



# Regular Expression Refinement Types

## Progress Report

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WARWICK



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# 1. Introduction

Information security vulnerabilities often arise due to improper input handling. From SQL injection to cross-site scripting, vulnerabilities of this class are found on a daily basis in production applications by security professionals. It is desirable to try to detect and report on potentially insecure code as early as possible in the development process in order to maximise the probability that the issue is mitigated (Sadowski et al., 2018).

Tooling exists to perform static analysis and taint tracking, but is often unable to evaluate the effectiveness of input validation code that may already be in place. As a result, these tools lend themselves to generating false positives. In Appendix A we proposed a system which makes use of *refinement types* in order to determine whether existing regular expression based input validation is effective by trying to find situations where input could fail to be matched by a regular expression.

Within type systems, refinement types allow for predicate-based constraints to be applied to types in order to restrict the domain of elements which belong to the type.

For example, a local variable used to store natural numbers could be constrained via  $\{n : \mathbb{N} \mid n \leq 5\}$ . Only  $\{0, 1, 2, 3, 4, 5\}$  would be permitted for values of  $n$  under this refinement type.

This project applies refinement types to strings which enforce membership of  $L(R)$  for some regular expression  $R$ . For example,  $\{s : \Sigma^* \mid s \in L(ab+)\}^1$  would allow "ab" to be assigned as a value of some variable  $s$ , but not "a".

Designing a proof-of-concept language with syntax for expressing such refinement types and implementing a type checker allows for the feasibility of such compile-time checks to be evaluated.

Per the specification included in Appendix A, Weeks 1-9 of the project were scheduled to involve implementing and testing a prototype parser and type checker for the language.

## 2. Project State

Early on in the project lifetime we decided to begin prototyping work with a simplified goal, in order to gain experience working with refinement types and type checkers in general. Once complete, work would continue in a 2nd phase which introduced regular expressions.

The project is currently ahead of schedule. By week 7, both phases 1 and 2 have been completed to a satisfactory standard.

### Phase 1

Prototype work began with simple refinement types which could be applied to natural numbers. The final syntax was similar to the example presented in the specification:

```
function Main(id: uint): uint[< 4] {
    // A simple function declaration, returns an int less than 4
    return 0
}
function StackOne(): uint[> 5] {
    // This function must return an unsigned int greater than 5
    return Main(1)
}
```

As the `Main()` function returns an integer less than 4, a violation is present within `StackOne()` where it is returned. This violation arises because `StackOne`'s return type is constrained to be greater than 5.

Running this simple program with the prototype tool yields the following output:

<sup>1</sup>For some regular expression  $R$ ,  $L(R)$  is used to denote the language that it accepts  
Adam Williams

```

→ PocLang (git:master) cat input.txt | ./gradlew run
> Task :run
Reading program from stdin (use Ctrl+D when finished)...
Violation via value 0
L7:4 Return type uint [( < x 4)] of function Main didn't satisfy uint [( > x 5)]

```

The prototype tool has found a valid value (here, 0) which satisfies  $x < 4$  but violates  $x > 5$ . If integrated into a “real” programming language, this would be identified at compile time and prevent successful compilation.

This initial version of the prototype which operated exclusively on the natural numbers was built using the following tools, libraries and languages:

**JavaSMT** Library which provides an abstraction layer over a variety of different SMT solvers (such as Z3 and MathSAT) and provides added type safety (Karpenkov et al., 2016).

**ANTLR 4** An  $LL(*)$  lexer and parser generator which can target languages such as Java, Go and C# (Parr and Fisher, 2011). In the initial prototype, ANTLR was used to generate a combined lexer-parser using a composite grammar in which both non-terminals and terminal symbols (tokens) are specified.

**JUnit** A unit testing framework for Java. Used to build a collection of unit and integration tests to support refactoring and a test-driven development approach.

**Gradle** Industry-standard build automation system which co-ordinates the grammar generation, Java class compilation, construction of a JAR file with shaded dependencies and running the unit tests.

**IntelliJ IDEA** An advanced Java IDE with leading code inspection and analysis capabilities (Wedyan et al., 2009) (Jemerov, 2008). Used in conjunction with the official ANTLR plugin which provides grammar syntax highlighting and analysis.

The general steps involved in the process are described below.

## Parsing


 Parsing

Initial walk

Type checking

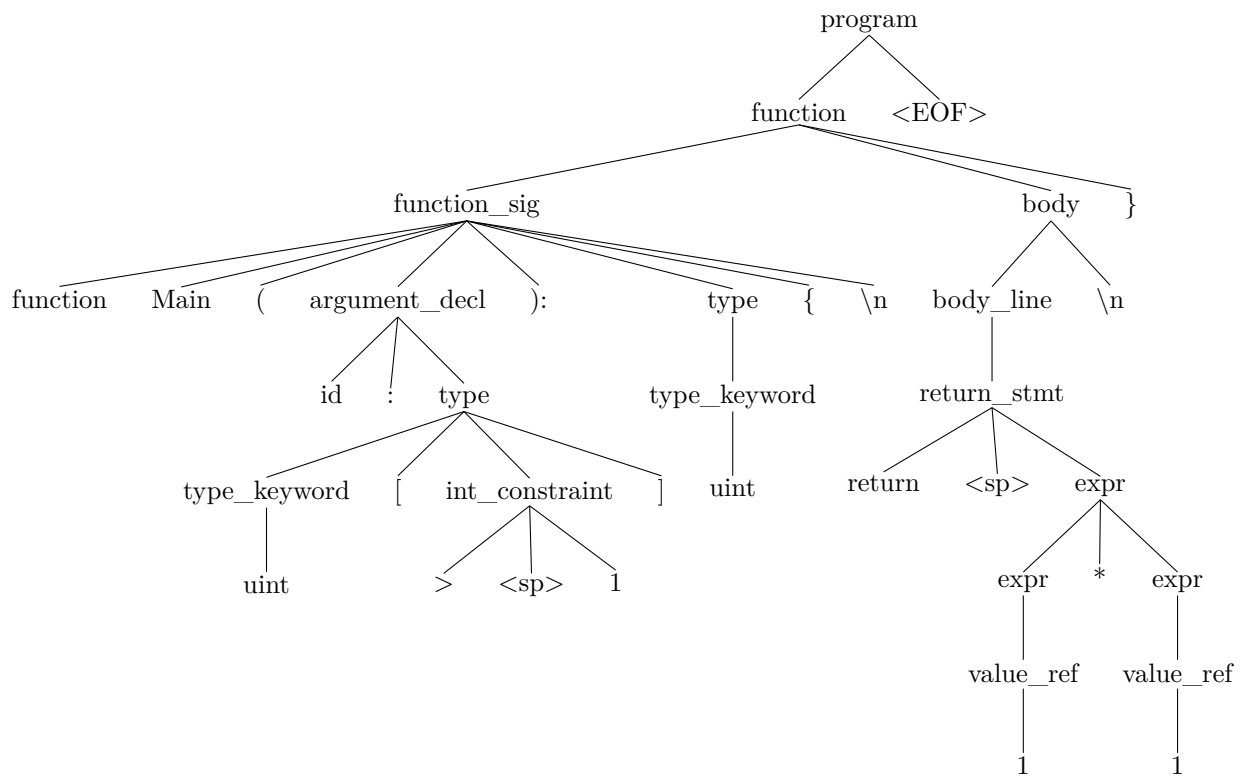
Reporting

In the **Parsing** step, the ANTLR parser is used to generate a parse tree from the input program. For example, consider the following simple function declaration below. The parse tree generated for this function definition is shown in figure 1.

```

function Main(id: uint[> 1]): uint { // accepts one argument id, which must be greater than 1
    return 1*1
}

```

Figure 1: Parse tree for the **Main** function.

For the phase 1 prototype, the lexer and parser are both generated from the same grammar file. Any *syntactical* errors are found during this step, these must be fixed before the type checking will be carried out.

## Initial Walk

⚙️ Parsing

🔍 Initial walk

✅ Type checking

📄 Reporting

The language designed for this prototype allows for functions to be called from within functions that may occur anywhere within the program code. As a result, it is necessary to perform one initial pass through the parse tree in order to collect function names to store in the function table. This table stores the identifier (**Main** in the example used previously) and the return type.

ANTLR provides a **BaseListener** class which can be extended in order to create a listener which is called for each non-terminal encountered when walking the parse tree.

The proof-of-concept language implementation uses one listener which is parametrised with a **VisitorPhase** value to specify the stage at which the listener should operate. This is set to **COLLECTING\_FUNCTIONS** for the **Initial walk** stage.

It is within this stage that function re-declarations can be discovered and reported. Errors are stored centrally and associated with the input token closest to the origin of the problem.

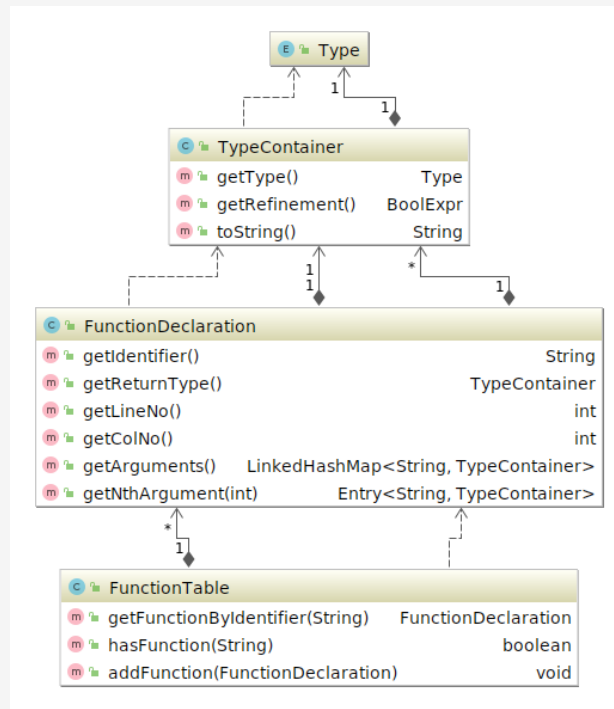


Figure 2: Dependency diagram showing how the functions declarations are stored and the data stored alongside them.

## Type Checking

⚙️ Parsing

🔍 Initial walk

🟢 Type checking

📄 Reporting

Once the function definitions have been collected, the main type checking phase can begin. This covers validating function calls, variable assignments and return statements.

This is mainly achieved by visiting function bodies and initialising a stack for scoped storage of local variables and function arguments as is standard in most programming languages (Watt, 2004, p. 88). Function calls are checked to ensure that the function identifier has been encountered before and exists in the function table. Variable assignments are checked to ensure that the type of the right-hand side expression satisfies the type declaration for the variable.

For types with a provided constraint, the JavaSMT library is used to check the inverted *expected* type against the *actual* type.

For example, consider the code below:

```

function Main(): uint[> 4] {
    var u: uint[< 10]
    return u
}
  
```

In this case, the return value of **Main** is constrained as  $\{x : \mathbb{N} \mid x > 4\}$ . When the **return u** statement is checked, the *expected* type is  $\{x : \mathbb{N} \mid x > 4\}$  and the *actual* type is  $\{x : \mathbb{N} \mid x < 10\}$ . It should be apparent that *u* could be a value such as 2 (since  $2 < 10$ ) which would violate the return type constraint.

To find this, the *expected* type is negated to give  $\{x : \mathbb{N} \mid x \leq 4\}$  and this constraint, along with the constraint defined by the *actual* type are passed to the SMT solver to find a model. This model will include a value for *x* that satisfies the conjunction of the two constraints  $x \leq 4 \wedge x < 10$ . The code below shows how the JavaSMT API allows these problems to be configured and solved:

```
IntegerFormulaManager imgr = context.getFormulaManager().getIntegerFormulaManager();
```

```
IntegerFormula x = imgr.makeVariable("x");

BooleanFormula expectedNegated = imgr.lessOrEquals(x, x.makeNumber(4)); // x <= 4
BooleanFormula actual = imgr.lessThan(x, x.makeNumber(10)); // x < 10

try (ProverEnvironment prover = context.newProverEnvironment(ProverOptions.GENERATE_MODELS)) {
    prover.addConstraint(expectedNegated);
    prover.addConstraint(actual); // both constraints must hold
    boolean isUnsat = prover.isUnsat(); // isUnsat = false here.
    try (Model model = prover.getModel()) {
        // Prints the value of x found for which the two constraints hold
        // (i.e. a violation of the refinement type has been found)
        System.out.printf("Violation found with: ", model.evaluate(x));
    }
}
```

If the SMT theorem is satisfiable, we have found a violation – it is possible for the refinement type constraints to not hold during execution. These are reported via the central error reporting mechanism.

## Reporting

⚙️ Parsing   🔍 Initial walk   🔍 Type checking   📄 Reporting

During the 4th and final step of execution, the prototype application reports the errors discovered previously. Each of these includes a line number and message to describe the problem.

These are simply printed to the standard error stream at the command line, but a real language could show these violations in an IDE to highlight problems inline.

## Phase 2

Once unsigned integer constraints were complete and a set of passing test cases had been written, the focus shifted to adding `string` support. A new type keyword was added, and the grammar was modified to accept regular expression constraints as shown in the example below.

```
function LookupUserById(): string[/g+/] {
    return "f"
}
```

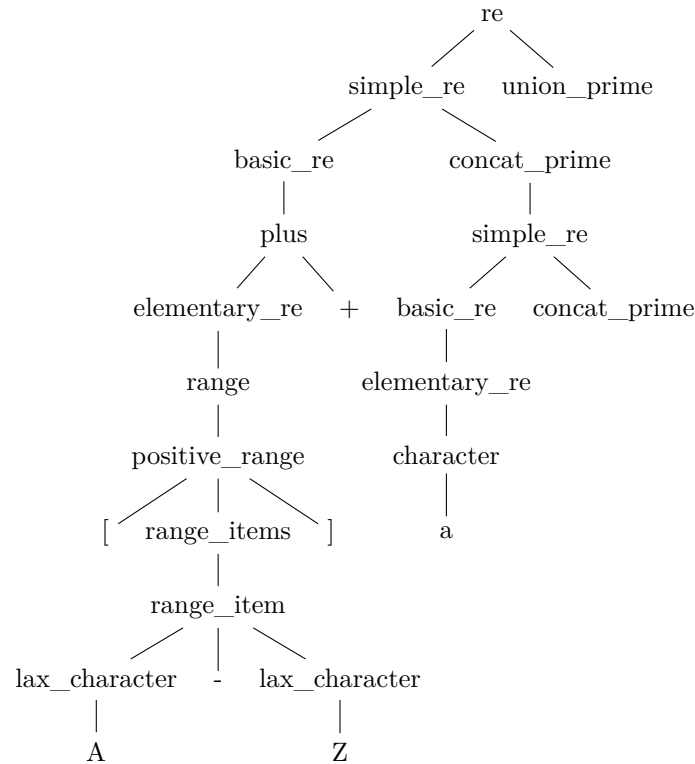
Adding support for these constraints required being able to parse regular expressions. This was more challenging than anticipated – although BNF descriptions of regular expressions are readily available, they are indirectly left-recursive. ANTLR, along with all *LL* parser generators, requires that such production rules are removed before a working parser can be generated (Dick and Ceriel, 1990).

It is reasonably straightforward to remove left-recursion by introducing new production rules, however another issue arised with the programming language grammar's tokens:

```
IDENTIFIER : [A-Za-z_] [A-Za-z_0-9]* ;
CHARACTER  : ~('\n'|\r'|'.'|'('|')'|'['|']'|'*'|+'|'/'|'|') | ESCAPED_META;
```

The `IDENTIFIER` token was used for function and variable names. The `CHARACTER` token was used for single characters within a regular expression. As the two token definitions overlapped, only one would be identified by the lexer which had the effect of breaking the parsing of either the regular expressions, or the function definitions.

The fix for this issue was to use lexical modes. When the start of a string constraint is detected, the lexer should switch into a `REGEX` mode and match arbitrary characters with the `CHARACTER` token. At the end of the regular expression the mode should return to the default. Unfortunately, lexical modes are not supported in ANTLR's composite grammars and it was therefore necessary to split the parser and lexer into separate grammar files.

Figure 3: Parse tree for regular expression `[A-Z]+`.

Once this parsing was complete, it should have simply been a matter of taking advantage of the SMT solver’s regular language membership support to find violations in much the same way as was performed on the integers. String (and regular expression support) is not universal amongst SMT solvers, however – and JavaSMT did not provide an abstraction layer over such functionality.

As a result, the decision was made to build Z3 from source and use its Java bindings instead of the JavaSMT library. Z3 includes Z3str3 which is able to efficiently support solving string equations and predicates involving regular language membership (Berzish et al., 2017). The original code which used the JavaSMT APIs to solve constraint problems with integers was then modified to use Z3. An adapter was written to construct a Z3 regular expression object from a parse tree.

The final prototype allows us to write a program like the one below:

```

function SecondaryFunction(): string[/g+|f+/] { // must return one or more 'g's OR one or more 'f's
    return "f"
}
function Main(): string[/f+/] { // must return one or more 'f's
    return SecondaryFunction()
}
  
```

It will correctly determine that the union of `g+` in the constraint of `SecondaryFunction`’s return type is incompatible with `Main`’s return type:

```

→ PocLang (git:master) cat input.txt | ./gradlew run
> Task :run
Reading program from stdin (use Ctrl+D when finished)...
Violation via value "gggg"
L5:4 Return type string [(str.in.re x (re.union (re.+ (str.to.re "g")) (re.+ (str.to.re "f"))))] of function SecondaryFunction didn't satisfy string [(str.in.re x (re.+ (str.to.re "f")))]
  
```

The string which the SMT solver has found, “gggg”, matches `/g+|f+/` (and so is a valid return value for



**SecondaryFunction**) – however, it does not match `/f+/. In this way, it would be possible for the Main function at runtime to violate the contract constraining the values it can return.`

### 3. Project Management

The following objectives were described in the project specification (Appendix A):

1. Formalise a type system that supports types predicated with a regular expression pattern that elements of the refined type will satisfy (be matched by).
  - (a) Explore the consequences of typical string operations (e.g. concatenation) and define the type of their return value when applied to elements of the regular expression type.
  - (b) At minimum, this should allow for simple functions to be declared that can safely accept/return a particular regular expression input.
  - (c) Evaluate the rate of false positives when compared to existing static analysis
2. Implement such a type system that can guarantee type safety, built against a simplified proof-of-concept language.
  - (a) Test the implementation against a variety of test cases. The testing strategy should make use of automated unit tests, and manual system testing considering both general expected input as well as any relevant “edge-cases” that need to be handled.

Objective 2 and the sub-objective related to testing has been completed as of the time of writing. 26 individual passing JUnit test methods have been defined which cover the broad areas described below:

**Parsing** Tests for simple syntactically valid and invalid programs, as well as parser regression tests for functions that were incorrectly parsed during development and subsequently fixed.

**Simple type checks** Such as returning a string from a function marked as returning a string.

**Other checks** Including function/variable re-declaration.

**Integer refinement types** As described above, constraint violations for integer inequalities.

**Regex refinement types** As described above, constraint violations for regular language membership.

```
→ PocLang (git:master) ./gradlew test --rerun-tasks
```

```
BUILD SUCCESSFUL in 4s
4 actionable tasks: 4 executed
```

Manual testing has taken place throughout and has been used to influence development of new unit tests.

Objective 1. (b) has been completed, in addition to local variable type constraints. Objectives 1. (a)<sup>2</sup> and (c) have not yet been completed.

This level of progress is in line with the original schedule, which allocated false positive rate evaluation to occur in early February of 2019 (with implementation to be finished in late November and testing to take place from December until January).

There were some setbacks due to the initial use of JavaSMT. In hindsight, evaluating the effectiveness of the JavaSMT abstraction layer for use with strings *prior* to creating the prototype with unsigned integers would have saved time. It is likely we would have used Z3 from the start.

The immediate next steps once these objectives are complete include making the prototype language more expressive by introducing constructs to control execution flow. If time permits, the *stretch objectives* will also be considered. There does not appear to be a need to make changes to the schedule at this time.

<sup>2</sup>It should be reasonably trivial to define the plus operation for strings and infer the type constraint to be the concatenation of all involved regular expressions.

## 4. Conclusion

In conclusion, development has proceeded reasonably well. There were some setbacks – parsing challenges as well as needing to replace the SMT solver library which required refactoring time – but the end result is a working prototype which implements refinement types for both integer inequalities and regular language membership.

Most of the objectives for the project have been met, including some which were scheduled to be completed later in the project's life. As a result, the project is on track for completion.

## 5. References

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## Appendix A – Specification

The original specification as submitted at the start of Term 1 is included overleaf.

# Introduction

Within information security, entire classes of application vulnerabilities arise due to problematic user input handling (Christey and Martin, 2007). This covers cross-site scripting (XSS), injection (SQL, LDAP, etc), insecure deserialisation and file inclusion vulnerabilities – all of which are regularly discovered in major software products.

There are many existing products that aim to detect problems within an application. Sadowski et al. (2018) describe the benefits of static analysis tooling deployed within Google which allow checks for common issues to be performed as part of the compilation process. The authors explain one of the main challenges with developer adoption as *trustworthiness* “users do not trust to results due to, say, false positives“ and highlight the importance of reporting issues early: “survey participants deemed 74% of the issues flagged at compile time as real problems, compared to 21% of those found in checked-in code”.

In the context of application security, tooling can be broadly categorised into the two broad areas of DAST (dynamic application security testing) and SAST (static application security testing) tooling. SAST tooling can analyse a codebase at rest and lends itself to generating much more immediate results that can take the entire codebase into account. DAST tooling allows for assessment from a black-box perspective but is much more limited. Research into the effectiveness of DAST-based scanning tools by Doupé et al. (2010) drew the conclusion that commonly available tools of this kind often failed to crawl more complex parts of an application which resulted in decreased coverage from a security perspective.

Existing static analysis tools can provide useful warnings that help prevent introduction of vulnerabilities. In the .NET ecosystem, tools such as *Roslyn Security Guard* can detect e.g. injection vulnerabilities by tainting user input and then using information flow analysis – first described in Denning and Denning (1977) – to determine when unsafe input is passed to a dangerous *sink* function (Arteau, 2016). Of course, this approach is limited. All user input is deemed unsafe by virtue of being user input and prior validation (as is commonly performed using regular expressions) is not taken into account when deciding if an alert needs to be raised or not. This leads to false positive reports where a program is secure by virtue of already performing validation to prevent a vulnerability.

The main objective of this project is to explore the use of a type system which uses regular-expression based refinement types applied to user input. A refinement type in the context of a type system is a type that is subject to a particular predicate (Pierce, 2002, p. 207). By considering flow of data that belongs to a refinement type for a particular pattern, it will be possible to make inferences about vulnerabilities that may be present in a codebase based on declared safe argument types. Use of refinement types in this way provides for a more informed evaluation of a particular risk than base types alone and should therefore enable reporting of fewer false positive issues.

```
function LookupName(userId: /[A-Za-z0-9]+)/): string {
    var name: string = GetNameByUserId(userId); // safe
    GetNameByUserId("; DROP TABLE users;"); // type error
    return name;
}

function GetNameByUserId(query: /^[^"]+$/): /[A-Za-z ]+/ { /* database lookup.. */ }
```

Listing 1: Example code illustrating a potential syntax. `userId` and `query` use the refinement type.

## Objectives

### Primary Objectives

- Formalise a type system that supports types predicated with a regular expression pattern that elements of the refined type will satisfy (be matched by).
  - Explore the consequences of typical string operations (e.g. concatenation) and define the type of their return value when applied to elements of the regular expression type.

- At minimum, this should allow for simple functions to be declared that can safely accept/return a particular regular expression input<sup>1</sup>.
  - Evaluate the rate of false positives when compared to existing static analysis
- Implement such a type system that can guarantee type safety, built against a simplified proof-of-concept language.
  - Test the implementation against a variety of test cases. The testing strategy should make use of automated unit tests, and manual system testing considering both general expected input as well as any relevant “edge-cases” that need to be handled.

## Additional Objectives

- Apply the theory explored in the primary phase of the project to produce a type analysis tool which works against type annotations applied to a commonly-used language such as C# or Scala. This tooling could be integrated into an IDE or CI pipeline.

**i** Primary objectives are expected to be completed during the lifetime of the project. Additional objectives are identified as potential goals to pursue beyond the original scope of the project, if time permits.

## Schedule

Time Window	Work
October 1 <sup>st</sup> – October 14 <sup>th</sup>	Specification completion, research into prior related works. Study of elementary programming language and type system theory (e.g. simply typed $\lambda$ -calculus, SLam).
October 15 <sup>th</sup> – October 28 <sup>th</sup>	Begin writing background for report, work on formalisation of regular expression refinement type. <b>Deadline:</b> CS353 presentation, 24 <sup>th</sup> October
October 29 <sup>th</sup> – November 11 <sup>th</sup>	Explore and document properties of type system. Begin implementation of ideas to produce a concrete proof-of-concept.
November 12 <sup>th</sup> – November 25 <sup>th</sup>	Completion of progress report, continued implementation work.
November 26 <sup>th</sup> – December 9 <sup>th</sup>	Testing of implemented proof-of-concept. <b>Deadline:</b> CS915 coursework, 26 <sup>th</sup> November
December 10 <sup>th</sup> – January 6 <sup>th</sup>	Slack time (to use if behind schedule, else to make a start on year scheduled in 2019).
January 7 <sup>th</sup> – January 20 <sup>th</sup>	Finalise testing of implementation, write-up test cases. <b>Deadline:</b> CS324 coursework
January 21 <sup>st</sup> – February 3 <sup>rd</sup>	Evaluate false positive rates against existing systems based exclusively on taint tracking.
February 4 <sup>th</sup> – February 17 <sup>th</sup>	Report work, project presentation preparation
February 18 <sup>th</sup> – March 3 <sup>rd</sup>	Project presentation preparation, report work
March 4 <sup>th</sup> – March 17 <sup>th</sup>	Project presentation delivery, report finalisation.

Table 1: Projected work by time period. Deadlines for other modules included where known.

<sup>1</sup>As a simplified example, an `unsafe_shell_exec` function might safely be able to accept any input that matches `^[~]*$`



Table 1 provides a breakdown of the project time into periods for each fortnight, along with the expected work to be completed. A meeting will be scheduled for each week to discuss progress and any road-blocks that arise with the project supervisor

## Methodology

### Software Engineering

This project includes an element of software engineering. Namely, the design and implementation of a proof of concept language which supports a type system incorporating regular expression refinement types.

This implementation work will be carried out in an Agile fashion to fit in with the short timescales inherent to the project and allow for greater flexibility. Time periods in the schedule which involve development work will be treated as a number of week-long development sprints with priorities formalised prior to the commencement of each period. Progress will be reviewed in weekly supervision meetings.

Testing will be automated via the use of unit testing to ensure that specific components function according to their specification in isolation. Where appropriate, integration and system testing can be used to test the solution as a whole (for example, an entire program as a test case would fit into this part of the testing process).

### Evaluation

Towards the end of the implementation phase, the false positive rate of the proof of concept tool should be compared with that of existing static analysis tooling based on taint tracking alone.

Logically equivalent test cases should be built for each tool under evaluation in the necessary programming language. Both safe and unsafe function invocations should be included in each test case for completeness.

## Resources and risks

The project is reliant on a number of resources. Use of these resources is subject to the risks outlined in table 2. These risks should be evaluated and managed to minimise any potential impact on the project.

Resource	Applicable risk(s)	Impact
<b>VCS hosting: GitHub</b> Storing and tracking code and report changes	Loss of availability due to outage	Minimal, <i>git</i> is decentralised so copy of files always available locally and at off-site backup
<b>Report authoring: L<sup>A</sup>T<sub>E</sub>X</b> Writing and compiling the report, tracking bibliography	Obsolescence	Unlikely, TeX tooling has been used for decades. Even if particular packages ceased working, the bulk of the content would still be accessible as plain text.
<b>C# analysis: Roslyn library</b> Fulfilling the additional objective by analysing C# code	Loss of availability due to license change	Minimal. Even if Roslyn's OSS status changes, there is no requirement to integrate with C#, other languages would illustrate the potential just as well. This would also not impact a primary project objective.
<b>Self</b> Project work	Illness, coursework deadlines	Minimised by scheduled slack time and identification of applicable coursework deadlines.

Table 2: Resources and associated risks.

# Legal, social, ethical and professional issues

As a project with some security motivation, it is possible that legal, social, ethical and professional issues will arise. In particular, evaluation of existing static analysis tooling must be performed with care to ensure that use of any particular external test cases is permitted by the *Copyright, Designs and Patents Act 1988* within the UK.

Additionally, in order to comply with the *Computer Misuse Act 1988*, any static analysis of external code should only be conducted with permission. Discovered issues should be disclosed responsibly.

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