Given and Required:

$$kJ := 1000J$$

Determine the specific volume of R-134a at 1 MPa and 50°C. Use the ideal gas equation and also use the compressibility chart. What is it listed as in the tables in the back of your textbook?

$$P_1 := 1 MPa$$
 $T_1 := 50 \,^{\circ}C$

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Solution:

Going to Table A-1 @ R-134a shows

$$R_{R134a} := 0.08149 \frac{kJ}{kg \cdot K}$$
 $T_{cr} := 374.2K$ $P_{cr} := 4.059MPa$

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Beginning with the IGL.

$$P \cdot V = m \cdot R \cdot T$$

Solving for specific volume yields

$$\nu = \frac{V}{m} = \frac{R \cdot T}{P}$$

$$v = \frac{V}{m} = \frac{R \cdot T}{P}$$
 or $v_a := \frac{R_{R134a} \cdot T_1}{P_1} = 0.02633 \frac{m^3}{kg}$

To use the compressibility chart, the reduce temperature and pressure values, T_R and P_R, must be calculated. This is shown below.

$$T_R := \frac{T_1}{T_{or}} = 0.864$$

$$T_R := \frac{T_1}{T_{cr}} = 0.864$$
 $P_R := \frac{P_1}{P_{cr}} = 0.246$

Going to Figure A-15 @ $T_R = 0.864 \,$ & $P_R = 0.246 \,$ shows

$$z := 0.84$$

Now the specific volume may be calculated with the compressibility factor accounted for. This is shown below.

$$\nu = \frac{V}{m} = z \cdot \frac{R \cdot T}{R}$$

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 or $v_b := z \cdot \frac{R_{R134a} \cdot T_1}{P_1} = 0.02212 \frac{m^3}{\text{kg}}$

To look up the specific volume from the table, we start at Table A-12 @ $P := P_1 = 1000 \, kPa$ showing

$$T_{sat} := 39.37 \,^{\circ}C$$

Since the temperature is greater than the saturation temperature at the pressure given (i.e. $T_1 > T_{sat}$), the state is superheated. Going to Table A-13 @ P := P $_1$ = $1 \cdot MPa$ & T := T $_1$ = $50 \cdot ^{\circ}C$ shows

$$\nu_{\rm c} := 0.021796 \frac{{\rm m}^3}{{\rm kg}}$$

Comparing the results of using the IGL and the method using compressibility chart to the table values shows the percent error as

$$e_a := \left| \frac{v_a - v_c}{v_a} \right| = 20.818 \cdot \%$$

$$\%e_{a} := \left| \frac{\nu_{a} - \nu_{c}}{\nu_{c}} \right| = 20.818 \cdot \%$$
 $\%e_{b} := \left| \frac{\nu_{b} - \nu_{c}}{\nu_{c}} \right| = 1.487 \cdot \%$

It should be noted that the table value is considered the most accurate of the three methods and for this reason the other two methods are compared to it.