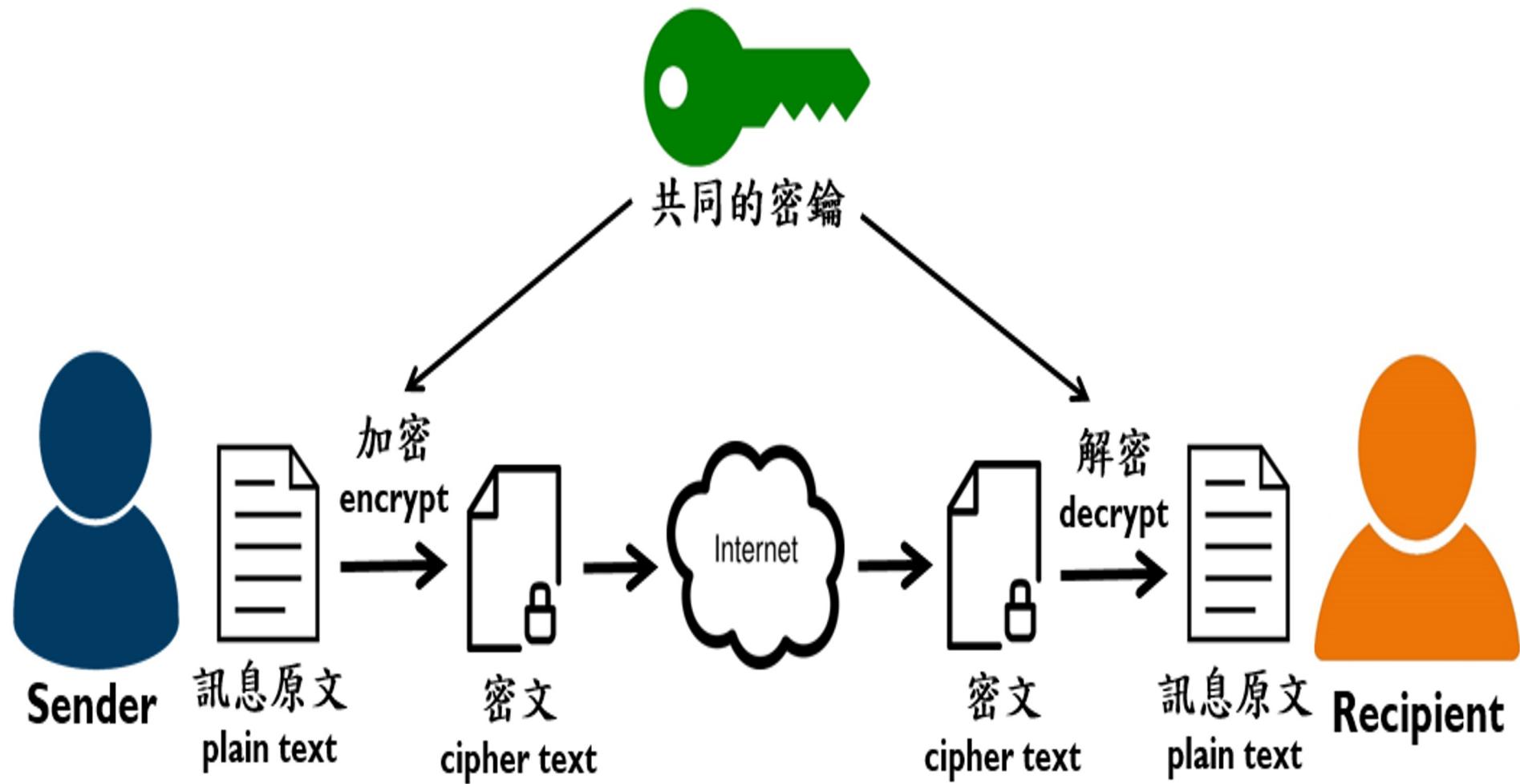


---

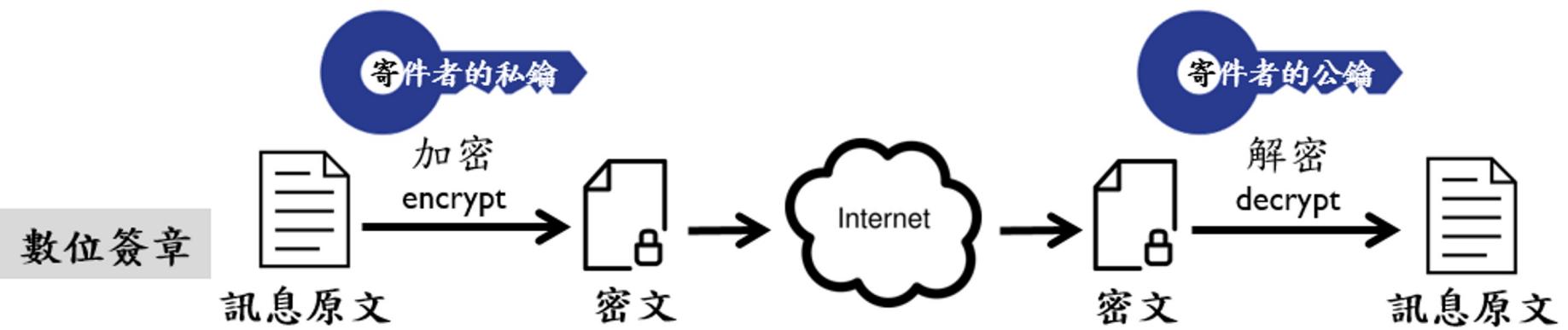
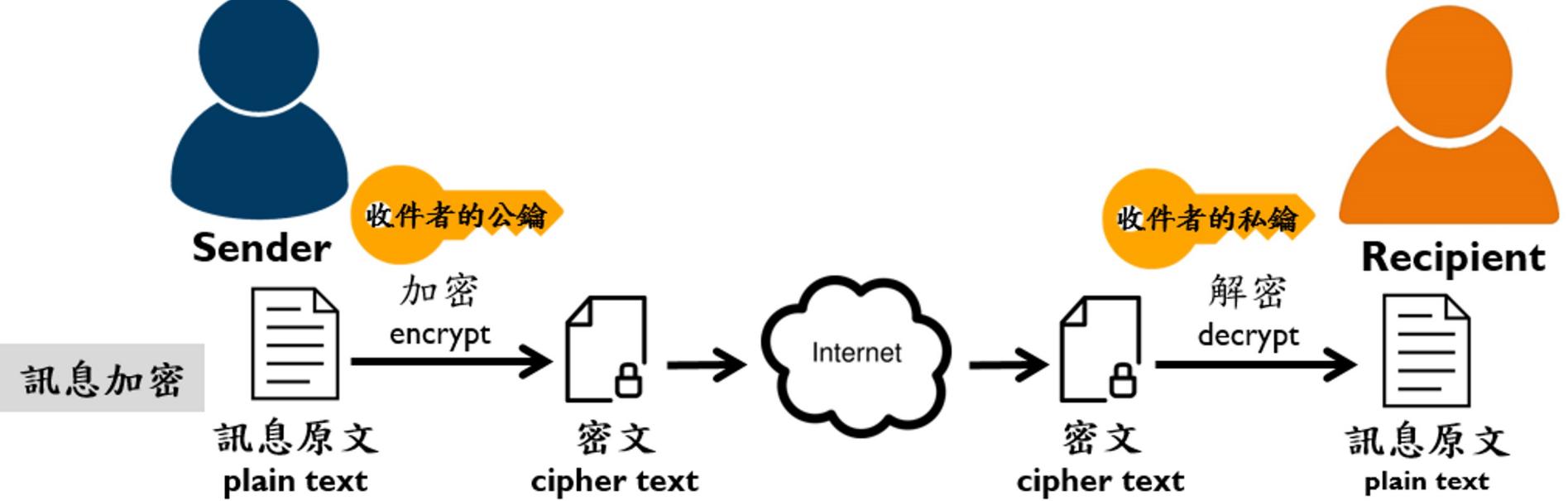
# 接觸史文件



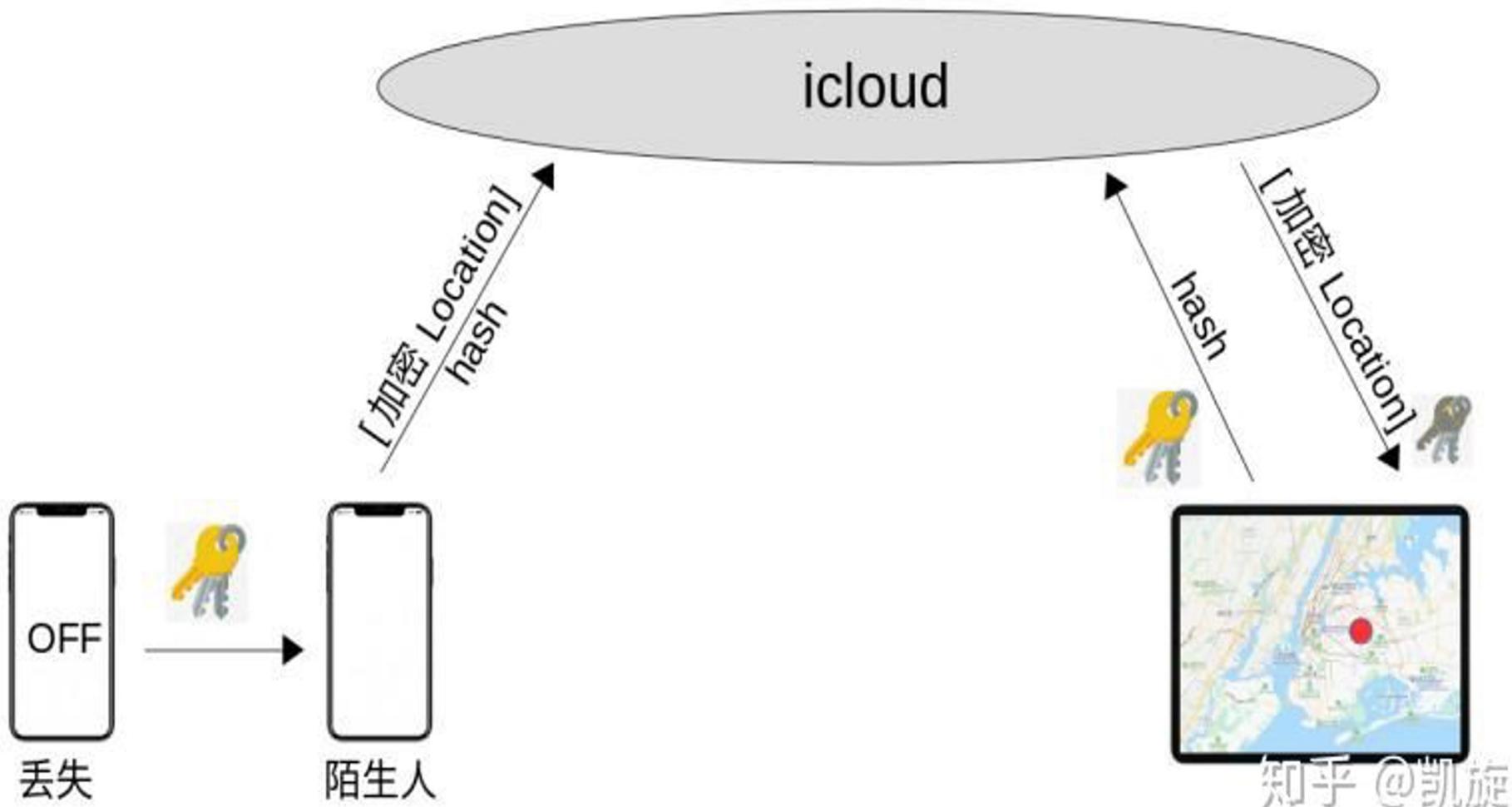
# 對稱加密



# 非對稱加密



# Apple - Find My Phone



回到正題...

# TK (Tracing Key)

## TK (Tracing Key)

1. 每個手機只生成一次，生成後固定不變
1. 32字節長度，通過算法保證每個用戶唯一
1. 該密鑰由操作系統組件生成

$$tk \leftarrow CRNG(32)$$

# **DTK(Daily Tracing Key)**

## DTK (Daily Tracing Key)

1. 每天變化一次
2. 16字節長度

$$dtk_i \leftarrow HKDF(tk, \text{NULL}, (\text{UTF8}("CT-DTK") || D_i), 16)$$

## Di (DayNumber)

從1970年1月1日到當前的天數，其算法如下：

$$\text{DayNumber} \leftarrow \frac{\text{Number of Seconds since Epoch}}{60 \times 60 \times 24}$$

# RPI (Rolling Proximity Identifier)

## RPI (Rolling Proximity Identifier)

1. 每10分鐘變化一次
2. 為藍牙向外廣播的內容資料

$$RPI_{i,j} \leftarrow \text{Truncate}(HMAC(dkt_i, (\text{UTF8("CT-RPI")} || TIN_j)), 16)$$

## TIN (TimeIntervalNumber)

1. 從每一天的0點開始初始化為0
2. 每過10分鐘累加1
3. 取值範圍[0-143]

$$\text{TimeNumberInterval} \leftarrow \frac{\text{Seconds Since Start of DayNumber}}{60 \times 10}$$

# **DK (Diagnosis Keys)**

## DK (Diagnosis Keys)

1. 一組每日追蹤密鑰的集合

1. [Daily Tracing Key, 產生日期]，一般是14組。

Unique per User

## Tracing Key

Key Derivation

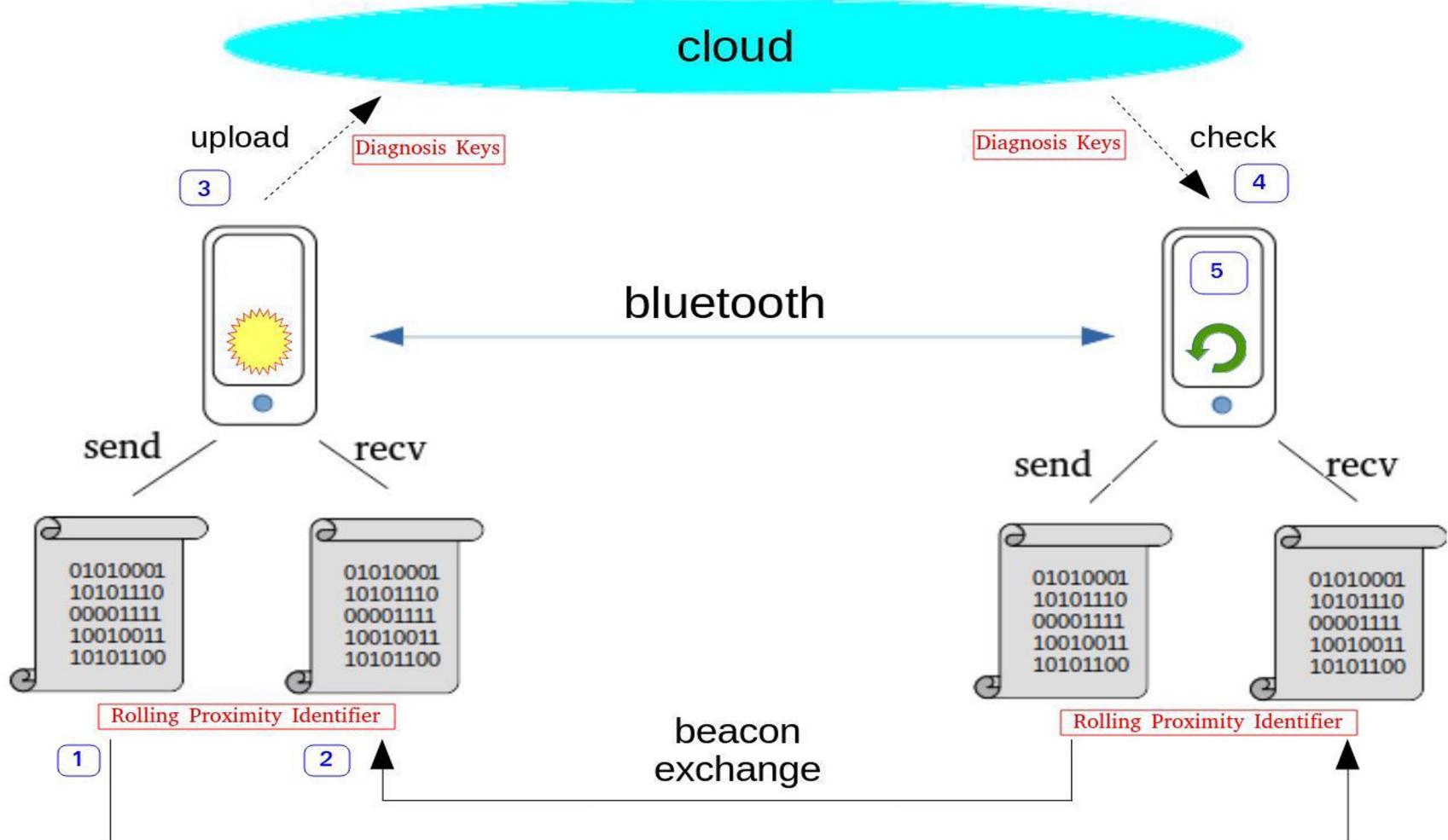
One per Day

## Daily Tracing Key

Message Authentication Code

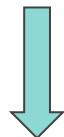
One per  
Broadcasting  
Rotation Interval

## Rolling Proximity Identifier

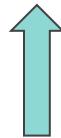


0x03

透過ServiceUUID告知此設備所支持的Service



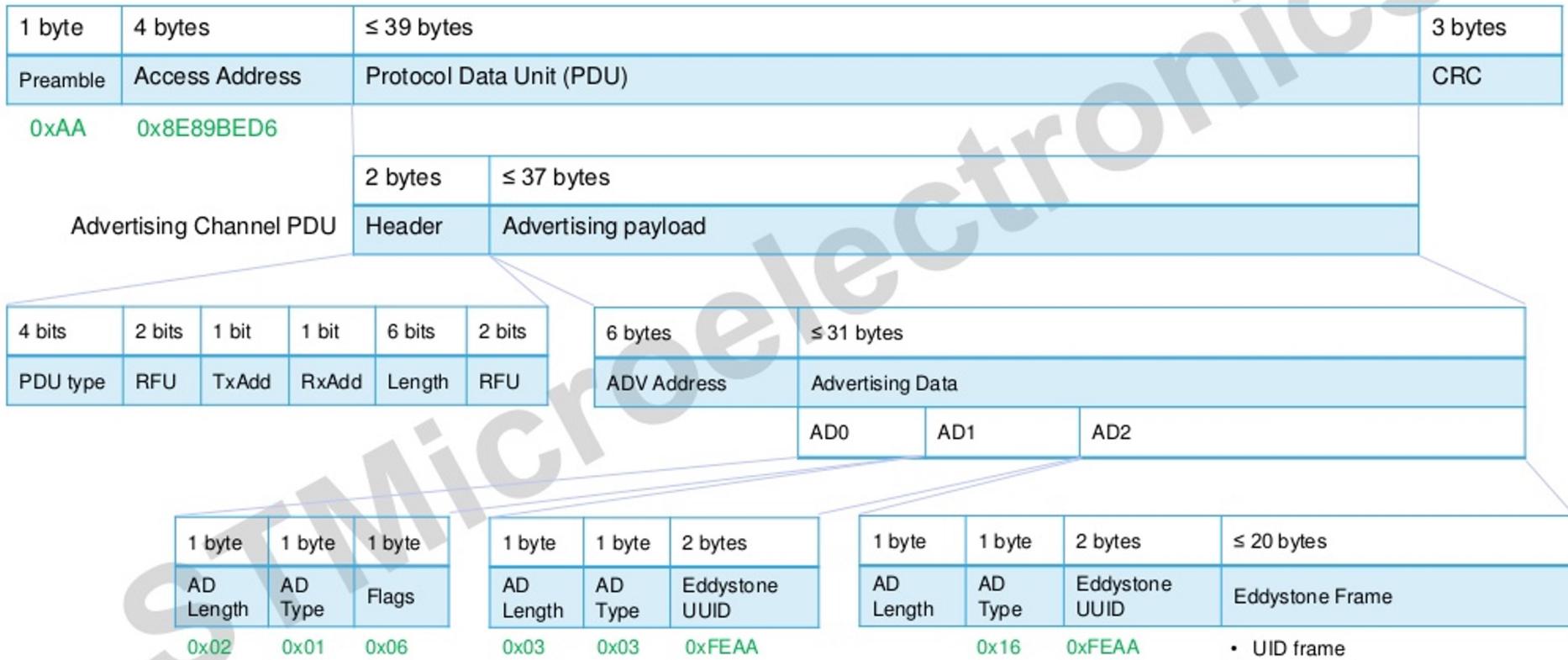
Flags			Complete 16-bit ServiceUUID			Service Data - 16 bit UUID			
Length	Type	Flags	Length	Type	ServiceUUID	Length	Type	ServiceData	
0x02	0x01 (Flag)	0x1A	0x03	0x03 (Complete 16-bit ServiceUUID)	0xFD6F (Contact Detection Service)	0x13	0x16 (Service Data - 16 bit UUID)	0xFD6F (Contact Detection Service)	16 bytes Rolling Proximity Identifier



0x16

前兩個byte 為 Service UUID  
後面為自定義資料

# Advertising Packet : Eddystone Beacon



```
private List<ScanFilter> generateScanFilters() {  
    List<ScanFilter> filters = new ArrayList<>();  
    ScanFilter filter = new ScanFilter.Builder()  
        .setServiceUuid(ParcelUuid.fromString("0xFD6F"))  
        .build();  
    filters.add(filter);  
    return filters;  
}
```

# HMAC

## HMAC (Keyed-hash message authentication code)

1. 避免使用同樣數據總是得到相同Hash 值
  1. 額外加入一個Key
  1. 使用不同的key 就能得出不同的Hash值

$\text{Output} \leftarrow HMAC(\text{Key}, \text{Data})$

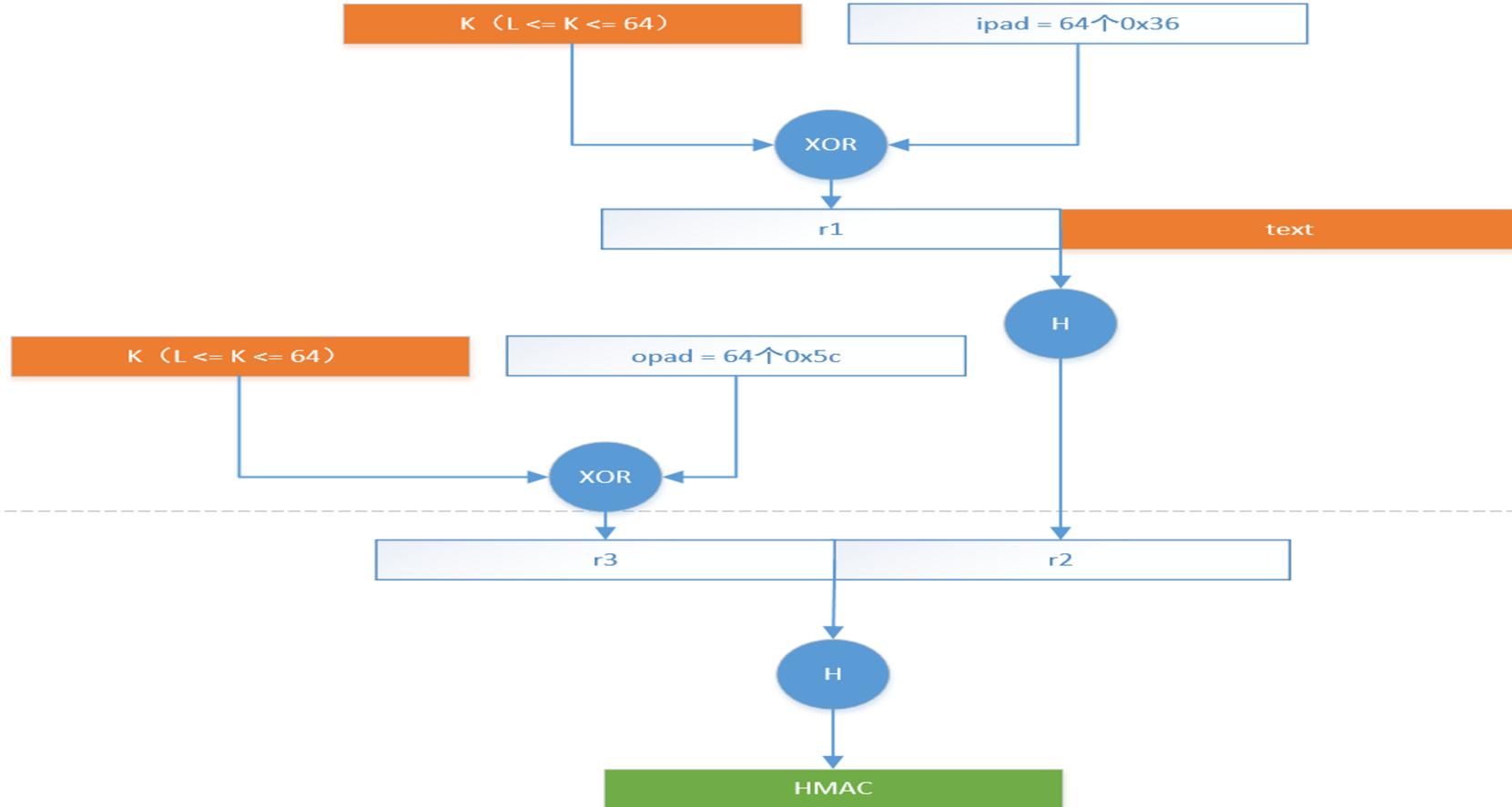
$$\text{HMAC}(K, m) = \text{H} \left( (K' \oplus opad) \parallel \text{H} \left( (K' \oplus ipad) \parallel m \right) \right)$$

$$K' = \begin{cases} \text{H}(K) & K \text{ is larger than block size} \\ K & \text{otherwise} \end{cases}$$

ipad -> 64個0x36

opad-> 64個0x5c

## HMAC





HKDF



# HKDF (HMAC-based Key Derivation Function)

1. 將較短的key擴展成較長的key

1. 保證隨機性

1. 有以下兩個步驟

(a) HKDF-Extract

(a) HKDF-Expand

$\text{Output} \leftarrow \text{HKDF}(\text{Key}, \text{Salt}, \text{Info}, \text{OutputLength})$

**Salt**

```
<?php
function hash($a) {
    $salt="WIKIPEDIA"; //定義一個加鹽字串(WIKIPEDIA)
    $b=$a.$salt; //把密碼與加鹽結合
    $b=sha($b);
    return $b;
}
?>
```

# HKDF-Extract

HKDF-Extract(salt, IKM) => PRK

1. SHA-256 => Length = 32 bytes
1. 如果沒有salt，默認是32個的0
1. salt => key , IKM => original key => data

HKDF- Extract (H, salt, IKM)



HMAC- Hash (H, salt, IKM)

1. 輸出結果為 PRK

# HKDF-Expand

$\text{HKDF-Expand}(\text{PRK}, \text{info}, L) \Rightarrow \text{OKM}$

1. SHA-256  $\Rightarrow$  Length = 32 bytes

1. HKDF-Extract 所生成的PRK

1. 隨機元info，可以為空

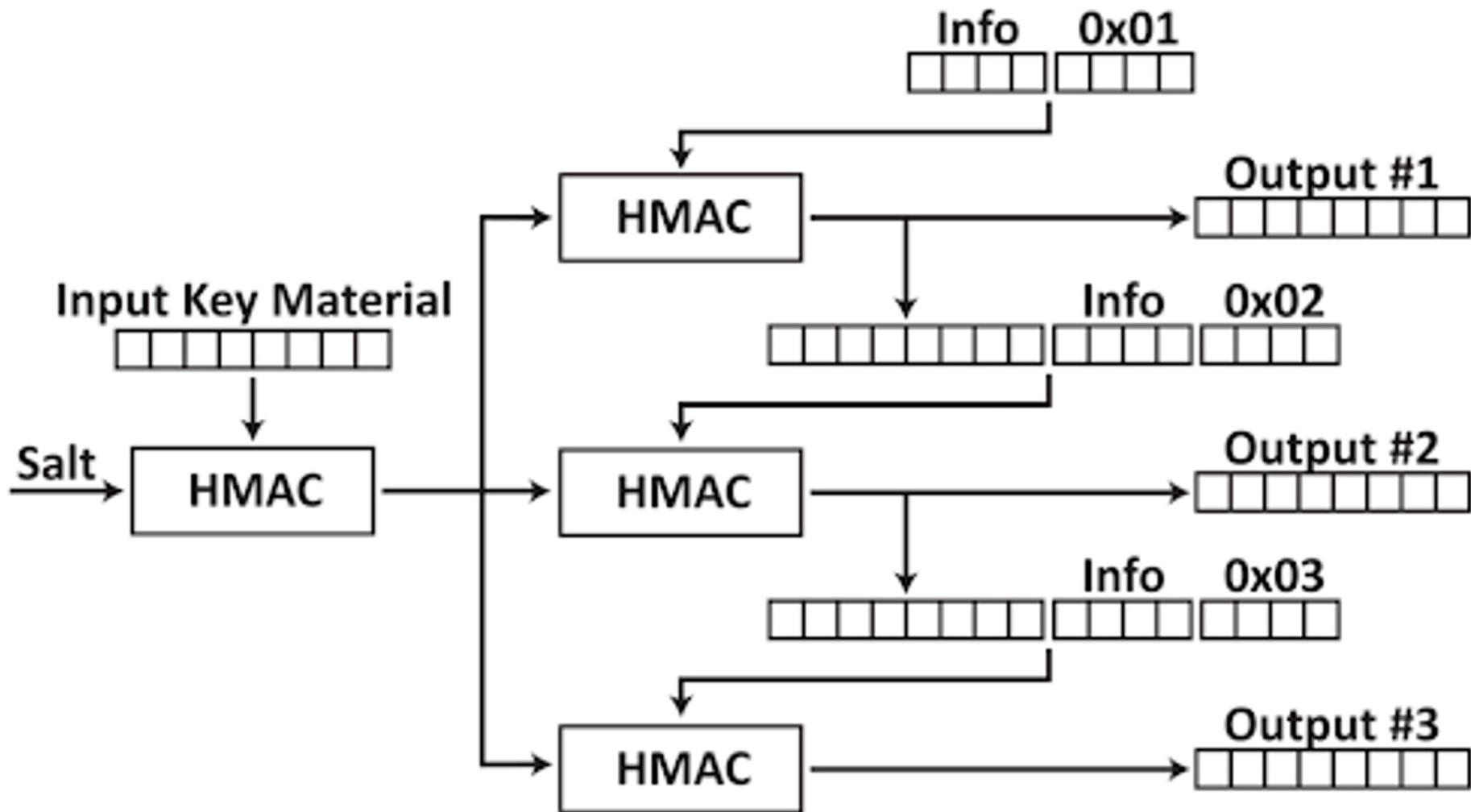
1. 指定密鑰長度

1. 輸出結果為 OKM

```
N = ceil(L/HashLen)
T = T(1) | T(2) | T(3) | ... | T(N)
OKM = first L octets of T
```

where:

```
T(0) = empty string (zero length)
T(1) = HMAC-Hash(PRK, T(0) | info | 0x01)
T(2) = HMAC-Hash(PRK, T(1) | info | 0x02)
T(3) = HMAC-Hash(PRK, T(2) | info | 0x03)
...
...
```



新版

# TEK (Temporary Exposure Key)

- 每天生成一次
- 16字節長度，通過算法保證每個用戶唯一
- 該密鑰由操作系統組件生成

$$tek_i \leftarrow CRNG(16)$$

## EKRollingPeriod

一天當中有幾個10分鐘 => 144

## ENIntervalNumber

從1970年1月1日到當前有幾個十分鐘，其算法如下：

$$\text{ENIntervalNumber}(\text{Timestamp}) \leftarrow \frac{\text{Timestamp}}{60 \times 10}$$

## RPIK (Rolling Proximity Identifier Key)

$$\text{RPIK}_i \leftarrow \text{HKDF}(\text{tek}_i, \text{NULL}, \text{UTF8}(\text{"EN-RPIK"}), 16)$$

## RPI (Rolling Proximity Identifier)

其中 PaddedData :

- PaddedData [0-5] = UTF-8( “EN-RPI” )
- PaddedData [6-11] = 0x000000000000
- PaddedData [12-15] = ENIntervalNumber

$$\text{RPI}_{i,j} \leftarrow \text{AES}_{128}(\text{RPIK}_i, \text{PaddedData}_j)$$

## AEMK (Associate Encrypted MetaData Key)

$$AEMK_i \leftarrow HKDF(tek_i, \text{NULL}, \text{UTF8}(\text{"CT-AEMK"}), 16)$$

## AEM (Associate Encrypted MetaData)

其中 MetaData :

- MetaData [0] = 藍牙版本號
- MetaData [1] = 信號強度(Rssi)
- MetaData [2-3] = 暫時保留

$$\text{Associated Encrypted Metadata}_{i,j} \leftarrow AES_{128-CTR}(AEMK_i, RPI_{i,j}, \text{Metadata})$$

V1.1

V1.2

TK (Tracing Key)

TEK (Temporary Exposure Key)

DTK (Daily Tracing Key)

DayNumber

EKRollingPeriod

TimeIntervalNumber

EnIntervalNumber

RPI (Rolling Proximity Identifier)

RPIK(Rolling Proximity Identifier key)

RPI (Rolling Proximity Identifier)

AEMK (Associated Encrypted Metadata Key)

AEM (Associated Encrypted Metadata)

## V1.1

Flags			Complete 16-bit ServiceUUID			Service Data - 16 bit UUID				
Length	Type	Flags	Length	Type	ServiceUUID	Length	Type	ServiceData		
0x02	0x01 (Flag)	0x1A	0x03	0x03 (Complete 16-bit ServiceUUID)	0xFD6F (Contact Detection Service)	0x13	0x16 (Service Data - 16 bit UUID)	0xFD6F (Contact Detection Service)	16 bytes	Rolling Proximity Identifier

## V1.2

Flags			Complete 16-bit Service UUID			Service Data - 16 bit UUID				
Length	Type	Flags	Length	Type	Service UUID	Length	Type	Service Data		
0x02	0x01 (Flag)	0x1A	0x03	0x03 (Complete 16-bit Service UUID)	0xFD6F (Exposure Notification Service)	0x17	0x16 (Service Data - 16 bit UUID)	0xFD6F (Exposure Notification Service)	16 bytes	4 bytes Associated Encrypted Metadata



**AES 128**

# AES 128 (Advanced Encryption Standard)

1. AddRoundKey

1. SubBytes

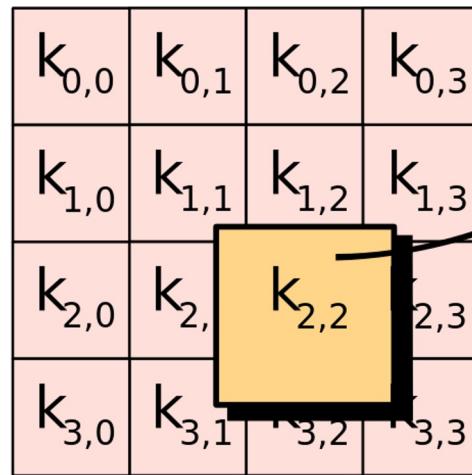
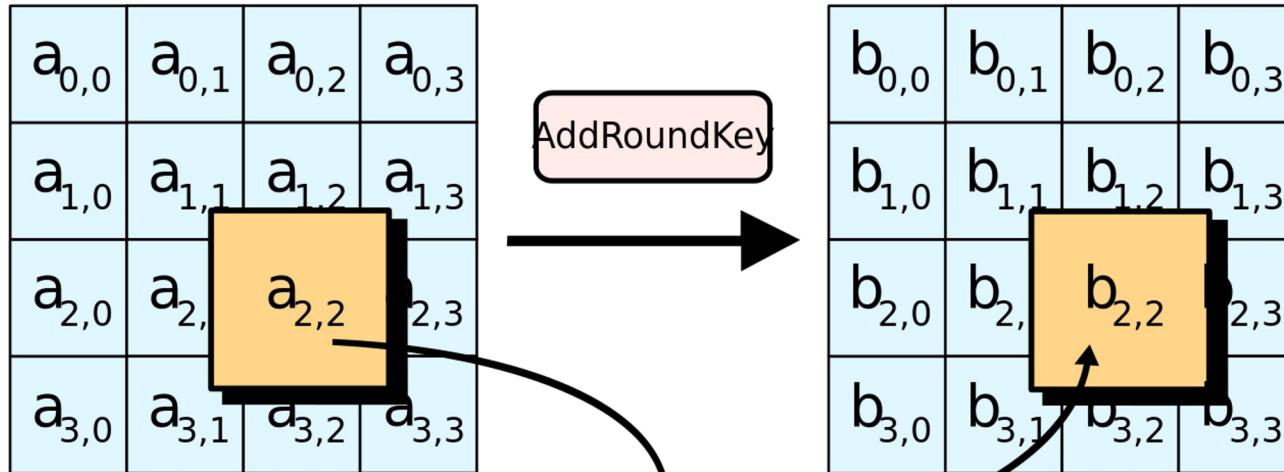
1. ShiftRows

1. MixCoulmns



# AddRoundKey







# SubBytes



$a_{0,0}$	$a_{0,1}$	$a_{0,2}$	$a_{0,3}$
$a_{1,0}$	$a_{1,1}$	$a_{1,2}$	$a_{1,3}$
$a_{2,0}$	$a_{2,1}$	$a_{2,2}$	$a_{2,3}$
$a_{3,0}$	$a_{3,1}$	$a_{3,2}$	$a_{3,3}$

SubBytes



$b_{0,0}$	$b_{0,1}$	$b_{0,2}$	$b_{0,3}$
$b_{1,0}$	$b_{1,1}$	$b_{1,2}$	$b_{1,3}$
$b_{2,0}$	$b_{2,1}$	$b_{2,2}$	$b_{2,3}$
$b_{3,0}$	$b_{3,1}$	$b_{3,2}$	$b_{3,3}$

S

# 轉換-取代(SubBytes)

- 範例 3.2 展示一組狀態如何使用 SubBytes 進行轉換。

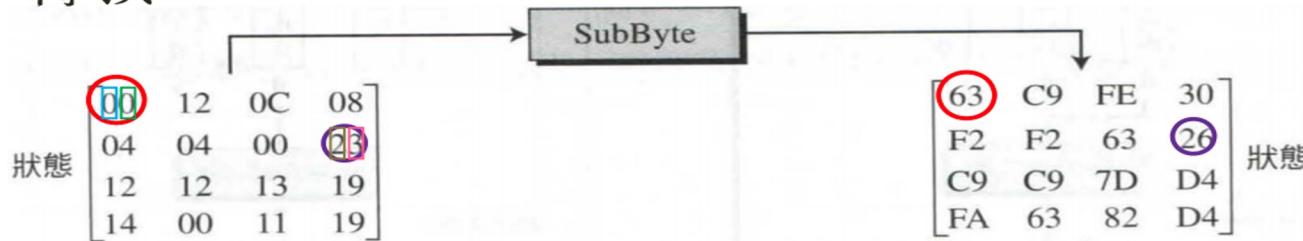


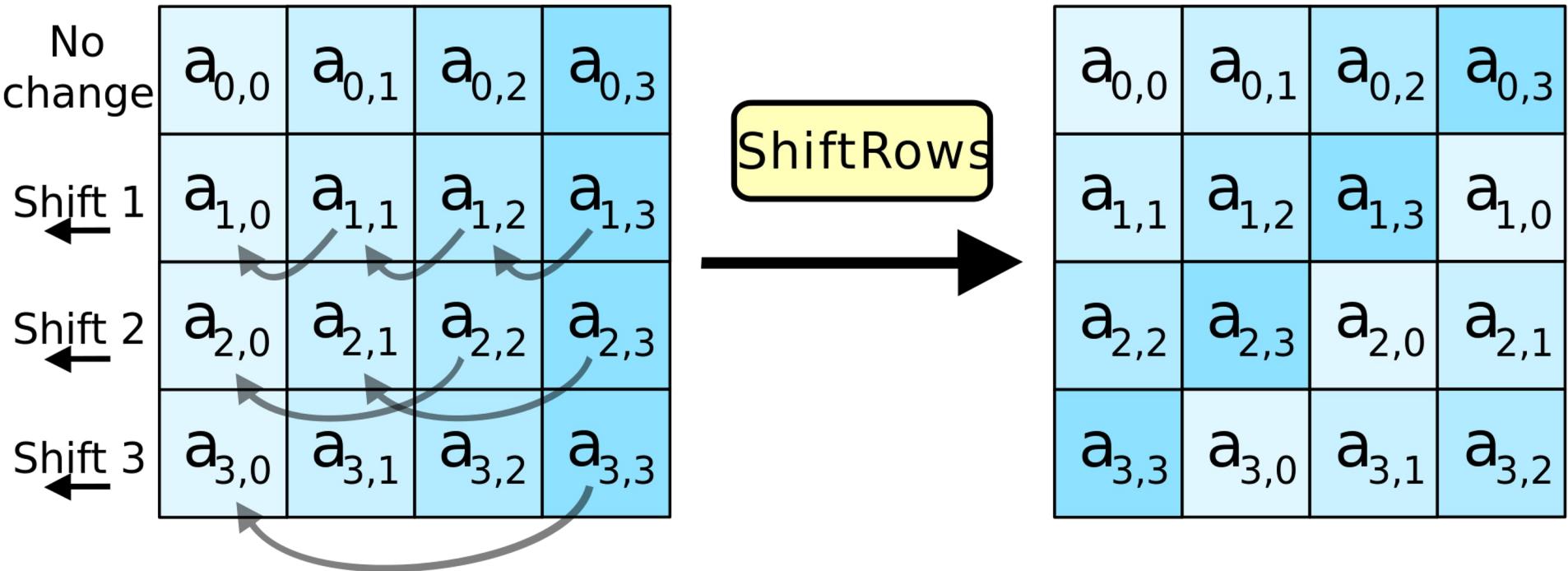
表 7.1 SubBytes 轉換表

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	B3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	E4	79	
B	E7	CB	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	C1	1D	9E
E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16

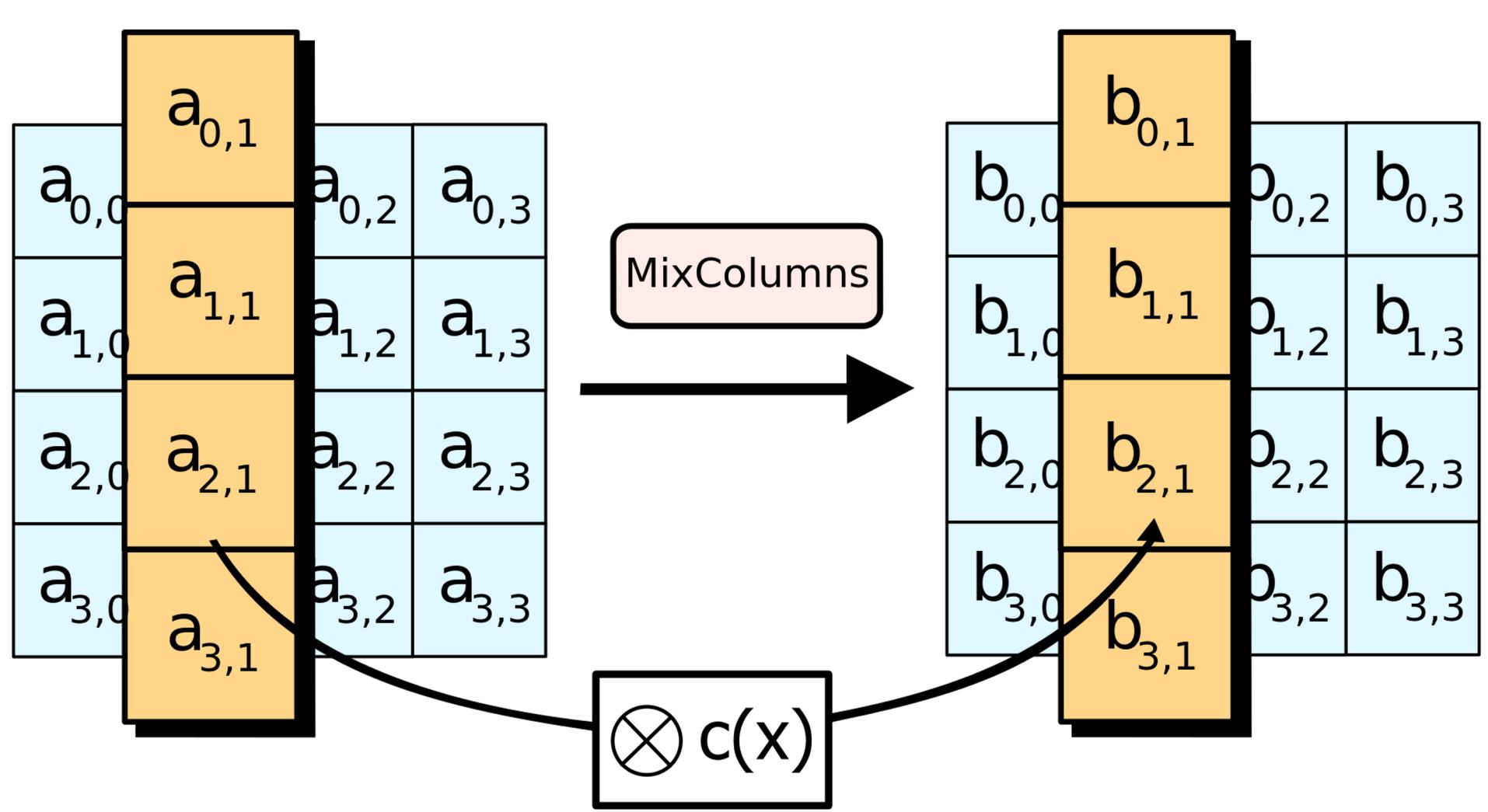
表 7.2 InvSubBytes 轉換表

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	B3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	E4	79	
B	E7	CB	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	C1	1D	9E
E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16

# ShiftRows

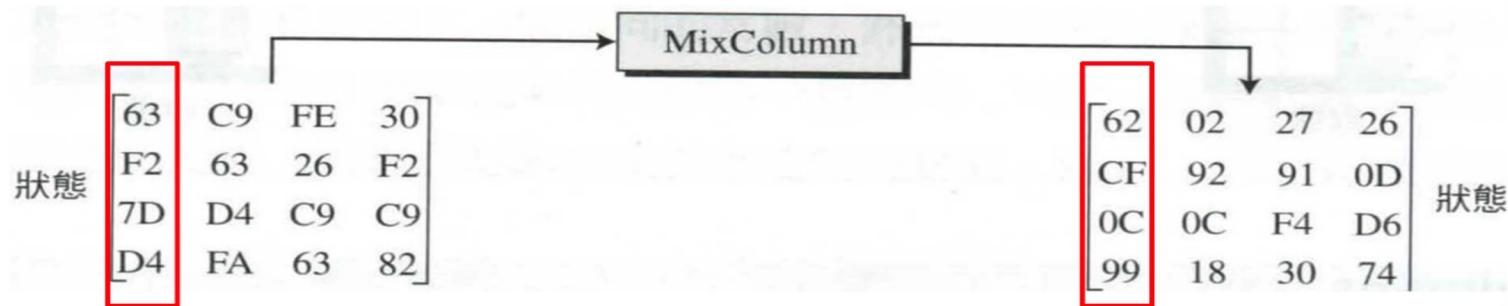


# MixColumns



# 轉換-混合(MixColumns)

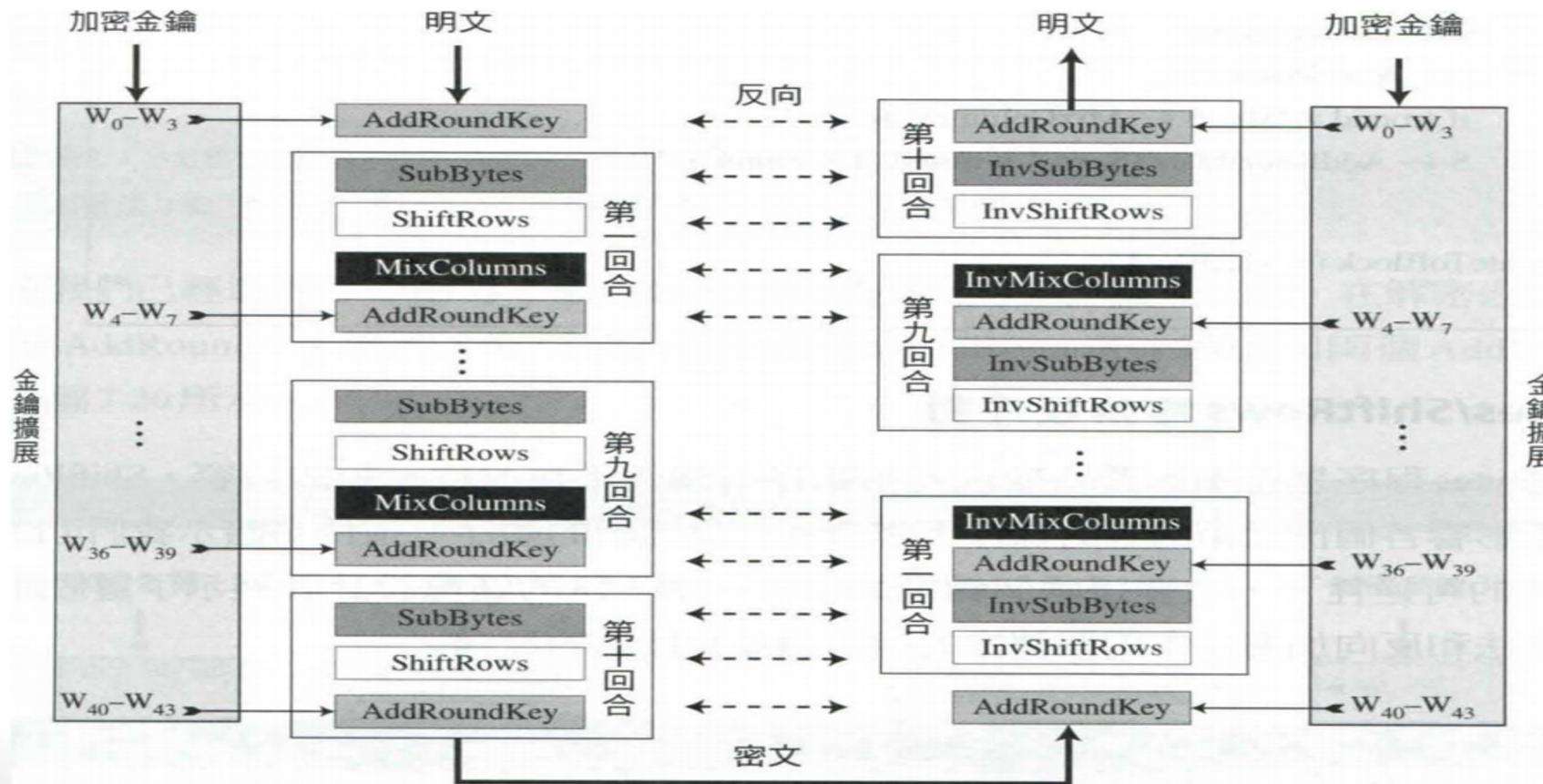
- 例題3.7 展示一組狀態如何使用 MixColumns 進行轉換。



$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \cdot \begin{bmatrix} 63 \\ F2 \\ 7D \\ D4 \end{bmatrix} = \begin{bmatrix} s_{0,0} \\ s_{1,0} \\ s_{2,0} \\ s_{3,0} \end{bmatrix} \Rightarrow \begin{cases} s_{0,0}(\text{new}) = (\{02\} \cdot 63) \oplus (\{03\} \cdot F2) \oplus 7D \oplus D4 \\ s_{1,0}(\text{new}) = (\{02\} \cdot F2) \oplus (\{03\} \cdot 7D) \oplus D4 \oplus 63 \\ s_{2,0}(\text{new}) = (\{02\} \cdot 7D) \oplus (\{03\} \cdot D4) \oplus 63 \oplus F2 \\ s_{3,0}(\text{new}) = (\{02\} \cdot D4) \oplus (\{03\} \cdot 63) \oplus F2 \oplus 7D \end{cases}$$

# AES進階加密法

- 進階加密法的加密



# AES範例

- 展示第一回合的狀態值變化。

	回合				輸入狀態				輸出狀態				回合金鑰															
	1	2	3	4	24	26	3D	1B	71	71	E2	89	B0	44	01	4D	A7	88	11	9E	6C	44	13	BD	89	BD	8C	9F
					1																							

- 1. 首先將輸入狀態對應SubByte轉換表

24	26	3D	1B
71	71	E2	89
B0	44	01	4D
A7	88	11	9E

輸入狀態

表 7.1 SubBytes 轉換表

0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F	
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	B3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
B	E7	CB	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	C1	1D	9E
E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16

36	F7	27	AF
A3	A3	98	A7
E7	1B	7C	E3
5C	C4	82	0B

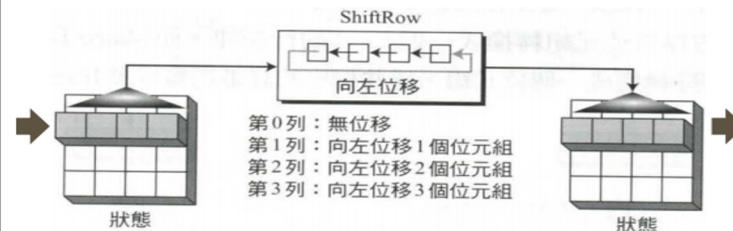
SubByte程序後

# AES範例

- 2. 經 ShiftRows 左移位元組

36	F7	27	AF
A3	A3	98	A7
E7	1B	7C	E3
5C	C4	82	0B

SubByte 程序後

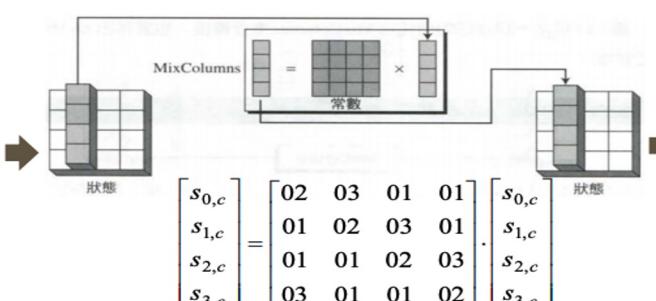


36	F7	27	AF
A3	98	A7	A3
7C	E3	E7	1B
0B	5C	C4	82

ShiftRows 程序後

- 3. 使用 MixColumns 計算值

36	F7	27	AF
A3	98	A7	A3
7C	E3	E7	1B
0B	5C	C4	82

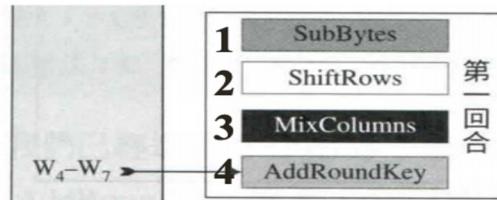


E5	F9	9F	22
E4	BE	84	5D
70	56	02	A7
93	C1	BA	4D

MixColumns 程序後

# AES範例

- 4. 最後加入回合金鑰(第一回合金鑰W<sub>4</sub>-W<sub>7</sub>)，且第一回合的密文輸出。



E5	F9	9F	22
E4	BE	84	5D
70	56	02	A7
93	C1	BA	4D

MixColumns 程序後

(第一回合金鑰W<sub>4</sub>-W<sub>7</sub>)

回合	回合金鑰
1	89 BD 8C 9F 55 20 C2 68 B5 E3 F1 A5 CE 46 46 C1

輸出狀態
6C 44 13 BD
B1 9E 46 35
C5 B5 F3 02
5D 87 FC 8C

$$E5 \oplus 89 = 11100101 \oplus 10001001 = 01101100$$

$$56 \oplus E3 = 01010110 \oplus 11100011 = \underline{10110101}$$

**END**