

George Gabricht
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ICS 46 - HW 9 Report

1) Code Implementation

```
12 // O(|E + V| log V)
13 void dijkstras(Graph & g, int src, int * dist, int * prv) {
14     dist[src] = 0; // 1
15     int num_vertex = g.numVert(); // 1
16     PriorityQueue<vNode> pq(num_vertex); // 1
17     // Total = V log V
18     for (int ndx = 0; ndx < num_vertex; ndx++) { // V
19         if (ndx != src) { // 1
20             dist[ndx] = INT_MAX; // 1
21         }
22         prv[ndx] = UNDF; // 1
23         vNode newNode(ndx, dist[ndx]); // 1
24         pq.enqueue(newNode); // log V
25     }
26     while (!pq.isEmpty()) { // V -> e*V = E since all edges from each vertex = Edges E
27         vNode curNode = pq.dequeue(); // log V
28         Vertex curVert = g.getVert()[curNode.vertex]; // 1
29         for (Edge eg : curVert.getEdges()) { // e = # edges in vertex
30             int newWeight; // 1
31             if (curNode.weightSum == INT_MAX) { // 1
32                 newWeight = eg.getWeight(); // 1
33             } else {
34                 newWeight = curNode.weightSum + eg.getWeight(); // 1
35             }
36             if (newWeight < dist[eg.getDst()]) { // 1
37                 dist[eg.getDst()] = newWeight; // 1
38                 prv[eg.getDst()] = curNode.vertex; // 1
39                 vNode newNode(eg.getDst(), newWeight); // 1
40                 pq.enqueue(newNode); // log V
41             }
42         }
43     }
44 }
45 }

46 struct vNode {
47     int vertex, weightSum;
48     vNode() : vertex(UNDF), weightSum(INT_MAX) {}
49     vNode(int v, int sum) : vertex(v), weightSum(sum) {}
50 }
```

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```
int getKey() {
    return vertex;
}
int getVal() {
    return weightSum;
}
};

74 // O(log N)
75 void PriorityQueue<vNode>::insert(Type val) {
76     if (isFull()) { // 1
77         cerr << "Error, Priority Queue is Full!" << endl;
78         return;
79     }
80     values[size] = val; // 1
81     ndxs[val.getKey()] = size; // 1
82     PriorityQueue<Type>::siftUp(size++); // log N
83 }
84
85
86 // O(log N)
87 Type extractMin() {
88     if (isEmpty()) { // 1
89         cerr << "Could not extract min! Priority Queue is Empty!" << endl; // 1
90         return Type(); // 1
91     }
92     Type min = values[ROOT]; // 1
93     ndxs[values[ROOT].getKey()] = UNDF; // 1
94     values[ROOT] = values[-size]; // 1
95     PriorityQueue<Type>::heapify(ROOT); // log N
96     return min; // 1
97 }
98
99
100
101 // O(log N)
102 void decreaseKey(int ndx, Type val) {
103     ndxs[val.getKey()] = ndx; // 1
104     values[ndx] = val; // 1
105     PriorityQueue<Type>::siftUp(ndx); // log N
106 }
107
108 // O(log N)
109 void siftUp(int ndx) {
110     int parNdx = parent(ndx); // 1
111     for (int curNdx = ndx; curNdx > 0; curNdx = parNdx, parNdx = parent(curNdx)) { // log N
112         if (values[curNdx].getVal() > values[parNdx].getVal()) { // 1
113             break; // 1
114         }
115     }
116     swap(curNdx, parNdx); // 1
117     std::swap(ndxs[values[curNdx].getKey()], ndxs[values[parNdx].getKey()]); // 1
118 }
119 }
120 }
```

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```
122 // O(log N)
123 void heapify(int ndx) {
124     int min = ndx; // 1
125     int left = leftChild(ndx); // 1
126     int right = rightChild(ndx); // 1
127     if (left < size && values[left].getVal() < values[min].getVal()) { // 1
128         min = left; // 1
129     }
130     if (right < size && values[right].getVal() < values[min].getVal()) { // 1
131         min = right; // 1
132     }
133     if (min != ndx) { // 1
134         PriorityQueue<Type>::swap(min, ndx); // 1
135         std::swap(ndxs[values[min].getKey()], ndxs[values[ndx].getKey()]); // 1
136         PriorityQueue<Type>::heapify(min); // log N
137     }
138 }
139
140
141 }

179 // O(log N)
180 void enqueue(Type newVal) {
181     int ndx = ndxs[newVal.getKey()]; // 1
182     if (ndx > UNDF) { // 1
183         PriorityQueue<Type>::decreaseKey(ndx, newVal); // log N
184         return; // 1
185     }
186     PriorityQueue<Type>::insert(newVal); // log N
187 }
188 }

189
190 // O(log N)
191 Type dequeue() {
192     return PriorityQueue<Type>::extractMin(); // log N
193 }
194 }

195
196 // O(1)
197 Type peek() {
198     return values[ROOT]; // 1
199 }
200

201 // O(N)
202 void print(ostream & out) {
203     out << "PQ: " << endl; // 1
204     for (int ndx = 0; ndx < size; ndx++) { // N
205         out << "Ndx: " << ndx << "\tVal: " << values[ndx].getKey(); // 1
206         out << "\t" << values[ndx].getVal() << endl; // 1
207     }
208     out << endl; // 1
209 }

100 // O(V + E)
```

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```
101     Graph(string file_name)
102     : num_vertex(0), num_edge(0) {
103         ifstream iFile(file_name); // 1
104         if (!iFile.is_open()) { // 1
105             cerr << "File could not be opened! Goodbye!" << endl;
106             exit(-1);
107         }
108         string curLine; // 1
109         getline(iFile, curLine); // 1
110         num_vertex = stoi(curLine); // 1
111         vertices = new Vertex[num_vertex]; // 1
112         for (int ndx = 0; ndx < num_vertex; ndx++) { // V
113             vertices[ndx] = Vertex(ndx); // 1
114         }
115         while (getline(iFile, curLine)) { // E
116             int src, dst, weight; // 1
117             istringstream strm(curLine); // 1
118             strm >> src; // 1
119             strm >> dst; // 1
120             strm >> weight; // 1
121             add_edge(src, dst, weight); // 1
122         }
123         iFile.close(); // 1
124     }

125     // O(1)
126     void add_edge(int src, int dst, int weight) {
127         const Edge eg(src, dst, weight); // 1
128         vertices[src].add_edge(eg); // 1
129         edges.push_back(eg); // 1
130         num_edge++; // 1
131     }
132 }
```

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Test Run Outputs

```
ggabrich@andromeda-17 23:35:48 ~/ics46/hw/ggabrich_hw9
$ make
echo -----compiling testMain.cpp to create executable program dijkstras-----
-----compiling testMain.cpp to create executable program dijkstras-----
g++ -ggdb -std=c++11 -fPIC -Wall -Wextra -Werror -Wno-null-pointer-constant testMain.cpp -o dijkstras
ggabrich@andromeda-17 00:27:15 ~/ics46/hw/ggabrich_hw9
$ valgrind dijkstras 0 small.graph.txt
==13627== Memcheck, a memory error detector
==13627== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==13627== Using Valgrind-3.13.0 and LibVEX; rerun with -h for copyright info
==13627== Command: dijkstras 0 small.graph.txt
==13627==
Results for Shortest Path Single Source from Vertex: 0
0 [ 0 ] ( 0 )
1 [ 0-1 ] ( 19 )
2 [ 0-2 ] ( 14 )
3 [ 0-2-3 ] ( 18 )
4 [ 0-2-3-4 ] ( 38 )
==13627==
==13627== HEAP SUMMARY:
==13627==     in use at exit: 0 bytes in 0 blocks
==13627==   total heap usage: 44 allocs, 44 frees, 82,688 bytes allocated
==13627==
==13627== All heap blocks were freed -- no leaks are possible
==13627==
==13627== For counts of detected and suppressed errors, rerun with: -v
==13627== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
ggabrich@andromeda-17 00:27:47 ~/ics46/hw/ggabrich_hw9
$ valgrind dijkstras 0 large.graph.txt
==13646== Memcheck, a memory error detector
==13646== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==13646== Using Valgrind-3.13.0 and LibVEX; rerun with -h for copyright info
==13646== Command: dijkstras 0 large.graph.txt
==13646==
Results for Shortest Path Single Source from Vertex: 0
0 [ 0 ] ( 0 )
1 [ 0-1 ] ( 1 )
2 [ 0-2 ] ( 3 )
3 [ 0-3 ] ( 6 )
4 [ 0-4 ] ( 4 )
5 [ 0-5 ] ( 8 )
6 [ 0-2-5 ] ( 9 )
7 [ 0-3-7 ] ( 8 )
8 [ 0-3-7-8 ] ( 16 )
9 [ 0-3-7-9 ] ( 15 )
10 [ 0-3-7-10 ] ( 13 )
11 [ 0-3-7-11 ] ( 18 )
12 [ 0-3-7-11-12 ] ( 17 )
13 [ 0-3-7-9-13 ] ( 21 )
14 [ 0-3-7-11-16 ] ( 12 )
15 [ 0-3-7-8-12-15 ] ( 23 )
16 [ 0-3-7-11-14-13 ] ( 13 )
17 [ 0-3-7-11-14-16-17 ] ( 18 )
18 [ 0-3-7-11-14-16-18 ] ( 22 )
19 [ 0-3-7-11-14-16-19 ] ( 19 )
20 [ 0-3-7-11-14-16-20 ] ( 21 )
21 [ 0-3-7-11-16-16-20-21 ] ( 23 )
22 [ 0-3-7-11-14-16-20-22 ] ( 35 )
23 [ 0-3-7-11-14-16-19-23 ] ( 28 )
24 [ 0-3-7-11-14-16-20-24 ] ( 36 )
25 [ 0-3-7-11-14-16-20-21-25 ] ( 38 )
26 [ 0-3-7-11-14-16-19-23-26 ] ( 33 )
27 [ 0-3-7-11-14-16-19-23-26-27 ] ( 34 )


```

```
96 [ 27-31-36-37-39-45-47-51-55-56-59-63-67-70-73-75-78-80-84-87-89-92-94-96 ] ( 85 )
97 [ 27-31-36-37-39-42-47-51-55-56-59-63-67-69-73-75-78-80-84-87-90-92-94-96-97 ] ( 84 )
98 [ 27-31-34-37-39-43-47-51-55-56-59-63-67-69-73-75-78-80-84-87-91-95-98 ] ( 84 )
99 [ 27-31-34-37-39-43-47-51-55-56-59-63-67-69-73-75-78-80-84-87-91-95-98-99 ] ( 87 )
==13656== HEAP SUMMARY:
==13656==     in use at exit: 0 bytes in 0 blocks
==13656==   total heap usage: 1,070 allocs, 1,070 frees, 135,804 bytes allocated
==13656==
==13656== All heap blocks were freed -- no leaks are possible
==13656==
==13656== For counts of detected and suppressed errors, rerun with: -v
==13656== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
ggabrich@andromeda-17 00:28:15 ~/ics46/hw/ggabrich_hw9
$ genGraph > rdm.graph.txt
ggabrich@andromeda-17 00:28:29 ~/ics46/hw/ggabrich_hw9
$ valgrind dijkstras rdm.graph.txt
==13679== Memcheck, a memory error detector
==13679== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==13679== Using Valgrind-3.13.0 and LibVEX; rerun with -h for copyright info
==13679== Command: dijkstras 0 rdm.graph.txt
==13679==
Results for Shortest Path Single Source from Vertex: 0
0 [ 0 ] ( 0 )
1 [ 0-1 ] ( 3 )
2 [ 0-2 ] ( 14 )
3 [ 0-3 ] ( 4 )
4 [ 0-4 ] ( 4 )
5 [ 0-4-5 ] ( 12 )
6 [ 0-5-6 ] ( 6 )
7 [ 0-6-7 ] ( 18 )
8 [ 0-7-8 ] ( 12 )
9 [ 0-4-7-9 ] ( 12 )
10 [ 0-3-6-10 ] ( 14 )
11 [ 0-4-7-11 ] ( 15 )
12 [ 0-4-7-11-12 ] ( 18 )
13 [ 0-3-6-10-13 ] ( 18 )
14 [ 0-3-6-10-14 ] ( 16 )
15 [ 0-3-6-10-15 ] ( 24 )
16 [ 0-3-6-10-15-16 ] ( 20 )
17 [ 0-3-6-10-14-17 ] ( 20 )
18 [ 0-3-6-10-13-16-18 ] ( 24 )
19 [ 0-3-6-10-13-16-19 ] ( 26 )
20 [ 0-3-6-10-14-17 ] ( 24 )
21 [ 0-3-6-10-13-16-17-21 ] ( 28 )
22 [ 0-3-6-10-14-17-21 ] ( 27 )
23 [ 0-3-6-10-13-16-19-23 ] ( 27 )
24 [ 0-3-6-10-14-17-20-24 ] ( 27 )
25 [ 0-3-6-10-13-16-19-22-25 ] ( 39 )
26 [ 0-3-6-10-14-17-20-24-26 ] ( 33 )
27 [ 0-3-6-10-14-17-20-24-27 ] ( 32 )
28 [ 0-3-6-10-14-17-20-24-28 ] ( 35 )
29 [ 0-3-6-10-14-17-20-24-27-30 ] ( 33 )
30 [ 0-3-6-10-14-17-20-24-28-38 ] ( 48 )
31 [ 0-3-6-10-14-17-20-24-27-31 ] ( 35 )
32 [ 0-3-6-10-14-17-20-24-27-29-32 ] ( 36 )
33 [ 0-3-6-10-14-17-20-24-27-31-33 ] ( 38 )
34 [ 0-3-6-10-14-17-20-24-27-31-34 ] ( 46 )
35 [ 0-3-6-10-14-17-20-24-27-31-35 ] ( 46 )
36 [ 0-3-6-10-14-17-20-24-27-29-32-36 ] ( 39 )
37 [ 0-3-6-10-14-17-20-24-27-29-32-37 ] ( 43 )
38 [ 0-3-6-10-14-17-20-24-27-29-32-36-38 ] ( 57 )
39 [ 0-3-6-10-14-17-20-24-27-31-33-37-39 ] ( 45 )


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[ 9 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 98 ] ( 13 )
[ 9 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 97 - 98 ] ( 22 )
[ 91 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 98 - 91 ] ( 19 )
[ 92 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 99 - 92 ] ( 28 )
[ 93 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 99 - 93 ] ( 29 )
[ 94 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 99 - 92 - 94 ] ( 22 )
[ 95 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 98 - 99 - 100 ] ( 23 )
[ 96 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 99 - 92 - 94 - 96 ] ( 26 )
[ 97 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 99 - 92 - 94 - 97 ] ( 38 )
[ 98 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 88 - 91 - 95 - 98 ] ( 24 )
[ 99 ] [ 0 - 3 - 7 - 11 - 14 - 16 - 19 - 23 - 26 - 29 - 33 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 85 - 89 - 92 - 94 - 96 - 99 ] ( 28 )

==13645==

==13645== HEAP SUMMARY:
==13645==     in use at exit: 0 bytes in 0 blocks
==13645==   total heap usage: 1,857 allocs, 1,857 frees, 135,348 bytes allocated
==13645==

==13645== All heap blocks were freed -- no leaks are possible
==13645==

==13645== For counts of detected and suppressed errors, rerun with: -v
==13645== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
gabrabit@andromeda:~ 00:28:04 ~/ics46/hw/gabrabit_hw9
$ valgrind djikstras 27 large.graph.txt
==13645== Using Valgrind-3.13.0 and LibXt; rerun with -h for copyright info
==13645== Using Valgrind-3.13.0 and LibXt; rerun with -h for copyright info
==13645== Command: djikstras 27 large.graph.txt
==13645==

Results for Shortest Path Single Source from Vertex 27
[ 0 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 0 ] ( 101 )
[ 1 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 1 ] ( 97 )
[ 2 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 ] ( 93 )
[ 3 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 3 ] ( 96 )
[ 4 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 4 ] ( 94 )
[ 5 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 ] ( 98 )
[ 6 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 6 ] ( 99 )
[ 7 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 7 ] ( 98 )
[ 8 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 4 - 9 ] ( 189 )
[ 9 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 10 ] ( 189 )
[ 10 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 4 - 10 ] ( 185 )
[ 11 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 4 - 11 ] ( 117 )
[ 12 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 4 - 12 ] ( 118 )
[ 13 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 9 ] ( 115 )
[ 14 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 ] ( 16 )
[ 15 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 ] ( 9 )
[ 16 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 ] ( 7 )
[ 17 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 ] ( 1 )
[ 18 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 ] ( 15 )
[ 19 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 ] ( 9 )
[ 20 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 21 ] ( 18 )
[ 21 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 21 ] ( 7 )
[ 22 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 21 - 22 ] ( 24 )
[ 23 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 23 ] ( 18 )
[ 24 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 24 ] ( 20 )
[ 25 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 25 ] ( 14 )
[ 26 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 26 ] ( 31 )
[ 27 ] [ 27 - 31 - 34 - 37 - 39 - 43 - 47 - 51 - 55 - 56 - 59 - 63 - 67 - 73 - 75 - 78 - 80 - 84 - 87 - 91 - 95 - 98 - 2 - 5 - 6 - 9 - 13 - 17 - 26 ] ( 31 )
[ 28 ] [ 27 - 28 - 29 ] ( 3 )
[ 29 ] [ 27 - 29 - 1 ] ( 12 )
[ 30 ] [ 27 - 29 - 31 ] ( 17 )
[ 31 ] [ 27 - 31 - 1 ] ( 6 )
[ 32 ] [ 27 - 31 - 32 ] ( 7 )
[ 33 ] [ 27 - 29 - 33 ] ( 13 )
[ 34 ] [ 27 - 31 - 34 ] ( 12 )

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34 [ 27-31-34 ] ( 12 )
35 [ 27-31-32-35 ] ( 12 )
36 [ 27-31-34-37 ] ( 10 )
37 [ 27-31-34-37-38 ] ( 21 )
38 [ 27-31-34-37-38 ] ( 21 )
39 [ 27-31-34-37-39 ] ( 22 )
40 [ 27-31-34-37-40 ] ( 21 )
41 [ 27-31-34-37-41 ] ( 23 )
42 [ 27-31-34-37-41-42 ] ( 25 )
43 [ 27-31-34-37-41-42 ] ( 23 )
44 [ 27-31-34-37-41-42 ] ( 25 )
45 [ 27-31-34-37-39-43-45 ] ( 29 )
46 [ 27-31-34-37-41-42-44 ] ( 29 )
47 [ 27-31-34-37-39-43-47 ] ( 29 )
48 [ 27-31-34-37-40-44-48 ] ( 38 )
49 [ 27-31-34-37-41-42-46-49 ] ( 34 )
50 [ 27-31-34-37-41-42-46-49-50 ] ( 38 )
51 [ 27-31-34-37-41-42-46-49-51 ] ( 36 )
52 [ 27-31-34-37-41-42-46-49-52 ] ( 41 )
53 [ 27-31-34-37-41-42-46-49-53 ] ( 38 )
54 [ 27-31-34-37-41-42-46-49-53-54 ] ( 49 )
55 [ 27-31-34-37-39-43-47-51-55-56 ] ( 35 )
56 [ 27-31-34-37-39-43-47-51-55-56 ] ( 36 )
57 [ 27-31-34-37-41-42-46-49-53-54-57 ] ( 45 )
58 [ 27-31-34-37-39-43-47-51-55-56-58 ] ( 39 )
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