

Semester	AUG 2023
Open to semester	3
Course code	PH2123
Course title	Mathematical Methods for Physics (Elective)
Credits	3 /
Course Coordinator & participating faculty (if any)	Bijay Kumar Agarwalla *, Sachin Jain
Nature of Course	Lectures and Tutorials
Pre-requisites	Basic knowledge of mathematics and physics
Objectives (goals, type of students for whom useful, outcome etc)	To provide the key mathematical tools needed for a physics student. This is a key course for students wanting to study physics. Students from other disciplines will also find it useful if they plan to study any quantitative science.
Course contents (details of topics /sections with no. of lectures for each)	<p>Infinite series, power series: 4 lectures Convergent and divergent series, convergence tests, alternating series and conditional convergence, Taylor expansion, radius of convergence, expanding functions in power series, error in series expansions.</p> <p>Complex Algebra: 2 lectures Complex numbers and functions, Algebraic properties of complex numbers, polar representation, power and roots of complex numbers, derivatives,</p> <p>Linear Algebra: 6 Lectures Linear simultaneous equations, row operations, rank, determinants, minors and cofactors, inverse, Cramer's rule. Functions of matrices, Baker-Campbell-Hausdorff relation. Special types of matrices: linear conditions (symmetric, anti-symmetric, Hermitian) and quadratic conditions (orthogonal, unitary). Basis for matrices satisfying linear conditions. Lie algebra and Lie group for $U(2)$ and $SU(2)$. Eigenvalues and eigenvectors, diagonalization of matrices, change of basis. Degenerate eigenvalues and Gram-Schmidt Orthogonalization, Cayley-Hamilton theorem.</p> <p>Fourier Series and transformation: 4 lectures Periodic functions, Orthogonality of trigonometric functions,</p>

	<p>Expansion of functions in Fourier series, complex form of Fourier series, Parseval's identity, Fourier integral, Inverse transformation.</p> <p>Probability and statistics: 3 lectures Sample space, probability axioms, conditional probability and Bayes theorem, Probability distribution of a random variable, discrete and continuous random variables, moments and generating functions, multiple random variables, some special distributions, large sample theory, Central limit theorem.</p> <p>Differential Equations: 5 lectures Linear differential operators, 1st order ODE, 2nd order ODE, Number of independent sol, Wronskian, homogeneous and inhomogeneous ODE, power series solution, Fourier transform to solve differential equation.</p>
Evaluation /assessment	<p>End-Sem Examination-35%</p> <p>Mid-Sem Examination-35%</p> <p>Others-30%</p>
Suggested readings (with full list of authors, publisher, year, edn etc.)	<ol style="list-style-type: none"> 1. Mathematical Methods for Physicists: G. Arfken and H. Weber (2012) 7th edition, Academic Press 2. Mathematical Physics, Mary L. Boas, 2nd edition, John Wiley & Sons (1983). 3. Mathematics for Physicists – Denner and Krzywicki, Dover. 4. Mathematical Methods for physics and engineering-- Riley, Hobson, and Bence