

**Given and Required:**

Determine the energy necessary to stretch a spring (with a spring constant of  $200 \frac{\text{lbf}}{\text{in}}$ ) 4 inches. Express your answer in BTU.

$$1 \text{ BTU} = 778.169 \text{ ft lbf}$$

**Solution:**

The spring constant is defined as

$$k := 200 \frac{\text{lbf}}{\text{in}}$$

The length for the spring to be stretch is defined as

$$L := 4 \text{ in}$$

The energy necessary to stretch the spring will be determined by the work required to stretch the spring. The work necessary to stretch a spring is given by

$$\bar{W} = \int_1^2 F \, dx$$

where  $F$  is the force applied to the spring and  $dx$  is the distance that the force is applied. The force necessary to stretch the spring is given by Hooke's Law or simple

$$\bar{W} = \int_1^2 kx \, dx$$

The limits of the integral will be from 0 to  $L$  (or 4 in). This is shown below.

$$\bar{W} := \int_0^L k \cdot x \, dx = 1600 \text{ in lbf}$$

Knowing the conversion between Btu and in lbf, the energy required in BTU may be found by a simple unit conversion. However, since this solution is beeing done in Smath Solver, Smath Solver can do it for us.

$$\bar{W} = 0.1713 \text{ BTU}$$