

Given:

Air is compressed from an initial state of 100 kPa and 17°C to a final state of 600 kPa and 57°C.

$$P_1 := 100 \text{ kPa} \quad T_1 := 17 \text{ }^{\circ}\text{C} \quad P_2 := 600 \text{ kPa} \quad T_2 := 57 \text{ }^{\circ}\text{C}$$

Required:

Determine the entropy change of air during this compression process

- (a) by using the property tables and
- (b) by using an average specific heat.

Solution:

Going to Table A-2(a) @ air shows

$$R_{air} := 0.287 \frac{\text{kJ}}{\text{kg K}}$$

Going to Table A-17 @ $T_1 = 290.2 \text{ K}$ shows that interpolation is needed. This is shown below.

$$\begin{aligned} T_a &:= 290 \text{ K} & T_b &:= 295 \text{ K} \\ s_a^{\circ} &:= 1.66802 \frac{\text{kJ}}{\text{kg K}} & s_b^{\circ} &:= 1.68515 \frac{\text{kJ}}{\text{kg K}} \\ s_1^{\circ} &:= \frac{T_1 - T_a}{T_b - T_a} \cdot (s_b^{\circ} - s_a^{\circ}) + s_a^{\circ} = 1.669 \frac{\text{kJ}}{\text{kg K}} \end{aligned}$$

Going to Table A-17 @ $T_2 = 330.2 \text{ K}$ shows that interpolation is needed. This is shown below.

$$\begin{aligned} T_a &:= 330 \text{ K} & T_b &:= 340 \text{ K} \\ s_a^{\circ} &:= 1.79783 \frac{\text{kJ}}{\text{kg K}} & s_b^{\circ} &:= 1.82790 \frac{\text{kJ}}{\text{kg K}} \\ s_2^{\circ} &:= \frac{T_2 - T_a}{T_b - T_a} \cdot (s_b^{\circ} - s_a^{\circ}) + s_a^{\circ} = 1.798 \frac{\text{kJ}}{\text{kg K}} \end{aligned}$$

The change in entropy is then found by

$$\Delta s_{table} := s_2^{\circ} - s_1^{\circ} - R_{air} \cdot \ln \left(\frac{P_2}{P_1} \right) = -0.3845 \frac{\text{kJ}}{\text{kg K}} \quad (\text{a})$$

The average temperature is found by

$$T_{avg} := \frac{T_1 + T_2}{2} = 310.15 \text{ K}$$

Going to Table A-2(b) @ $T_{avg} = 310.2 \text{ K}$ and air shows that interpolation is needed. This is shown below.

$$\begin{aligned} T_a &:= 300 \text{ K} & T_b &:= 350 \text{ K} \\ c_a &:= 1.005 \frac{\text{kJ}}{\text{kg K}} & c_b &:= 1.008 \frac{\text{kJ}}{\text{kg K}} \\ c_{p,avg} &:= \frac{T_{avg} - T_a}{T_b - T_a} \cdot (c_b - c_a) + c_a = 1.006 \frac{\text{kJ}}{\text{kg K}} \end{aligned}$$

The change in entropy when using an average specific heat value is then found by

$$\Delta s_{avg,cp} := c_{p,avg} \cdot \ln \left(\frac{T_2}{T_1} \right) - R_{air} \cdot \ln \left(\frac{P_2}{P_1} \right) = -0.3844 \frac{\text{kJ}}{\text{kg K}}$$

$$\%diff := \left| \frac{\Delta s_{table} - \Delta s_{avg,cp}}{\Delta s_{table}} \right| = 0.03285 \%$$