

Opportunism and ordering strategies in derivative-free optimization

Loïc Anthony Sarrazin-Mc Cann
Charles Audet, Sébastien Le Digabel and Christophe Tribes

Department of Mathematics and Industrial Engineering
École Polytechnique de Montréal

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Presentation Outline

- 1 What are Derivative-Free and Blackbox Optimization?
- 2 Direct-search Methods
- 3 Opportunism and ordering
- 4 Numerical results
- 5 Conclusion

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Derivative-Free and Blackbox Optimization

Optimization problem :

$$\left\{ \begin{array}{ll} \min_{x \in \mathbb{R}^n} & f(x) \\ \text{s.t.} & c_j(x) \leq 0 \quad \forall j \in \{1, \dots, m\} \\ & l_i \leq x_i \leq u_i \quad \forall i \in \{1, \dots, n\} \end{array} \right.$$

Derivative-Free and Blackbox Optimization

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- $f(x)$ and $c_j(x)$ are treated as blackboxes.

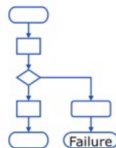
Blackbox



Long runtime



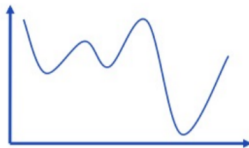
Large memory
requirement



Software
might fail



No derivatives
available



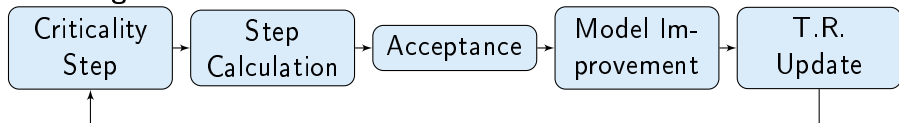
Local
optima



Non-smooth,
noisy

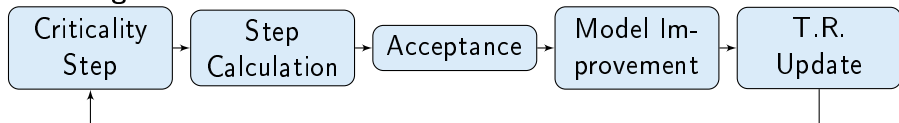
DFO and BBO methods

Trust Region Methods

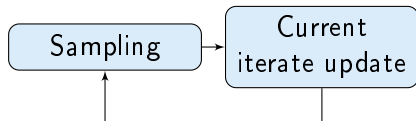


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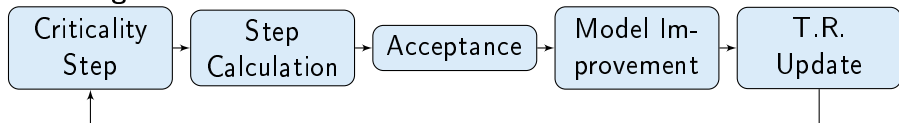


Direct-search Methods

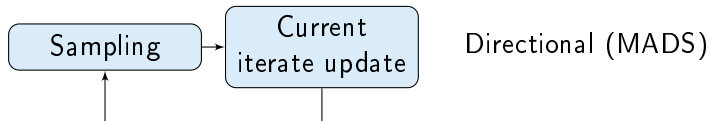


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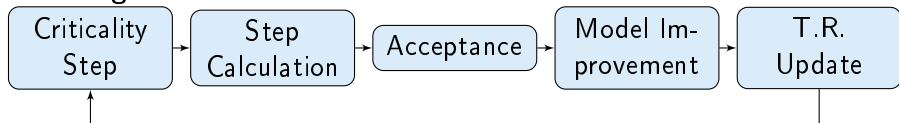


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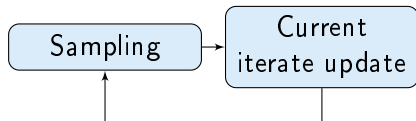


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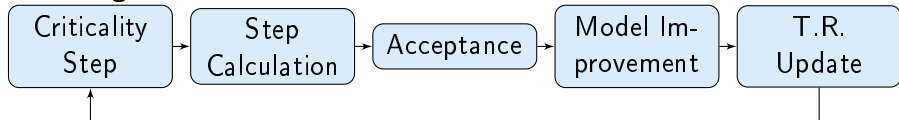
Direct-search Methods



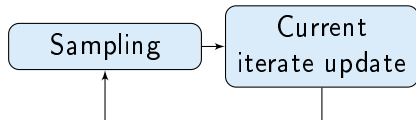
Directional (MADS)
Simplicial (Nelder-Mead)

DFO and BBO methods

Trust Region Methods



Direct-search Methods



Directional (MADS)
Simplicial (Nelder-Mead)

Other methods

DFO and BBO methods

Trust Region Methods



Direct-search Methods

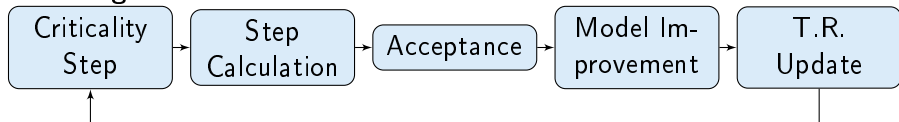


Other methods

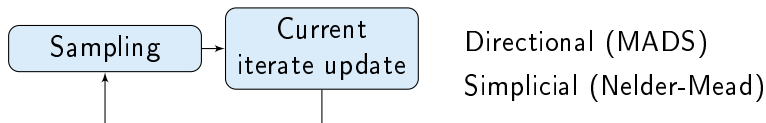
Heuristics (Particle Swarm, Simulated Annealing)

DFO and BBO methods

Trust Region Methods



Direct-search Methods



Other methods

Heuristics (Particle Swarm, Simulated Annealing)

Hybrids (Implicit Filtering)

What Are We Trying to Achieve?

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The opportunistic strategy designates the premature termination of an algorithmic step as soon as the necessary conditions to proceed to the next step are met.

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Opportunistic Strategy

The opportunistic strategy designates the premature termination of an algorithmic step as soon as the necessary conditions to proceed to the next step are met.

Often mentionned but never studied per se.

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Question 1.

For which methods is the opportunistic strategy applicable?

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- Same as direct-search methods, but might impact performance.

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Heuristics ?

- Highly dependent on the heuristic.

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- Samples $f(x)$ and $c(x)$ on \mathcal{L}^k , a list of point specific to the k^{th} iteration.

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Algorithm 1 Direcitonal direct-search framework

for $k = 1, 2, \dots$ **do**

Search : Evaluate $f(x)$ at a finite set of point S^k .

If successful, update x^k

Poll : Evaluate $f(x)$ at a finite set of point

$P^k := \{x^k + \delta^k d : d \in D\}$, where D is a positive spanning set of **directions**.

If successful, update x^k and mesh parameters.

end for

Remark : this work only encompasses the study of the impact of the opportunistic strategy on poll steps.

Coordinate Search (CS)

Algorithm 2 Coordinate Search

for $k = 1, 2, \dots$ **do**

Poll : Evaluate $f(x)$ at

$P^k := \{x^k + \delta^k d : d \in D_{\oplus}\}$, where

$D_{\oplus} := \{\pm e_1, \pm e_2, \dots, \pm e_n\}$.

If $\exists t$ for which $f(t) < f(x^k)$, $t \in P^k$

Successful step

update $x^{k+1} \leftarrow t$ et $\delta^{k+1} \leftarrow \delta^k$.

Else $\nexists t$ for which $f(t) < f(x^k)$, $t \in P^k$

Unsuccessful step

update $x^{k+1} \leftarrow x^k$ et $\delta^{k+1} \leftarrow \frac{\delta^k}{2}$.

end for

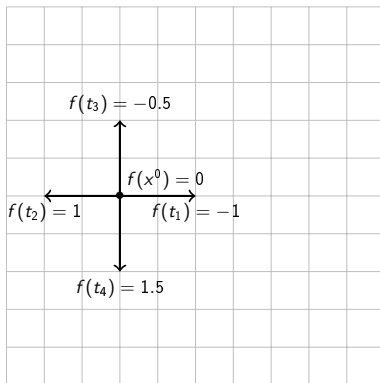


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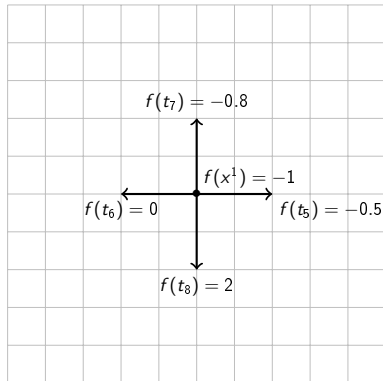


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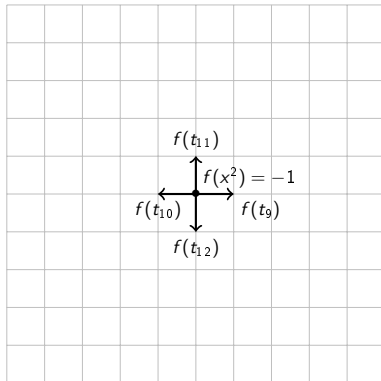


Figure: CS

Generalized Pattern Search (GPS)

Algorithm 3 Generalized Pattern Search

for $k = 1, 2, \dots$ **do**

with $\tau \in \{0, 1\}$.

Poll : Evaluate $f(x)$ at

$P^k := \{x^k + \delta^k d : d \in D\}$, where

D is a positive spanning set.

If $\exists t$ for which $f(t) < f(x^k)$, $t \in P^k$

Successful step

update $x^{k+1} \leftarrow t$ et $\delta^{k+1} \leftarrow \tau^{-1} \delta^k$.

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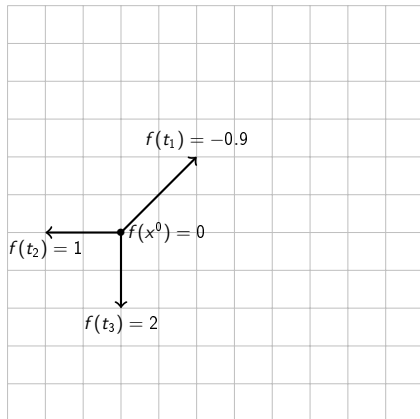


Figure: GPS

Generalized Pattern Search (GPS)

Algorithm 4 Generalized Pattern Search

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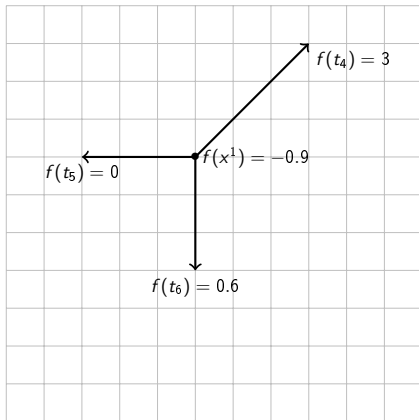


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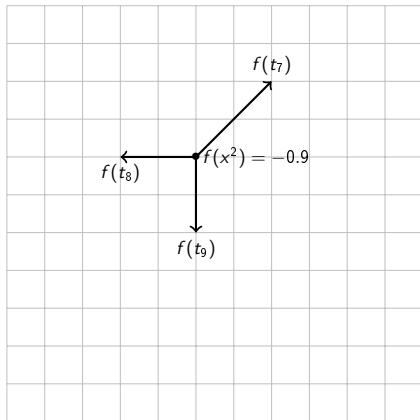


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Generating Set Search (GSS)

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Poll : Evaluate $f(x)$ at
 $P^k := \{x^k + \delta^k d : d \in D\}$, where
 D is a positive spanning set
 respecting multiple conditions.
 If $\exists t$ for which $f(t) < f(x^k)$, $t \in P^k$
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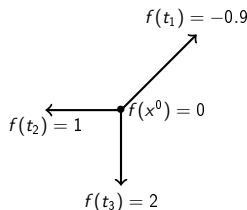


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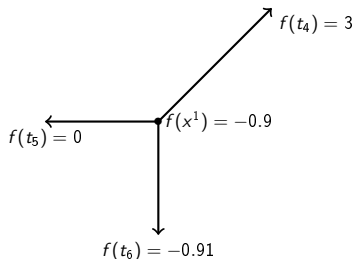


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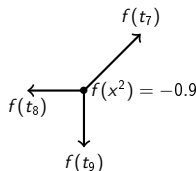


Figure: GSS

Mesh Adaptive Direct Search (MADS)

Algorithm 5 Mesh Adaptive Direct Search

```

for  $k = 1, 2, \dots$  do
  with  $\tau \in \{0, 1\}$ .
  Update :  $\delta^k \leftarrow \min(\Delta^k, (\Delta^k)^2)$ 
  Poll : Evaluate  $f(x)$  at
     $P^k := \{x^k + \delta^k d : d \in D\}$ , where
     $D \subset F^k$ , with  $F^k$  frame of size  $\Delta^k$ .

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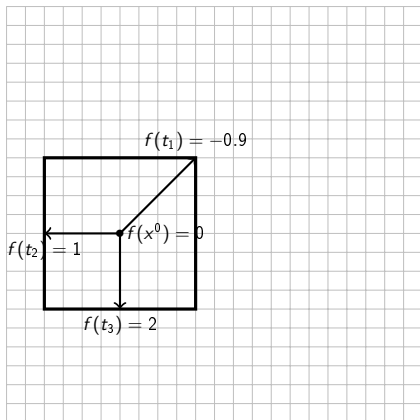


Figure: MADS

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If $\exists t$ for which $f(t) < f(x^k)$, $t \in P^k$

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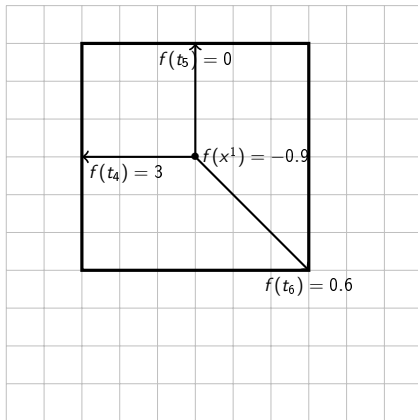


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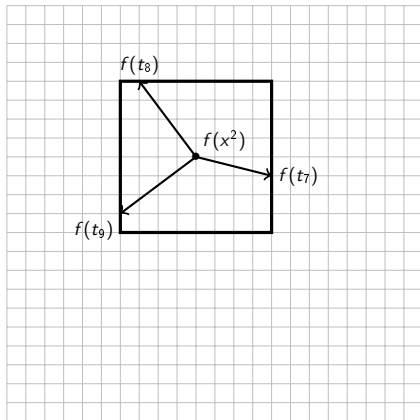


Figure: MADS

Implicit Filtering (IMFIL)

Algorithm 6 Implicit Filtering

for $k = 1, 2, \dots$ **do**

Poll : Evaluate $f(x)$ at

$P^k := \{x^k + \delta^k d : d \in D_\oplus\}$, where

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If $\exists t$ for which $f(t) < f(x^k)$, $t \in P^k$

Successful step

Line search following $-\nabla_s f(x^k)$.

update $x^{k+1} \leftarrow t$ et $\delta^{k+1} \leftarrow \delta^k$.

Else $\nexists t$ for which $f(t) < f(x^k)$, $t \in P^k$

Unsuccessful step

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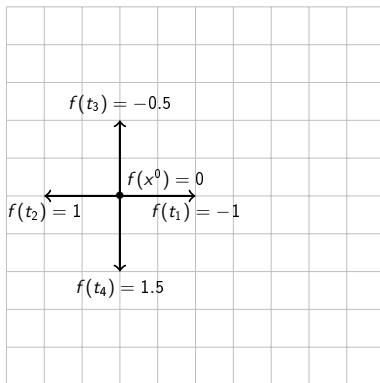


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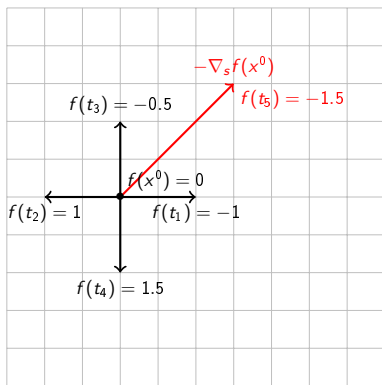


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Line search following $-\nabla_s f(x^k)$.

update $x^{k+1} \leftarrow t$ et $\delta^{k+1} \leftarrow \delta^k$.

Else $\nexists t$ for which $f(t) < f(x^k)$, $t \in P^k$

Unsuccessful step

update $x^{k+1} \leftarrow x^k$ et $\delta^{k+1} \leftarrow \frac{\delta^k}{2}$.

end for

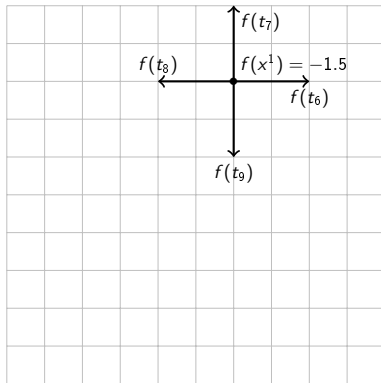


Figure: IMFIL

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Opportunistic strategies

Complete polling

Designates the evaluation of $f(x)$ and $c(x)$ at every point generated in the poll step.

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Rule guiding the ordering of points in a set \mathcal{L} .

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where $\tilde{f}(x)$ is a dynamic quadratic surrogate of $f(x)$.

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No practical use, for comparison only.

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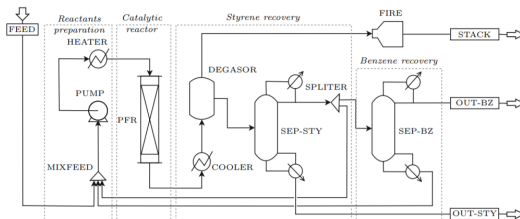


Figure: Styrene production chart [Audet, Béchard, Le Digabel 2008]

Opportunistic strategies comparison

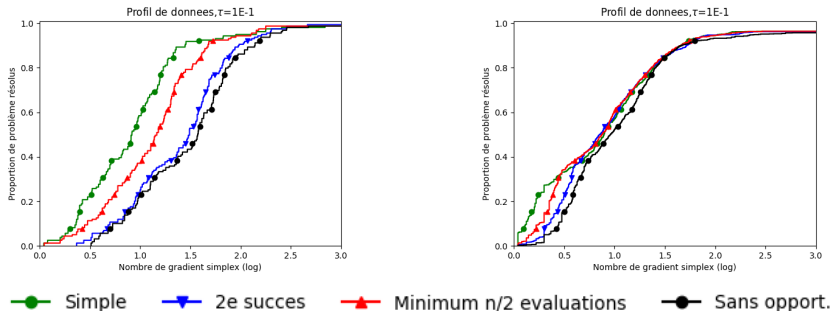


Figure: Left : CS on Moré-Wild, Right MADS on Moré-Wild

Opportunistic strategies comparison

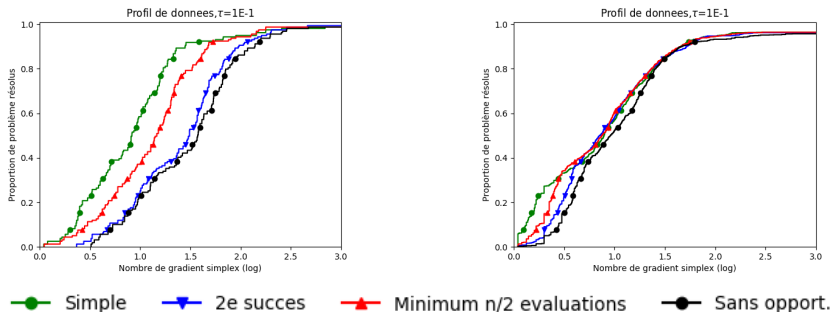


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① Model ordering used.

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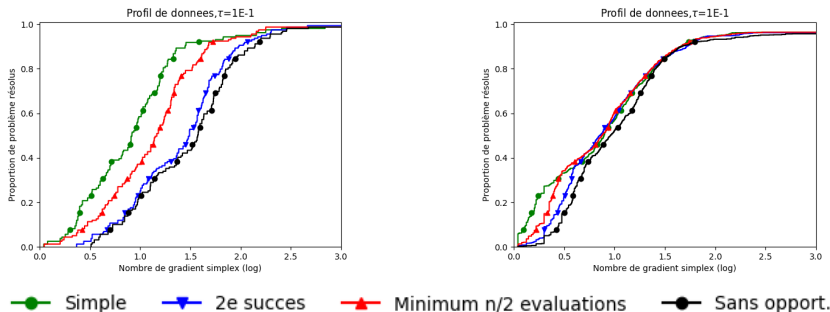


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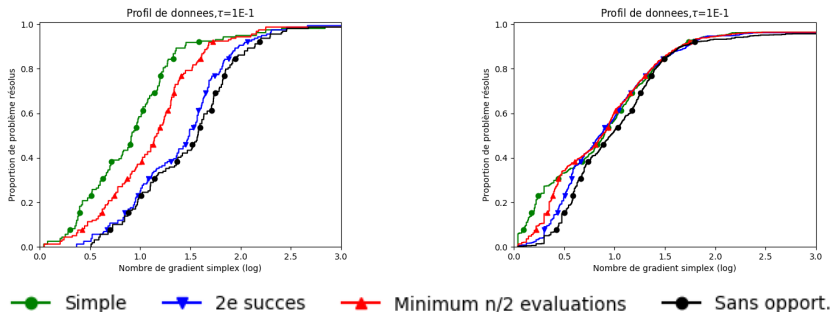


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- ① Model ordering used.
- ② Most efficient opportunistic strategy : simple
- ③ Impact less important on MADS.

Ordering strategies comparison

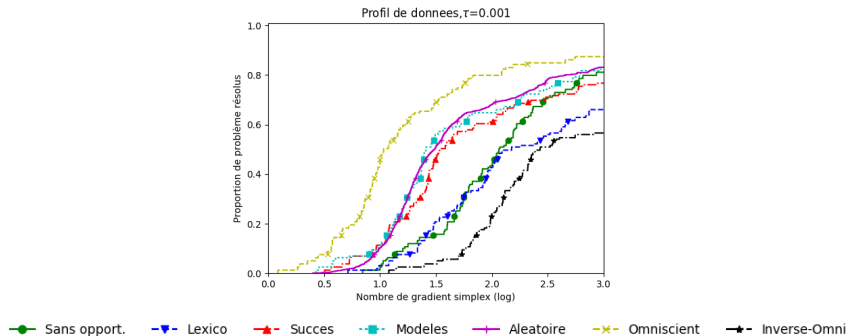
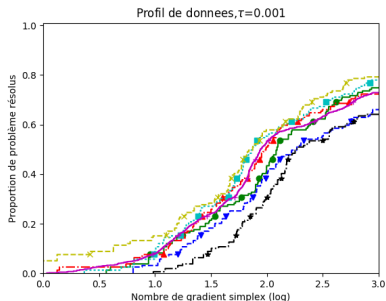


Figure: CS on Moré-Wild

Ordering strategies comparison



—●— Sans opport.
 -▼- Lexico
 -▲- Succes
 -■- Modeles
 -+- Aleatoire
 -x- Omniscient
 -*- Inverse-Omni

Figure: GPS on Moré-Wild

Ordering strategies comparison

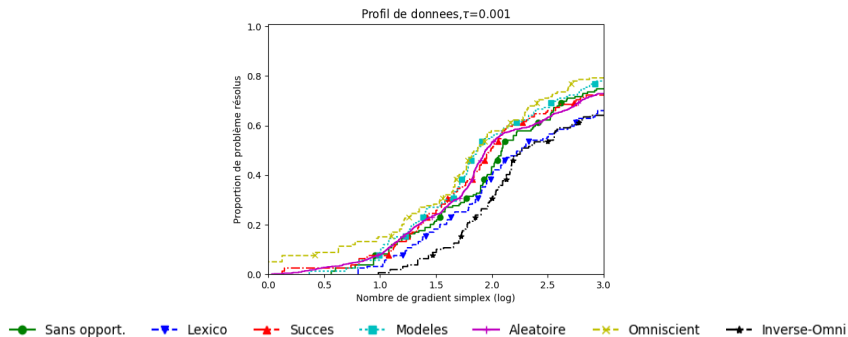


Figure: GPS on Moré-Wild

- 1 Omniscient strategy less dominant.

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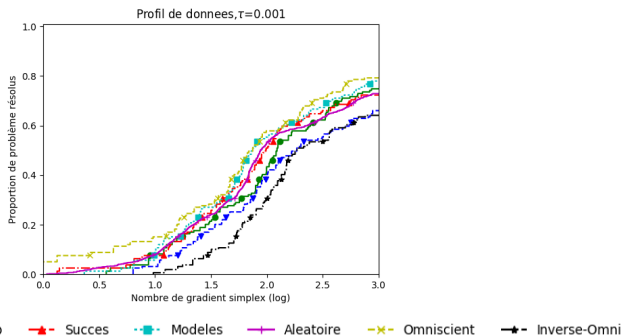


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- 2 Somewhat similar hierarchy.

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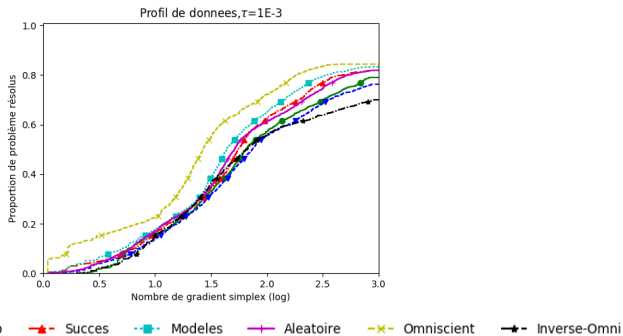


Figure: MADS on Moré-Wild

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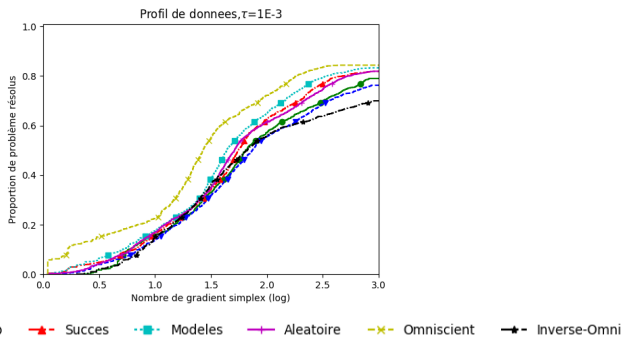


Figure: MADS on Moré-Wild

1 Impact less visible on MADS.

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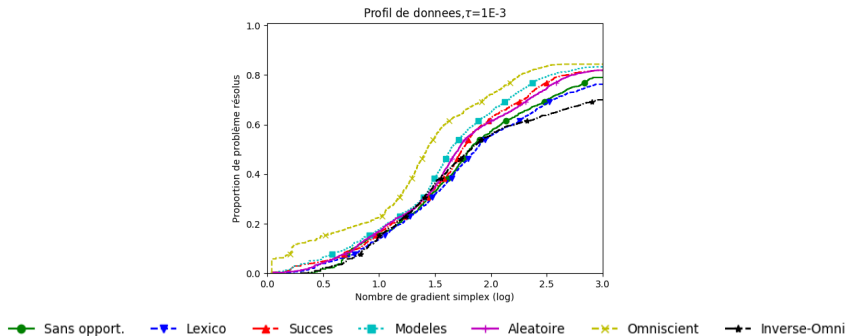


Figure: MADS on Moré-Wild

- ① Impact less visible on MADS.
- ② Different ranking of strategies on CS and MADS.

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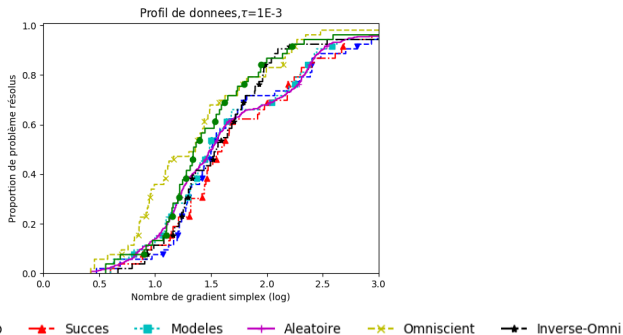


Figure: IMFIL on Moré-Wild

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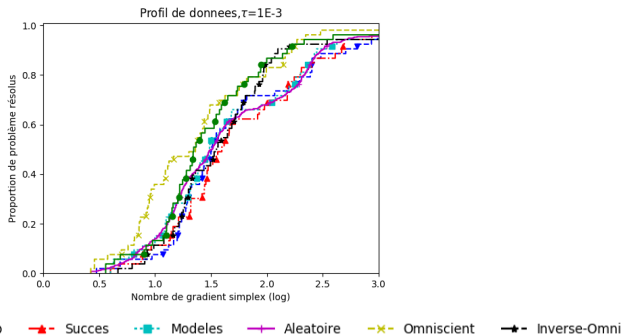


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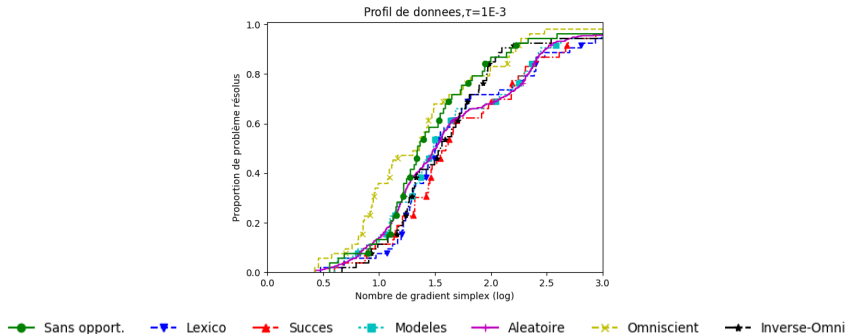


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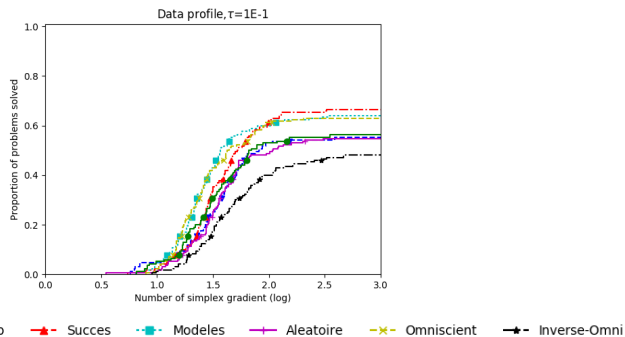


Figure: Constrained problems with MADS

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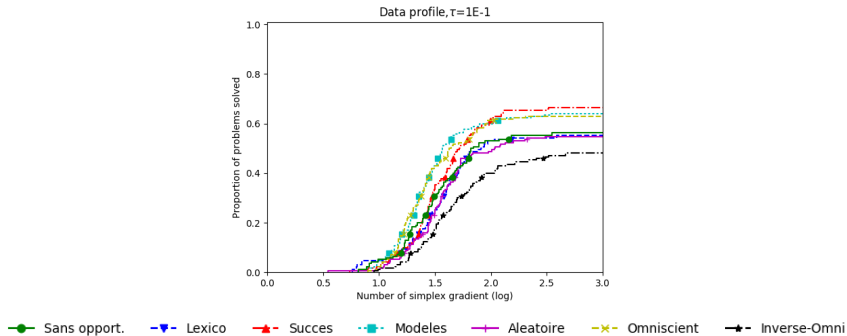


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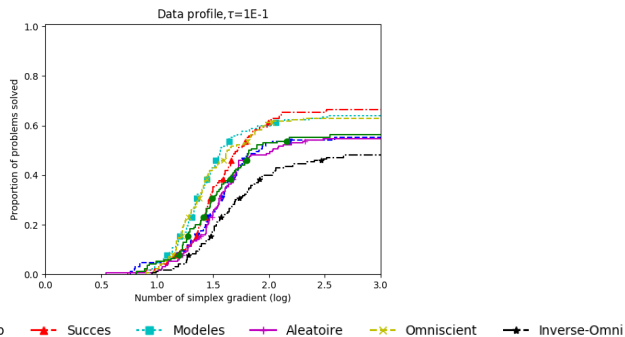


Figure: Constrained problems with MADS

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- 2 Surrogate ordering with progressive barrier might not be optimal.

Ordering strategies comparison

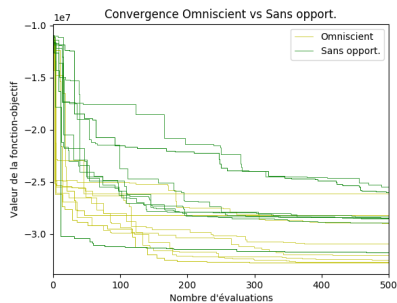
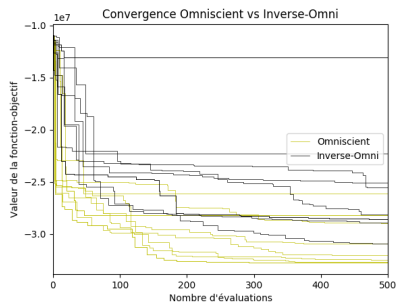


Figure: Comparing omniscient, reverse-omniscient and complete polling

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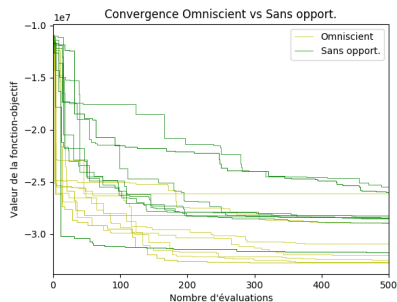
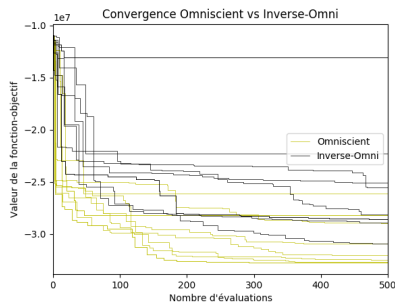


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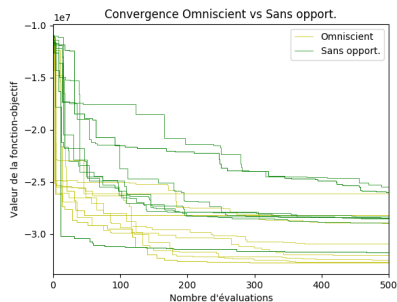
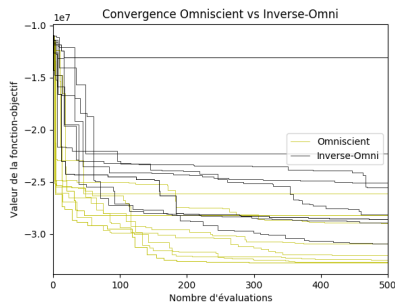


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Ordering strategies comparison

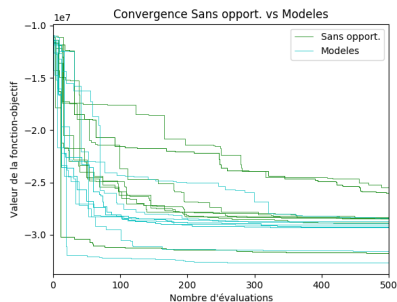
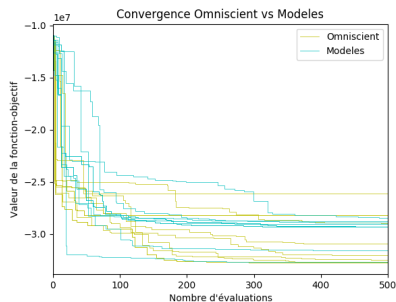


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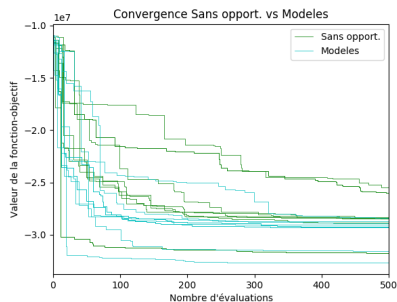
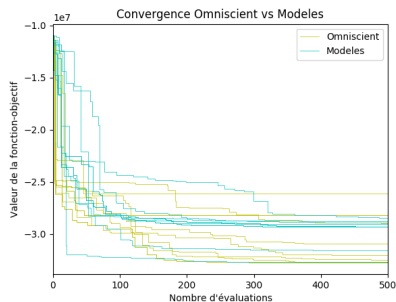


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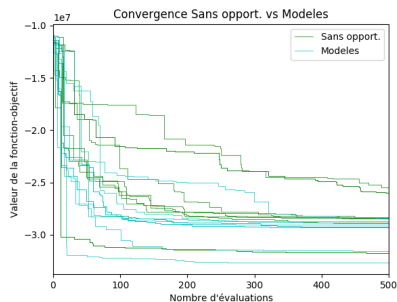
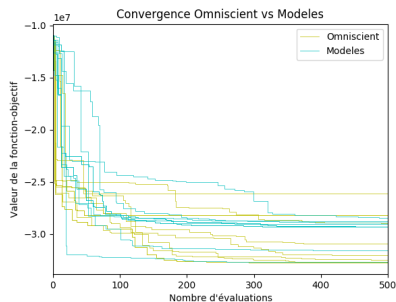


Figure: Comparing omniscient, model ordering and complete polling

- 1 Model ordering converges faster than complete polling.
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References



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QUESTIONS?