

# **Modelling and Solving Exercises in MiniZinc - 2**

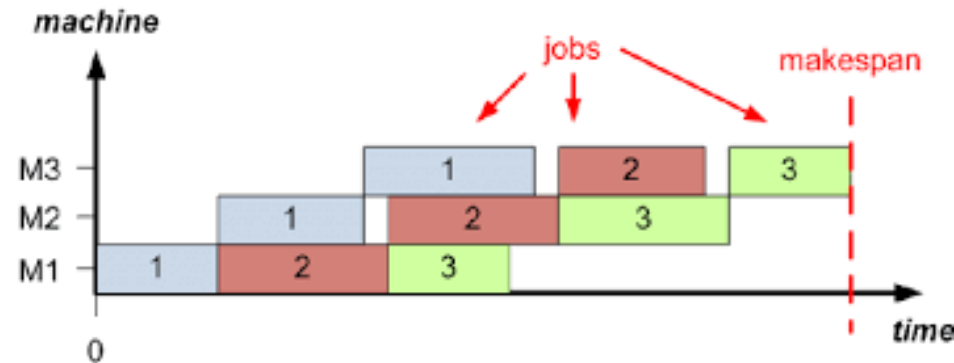


# Before Starting

- Use a separate folder for each problem.
- Create a project file (.mzp) for the problem.
  - Add the model files (\*.mzn)
  - Add the data files (\*.dzn)
- Configure the solver to obtain the solution statistics, to search for one or all solutions, and to set a time limit when needed.

# A Disjunctive Scheduling Problem

- Given:
  - a set of machines and a set of jobs, each composed of a sequence of tasks where each task  $i$  requires a machine  $i$ ,
  - durations of the job tasks,
- decide:
  - when to execute each job task so as to minimize the makespan, subject to task precedence and disjunctive resource constraints.



# A Disjunctive Scheduling Problem

- # tasks = # machines
- Variables and Domains
  - Start time  $S_{ji}$  for each job  $j$  and its task  $i$  with domain?
- Constraints
  - Precedence constraints on consecutive tasks of each job.
  - Disjunctive constraints for each machine.
- Objective function
  - Makespan as a dummy activity with the lowest precedence in the schedule.
- Objective
  - Minimize makespan.

# A Disjunctive Scheduling Problem

- Implement the model using the **disjunctive** global constraint.
- Implement another by decomposing **disjunctive**.
- Search for the optimal solution to the provided instances using Gecode and the input order of the variables and the values, with a time limit of 5 mins (300 secs).

```
solve :: int_search(s, input_order, indomain_min) minimize end;
```

- Compare the objective value and the total time.

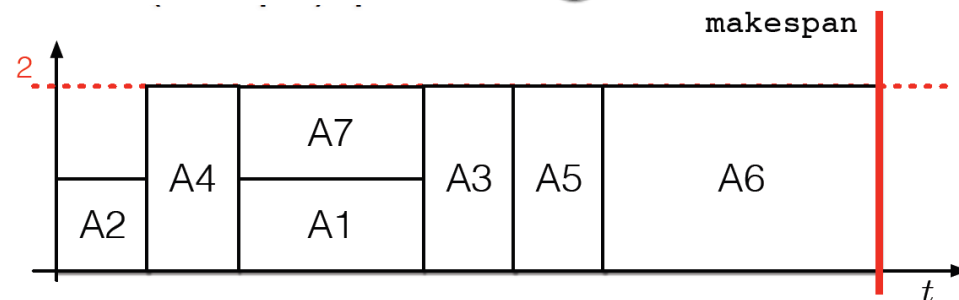
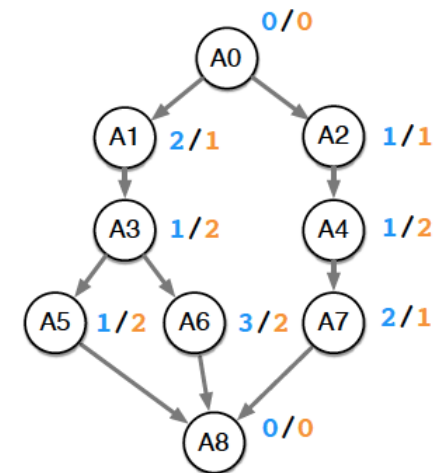
# A Cumulative Scheduling Problem

- Given:
  - a set of cumulative resources,
  - a set of tasks with durations and resource requirements,
  - precedence constraints between some tasks,

decide:

- when to execute each task so as to minimize the makespan, subject to precedence and cumulative resource constraints.

■ duration  
■ req for  $r_0$  ( $c_0 = 2$ )



# A Cumulative Scheduling Problem

- Variables and Domains
  - Start time  $S_i$  for each task with domain?
- Constraints
  - Precedence constraints for each given  $i \rightarrow j$
  - Cumulative constraints for each resource  $r$ .
- Objective function
  - Makespan as the maximum  $S_i + d_i$ .
- Objective
  - Minimize makespan.

# A Cumulative Scheduling Problem

- Implement the model using the **cumulative** global constraint.
- Can you add any **implied constraints** to the model?
- Search for the optimal solution to the provided instances using the default search of Gecode, with a time limit of 5 mins (300 secs).

```
solve minimize makespan;
```

- For the difficult instances, experiment with Chuffed using its default search.
- Compare the objective value and the total time.