

**Given:**

A 50 kg iron block at 80°C is dropped into an insulated tank that contains 0.5 m<sup>3</sup> of liquid water at 25°C.

$$m_{fe} := 50 \text{ kg} \quad T_{1fe} := 80 \text{ }^{\circ}\text{C} = 353.2 \text{ K} \quad V_w := 0.5 \text{ m}^3 \quad T_{1w} := 25 \text{ }^{\circ}\text{C} = 298.2 \text{ K}$$

**Required:**

Determine the temperature when thermal equilibrium is reached.

**Solution:**

Using the hint given, the following is true.

$$\Delta U_{fe} + \Delta U_w = 0$$

$$m_{fe} \cdot (u_{2fe} - u_{1fe}) + m_w \cdot (u_{2w} - u_{1w}) = 0$$

Assuming the specific heat value of both the iron and water remain constant over the temperature range of this process, the expression becomes

$$m_{fe} \cdot c_{fe} \cdot (T_{2fe} - T_{1fe}) + m_w \cdot c_w \cdot (T_{2w} - T_{1w}) = 0$$

If the final state is in thermal equilibrium, then the final temperature of the iron and water will be the same so

$$T_{2fe} = T_{2w} = T_2 \quad \text{thus} \quad m_{fe} \cdot c_{fe} \cdot (T_2 - T_{1fe}) + m_w \cdot c_w \cdot (T_2 - T_{1w}) = 0$$

Solving for the final temperature yields

$$T_2 = \frac{m_{fe} \cdot c_{fe} \cdot T_{1fe} + m_w \cdot c_w \cdot T_{1w}}{m_{fe} \cdot c_{fe} + m_w \cdot c_w}$$

Assuming the density of water is  $1000 \frac{\text{kg}}{\text{m}^3}$ , the mass of the water may be found by

$$m_w := 1000 \frac{\text{kg}}{\text{m}^3} \cdot V_w = 500 \text{ kg}$$

Going to Table A-3(a) @ water at 25°C shows

$$c_w := 4.18 \cdot \frac{\text{kJ}}{\text{kg K}}$$

Going to Table A-3(b) @ iron shows

$$c_{fe} := 0.45 \cdot \frac{\text{kJ}}{\text{kg K}}$$

The final temperature is then

$$T_2 := \frac{m_{fe} \cdot c_{fe} \cdot T_{1fe} + m_w \cdot c_w \cdot T_{1w}}{m_{fe} \cdot c_{fe} + m_w \cdot c_w} = 298.7 \text{ K}$$

$$T_2 = 25.6 \text{ }^{\circ}\text{C}$$