

UNIVERSITY OF OTTAWA

DOCTORAL THESIS

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## A doctoral thesis title

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*A thesis submitted in fulfillment of the requirements  
for the degree of Doctor of Philosophy*

*in the*

Informatics Program  
Department of Mathematics



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- I have acknowledged all main sources of help.
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*“Thanks to my solid academic training, today I can write hundreds of words on virtually any topic without possessing a shred of information, which is how I got a good job in journalism.”*

Dave Barry



UNIVERSITY OF OTTAWA

*Abstract*

Applied Math Group  
Department of Mathematics

Doctor of Philosophy

**A doctoral thesis title**

by Lona Frießner

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## *Acknowledgements*

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# List of Abbreviations

**LAH** List Abbreviations Here  
**WSF** What (it) Stands For



# List of Symbols

$a$	distance	m
$P$	power	W (J s <sup>-1</sup> )
$\omega$	angular frequency	rad



*For Elsa*



## Chapter 1

# Introduction



## Chapter 2

# Methods

### 2.1 Data generation

A simulation study was conducted to compare the methods of missing data handling.  
(erklären, was eine Simulationsstudie ist)

Data was generated from a parametric model with known parameters.

### 2.2 Data-generating model

The data-generating model was a two-level random intercept model:

$$Y_{ij} = \dots \quad (2.1)$$

First,

### 2.3 Missing data generation

### 2.4 Factors and simulation conditions

#### 2.4.1 Constants

#### 2.4.2 Level-2 sample size

As the small-sample performance of the methods is of interest, three different group sizes are used: - N2 = 15 - N2 = 30 - N2 = 60 These sizes are chosen to reflect McNeish's (2017) summary, that group sizes below 25 almost certainly face issues and below 50 there is a susceptibility to small sample biases. These ranges should therefore cover problematic, likely problematic and not problematic level-2 sample sizes. ### Effect size of the group-level effect { 01 } The effect size of the group-level effect of X is varied between 0.0 and 0.30. This is to investigate the performance both with a null effect of the parameter of interest as well as a substantive effect.

#### 2.4.3 ICC of X and residual Y

#### 2.4.4 Missing data mechanism

Missing data mechanism is set to either MCAR or MAR. For MAR, the strength of relationship between W and missing of X is set to 0.4, which corresponds to 0.4^2 % 100% explanation of variance in missingness through W.



## Chapter 3

# Methods

### 3.1 Estimands

### 3.2 Performance measures

### 3.3 Execution of simulation