



### II) Forward Pass:

- All the outputs from the 1st hidden layer will be the same:

$$0 \cdot 0 + (-0.528926) \cdot 0 + 0 \cdot 0 + (-1.0) \cdot 0 + (-0.005701) \cdot 0 + 0.357576 \cdot 0 + 0.461644 \cdot 0 + (-0.143626) \cdot 0 + (-1.0) \cdot 0 + (-1.0) \cdot 0 + (-0.111111) \cdot 0 = 0$$

Activation Sigmoid:  $\frac{1}{1+e^{-x}} \Rightarrow \frac{1}{1+e^0} = \frac{1}{2}$

- All the inputs to the 2nd hidden layer will be the same:

$$1 \cdot 1 + \frac{1}{2} \cdot 1 + \frac{1}{2} \cdot 1 + \frac{1}{2} \cdot 1 + \frac{1}{2} \cdot 1 + \frac{1}{2} \cdot 1 = 1 + 5 \cdot \frac{1}{2} = \frac{7}{2}$$

$$\frac{1}{1+e^{-\frac{7}{2}}} = 0.970687769 \text{ (the output of each neuron in the 2nd hidden layer)}$$

- Output:

$$1 \cdot 1 + 5 \cdot (1 \cdot 0.970687769) = 5.853438846$$

$$y_{\text{predicted}} = \frac{1}{1+e^{-5.853438846}} = \underline{\underline{0.997138201}}$$

$$MSE = \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2 \Rightarrow MSE = (0 - 0.997138201)^2 = \underline{\underline{0.994284591}}$$

## II) Backpropagation:

$$\eta = 0,01$$

- Output layer weights should be the same:

$$\delta_j = \text{Output}_j (1 - \text{Output}_j) (\text{actual}_j - \text{output}_j)$$

$$\begin{aligned} \delta_{\text{out}} &= y_{\text{predicted}} (1 - y_{\text{pred}}) (y_{\text{actual}} - y_{\text{pred}}) = \\ &= 0,997138201 (1 - 0,997138201) (-0,997138201) = -0,002845443 \end{aligned}$$

$$W_{\text{bias out, new}} = W_{\text{bias out, curr}} + \eta \delta_{\text{out}} \text{bias} = 1 + 0,01 \cdot (-0,002845443) \cdot 1 = 0,999971546$$

$$W_{2nd, new} = W_{2nd, curr} + \eta \cdot \delta_2 \cdot N2 = 1 + 0,01 \cdot (-0,002845443) \cdot 0,970687769 = 0,99997238$$

$$\begin{aligned} \delta_{\text{hidden}} &= \text{Output}_j (1 - \text{output}_j) \sum W_{jk} \delta_j \\ \delta_{2nd, hidden} &= 0,970687769 (1 - 0,970687769) \cdot 1 \cdot (-0,002845443) = \\ &= -0,000080961 \end{aligned}$$

$$W_{\text{bias, new}} = W_{\text{bias, curr}} + \eta \cdot \delta_{2nd, hidden} \cdot \text{bias} = 1 + 0,01 \cdot (-0,000080961) \cdot 1 = 0,99999919$$

$$\begin{aligned} W_{1st, new} &= W_{1st, curr} + \eta \cdot \delta_{2nd, hidden} \cdot N1 = 1 + 0,01 \cdot (-0,000080961) \cdot \frac{1}{2} = \\ &= 0,999999595 \end{aligned}$$