

**Thermodynamics: An Engineering Approach**

**8th Edition**

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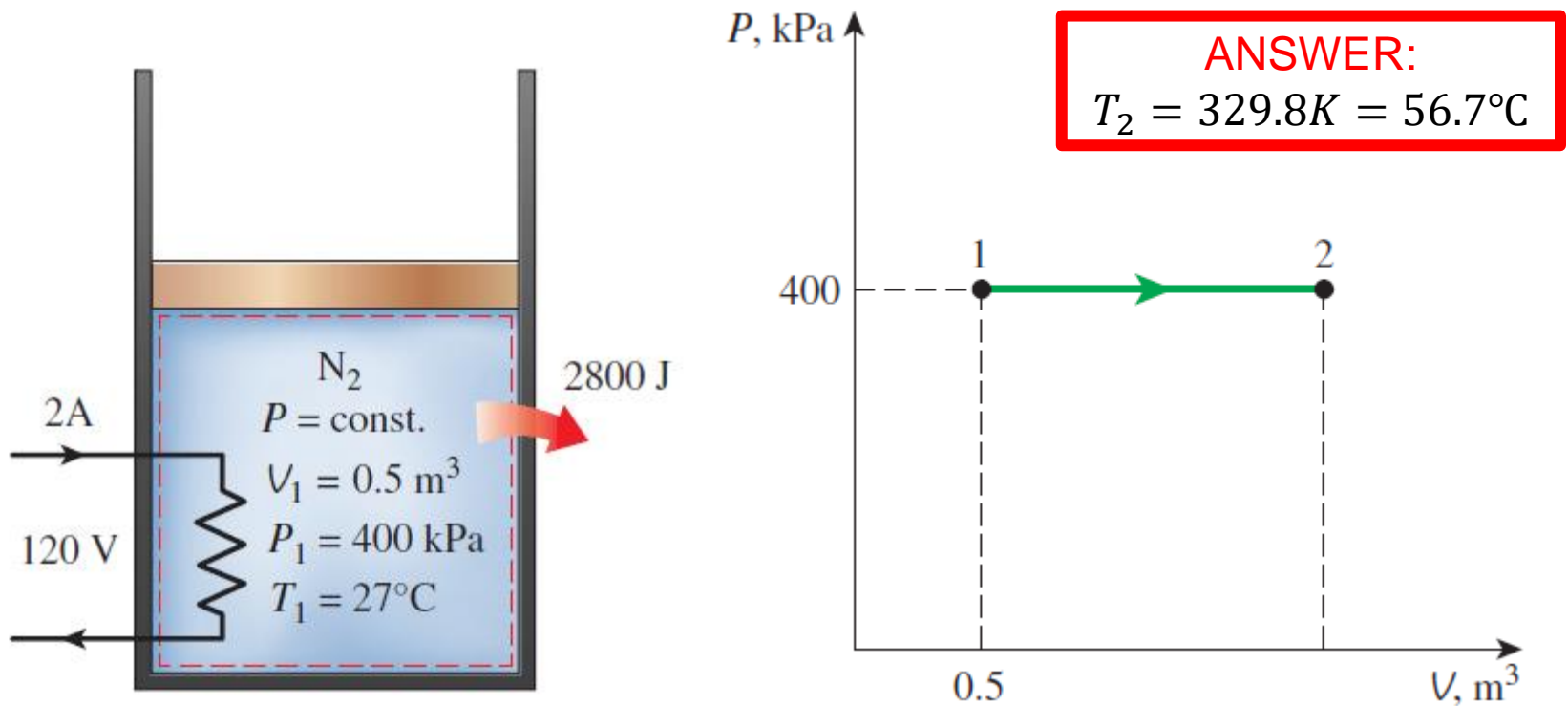
**McGraw-Hill, 2015**

## **Topic 7**

# **Efficiency, Environmental Concerns, and Mass Conservation**

# Practice Problem

A piston cylinder device initially contains  $0.5 \text{ m}^3$  of nitrogen gas at  $400 \text{ kPa}$  and  $27^\circ\text{C}$ . An electric heater within the device uses  $2 \text{ A}$  of current from a  $120 \text{ V}$  source for  $5 \text{ minutes}$ . As the nitrogen expands, a heat loss of  $2800 \text{ J}$  occurs during the process. Determine the final temperature.



# Objectives

- Define energy conversion efficiencies.
- Discuss the implications of energy conversion on the environment.
- Develop the conservation of mass principle.
- Apply the conservation of mass principle to various systems including steady- and unsteady-flow control volumes.
- Apply the first law of thermodynamics as the statement of the conservation of energy principle to control volumes.
- Identify the energy carried by a fluid stream crossing a control surface as the sum of internal energy, flow work, kinetic energy, and potential energy of the fluid and to relate the combination of the internal energy and the flow work to the property enthalpy.

# ENERGY CONVERSION EFFICIENCIES

**Efficiency** is one of the most frequently used terms in thermodynamics, and it indicates how well an energy conversion or transfer process is accomplished.

$$\text{Efficiency} = \frac{\text{Desired output}}{\text{Required input}}$$

**Efficiency of a water heater:** The ratio of the energy delivered to the house by hot water to the energy supplied to the water heater.

Type	Efficiency
Gas, conventional	55%
Gas, high-efficiency	62%
Electric, conventional	90%
Electric, high-efficiency	94%

**FIGURE 2–53**

Typical efficiencies of conventional and high-efficiency electric and natural gas water heaters.



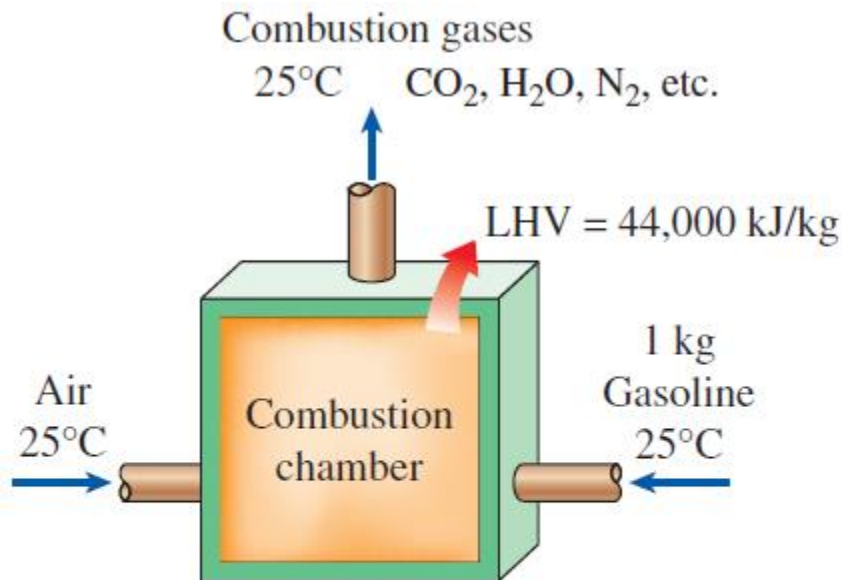
Water heater

$$\eta_{\text{combustion}} = \frac{Q}{HV} = \frac{\text{Amount of heat released during combustion}}{\text{Heating value of the fuel burned}}$$

**Heating value of the fuel:** The amount of heat released when a unit amount of fuel at room temperature is completely burned and the combustion products are cooled to the room temperature.

**Lower heating value (LHV):** When the water leaves as a vapor.

**Higher heating value (HHV):** When the water in the combustion gases is completely condensed and thus the heat of vaporization is also recovered.



**FIGURE 2-54**

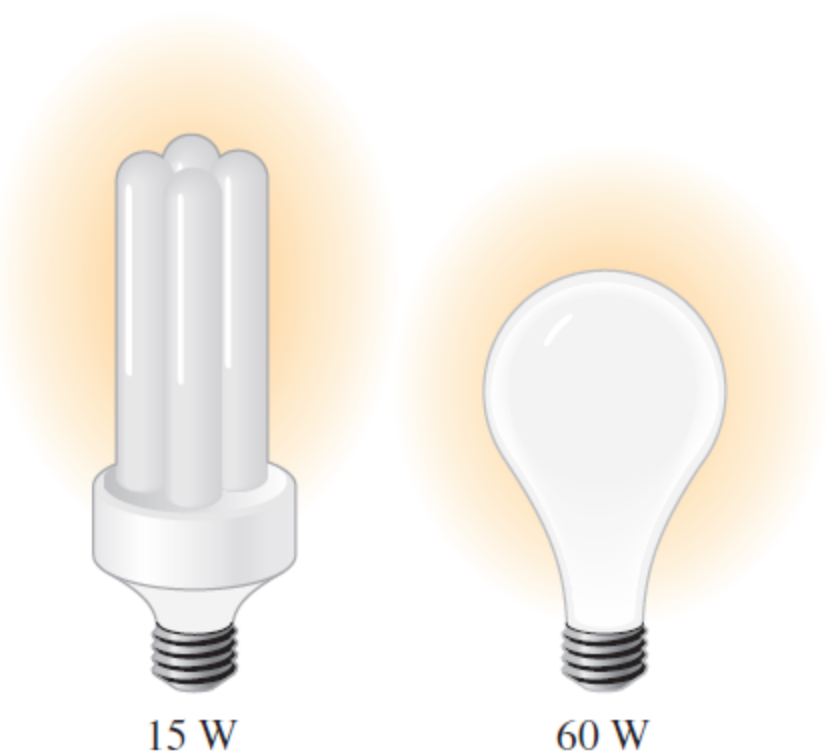
The definition of the heating value of gasoline.

The efficiency of space heating systems of residential and commercial buildings is usually expressed in terms of the **annual fuel utilization efficiency (AFUE)**, which accounts for the combustion efficiency as well as other losses such as heat losses to unheated areas and start-up and cooldown losses.

## Overall efficiency of a power plant

$$\eta_{\text{overall}} = \eta_{\text{combustion}} \eta_{\text{thermal}} \eta_{\text{generator}} = \frac{\dot{W}_{\text{net,electric}}}{\text{HHV} \times \dot{m}_{\text{fuel}}}$$

- **Generator:** A device that converts mechanical energy to electrical energy.
- **Generator efficiency:** The ratio of the electrical power output to the mechanical power input.
- **Thermal efficiency of a power plant:** The ratio of the net electrical power output to the rate of fuel energy input.



**FIGURE 2–55**

A 15-W compact fluorescent lamp provides as much light as a 60-W incandescent lamp.

**TABLE 2–1**

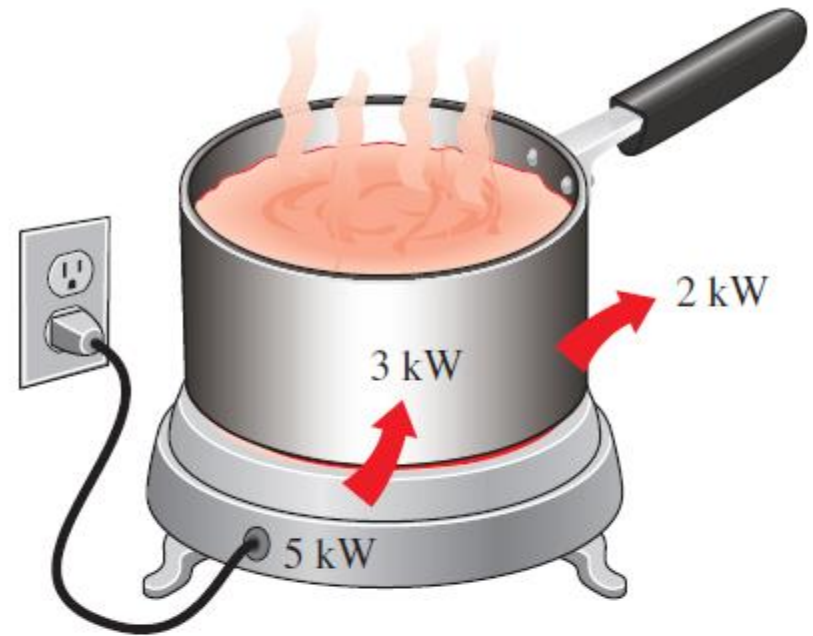
The efficacy of different lighting systems

Type of lighting	Efficacy, lumens/W
<i>Combustion</i>	
Candle	0.3
Kerosene lamp	1–2
<i>Incandescent</i>	
Ordinary	6–20
Halogen	15–35
<i>Fluorescent</i>	
Compact	40–87
Tube	60–120
<i>High-intensity discharge</i>	
Mercury vapor	40–60
Metal halide	65–118
High-pressure sodium	85–140
Low-pressure sodium	70–200
<i>Solid-State</i>	
LED	20–160
OLED	15–60
Theoretical limit	300*

**Lighting efficacy:** The amount of light output in lumens per W of electricity consumed.

\*This value depends on the spectral distribution of the assumed ideal light source. For white light sources, the upper limit is about 300 lm/W for metal halide, 350 lm/W for fluorescents, and 400 lm/W for LEDs. Spectral maximum occurs at a wavelength of 555 nm (green) with a light output of 683 lm/W.

- Using energy-efficient appliances **conserve energy**.
- It helps the **environment** by reducing the amount of pollutants emitted to the atmosphere during the combustion of fuel.
- The combustion of fuel produces
  - **carbon dioxide**, causes global warming
  - **nitrogen oxides** and **hydrocarbons**, cause smog
  - **carbon monoxide**, toxic
  - **sulfur dioxide**, causes acid rain.



$$\begin{aligned}\text{Efficiency} &= \frac{\text{Energy utilized}}{\text{Energy supplied to appliance}} \\ &= \frac{3 \text{ kWh}}{5 \text{ kWh}} = 0.60\end{aligned}$$

**FIGURE 2–56**

The efficiency of a cooking appliance represents the fraction of the energy supplied to the appliance that is transferred to the food.



# Example

The efficiency of cooking appliances affects the internal heat gain from them since an inefficient appliance consumes a greater amount of energy for the same task, and the excess energy consumed shows up as heat in the living space. The efficiency of open burners is determined to be 73 percent for electric units and 38 percent for gas units. Consider a 2-kW electric burner at a location where the unit costs of electricity and natural gas are \$0.09/kWh and \$1.20/therm, respectively. Determine the rate of energy consumption by the burner and the unit cost of utilized energy for both electric and gas burners.

Note: 1 therm = 29.3 kWh

Example 1

**TABLE 2-2****Energy costs of cooking a casserole with different appliances\***

[From J. T. Amann, A. Wilson, and K. Ackerly, *Consumer Guide to Home Energy Savings*, 9<sup>th</sup> ed., American Council for an Energy-Efficient Economy, Washington, D.C., 2007, p. 163.]

Cooking appliance	Cooking temperature	Cooking time	Energy used	Cost of energy
Electric oven	350°F (177°C)	1 h	2.0 kWh	\$0.19
Convection oven (elect.)	325°F (163°C)	45 min	1.39 kWh	\$0.13
Gas oven	350°F (177°C)	1 h	0.112 therm	\$0.13
Frying pan	420°F (216°C)	1 h	0.9 kWh	\$0.09
Toaster oven	425°F (218°C)	50 min	0.95 kWh	\$0.09
Crockpot	200°F (93°C)	7 h	0.7 kWh	\$0.07
Microwave oven	"High"	15 min	0.36 kWh	\$0.03

\*Assumes a unit cost of \$0.095/kWh for electricity and \$1.20/therm for gas.

# Efficiencies of Mechanical and Electrical Devices

## Mechanical efficiency

$$\eta_{\text{mech}} = \frac{\text{Mechanical energy output}}{\text{Mechanical energy input}} = \frac{E_{\text{mech,out}}}{E_{\text{mech,in}}} = 1 - \frac{E_{\text{mech,loss}}}{E_{\text{mech,in}}}$$

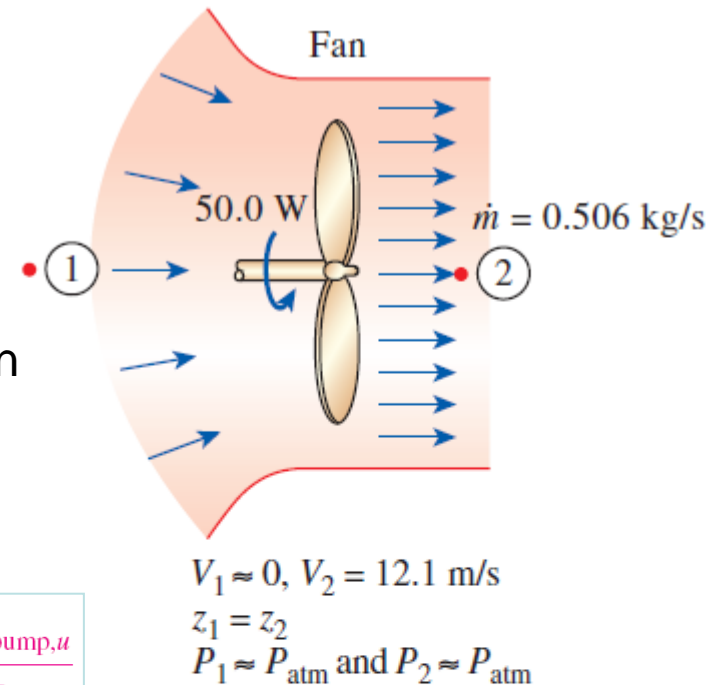
The effectiveness of the conversion process between the mechanical work supplied or extracted and the mechanical energy of the fluid is expressed by the **pump efficiency** and **turbine efficiency**,

$$\eta_{\text{pump}} = \frac{\text{Mechanical energy increase of the fluid}}{\text{Mechanical energy input}} = \frac{\Delta \dot{E}_{\text{mech,fluid}}}{\dot{W}_{\text{shaft,in}}} = \frac{\dot{W}_{\text{pump,u}}}{\dot{W}_{\text{pump}}}$$

$$\Delta \dot{E}_{\text{mech,fluid}} = \dot{E}_{\text{mech,out}} - \dot{E}_{\text{mech,in}}$$

$$\eta_{\text{turbine}} = \frac{\text{Mechanical energy output}}{\text{Mechanical energy decrease of the fluid}} = \frac{\dot{W}_{\text{shaft,out}}}{|\Delta \dot{E}_{\text{mech,fluid}}|} = \frac{\dot{W}_{\text{turbine}}}{\dot{W}_{\text{turbine,e}}} =$$

$$|\Delta \dot{E}_{\text{mech,fluid}}| = \dot{E}_{\text{mech,in}} - \dot{E}_{\text{mech,out}}$$



$$\eta_{\text{mech, fan}} =$$

**FIGURE 2–58**

The mechanical efficiency of a fan is the ratio of the rate of increase of the mechanical energy of air to the mechanical power input.

$$\eta_{\text{motor}} = \frac{\text{Mechanical power output}}{\text{Electric power input}} = \frac{\dot{W}_{\text{shaft,out}}}{\dot{W}_{\text{elect,in}}} \quad \text{Pump efficiency}$$

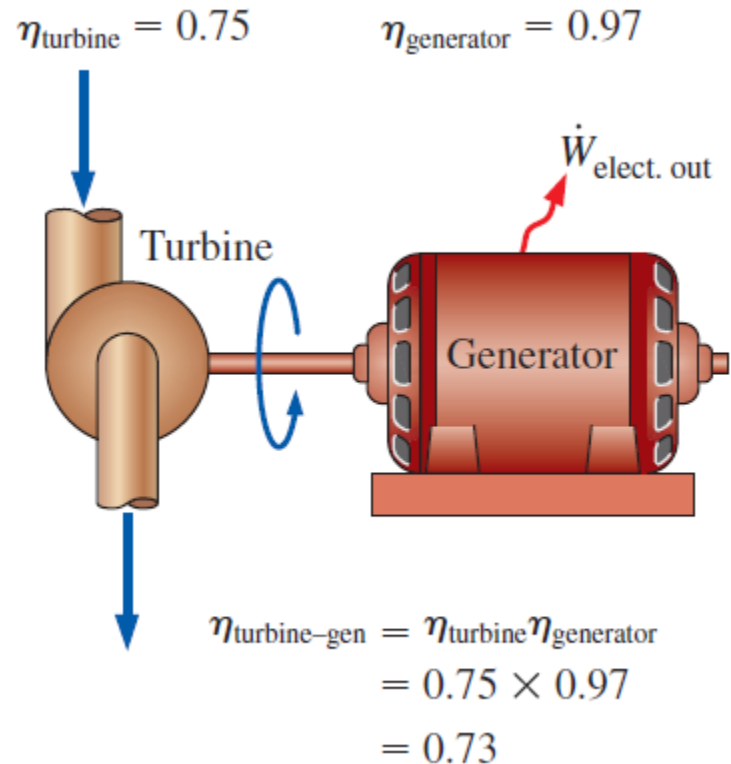
$$\eta_{\text{generator}} = \frac{\text{Electric power output}}{\text{Mechanical power input}} = \frac{\dot{W}_{\text{elect,out}}}{\dot{W}_{\text{shaft,in}}} \quad \text{Generator efficiency}$$

$$\eta_{\text{pump-motor}} = \eta_{\text{pump}} \eta_{\text{motor}} = \frac{\dot{W}_{\text{pump,u}}}{\dot{W}_{\text{elect,in}}} = \frac{\Delta \dot{E}_{\text{mech,fluid}}}{\dot{W}_{\text{elect,in}}} \quad \text{Pump-Motor overall efficiency}$$

$$\eta_{\text{turbine-gen}} = \eta_{\text{turbine}} \eta_{\text{generator}} = \frac{\dot{W}_{\text{elect,out}}}{\dot{W}_{\text{turbine,e}}} = \frac{\dot{W}_{\text{elect,out}}}{|\Delta \dot{E}_{\text{mech,fluid}}|} \quad \text{Turbine-Generator overall efficiency}$$

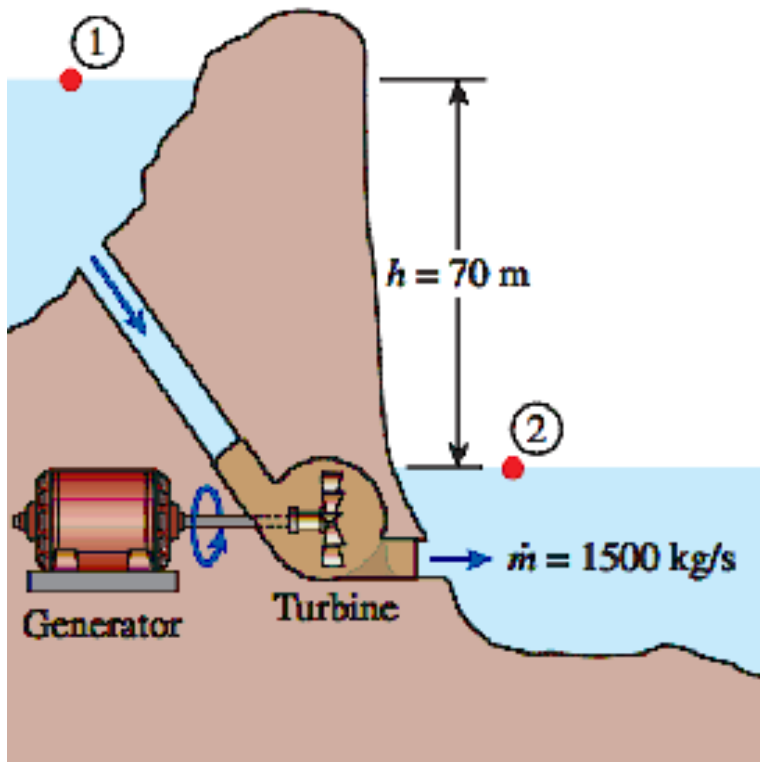
**FIGURE 2–59**

The overall efficiency of a turbine–generator is the product of the efficiency of the turbine and the efficiency of the generator, and represents the fraction of the mechanical power of the fluid converted to electrical power.



# Example

Electric power is to be generated by installing a hydraulic turbine–generator at a site 70 m below the free surface of a large water reservoir that can supply water at a rate of 1500 kg/s steadily. If the mechanical power output of the turbine is 800 kW and the electric power generation is 750 kW, determine the turbine efficiency and the combined turbine-generator efficiency of this plant. Neglect losses in the pipes.



**Example 2**

# ENERGY AND ENVIRONMENT

- The conversion of energy from one form to another often affects the environment and the air we breathe in many ways, and thus the study of energy is not complete without considering its impact on the environment.
- Pollutants emitted during the combustion of fossil fuels are responsible for **smog, acid rain**, and **global warming**.
- The environmental pollution has reached such high levels that it became a serious threat to **vegetation, wild life**, and **human health**.



**FIGURE 2–62**

Energy conversion processes are often accompanied by environmental pollution.



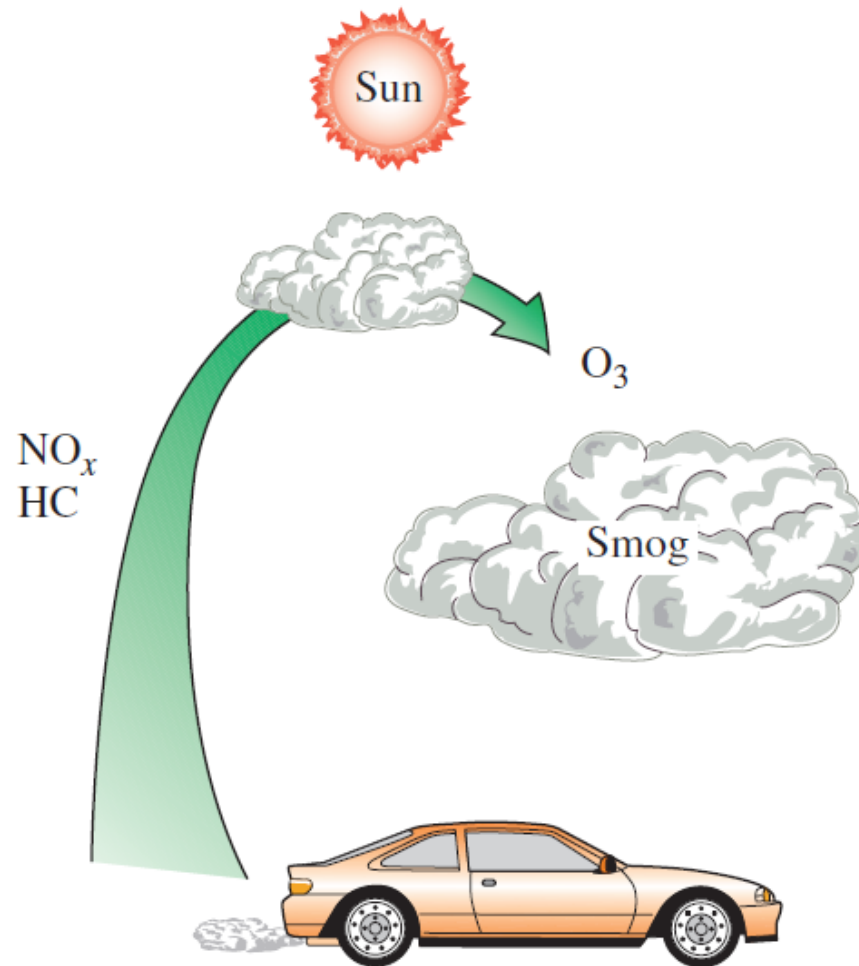
**FIGURE 2–63**

Motor vehicles are the largest source of air pollution.

# Ozone and Smog

- **Smog**: Made up mostly of ground-level ozone ( $O_3$ ), but it also contains numerous other chemicals, including carbon monoxide (CO), particulate matter such as soot and dust, volatile organic compounds (VOCs) such as benzene, butane, and other hydrocarbons.
- **Hydrocarbons** and **nitrogen oxides** react in the presence of sunlight on hot calm days to form ground-level ozone.
- **Ozone** irritates eyes and damages the air sacs in the lungs where oxygen and carbon dioxide are exchanged, causing eventual hardening of this soft and spongy tissue.
- It also causes shortness of breath, wheezing, fatigue, headaches, and nausea, and aggravates respiratory problems such as asthma.
- The other serious pollutant in smog is **carbon monoxide**, which is a colorless, odorless, poisonous gas.
- It is mostly emitted by motor vehicles.
- It deprives the body's organs from getting enough oxygen by binding with the red blood cells that would otherwise carry oxygen. It is fatal at high levels.
- Suspended **particulate matter** such as **dust** and **soot** are emitted by vehicles and industrial facilities. Such particles irritate the eyes and the lungs.



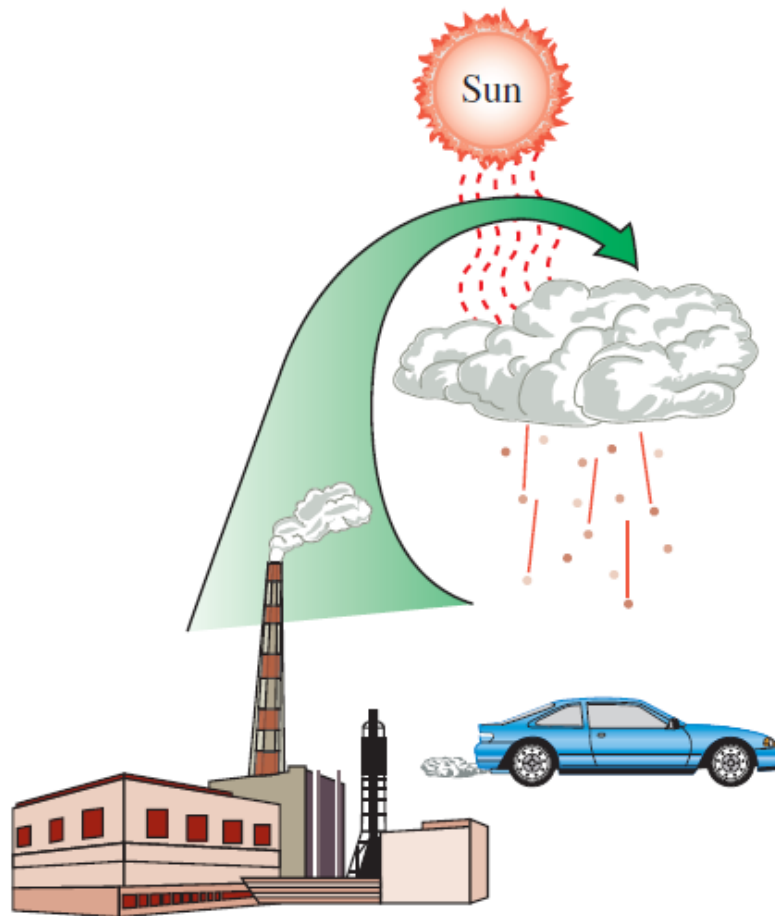


**FIGURE 2-64**

Ground-level ozone, which is the primary component of smog, forms when  $\text{HC}$  and  $\text{NO}_x$  react in the presence of sunlight in hot calm days.

# Acid Rain

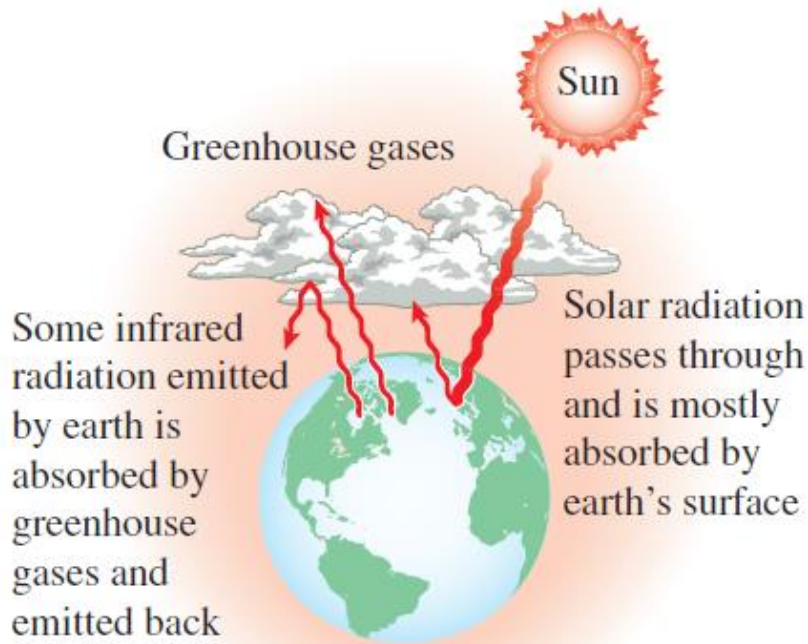
- The sulfur in the fuel reacts with oxygen to form sulfur dioxide ( $\text{SO}_2$ ), which is an air pollutant.
- The main source of  $\text{SO}_2$  is the electric power plants that burn high-sulfur coal.
- Motor vehicles also contribute to  $\text{SO}_2$  emissions since gasoline and diesel fuel also contain small amounts of sulfur.
- The sulfur oxides and nitric oxides react with water vapor and other chemicals high in the atmosphere in the presence of sunlight to form sulfuric and nitric acids.
- The acids formed usually dissolve in the suspended water droplets in clouds or fog.
- These acid-laden droplets, which can be as acidic as lemon juice, are washed from the air on to the soil by rain or snow. This is known as **acid rain**.



**FIGURE 2-65**

Sulfuric acid and nitric acid are formed when sulfur oxides and nitric oxides react with water vapor and other chemicals high in the atmosphere in the presence of sunlight.

# The Greenhouse Effect: Global Warming and Climate Change



**FIGURE 2–66**

The greenhouse effect on earth.

- CO<sub>2</sub> is produced by the burning of fossil fuels such as **coal**, **oil**, and **natural gas**.

- **Greenhouse effect:** Glass allows the solar radiation to enter freely but blocks the infrared radiation emitted by the interior surfaces. This causes a rise in the interior temperature as a result of the thermal energy buildup in a space (i.e., car).
- The surface of the earth, which warms up during the day as a result of the absorption of solar energy, cools down at night by radiating part of its energy into deep space as infrared radiation.
- **Carbon dioxide (CO<sub>2</sub>)**, water vapor, and trace amounts of some other gases such as methane and nitrogen oxides act like a blanket and keep the earth warm at night by blocking the heat radiated from the earth. The result is **global warming**.
- These gases are called “**greenhouse gases**,” with CO<sub>2</sub> being the primary component.

- **A 1995 report:** The earth has already warmed about **0.5°C** during the last century, and they estimate that the earth's temperature will rise another **2°C** by the year 2100.
- A rise of this magnitude can cause **severe changes in weather patterns** with storms and heavy rains and flooding at some parts and drought in others, major floods due to the melting of ice at the poles, loss of wetlands and coastal areas due to rising sea levels, and other negative results.
  - Improved energy efficiency,
  - energy conservation,
  - using renewable energy sources
- help minimize global warming.



**FIGURE 2–67**

The average car produces several times its weight in  $\text{CO}_2$  every year (it is driven 13,500 miles a year, consumes 600 gallons of gasoline, and produces 20 lbm of  $\text{CO}_2$  per gallon).



**FIGURE 2–68**

Renewable energies such as wind are called “green energy” since they emit no pollutants or greenhouse gases.

# CONSERVATION OF MASS

**Conservation of mass:** Mass, like energy, is a conserved property, and it cannot be created or destroyed during a process.

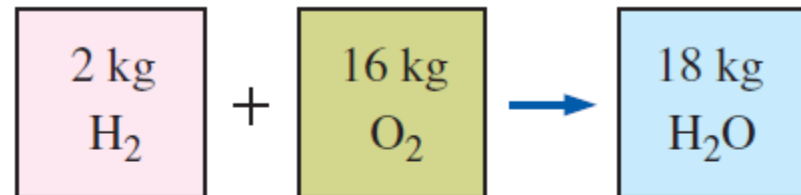
**Closed systems:** The mass of the system remain constant during a process.

**Control volumes:** Mass can cross the boundaries, and so we must keep track of the amount of mass entering and leaving the control volume.

Mass  $m$  and energy  $E$  can be converted to each other according to  $E = mc^2$

where  $c$  is the speed of light in a vacuum, which is  $c = 2.9979 \times 10^8$  m/s.

The mass change due to energy change is negligible.



**FIGURE 5–1**

Mass is conserved even during chemical reactions.



# Mass and Volume Flow Rates

$$\delta \dot{m} = \rho V_n dA_c$$

$$\dot{m} = \int_{A_c} \delta \dot{m} = \int_{A_c} \rho V_n dA_c$$

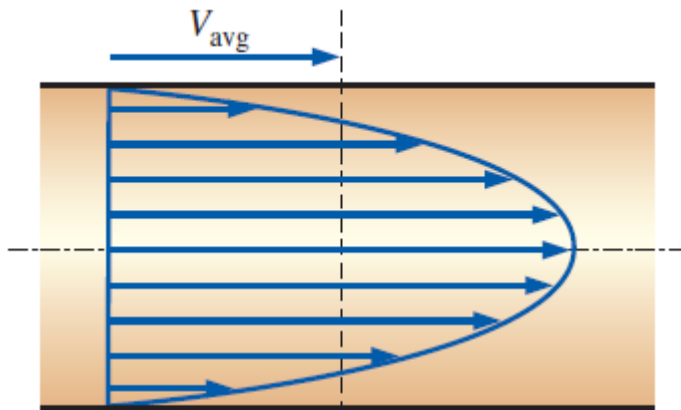
$$\dot{m} = \rho V_{\text{avg}} A_c \quad (\text{kg/s})$$

$$\dot{m} = \rho \dot{V} = \frac{\dot{V}}{v} \quad \text{Mass flow rate}$$

$$V_{\text{avg}} = \frac{1}{A_c} \int_{A_c} V_n dA_c \quad \text{Definition of average velocity}$$

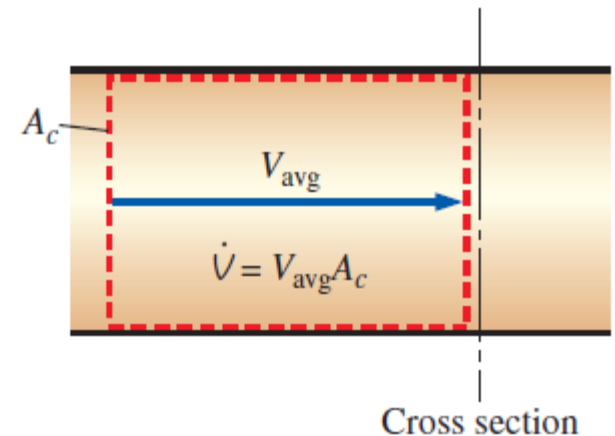
Volume flow rate

$$\dot{V} = \int_{A_c} V_n dA_c = V_{\text{avg}} A_c = VA_c \quad (\text{m}^3/\text{s})$$



**FIGURE 5–3**

The average velocity  $V_{\text{avg}}$  is defined as the average speed through a cross section.



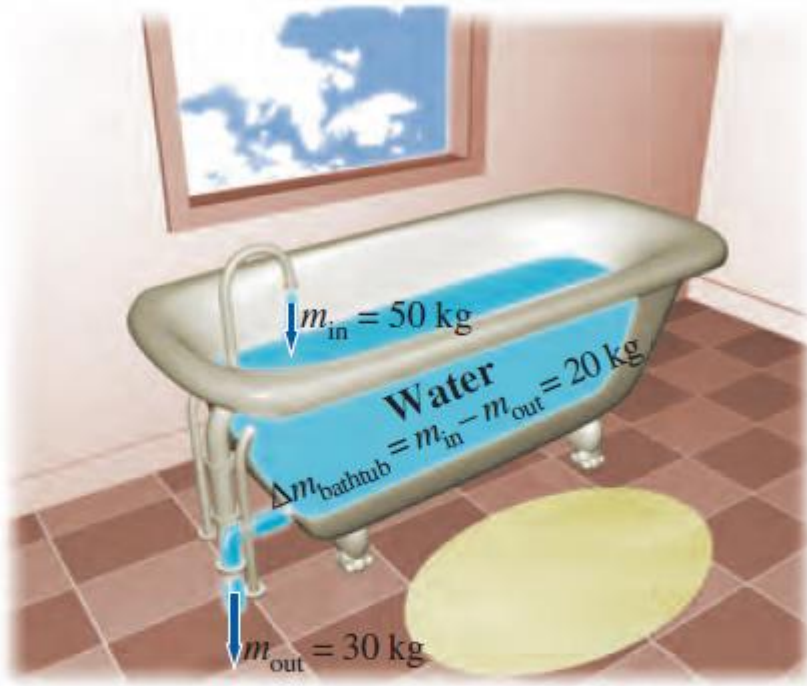
**FIGURE 5–4**

The volume flow rate is the volume of fluid flowing through a cross section per unit time.



# Conservation of Mass Principle

$$\left( \begin{array}{c} \text{Total mass entering} \\ \text{the CV during } \Delta t \end{array} \right) - \left( \begin{array}{c} \text{Total mass leaving} \\ \text{the CV during } \Delta t \end{array} \right) = \left( \begin{array}{c} \text{Net change of mass} \\ \text{within the CV during } \Delta t \end{array} \right)$$



**FIGURE 5–5**

Conservation of mass principle for an ordinary bathtub.

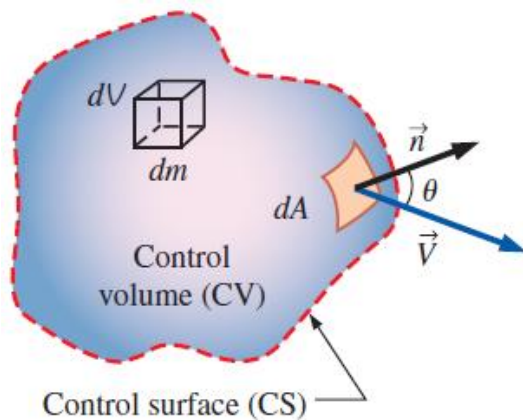
**The conservation of mass principle for a control volume:** The net mass transfer to or from a control volume during a time interval  $\Delta t$  is equal to the net change (increase or decrease) in the total mass within the control volume during  $\Delta t$ .

$$m_{in} - m_{out} = \Delta m_{CV} \quad (\text{kg})$$

$$\Delta m_{CV} = m_{final} - m_{initial}$$

$$\dot{m}_{in} - \dot{m}_{out} = dm_{CV}/dt \quad (\text{kg/s})$$

These equations are often referred to as the **mass balance** and are applicable to any control volume undergoing any kind of process.



**FIGURE 5-6**

The differential control volume  $dV$  and the differential control surface  $dA$  used in the derivation of the conservation of mass relation.

Total mass within the CV:  $m_{CV} = \int_{CV} \rho \, dV$

Rate of change of mass within the CV:  $\frac{dm_{CV}}{dt} = \frac{d}{dt} \int_{CV} \rho \, dV$

Normal component of velocity:  $V_n = V \cos \theta = \vec{V} \cdot \vec{n}$

Differential mass flow rate:  $\delta \dot{m} = \rho V_n \, dA = \rho (V \cos \theta) \, dA = \rho (\vec{V} \cdot \vec{n}) \, dA$

Net mass flow rate:  $\dot{m}_{net} = \int_{CS} \delta \dot{m} = \int_{CS} \rho V_n \, dA = \int_{CS} \rho (\vec{V} \cdot \vec{n}) \, dA$

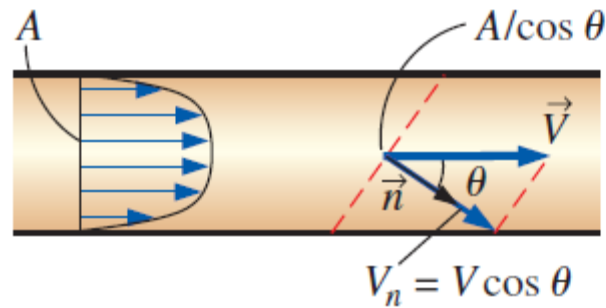
General conservation of mass:  $\frac{d}{dt} \int_{CV} \rho \, dV + \int_{CS} \rho (\vec{V} \cdot \vec{n}) \, dA = 0$

the time rate of change of mass within the control volume plus the net mass flow rate through the control surface is equal to zero.

$$\frac{d}{dt} \int_{CV} \rho \, dV + \sum_{out} \rho |V_n| \, dA - \sum_{in} \rho |V_n| \, dA = 0$$

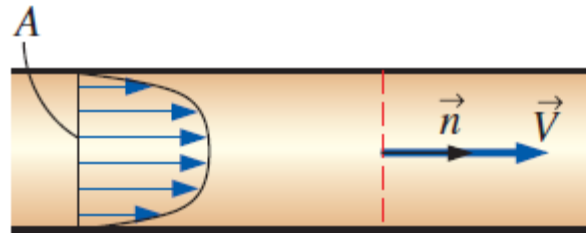
$$\frac{d}{dt} \int_{CV} \rho \, dV = \sum_{in} \dot{m} - \sum_{out} \dot{m} \quad \text{or} \quad \frac{dm_{CV}}{dt} = \sum_{in} \dot{m} - \sum_{out} \dot{m}$$

General  
conservation of  
mass in rate form



$$\dot{m} = \rho(V \cos \theta)(A/\cos \theta) = \rho VA$$

(a) Control surface *at an angle* to the flow



$$\dot{m} = \rho VA$$

(b) Control surface *normal* to the flow

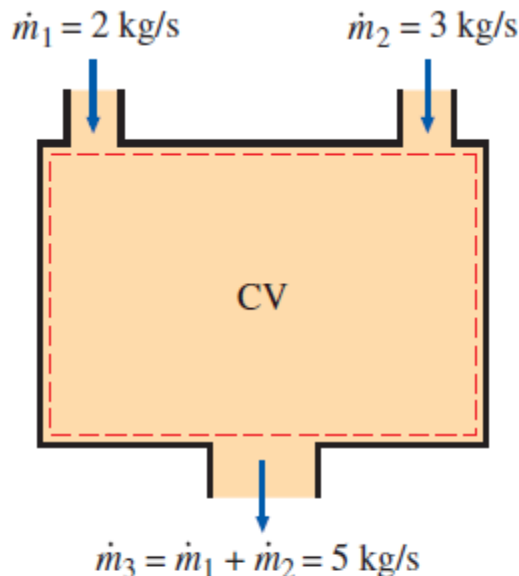
### FIGURE 5–7

A control surface should always be selected *normal to the flow* at all locations where it crosses the fluid flow to avoid complications, even though the result is the same.

# Mass Balance for Steady-Flow Processes

During a **steady-flow** process, the total amount of mass contained within a control volume does not change with time ( $m_{CV} = \text{constant}$ ).

Then the conservation of mass principle requires that **the total amount of mass entering a control volume equal the total amount of mass leaving it**.



**FIGURE 5–8**

Conservation of mass principle for a two-inlet–one-outlet steady-flow system.

For steady-flow processes, we are interested in the amount of mass flowing per unit time, that is, *the mass flow rate*.

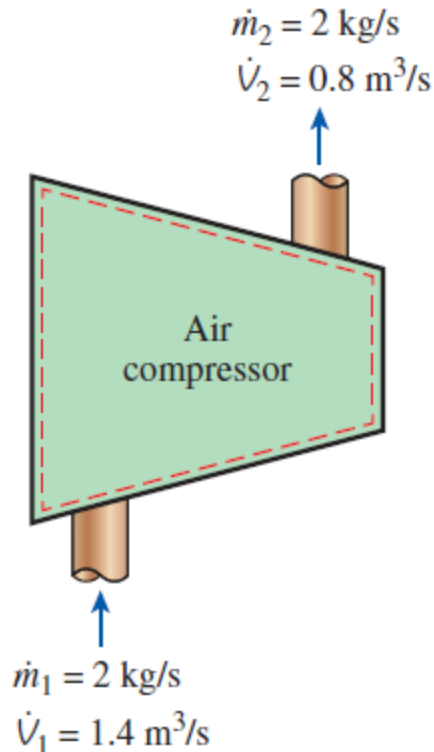
$$\sum_{\text{in}} \dot{m} = \sum_{\text{out}} \dot{m} \quad (\text{kg/s}) \quad \text{Multiple inlets and exits}$$

$$\dot{m}_1 = \dot{m}_2 \quad \rightarrow \quad \rho_1 V_1 A_1 = \rho_2 V_2 A_2 \quad \text{Single stream}$$

Many engineering devices such as nozzles, diffusers, turbines, compressors, and pumps involve a single stream (only one inlet and one outlet).

# Special Case: Incompressible Flow

The conservation of mass relations can be simplified even further when the fluid is incompressible, which is usually the case for liquids.



$$\sum_{\text{in}} \dot{V} = \sum_{\text{out}} \dot{V} \quad (\text{m}^3/\text{s}) \quad \text{Steady, incompressible}$$

$$\dot{V}_1 = \dot{V}_2 \rightarrow V_1 A_1 = V_2 A_2 \quad \text{Steady, incompressible flow (single stream)}$$

There is no such thing as a “conservation of volume” principle.

For steady flow of liquids, the volume flow rates, as well as the mass flow rates, remain constant since liquids are essentially incompressible substances.

**FIGURE 5–9**

During a steady-flow process, volume flow rates are not necessarily conserved although mass flow rates are.

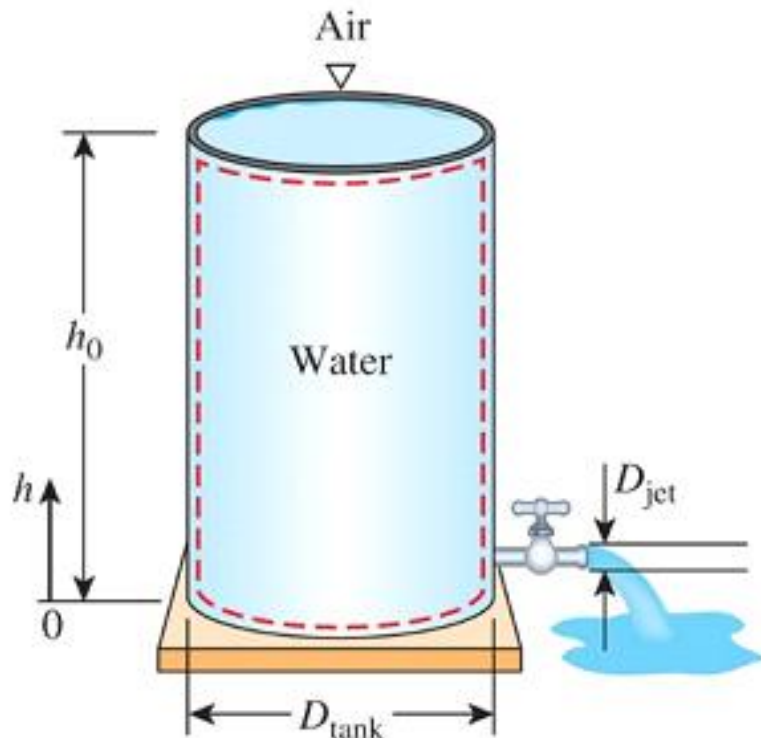
# Water Flow through a Hose Nozzle

A garden hose with a nozzle is used to fill a 10-gal bucket. The inner diameter of the hose is 2 cm and the diameter of the nozzle exit is 0.8 cm. If it takes 50 seconds to fill the bucket, determine (a) the volume and mass flow rates of water through the hose, (b) the average velocity of water inside the hose, and (c) the average velocity of water at the nozzle exit. (3.7854 L = 1 gallon)

## Example 3

# Discharge of Water from a Tank

A 4 ft high, 3 ft diameter cylindrical water tank whose top is open to the atmosphere is being drained. The diameter of the water jet that streams out the bottom is 0.5 in. Determine the velocity of the water leaving the tank and the time it takes to drain half of the tank.



**Example 4**

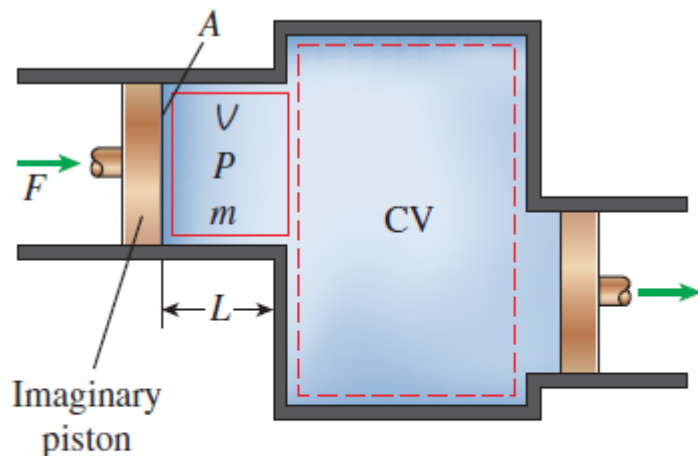
# FLOW WORK AND THE ENERGY OF A FLOWING FLUID

**Flow work, or flow energy:** The work (or energy) required to push the mass into or out of the control volume. This work is necessary for maintaining a continuous flow through a control volume.

$$F = PA$$

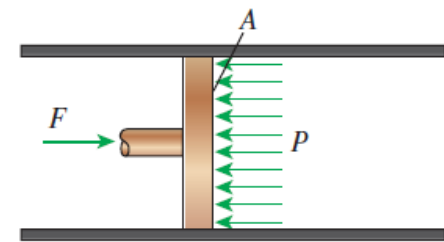
$$W_{\text{flow}} = FL = PAL = PV \quad (\text{kJ})$$

$$w_{\text{flow}} = Pv \quad (\text{kJ/kg})$$



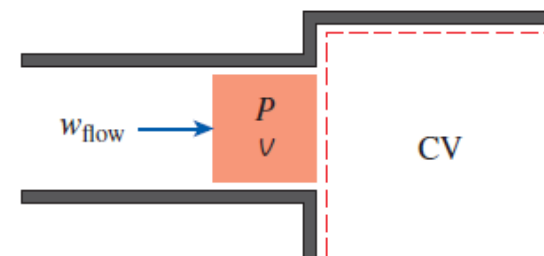
**FIGURE 5-12**

Schematic for flow work.

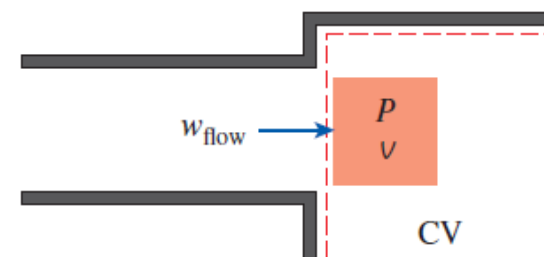


**FIGURE 5-13**

In the absence of acceleration, the force applied on a fluid by a piston is equal to the force applied on the piston by the fluid.



(a) Before entering



(b) After entering

**FIGURE 5-14**

Flow work is the energy needed to push a fluid into or out of a control volume, and it is equal to  $Pv$ .



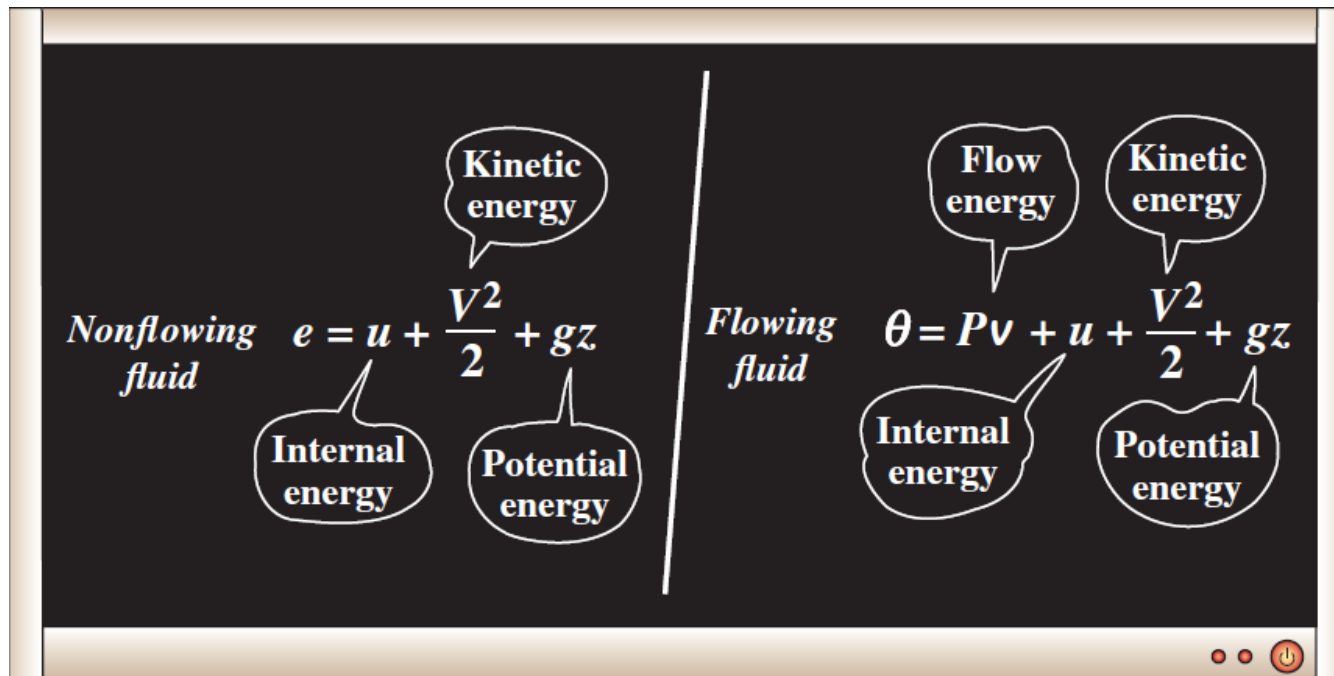
# Total Energy of a Flowing Fluid

$$e = u + \text{ke} + \text{pe} = u + \frac{V^2}{2} + gz \quad (\text{kJ/kg})$$

$$\theta = Pv + e = Pv + (u + \text{ke} + \text{pe}) \quad h = u + Pv$$

$$\theta = h + \text{ke} + \text{pe} = h + \frac{V^2}{2} + gz \quad (\text{kJ/kg})$$

The flow energy is automatically taken care of by enthalpy. In fact, this is the main reason for defining the property enthalpy.

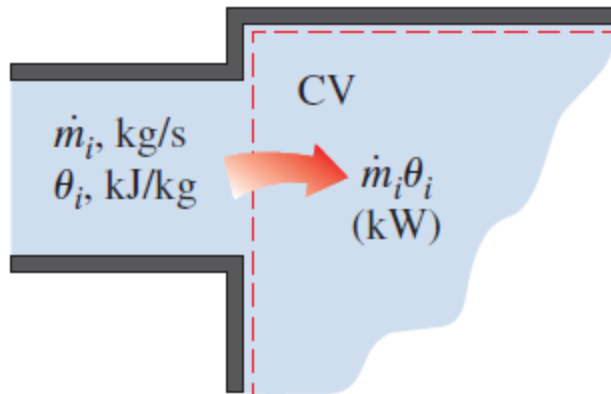


The total energy consists of three parts for a nonflowing fluid and four parts for a flowing fluid.

# Energy Transport by Mass

*Amount of energy transport:*  $E_{\text{mass}} = m\theta = m\left(h + \frac{V^2}{2} + gz\right) \quad (\text{kJ})$

*Rate of energy transport:*  $\dot{E}_{\text{mass}} = \dot{m}\theta = \dot{m}\left(h + \frac{V^2}{2} + gz\right) \quad (\text{kW})$



**FIGURE 5–16**

The product  $\dot{m}_i\theta_i$  is the energy transported into control volume by mass per unit time.

When the kinetic and potential energies of a fluid stream are negligible

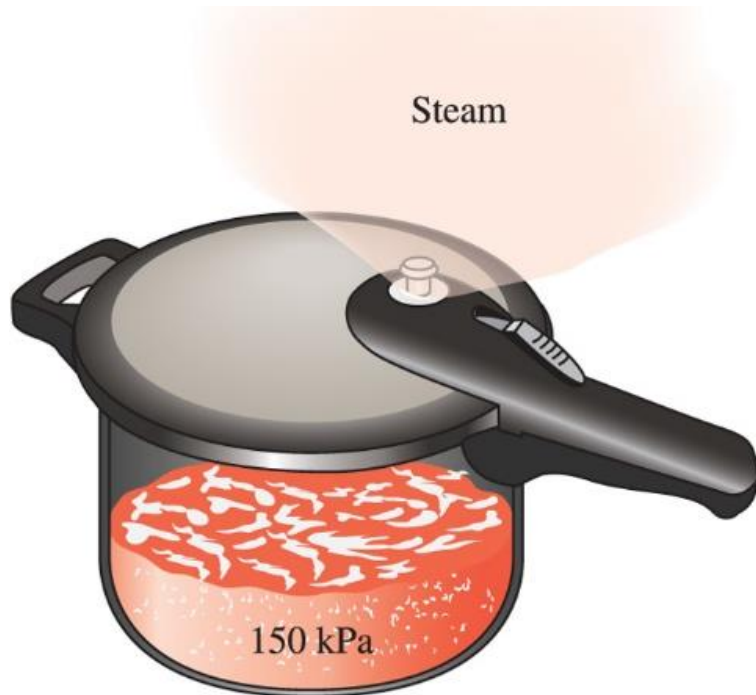
$$E_{\text{mass}} = mh \quad \dot{E}_{\text{mass}} = \dot{m}h$$

When the properties of the mass at each inlet or exit change with time as well as over the cross section

$$E_{\text{in,mass}} = \int_{m_i} \theta_i \delta m_i = \int_{m_i} \left( h_i + \frac{V_i^2}{2} + gz_i \right) \delta m_i$$

# Energy Transport in a Pressure Cooker

Steam is leaving a 4 L pressure cooker whose operating pressure is 150 kPa. It is observed that the amount of liquid in the cooker has decreased by 0.6 L in 40 minutes during the steady operating conditions. The cross-sectional area of the exit opening is 8 mm<sup>2</sup>. Determine (a) the mass flow rate of the steam and the exit velocity, (b) the flow and total energies of the steam (per unit mass), and (c) the rate at which energy leaves the cooker by steam.



**Example 5**

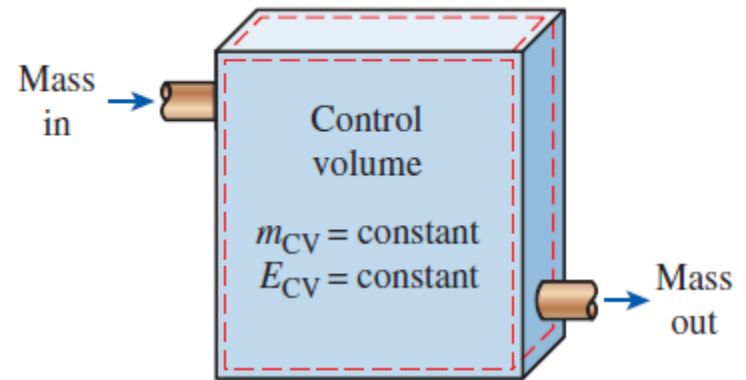
# ENERGY ANALYSIS OF STEADY-FLOW SYSTEMS

**Steady-flow process:** *A process during which a fluid flows through a control volume steadily.*



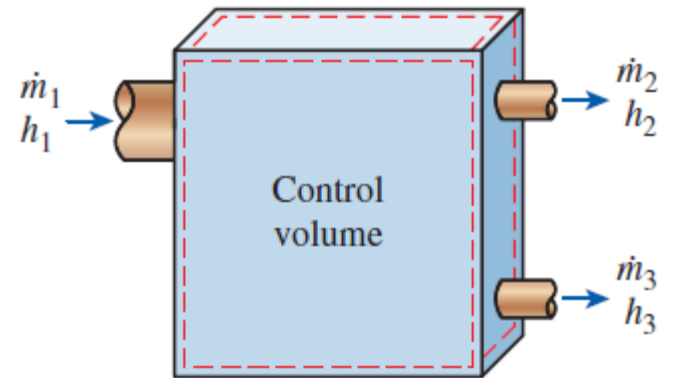
**FIGURE 5–18**

Many engineering systems such as power plants operate under steady conditions.



**FIGURE 5–19**

Under steady-flow conditions, the mass and energy contents of a control volume remain constant.



**FIGURE 5–20**

Under steady-flow conditions, the fluid properties at an inlet or exit remain constant (do not change with time).

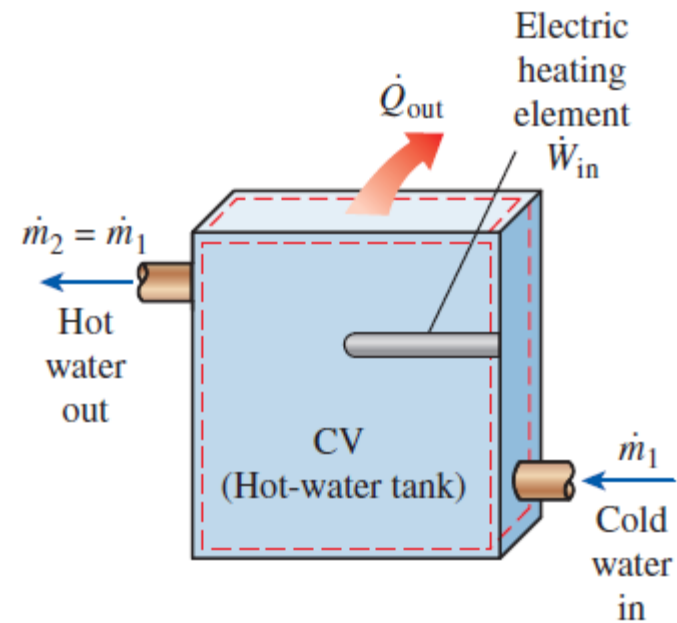
# Mass and Energy balances for a steady-flow process

$$\sum_{\text{in}} \dot{m} = \sum_{\text{out}} \dot{m} \quad (\text{kg/s})$$

$$\dot{m}_1 = \dot{m}_2$$

Mass  
balance

$$\rho_1 V_1 A_1 = \rho_2 V_2 A_2$$



**FIGURE 5–21**

A water heater in steady operation.

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\frac{dE_{\text{system}}/dt}_{\text{Rate of change in internal, kinetic, potential, etc., energies}}}_{\rightarrow 0 \text{ (steady)}} = 0$$

$$\underbrace{\dot{E}_{\text{in}}}_{\text{Rate of net energy transfer in by heat, work, and mass}} = \underbrace{\dot{E}_{\text{out}}}_{\text{Rate of net energy transfer out by heat, work, and mass}} \quad (\text{kW})$$

Energy balance

$$\dot{Q}_{\text{in}} + \dot{W}_{\text{in}} + \sum_{\text{in}} \dot{m}\theta = \dot{Q}_{\text{out}} + \dot{W}_{\text{out}} + \sum_{\text{out}} \dot{m}\theta$$

$$\dot{Q}_{\text{in}} + \dot{W}_{\text{in}} + \underbrace{\sum_{\text{in}} \dot{m} \left( h + \frac{V^2}{2} + gz \right)}_{\text{for each inlet}} = \dot{Q}_{\text{out}} + \dot{W}_{\text{out}} + \underbrace{\sum_{\text{out}} \dot{m} \left( h + \frac{V^2}{2} + gz \right)}_{\text{for each exit}}$$

## Energy balance relations with sign conventions (i.e., heat input and work output are positive)

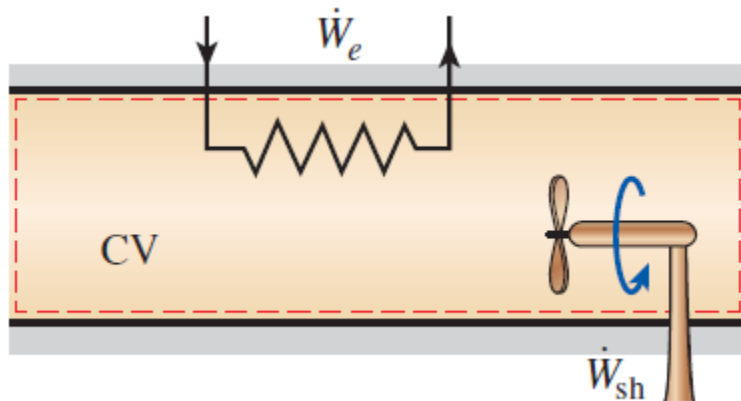
$$\dot{Q} - \dot{W} = \sum_{\text{out}} \dot{m} \underbrace{\left( h + \frac{V^2}{2} + gz \right)}_{\text{for each exit}} - \sum_{\text{in}} \dot{m} \underbrace{\left( h + \frac{V^2}{2} + gz \right)}_{\text{for each inlet}}$$

$$\dot{Q} - \dot{W} = \dot{m} \left[ h_2 - h_1 + \frac{V_2^2 - V_1^2}{2} + g(z_2 - z_1) \right]$$

$$q - w = h_2 - h_1 + \frac{V_2^2 - V_1^2}{2} + g(z_2 - z_1)$$

$$q - w = h_2 - h_1 \quad q = \dot{Q}/\dot{m} \quad w = \dot{W}/\dot{m}$$

when kinetic and potential energy changes are negligible



Under steady operation, shaft work and electrical work are the only forms of work a simple compressible system may involve.

$$\frac{\text{J}}{\text{kg}} \equiv \frac{\text{N} \cdot \text{m}}{\text{kg}} \equiv \left( \text{kg} \frac{\text{m}}{\text{s}^2} \right) \frac{\text{m}}{\text{kg}} \equiv \frac{\text{m}^2}{\text{s}^2}$$

$$\left( \text{Also, } \frac{\text{Btu}}{\text{lbm}} \equiv 25,037 \frac{\text{ft}^2}{\text{s}^2} \right)$$

The units  $\text{m}^2/\text{s}^2$  and  $\text{J/kg}$  are equivalent.

$V_1$	$V_2$	$\Delta \text{ke}$
m/s	m/s	kJ/kg
0	45	1
50	67	1
100	110	1
200	205	1
500	502	1

At very high velocities, even small changes in velocities can cause significant changes in the kinetic energy of the fluid.

# Summary

- Energy conversion efficiencies
  - Efficiencies of mechanical and electrical devices (turbines, pumps)
- Energy and environment
  - Ozone and smog
  - Acid rain
  - The Greenhouse effect: Global warming and climate change
- Conservation of mass
  - Mass and volume flow rates
  - Mass balance for a steady-flow process
  - Mass balance for incompressible flow
- Flow work and the energy of a flowing fluid
  - Energy transport by mass
- Energy analysis of steady-flow systems