

Given: $\text{kJ} := 1000\text{J}$ $\text{kmol} := 1000\text{mol}$

Air at 300 K and 200 kPa is heated at constant pressure to 600 K.

Required:

Determine the change in internal energy of air per unit mass, using

- (a) data from the air table
- (b) the functional form of the specific heat
- (c) the average specific heat value

Solution:

The given temperatures and pressure are defined below.

$$T_1 := 300\text{K} \quad P_0 := 200\text{kPa} \quad T_2 := 600\text{K}$$

Going to Table A-17 @ $T_1 = 300\text{K}$ and $T_2 = 600\text{K}$ shows

$$u_1 := 214.07 \frac{\text{kJ}}{\text{kg}} \quad u_2 := 434.78 \frac{\text{kJ}}{\text{kg}}$$

The change of specific internal energy is then

$$\Delta u_a := u_2 - u_1 = 220.71 \frac{\text{kJ}}{\text{kg}} \quad (\text{a})$$

Going to Table A-2(c) @ air shows

$$a := 28.11 \quad b := 0.1967 \cdot 10^{-2} \quad c := 0.4802 \cdot 10^{-5} \quad d := -1.966 \cdot 10^{-9}$$

Thus the molar specific heat at constant pressure of air is given by

$$\bar{c}_p(T) := \left[a + b \cdot \frac{T}{\text{K}} + c \cdot \left(\frac{T}{\text{K}} \right)^2 + d \cdot \left(\frac{T}{\text{K}} \right)^3 \right] \cdot \frac{\text{kJ}}{\text{kmol} \cdot \text{K}}$$

The molar specific heat at constant volume for an ideal gas is then given by

$$\bar{c}_v(T) := \bar{c}_p(T) - R_u \quad \text{where} \quad R_u := 8.314 \frac{\text{kJ}}{\text{kmol} \cdot \text{K}}$$

The molar change of internal energy of air is then given by

$$\Delta \bar{u} := \int_{T_1}^{T_2} \bar{c}_v(T) dT = 6447 \frac{\text{kJ}}{\text{kmol}}$$

Going to Table A-1 @ air shows

$$M_{\text{air}} := 28.97 \frac{\text{kg}}{\text{kmol}}$$

The change of specific internal energy is then

$$\Delta u_b := \frac{\Delta \bar{u}}{M_{\text{air}}} = 222.546 \frac{\text{kJ}}{\text{kg}} \quad (\text{b})$$

Solution (cont.):

The average temperature between the two states is

$$\bar{T} := \frac{T_1 + T_2}{2} = 450 \text{ K}$$

Going to Table A-2(b) @ $\bar{T} = 450 \text{ K}$ shows

$$c_v := 0.733 \frac{\text{kJ}}{\text{kg}}$$

The change of specific internal energy is then

$$\boxed{\Delta u_c := c_v (T_2 - T_1) = 219.9 \text{ K} \frac{\text{kJ}}{\text{kg}}} \quad (\text{c})$$