

Basic Approaches for Missing Values

We will now discuss a few simple approaches to deal with missing values

- We cannot easily assess them on our traffic data
- ...Since we do not know the ground truth of each missing value

Therefore, we will initially use partially synthetic data

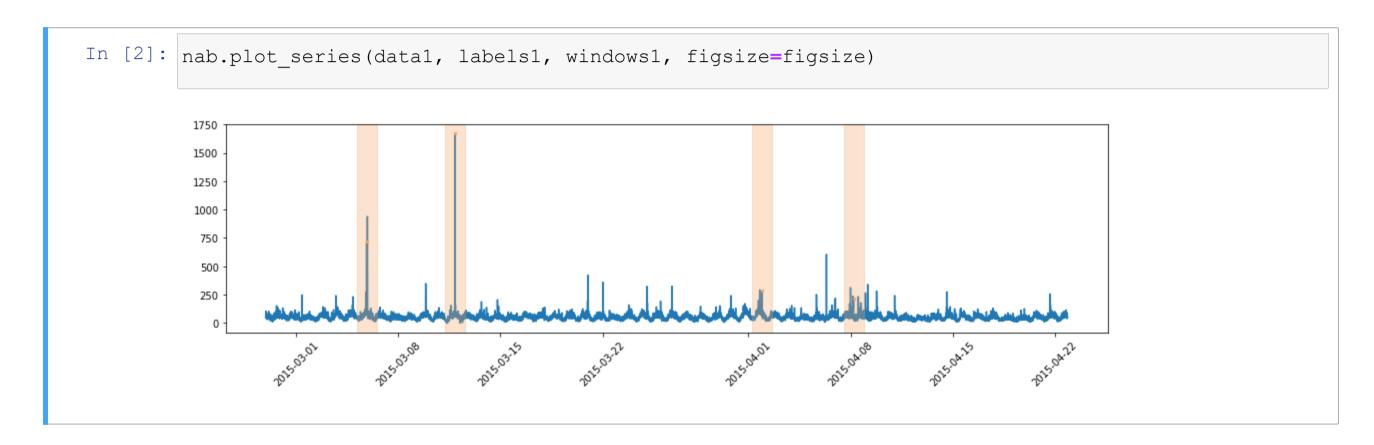
- We will start from a time series without any missing value, then remove values artificially
- ...And measure the accuracy of our filling approaches via the Root MSE

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=0}^{n} (\tilde{x}_i - \hat{x}_i)^2}$$

Where $ilde{x}_i$ is a value from the filled series and \hat{x}_i the ground truth

The Benchmark Dataset

Our benchmark dataset consists of twitter volume related to amazon.com



- There are a few anomalies, but we are not concerned with them
- Then series has a seasonal/periodic component

The Benchmark Dataset

We now introduce some missing values

First, we draw some starting points at random

```
In [3]: np.random.seed(42) # seed (to get reproducible results)
    mv_num = 30 # number of intervals with missing values
    mv_starts = np.random.choice(range(len(data1.index)), mv_num, replace=False)
    mv_starts.sort()
    mv_starts[:4]
Out[3]: array([ 88, 123, 169, 304])
```

Then, we clear values over increasingly long intervals:

```
In [4]: data1_mv = data1.copy()
    for i in range(mv_num):
        data1_mv.iloc[mv_starts[i]:mv_starts[i]+i+1] = np.NaN
```

■ The first interval contains 1 missing value, the second 2, the third 3...

The Benchmark Dataset

Let's have a look at the results around one of the "holes"

```
In [7]: idx, pad = 10, 20
        nab.plot series(data1 mv.iloc[mv starts[idx]-pad:mv starts[idx]+mv num+pad+1], figsize=figsize)
        plt.plot(data1.iloc[mv starts[idx]-1:mv starts[idx]+idx+2]);
         80
         60
         40
         20
```

■ The orange part corresponds to the removed values

Forward/Backward Filling

The easiest approach for missing values consists in replicating nearby observations

- Forward filling: propagate forward the last valid observation
- Backward filling: propagate backward the next valid observation

An important observation:

- When filling missing values, we have access to the whole series
- ...So we can reason both forward and backwards

Forward/backward filling are simple methods, but they can work well

- Rationale: most time series have a certain "inertia"
- ...I.e.: a strong level of local correlation
- For this reason, the last observation is a good predictor for the next one
- ...Remember the persistence predictor?

Forward/Backward Filling

Forward and backward filling are pre-implemented in pandas

They are available through the fillna method:

```
DataFrame.fillna(..., method=None, ...)
```

- fillna replaces NaN Values in a DataFrame Or Series
- The method parameter can take the values:
 - "pad" or "ffill": these correspond to forward filling
 - "backfill" or "bfill": these correspond to backward filling

They are generally applied to datasets with a dense index

■ Remember that our benchmark dataset already has a dense index

We can finally test forward/backward filling

```
In [8]: ffseries = data1_mv.fillna(method='ffill')
bfseries = data1_mv.fillna(method='bfill')
```

We can check the corresponding MSE:

```
In [9]: from sklearn.metrics import mean_squared_error
    rmse_ff = np.sqrt(mean_squared_error(data1, ffseries))
    rmse_bf = np.sqrt(mean_squared_error(data1, bfseries))
    print(f'RMSE for forwad filling: {rmse_ff:.2f}, for backward filling {rmse_bf:.2f}')
RMSE for forwad filling: 3.18, for backward filling 6.45
```

- In this case forward filling seems to work better
- The results are of course application-dependent

Let's have a close look at forward filling around some of the missing values

```
In [10]: idx, pad = 0, 20
         nab.plot series(data1.iloc[mv starts[idx]-pad:mv starts[idx]+mv num+pad+1], figsize=figsize)
         plt.plot(ffseries.iloc[mv starts[idx]-1:mv starts[idx]+idx+2]);
          70
          60
          50
          30
          20
          10
```

■ This is the first (and shortest) gap

Let's have a close look at forward filling around some of the missing values

```
In [11]: idx, pad = mv num / / 2, 20
         nab.plot series(data1.iloc[mv starts[idx]-pad:mv starts[idx]+mv num+pad+1], figsize=figsize)
         plt.plot(ffseries.iloc[mv_starts[idx]-1:mv_starts[idx]+idx+2]);
          30
          20
```

■ This is an intermediate-length gap

Let's have a close look at forward filling around some of the missing values

```
In [12]: | idx, pad = mv_num-1, 20
         nab.plot series(data1.iloc[mv starts[idx]-pad:mv starts[idx]+mv num+pad+1], figsize=figsize)
         plt.plot(ffseries.iloc[mv_starts[idx]-1:mv_starts[idx]+idx+2]);
          70
          60
          50
           40
          30
          20
          10
```

■ This is the longest gap

Forward/Backward Filling on the Traffic Data

Let's now consider the traffic data

We will limit ourselves to forward filling:

```
In [13]: ddata2 = data2.resample('5min').mean()
    ddata2_ff = ddata2.fillna(method='ffill')
```

data2 contains the traffic series

We now isolate the filled values

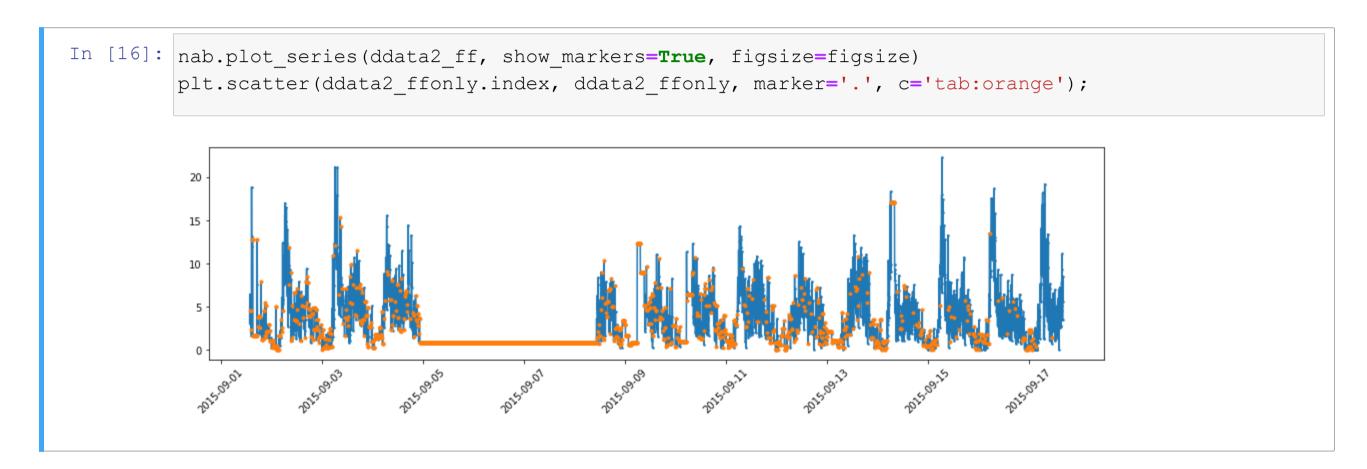
This is needed so that we can highlight them in the forthcoming plots

```
In [14]: ddata2_ffonly = ddata2_ff.copy()
    ddata2_ffonly[~ddata2['value'].isnull()] = np.nan
```

ffseries and bfseries now contain only the filled values

Forward/Backward Filling on the Traffic Data

Let us have a look at the results of forward filling:



Forward/Backward Filling on the Traffic Data

Forward filling works reasonably for small gaps

```
In [17]: mask = (ddata2_ff.index >= '2015-09-02 01:00') & (ddata2_ff.index < '2015-09-03 00:00')</pre>
          nab.plot series(ddata2 ff[mask], show markers=True, figsize=figsize)
          plt.scatter(ddata2_ffonly.index[mask], ddata2_ffonly[mask], marker='.', c='tab:orange');
           17.5
           15.0
           12.5
           10.0
           7.5
           5.0
           2.5
```

Forward/Backward Filling with our Series

...But it is not particularly effective for larger gaps

```
In [18]: mask = (ddata2_ff.index >= '2015-09-08 18:00') & (ddata2_ff.index < '2015-09-09 18:00')</pre>
         nab.plot series(ddata2 ff[mask], show markers=True, figsize=figsize)
         plt.scatter(ddata2_ffonly.index[mask], ddata2_ffonly[mask], marker='.', c='tab:orange');
          12
          10
```

(Geometric) Interpolation

A few more options are available via the interpolate method

```
DataFrame/Series.interpolate(method='linear', ...)
```

The method parameter determines how NaNs are filled:

- "linear" uses a linear interpolation, assuming uniformly spaced samples
- "time" uses a linear interpolation, but supports non-uniformly spaced samples
- "nearest" uses the closest value
- "polynomial" uses a polynomial interpolation
- Even "ffill" and "bfill" are available

Both "polynomial" and "spline" require to specify the additional parameter order

■ E.g. df.interpolate(method='polynomial', order='3')

(Geometric) Interpolation

Let us check the performance of some approaches

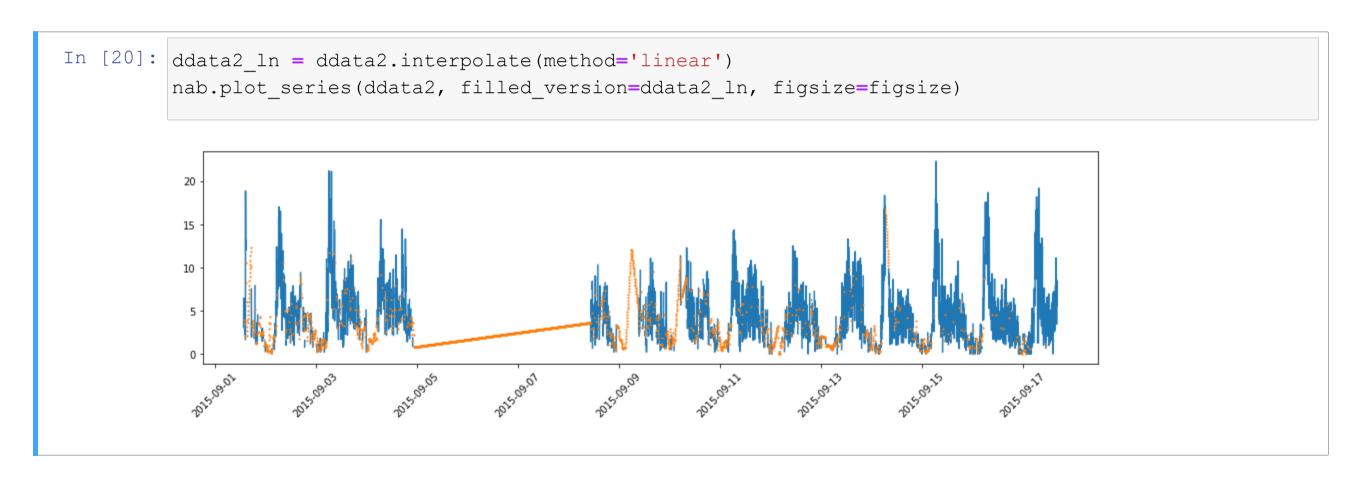
- "linear" and "time" are equivalent in this case (we have uniformly-spaced samples)
- "polynomial" is the most complex, and in this case also the worst

All perform worse than forward filling (at least in this case)!

Curve Interpolation on Traffic Data

On real data, we cannot (easily) compare interpolation methods

- This is because typically we have no ground truth
- For now, we will settle for a visual inspection



Considerations

All these methods for dealing with missing values:

- Work ok for small gaps, but loose effectiveness as the gap size grows
- This is true even for the more advanced filling methods!
- Better methods just degrade a bit more slowly

MSE comparisons can be very effective:

- But requires access to ground truth!
- An idea: make your ground truth by artificially removing values
- ...Then comparing filling methods based on their performance on the artificial gaps

MSE is not everything

- Every filling method makes mistakes: it's important not to make the wrong ones
- Think about how you plan to use your (filled) time series
- Can you expect the series to have uniform variance?