

## SYMMETRY RESULTS FOR CAFFARELLI-KOHN-NIRENBERG INEQUALITIES

The *Caffarelli-Kohn-Nirenberg inequalities* in space dimension  $N \geq 2$  can be written as

$$\left( \int_{\mathbb{R}^N} \frac{|w(x)|^p}{|x|^{bp}} dx \right)^{2/p} \leq C_{a,b}^N \int_{\mathbb{R}^N} \frac{|\nabla w(x)|^2}{|x|^{2a}} dx$$

for suitable parameters  $a, b, p$ . This talk is concerned with new symmetry results for the extremals of these inequalities in a range of parameters for which no explicit results of symmetry have previously been known. The method proceeds via spectral estimates. This is joint work with Jean Dolbeault and Maria Esteban.