

Given:

Air at 100 kPa and 280 K is compressed steadily to 600 kPa and 400 K. The mass flow rate of the air 0.02 kg/s, and a heat loss of 16 kJ/kg occurs during the process.

$$q_{out} := 16 \frac{\text{kJ}}{\text{kg}} \quad m' := 0.02 \frac{\text{kg}}{\text{s}}$$

$$P_1 := 100 \text{ kPa} \quad P_2 := 600 \text{ kPa}$$

$$T_1 := 280 \text{ K} \quad T_2 := 400 \text{ K}$$

Required:

Assuming changes in potential and kinetic energy are negligible, determine the necessary power input to the compressor.

Solution:

Beginning with the 1st Law

$$\frac{d}{dt} E_{sys} = \Sigma E'_{in} - \Sigma E'_{out}$$

For a steady flow device this becomes

$$0 = \Sigma E'_{in} - \Sigma E'_{out}$$

Assuming the compressor is rigid and changes in kinetic and potential energy are negligible, the 1st Law expression becomes

$$0 = \dot{W}'_{in} + m'_{in} \cdot h_{in} - \dot{Q}'_{out} - m'_{out} \cdot h_{out}$$

Rearranging yields

$$\dot{W}'_{in} = m' \cdot (q_{out} + h_{out} - h_{in}) \quad \text{when } m'_{in} = m'_{out}$$

Going to Table A-17 @ $T := T_1 = 280 \text{ K}$ and $T := T_2 = 400 \text{ K}$ shows

$$h_1 := 280.13 \frac{\text{kJ}}{\text{kg}} \quad h_2 := 400.98 \frac{\text{kJ}}{\text{kg}}$$

The necessary power input is then given by

$$\dot{W}'_{in} := m' \cdot (q_{out} + h_2 - h_1) = 2.737 \text{ kW}$$

