

Given:

The power output of an adiabatic steam turbine is 5 MW. The inlet and the outlet conditions are shown in the figure below.

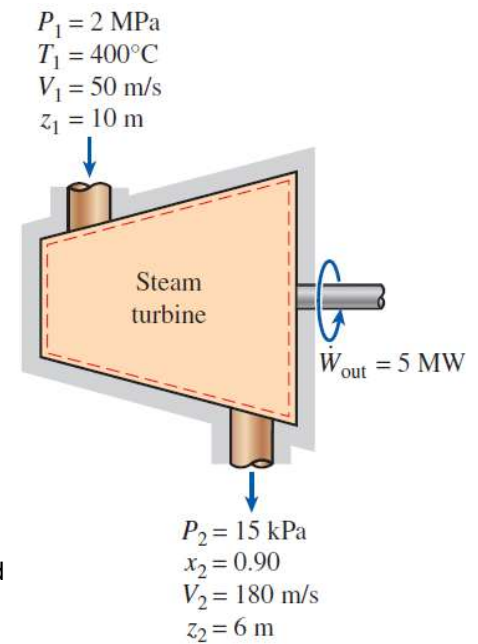
$$\dot{W}'_{out} := 5 \text{ MW}$$

$$P_1 := 2 \text{ MPa} \quad P_2 := 15 \text{ kPa}$$

$$T_1 := 400 \text{ }^\circ\text{C} \quad x_2 := 0.9$$

$$V_1 := 50 \frac{\text{m}}{\text{s}} \quad V_2 := 180 \frac{\text{m}}{\text{s}}$$

$$z_1 := 10 \text{ m} \quad z_2 := 6 \text{ m}$$

**Required:**

Determine

- The changes in specific enthalpy, kinetic energy, and potential energy and
- The mass flow rate of the steam.

Solution:

Going to Table A-5 @ $P := P_1 = 2 \text{ MPa}$ shows that the state is superheated.

Going to Table A-6 @ $P := P_1 = 2 \text{ MPa}$ and $T := T_1 = 400 \text{ }^\circ\text{C}$ shows

$$h_1 := 3248.4 \frac{\text{kJ}}{\text{kg}}$$

Since a quality is given for the outlet, the state is in the two phase region. Going to Table A-5 @ $P := P_2 = 15 \text{ kPa}$ shows

$$h_f := 225.94 \frac{\text{kJ}}{\text{kg}} \quad h_g := 2598.3 \frac{\text{kJ}}{\text{kg}}$$

$$h_2 := h_f + x_2 \cdot (h_g - h_f) = 2361 \frac{\text{kJ}}{\text{kg}}$$

The change in specific enthalpy is then given by

$$\Delta h := h_2 - h_1 = -887.3 \frac{\text{kJ}}{\text{kg}} \quad (\text{a1})$$

The change in specific kinetic energy is given by

$$\Delta ke := \frac{V_2^2 - V_1^2}{2} = 14.95 \frac{\text{kJ}}{\text{kg}} \quad (\text{a2})$$

The change in specific potential energy is given by

$$\Delta pe := g_e \cdot (z_2 - z_1) = -0.03923 \frac{\text{kJ}}{\text{kg}} \quad (\text{a3})$$

Beginning with the 1st Law

$$\frac{d}{dt} E_{sys} = \Sigma E'_{in} - \Sigma E'_{out}$$

For a steady flow device the 1st Law becomes

$$0 = \Sigma E'_{in} - \Sigma E'_{out}$$

Solution (contd.):

For an adiabatic, rigid turbine the expression becomes

$$0 = m'_{in} \cdot \left(h_{in} + \frac{V_{in}^2}{2} + g_e \cdot z_{in} \right) - \dot{W}'_{out} - m'_{out} \cdot \left(h_{out} + \frac{V_{out}^2}{2} + g_e \cdot z_{out} \right)$$

Knowing $m'_{in} = m'_{out}$ and rearranging yields

$$m' = \frac{-\dot{W}'_{out}}{h_{out} - h_{in} + \frac{V_2^2 - V_1^2}{2} + g_e \cdot (z_2 - z_1)}$$

or

$$m' := \frac{-\dot{W}'_{out}}{\Delta h + \Delta ke + \Delta pe} = 5.731 \frac{\text{kg}}{\text{s}}$$

(b)