

Given: $\text{kJ} := 1000\text{J}$

Steam at 7 MPa and 450°C is throttled in a valve to a pressure of 3 MPa during a steady-flow process.

$$P_1 := 7\text{MPa} \quad T_1 := 450^\circ\text{C} \quad P_2 := 3\text{MPa}$$

Required:

Determine the entropy generated during this process and whether it satisfies the Second Law of Thermodynamics.

Solution:

Starting with an entropy balance for a steady flow device shows

$$\frac{d}{dt}S_{\text{sys}} = \sum S'_{\text{in}} - \sum S'_{\text{out}} + S'_{\text{gen}}$$

$$0 = \sum S'_{\text{in}} - \sum S'_{\text{out}} + S'_{\text{gen}}$$

$$S'_{\text{gen}} = \sum S'_{\text{out}} - \sum S'_{\text{in}} = m' \cdot (s_2 - s_1)$$

The entropy generation on a specific basis is found by

$$s_{\text{gen}} = \frac{S'_{\text{gen}}}{m'} = \frac{m' \cdot (s_2 - s_1)}{m'} = s_2 - s_1$$

Going to Table A-5 @ $P_1 = 7000\text{kPa}$ shows

$$T_{\text{sat}} := 285.83^\circ\text{C}$$

Since $T_1 > T_{\text{sat}}$ the state is superheated. Going to Table A-6 @ $P_1 = 7\text{MPa}$ & $T_1 = 450^\circ\text{C}$ shows

$$s_1 := 6.6353 \frac{\text{kJ}}{\text{kg}\cdot\text{K}} \quad h_1 := 3288.3 \frac{\text{kJ}}{\text{kg}}$$

It's known for a throttling value the enthalpy remains constant so

$$h_2 := h_1 = 3288.3 \text{ K} \cdot \frac{\text{kJ}}{\text{kg}\cdot\text{K}}$$

Going to Table A-5 @ $P_2 = 3000\text{kPa}$ shows

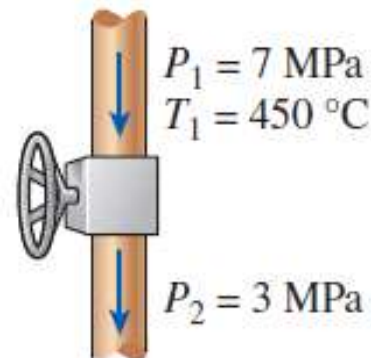
$$h_g := 2803.2 \frac{\text{kJ}}{\text{kg}}$$

Since $h_2 > h_g$ the state is superheated. Going to Table A-6 @ $P_2 = 3\text{MPa}$ & $h_2 = 3288.3 \frac{\text{kJ}}{\text{kg}}$ shows that interpolation is needed.

$$h_a := 3231.7 \frac{\text{kJ}}{\text{kg}} \quad h_b := 3344.9 \frac{\text{kJ}}{\text{kg}}$$

$$s_a := 6.9235 \frac{\text{kJ}}{\text{kg}\cdot\text{K}} \quad s_b := 7.0856 \frac{\text{kJ}}{\text{kg}\cdot\text{K}}$$

$$s_2 := \frac{h_2 - h_a}{h_b - h_a} \cdot (s_b - s_a) + s_a = 7.005 \frac{\text{kJ}}{\text{kg}\cdot\text{K}}$$



Solution (contd.):

The specific entropy generation is then

$$s_{\text{gen}} := s_2 - s_1 = 0.3693 \cdot \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

The Second Law of Thermodynamics is satisfied because s_{gen} is not negative.

It should be noted that the increase in entropy is a result of unrestrained expansion.