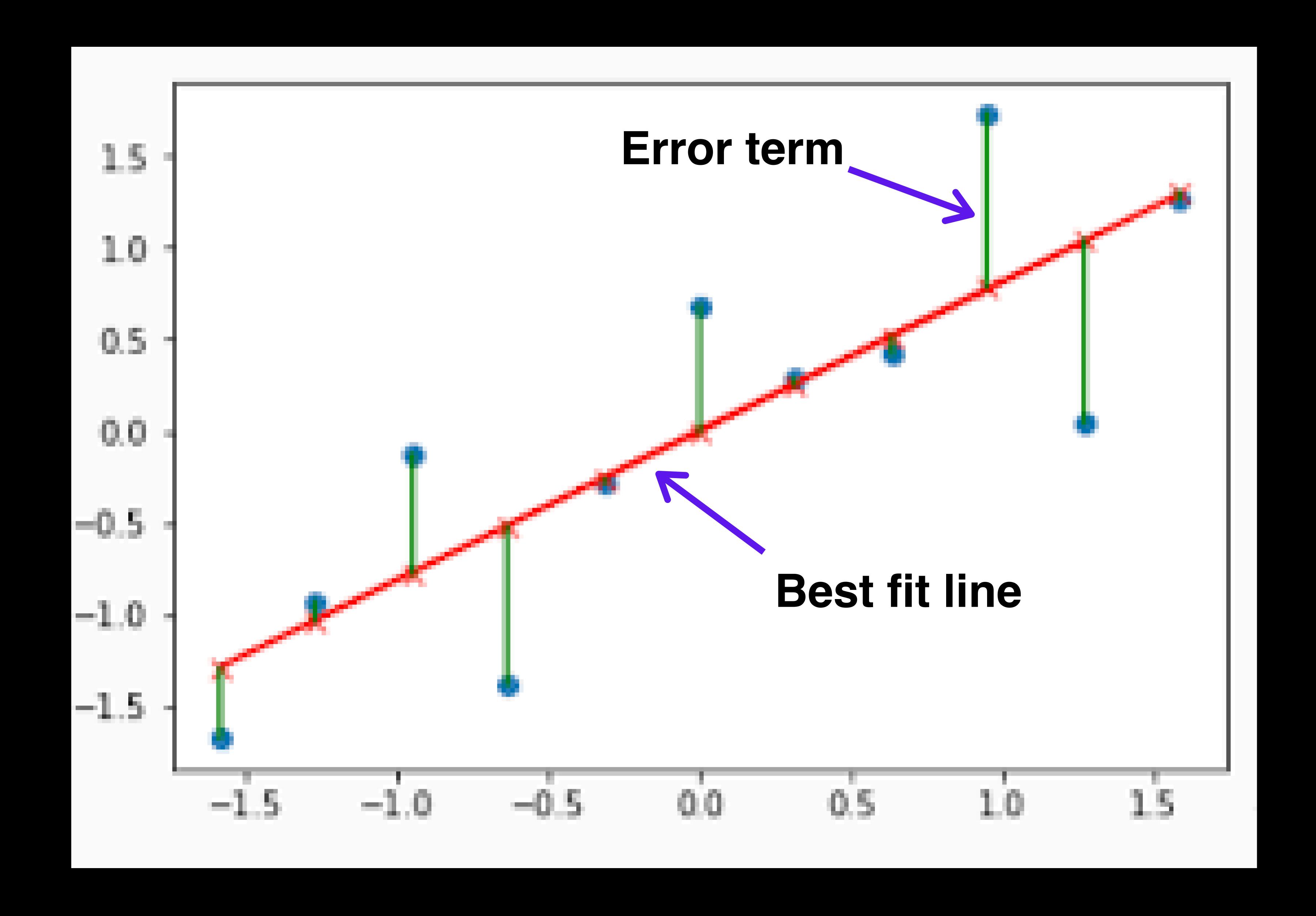
# What is Linear Regression?

This algorithm is used to find the relationship between 2 continuous variables (one independent variable and one dependent variable)

Linear regression is a linear model, e.g. a model that assumes a linear relationship between the input variables (x) and the single output variable (y). More specifically, y can be calculated from a linear combination of the input variables (x).

The equation is Y= W1\*X+b (for one input variable) where,

- Y = Dependent variable
- W1 = Gradient/slope/Weight
- X = Independent variable
- b = Bias



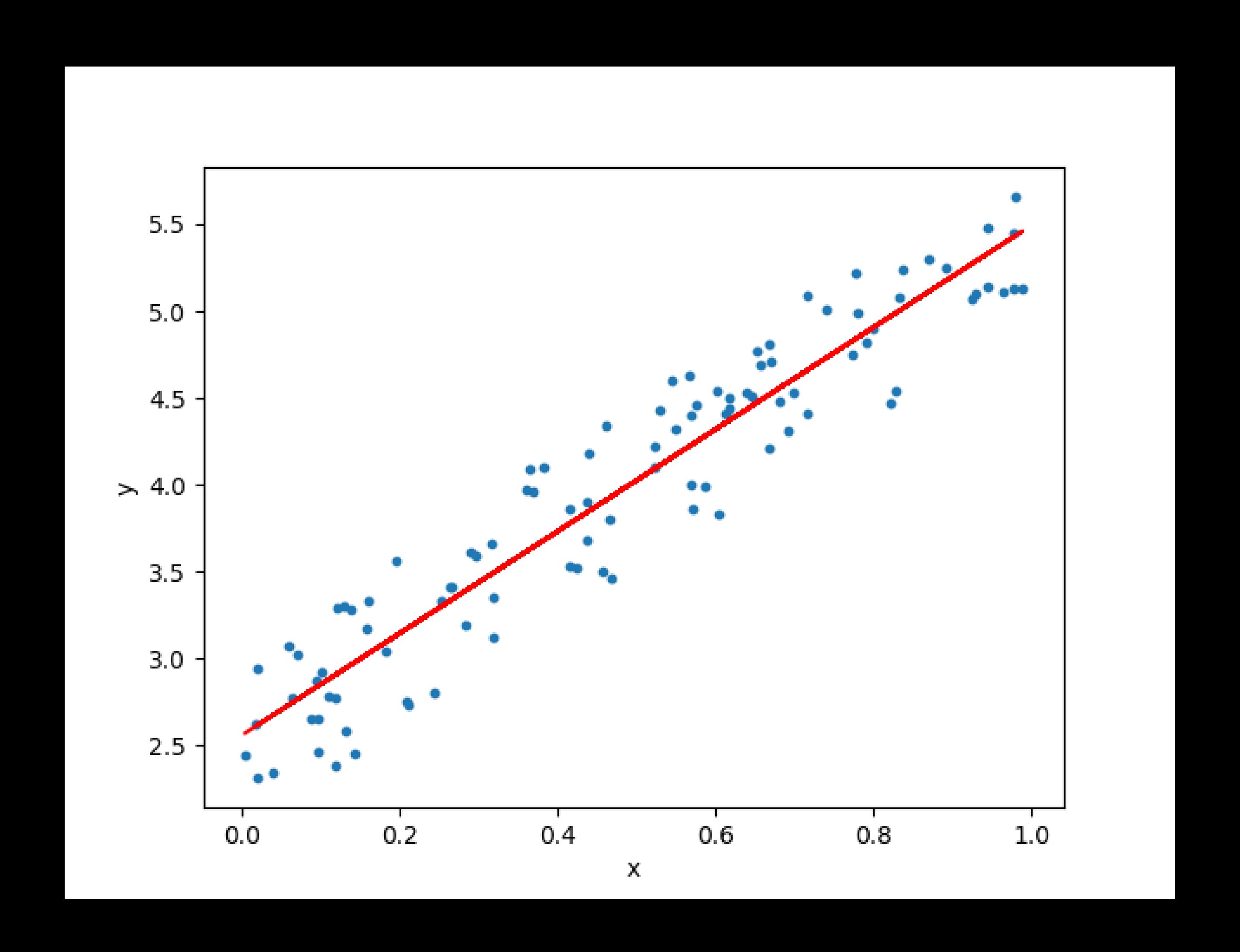
The equation Y = W1\*X+b is the same as that of a straight line (Y = MX+c)

The core idea is to obtain a line that best fits the data to which we get low prediction error. Error is the distance between the point to the best fit line.

The values m and b must be chosen in a way that minimizes the error rate.

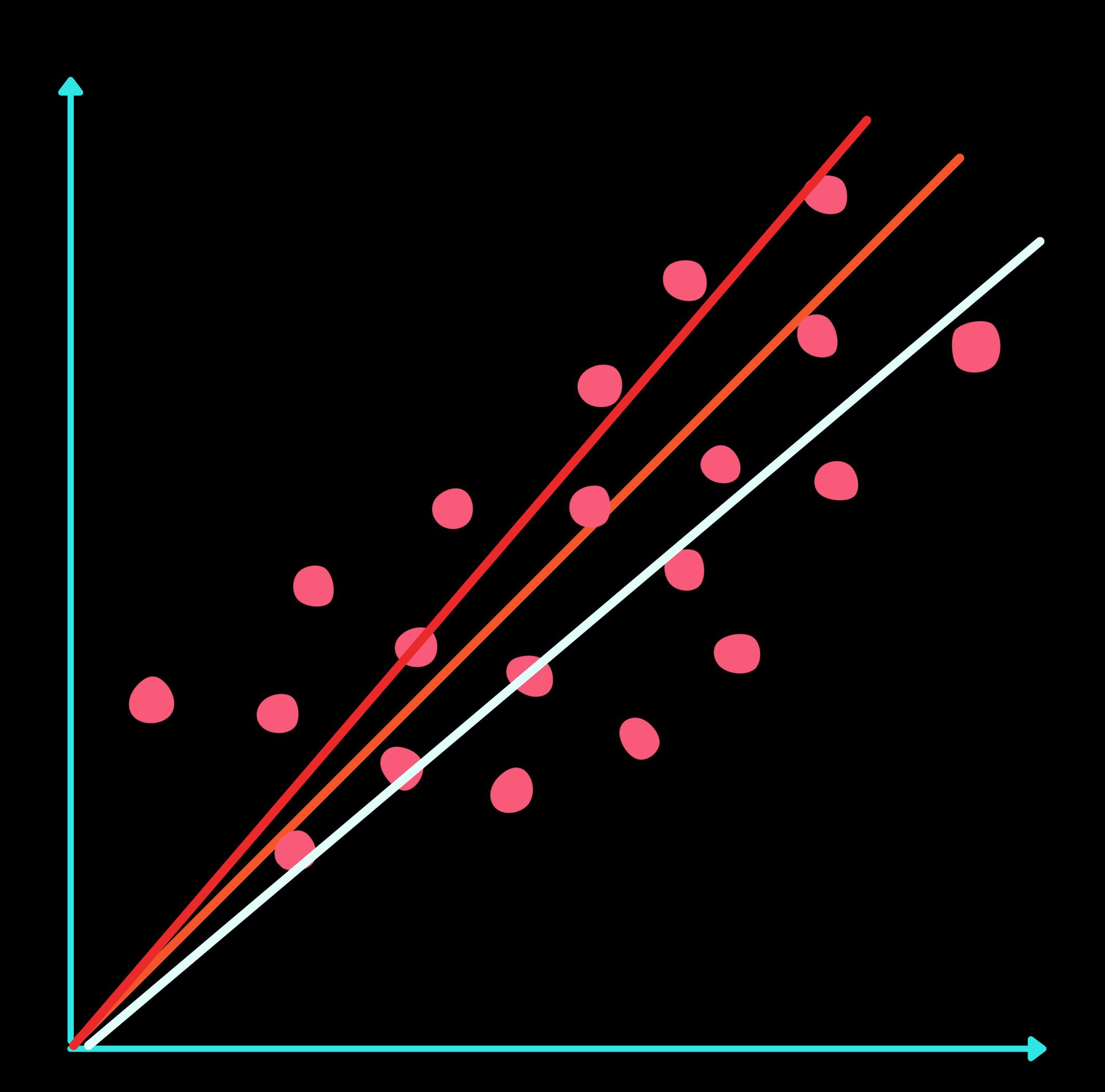
If the sum of squared errors ( $\Sigma(Y - Y)^2$ ) is taken as a metric to evaluate the model, the goal to obtain a line that gives the low error value.

We can train this algorithm using multiple methods, we can use the ordinary least squares method to calculate m and b or we can also use gradient descent to do that.



Goal is to find that red straight line (which is best fit) to the data. First lets talk about how to draw a linear line in the graph, In math we have an equation which is called linear equation y = mX+b

- m = slope,
- b = Y-intercept



so how can we calculate m and b values? and how do we know exact m and b values for the best fit line??

We take some random values of m and b and by taking all the X values we will find the Y values and we drew line with those Y values. We do this until we find the best fit line with low error value.

How do we change m and b values for the best fit line?? • Either we can use an algorithm called Gradient Descent Or we can use direct formulas from statistics. Let's first use the statistics formulas then we can go to GD.

$$m=rac{\sum\limits_{i=1}^{n}(x_{i}-\overline{X})(y_{i}-\overline{Y})}{\sum\limits_{i=1}^{n}(x_{i}-\overline{X})^{2}}$$
  $oldsymbol{b}=oldsymbol{ar{Y}}-oldsymbol{m}oldsymbol{ar{X}}$ 

$$m=rac{\sum\limits_{i=1}^{n}(x_{i}-\overline{X})(y_{i}-\overline{Y})}{\sum\limits_{i=1}^{n}(x_{i}-\overline{X})^{2}}$$
  $oldsymbol{b}=oldsymbol{ar{Y}}-oldsymbol{m}oldsymbol{ar{X}}$ 

Here x is the mean of all the values in the input X and y is the mean of all the values in the desired output Y. This is the Least Squares method.

And for prediction we just use the formula Y = mX + b and use the m and b values which we got from the above formula.



If you have any questions, please do let us know in the comments.



