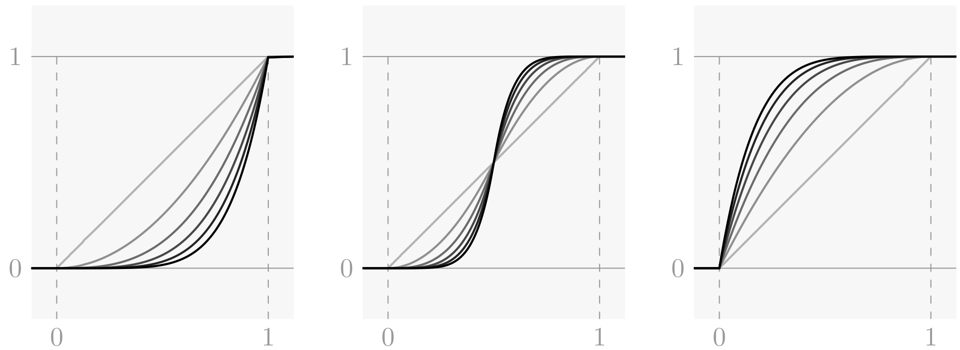


3.1.2 The pow shape and friends (linear, quad, cubic, quart, and quint)

Polynomial easing. The ease-in form is defined as t^n for $0 \leq t \leq 1$, where the exponent n is set by the PGF key `/easing/pow/exponent`, and should be greater than -1. The exponent defaults to 2.4.

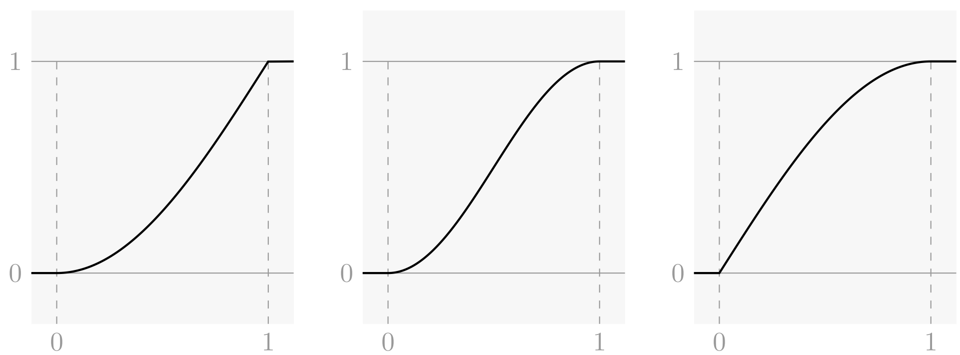
When $n = 1$, the function is linear between 0 and 1.

The shapes `linear`, `quad`, `cubic`, `quart`, and `quint` are the same functions as `pow` with $n = 1, \ldots, 5$, respectively. Computations for these shapes are implemented with TEX registers, which is a little faster and more accurate than setting the argument then evaluating the equivalent `pow` function.



3.1.3 The `sine` shape

An easing function that looks like a section of a sinusoid. The ease-out form is defined as $\sin(\frac{\pi}{2}t)$ for $0 \le t \le 1$.

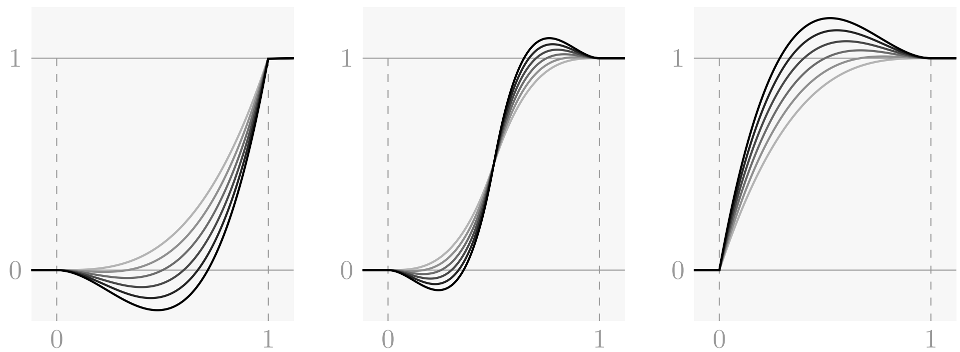


3.2 Other

3.2.1 The `back` shape

Anticipatory easing. The ease-in form is defined as $t^2(1-t)s + t^3$ for $0 \le t \le t$, where the parameter s is set by the PGF key `/easing/back/overshoot`. The parameter n defaults to 1.6.

When $s = 0$, there is no overshoot, and the function is equivalent to `pow` with $n = 3$.



4 Implementation

\ifeasing@withfpu
\easing@divide

This library uses TEX registers and PGF's mathematical engine for computations.

It is possible that the user is loading this library together with the floating point unit library. We save the basic routines from `pgfmath` so that when this happens, the FPU doesn't break everything when it does a switcharoo with the `pgfmath` macros.

```
\newif\ifeasing@withfpu
\expandafter\ifx\csname pgflibraryfpuifactive\endcsname\relax
\easing@withfpufalse
\else
\easing@withfputrue
\fi
\ifeasing@withfpu
\let\easing@divide\pgfmath@basic@divide@
\let\easing@cos\pgfmath@basic@cos@
\let\easing@exp\pgfmath@basic@exp@
\let\easing@ln\pgfmath@basic@ln@
\else
\let\easing@divide\pgfmathdivide@
\let\easing@cos\pgfmathcos@
\let\easing@exp\pgfmathexp@
\let\easing@ln\pgfmathln@
\fi
```

\easing@linearstep@ne
\easing@linearstep@fixed
\easing@linearstep@float
\easing@linearstep

In absence of the FPU, the next section of code defines `\easing@linearstep`, which expects as arguments plain numbers (i.e. things that can be assigned to dimension registers). The net effect of `\easing@linearstep{#1}{#2}{#3}` is to set `\pgfmathresult` to $\frac{\#3-\#1}{\#2-\#1}$, clamped to between 0 and 1.

If the FPU is loaded, `\easing@linearstep` is instead named `\easing@linearstep@fixed`, and we additionally define `\easing@linearstep@float`, which expects FPU-format floats as arguments. We do not format the output as a float since the FPU is smart enough to do that conversion quietly on its own.

The `\easing@linearstep` routine is the first step in the definition of all other routines that compute easing functions.

```
\def\easing@linearstep@ne#1{%
  \begingroup
  \pgf@x#1pt
  \ifdim1pt<\pgf@x\pgf@x 1pt\fi
  \ifdim0pt>\pgf@x\pgf@x 0pt\fi
  \pgfmathreturn\pgf@x
  \endgroup
}%
\expandafter\def
\csname easing@linearstep\ifeasing@withfpu @fixed\fi\endcsname#1#2#3{%
  \begingroup
  \pgf@xa#3pt
  \pgf@xb#2pt
  \pgf@xc#1pt
  \ifdim\pgf@xb=\pgf@xc
  \edef\pgfmathresult{\ifdim\pgf@xa>\pgf@xb 1\else 0\fi}%
  \else
  \advance\pgf@xa-\pgf@xc
  \advance\pgf@xb-\pgf@xc
  \easing@divide{\pgfmath@tonumber\pgf@xa}{\pgfmath@tonumber\pgf@xb}%
  \easing@linearstep@ne\pgfmathresult
  \fi
  \pgfmathsmuggle\pgfmathresult
  \endgroup
}%
\ifeasing@withfpu
\def\easing@linearstep@float#1#2#3{%
  \begingroup
  \pgfmathfloatsubtract{#3}{#1}%
  \edef\pgf@tempa{\pgfmathresult}%
  \pgfmathfloatsubtract{#2}{#1}%
  \edef\pgf@tempb{\pgfmathresult}%
  \pgfmathfloatifflags{\pgf@tempb}{0}{%
    \pgfmathfloatifflags{\pgf@tempa}{-}{%
      \edef\pgfmathresult{0}%
    }{%
      \edef\pgfmathresult{1}%
    }%
  }{%
    \pgfmathfloatdivide\pgf@tempa\pgf@tempb
    \pgfmathfloattofixed{\pgfmathresult}%
    \easing@linearstep@ne\pgfmathresult
  }%
  \pgfmathsmuggle\pgfmathresult
  \endgroup
}%
\def\easing@linearstep#1#2#3{%
```

```
  \pgflibraryfpuifactive{%
    \easing@linearstep@float{#1}{#2}{#3}}{%
    \easing@linearstep@fixed{#1}{#2}{#3}}%
}%
\fi
```

`\easing@linearstep@easein@ne`
`\easing@linearstep@easeout@ne`

The linear ease-in and ease-out functions are identitcal to the linear step function. We define the respective macros so as not to surprise the user with their absence.

```
\let\easing@lineareasein\easing@linearstep
\pgfmathdeclarefunction{lineareasein}{3}{%
  \easing@lineareasein{#1}{#2}{#3}}%
\let\easing@lineareaseout\easing@linearstep
\pgfmathdeclarefunction{lineareaseout}{3}{%
  \easing@lineareasein{#1}{#2}{#3}}%
```

`\easing@derive@easein@nefromstep@ne`
`\easing@derive@easeout@nefromstep@ne`
`\easing@derive@step@nefromeasein@ne`
`\easing@derive@easeout@nefromeasein@ne`

The pattern in general is that, for each shape, we define the one-parameter version of the step, ease-in, and ease-out routines interpolating between values 0 at 1 at the ends of the unit interval. Then by composing with `\easing@linearstep`, we obtain the three-parameter versions that allow the user to specify the begin and end points of the interpolation.

Most of the time it suffices to define just one of the three one-parameter versions of a shape to be able to infer the form of all three. This is done with the `\easing@derive`–`from`– macros.

```
\def\easing@derive@easein@nefromstep@ne#1{%
  \expandafter\def\csname easing@#1easein@ne\endcsname##1{%
    \begingroup
    \pgf@x##1 pt
    \divide\pgf@x 2
    \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
    \pgf@x\pgfmathresult pt
    \multiply\pgf@x 2
    \pgfmathreturn\pgf@x
    \endgroup
  }%
}%
\def\easing@derive@easeout@nefromstep@ne#1{%
  \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
    \begingroup
    \pgf@x##1 pt
    \divide\pgf@x 2
    \advance\pgf@x 0.5pt
    \csname easing@#1step@ne\endcsname{\pgfmath@tonumber\pgf@x}%
    \pgf@x\pgfmathresult pt
    \multiply\pgf@x 2
    \advance\pgf@x -1pt
    \pgfmathreturn\pgf@x
```

```
    \endgroup
  }%
}%
\def\easing@derive@step@nefromeasein@ne#1{%
  \expandafter\def\csname easing@#1step@ne\endcsname##1{%
  \begingroup
    \pgf@x##1 pt
    \multiply\pgf@x 2
    \ifdim\pgf@x<1pt
    \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
    \pgf@x\pgfmathresult pt
    \divide\pgf@x 2
    \else
    \multiply\pgf@x -1
    \advance\pgf@x 2pt
    \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
    \pgf@x\pgfmathresult pt
    \divide\pgf@x 2
    \multiply\pgf@x -1
    \advance\pgf@x 1pt
    \fi
    \pgfmathreturn\pgf@x
    \endgroup
  }%
}%
\def\easing@derive@easeout@nefromeasein@ne#1{%
  \expandafter\def\csname easing@#1easeout@ne\endcsname##1{%
    \begingroup
    \pgf@x##1pt
    \multiply\pgf@x -1
    \advance\pgf@x 1pt
    \csname easing@#1easein@ne\endcsname{\pgfmath@tonumber\pgf@x}%
    \pgf@x\pgfmathresult pt
    \multiply\pgf@x -1
    \advance\pgf@x 1pt
    \pgfmathreturn\pgf@x
    \endgroup
  }%
}
```

`\easing@pgfmathinstall` The three-parameter versions of each routine is installed into the mathematical engine, so that they are available in `\pgfmathparse`.

```
\def\easing@pgfmathinstall#1{%
  \pgfmathdeclarefunction{#1step}{3}{%
    \easing@linearstep{##1}{##2}{##3}%
    \csname easing@#1step@ne\endcsname\pgfmathresult
  }%
  \pgfmathdeclarefunction{#1easein}{3}{%
    \easing@linearstep{##1}{##2}{##3}%
```

```
    \csname easing@#1easein@ne\endcsname\pgfmathresult
  }%
  \pgfmathdeclarefunction{#1easeout}{3}{%
    \easing@linearstep{##1}{##2}{##3}%
    \csname easing@#1easeout@ne\endcsname\pgfmathresult
  }%
}%
```

`\easing@smoothstep@ne`
`\easing@smootheasein@ne`
`\easing@smootheaseout@ne`

The `smooth` shape.

```
\def\easing@smoothstep@ne#1{%
  \begingroup
  \pgf@x#1pt
  \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
  \multiply\pgf@x-2
  \advance\pgf@x 3pt
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@easein@nefromstep@ne{smooth}%
\easing@derive@easeout@nefromstep@ne{smooth}%
\easing@pgfmathinstall{smooth}%
```

`\easing@sinestep@ne`
`\easing@sineeasein@ne`
`\easing@sineeaseout@ne`

The `sine` shape.

We write down both the `easein` and `step` forms of this, since they are simple compared to what would have been obtained by `\easing@derive`–.

```
\def\easing@sineeasein@ne#1{%
  \begingroup
  \pgf@x#1pt
  \multiply\pgf@x 90
  \easing@cos{\pgfmath@tonumber\pgf@x}%
  \pgf@x\pgfmathresult pt
  \multiply\pgf@x -1
  \advance\pgf@x 1pt
  \pgfmathreturn\pgf@x
  \endgroup
}%
\def\easing@sinestep@ne#1{%
  \begingroup
  \pgf@x#1pt
  \multiply\pgf@x 180
  \easing@cos{\pgfmath@tonumber\pgf@x}%
  \pgf@x\pgfmathresult pt
  \divide\pgf@x 2
  \multiply\pgf@x -1
  \advance\pgf@x 0.5pt
```

```
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@easeout@nefromeasein@ne{sine}%
\easing@pgfmathinstall{sine}%
```

\easing@powstep@ne
\easing@poweasein@ne
\easing@poweaseout@ne

The pow shape.

Because of some wonkiness in the FPU, instead of invoking the pow function from pgfmath, we compute t^n approximately by computing $e^{n \ln t}$ using ln and exp instead (which is what pgfmath does anyway when the exponent is not an integer.)

```
\pgfkeys{/easing/.is family}%
\pgfkeys{easing,
  pow/exponent/.estore in=\easing@param@pow@exponent,
  pow/exponent/.default=2.4,
  pow/exponent}%
\def\easing@poweasein@ne#1{%
  \begingroup
  \pgf@x#1pt
  \ifdim\pgf@x=0pt
  \edef\pgfmathresult{0}%
  \else
  \easing@ln{#1}%
  \pgf@x\pgfmathresult pt
  \pgf@x\easing@param@pow@exponent\pgf@x
  \easing@exp{\pgfmath@tonumber\pgf@x}%
  \fi
  \pgfmathsmuggle\pgfmathresult
  \endgroup
}%
\easing@derive@easeout@nefromeasein@ne{pow}%
\easing@derive@step@nefromeasein@ne{pow}%
\easing@pgfmathinstall{pow}%
```

\easing@quadstep@ne
\easing@quadeasein@ne
\easing@quadeaseout@ne
\easing@cubicstep@ne
\easing@cubiceasein@ne
\easing@cubiceaseout@ne
\easing@quartstep@ne
\easing@quarteasein@ne
\easing@quarteaseout@ne
\easing@quintstep@ne
\easing@quinteasein@ne
\easing@quinteaseout@ne

The quad–, cubic–, quart–, and quint– routines have explicit definitions.

```
\def\easing@quadeasein@ne#1{%
  \begingroup
  \pgf@x#1pt
  \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
  \pgf@x\pgf@temp\pgf@x
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@step@nefromeasein@ne{quad}%
\easing@derive@easeout@nefromeasein@ne{quad}%
\easing@pgfmathinstall{quad}%

```

```
\def\easing@cubiceasein@ne#1{%
  \begingroup
  \pgf@x#1pt
  \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@step@nefromeasein@ne{cubic}%
\easing@derive@easeout@nefromeasein@ne{cubic}%
\easing@pgfmathinstall{cubic}%

\def\easing@quarteasein@ne#1{%
  \begingroup
  \pgf@x#1pt
  \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@step@nefromeasein@ne{quart}%
\easing@derive@easeout@nefromeasein@ne{quart}%
\easing@pgfmathinstall{quart}%

\def\easing@quinteasein@ne#1{%
  \begingroup
  \pgf@x#1pt
  \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@step@nefromeasein@ne{quint}%
\easing@derive@easeout@nefromeasein@ne{quint}%
\easing@pgfmathinstall{quint}%
```

`\easing@backstep@ne`
`\easing@backeasein@ne`
`\easing@backeaseout@ne`

The `back` shape.

```
\pgfkeys{easing,
  back/overshoot/.estore in=\easing@param@back@overshoot,
  back/overshoot/.default=1.6,
  back/overshoot}%
\def\easing@backeasein@ne#1{%
  \begingroup
```

```
  \pgf@x#1pt
  \edef\pgf@temp{\pgfmath@tonumber\pgf@x}%
  \advance\pgf@x -1pt
  \pgf@x\easing@param@back@overshoot\pgf@x
  \advance\pgf@x\pgf@temp pt
  \pgf@x\pgf@temp\pgf@x
  \pgf@x\pgf@temp\pgf@x
  \pgfmathreturn\pgf@x
  \endgroup
}%
\easing@derive@step@nefromeasein@ne{back}%
\easing@derive@easeout@nefromeasein@ne{back}%
\easing@pgfmathinstall{back}%
```