O O ... atb

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	$D_{n} = (a+b)D_{n-1} - \alpha \qquad b  a  o  \cdots  O$ $\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	$ = (a+b) D_{n+} - ab D_{n-2} $ $ D_{n-} aD_{n+} = b (D_{n+} - aD_{n-2})  D_{n-} bD_{n+} = a (D_{n-1} - bD_{n-2})  D_{1} = a+b  D_{2} = \alpha^{2} + a $ $ D_{n-} aD_{n+} = b^{n-2} (D_{2} - aD_{1}) = b^{n}  D_{n-} bD_{n+} = a^{n-2} (D_{2} - bD_{1}) = a^{n} $ $ \Rightarrow  \exists a \neq b ,  D_{n} = \frac{a^{n} b - b^{n+1}}{a - b}  ;  \exists a = b  ,  D_{n} = (n+1) a^{n} $ $ n = 1, 2                                  $
4.	$D_{n} = \begin{bmatrix} 1+\alpha_{1} & 1 & \dots & 1 \\ 1 & 1+\alpha_{2} & 1 \\ \vdots & \ddots & \vdots \\ 1 & \dots & 1+\alpha_{n} \end{bmatrix}$
	若 $0:$ 中至少有两个为零 ,则 $Dn = O$ (有两行相同) 若 $a:$ 中至多有一个为零 $/$ 不妨设 $O_1$ , , $O_{n-1}$ 均不为零 $D_n = \begin{vmatrix} O_1 & O & \cdots & O & -\Delta n \\ O & O_2 & \cdots & O & -\Delta n \\ \vdots & \vdots & \ddots & \vdots \\ O & O & \cdots & O & -\Delta n \\ \vdots & \vdots & \ddots & \vdots \\ O & O & \cdots & I & -\Delta n \\ O$
	$= \alpha_1 \alpha_2 \cdots \alpha_{n-1}  0  1 \cdots 0  -\frac{\alpha_n}{\alpha_2}$ $\vdots$ $0  0 \cdots 1  -\frac{\alpha_n}{\alpha_{n-1}}$ $0  0 \cdots 0  1 + \frac{\alpha_n}{\alpha_1} + \frac{\alpha_n}{\alpha_2} + \cdots + \frac{\alpha_n}{\alpha_{n-1}}$
	$= \alpha_1 \alpha_2 \cdots \alpha_{n-1} \cdot (-1)^{n+n} \left( 1 + \alpha_n t \frac{\alpha_n}{\alpha_1} + \cdots + \frac{\alpha_n}{\alpha_{n-1}} \right)$ $= \alpha_1 \cdots \alpha_{n-1} \left( 1 + \alpha_n t + \frac{\alpha_n}{\alpha_1} + \cdots + \frac{\alpha_n}{\alpha_{n-1}} \right)$ $\stackrel{\text{\( \lambda}}{=} \alpha_n \dots \alpha_n \dots \alpha_n \dots \alpha_n \dots \d$

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	5. $\begin{vmatrix} x & y & y & \cdots & y & y \\ y & z & z & x & y & \cdots & y & y \\ z & z & x & y & \cdots & y & y \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ z & z & z & \cdots & z & x \end{vmatrix} $
	法一 当 h≥ 2  Dn =
	$= \begin{vmatrix} x & y & y & \dots & y & 0 \\ z & x & y & \dots & y & 0 \\ z & z & x & \dots & y & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ z & z & z & \dots & z & x - y \end{vmatrix} + \begin{vmatrix} x & y & y & \dots & y & y \\ z & x & y & \dots & y & y \\ z & z & x & \dots & y & y \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ z & z & z & \dots & z & y \end{vmatrix}$ $= (x-y) D_{n+1} + \begin{vmatrix} x-z & y+x & 0 & \dots & 0 & 0 \\ x-z & y+x & 0 & \dots & 0 & 0 \end{vmatrix}$
	$= (x-y) p_{n-1} + \begin{vmatrix} x-2 & y-x & 0 & \cdots & 0 & 0 \\ 0 & x-2 & y-x & \cdots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \cdots & x-2 & 0 \\ z & z & z & \cdots & z & y \end{vmatrix}$ $= (x-y) p_{n-1} + (-1)^{n+n} y \cdot [x-z)^{n-1}$ $= (x-y) p_{n-1} + y (x-z)^{n-1}$
	由   A   =   A T   , 对 A T 用上述结论 , 得 Dn = (x-z) Dn-1 + Z (x-y) <sup>n+1</sup> 联立解得 Dn = \frac{y(x-z)^n-z(x-y)^n}{y-z}  n=  , 经过验证 , 上式同样成立
	法二 (感谢万骐滔同学提供的解答)  Dn =
	$= (x-y) D_{n-1} + (x-z) \cdot \begin{vmatrix} 0 & 0 & \cdots & 0 & y \\ z-x & x-y & \cdots & 0 & y \\ 0 & 0 & \cdots & 0 & y \\ \vdots & & & \vdots \\ 0 & 0 & \cdots & z-x & x \end{vmatrix}$
-	= (X-y) D <sub>n-1</sub> + (x-z)·(-1) 1+h+ · y·(z-x) <sup>n-2</sup> = (x-y) D <sub>n-1</sub> + y·(X-z) <sup>n-1</sup> 后同法—

法三	(感谢李-轲同学提供的解答)
. 1	(前同法一) 石更解数列通项: Dn=(X-Y)Dn+Y(X-Z)*-1 D1=X
	<b>这是一个一阶非齐次线性递推</b>
	齐次遂推 (Dn=(X-Y) Dn-1) 通解形式为 Dn→= C(xy,z) (X-Y)n-1
	非齐次递推 (Dn=(X-Y)Dn+Y(X-Z)n+) 有特解形如 Dn=K(X)XZ
	代回得 K(X-2) <sup>n-1</sup> = (X-y) K (X-2) <sup>n-2</sup> + Y (X-2) <sup>n-1</sup>
	K (X-Z) = (X-Y) K + Y (不妨设 X≠Z)
	$K = \frac{y(x-z)}{y-z}$
	$\Rightarrow D_n = D_n^{(p)} + D_n^{(h)} = C (x-y)^m + \frac{y(x-z)}{y-z} \cdot (x-z)^{n-1}$
	$D_1 = X \Rightarrow C = \frac{2(y-x)}{x-y}$
	故 $D_n = \frac{y(x-z)^n - z(x-y)^n}{y-z}$
	7-2
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