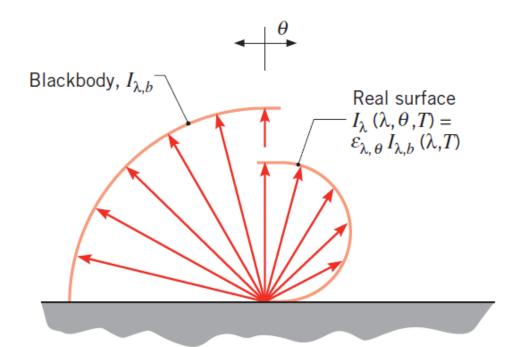
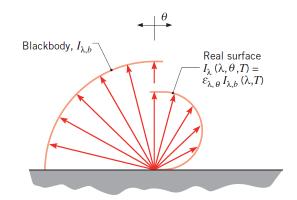
### **Surface Radiation**



#### Surface Emissivity

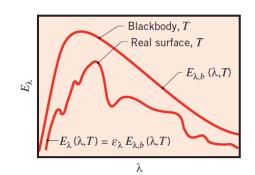
- Radiation emitted by a surface may be determined by introducing a property (the emissivity) that contrasts its emission with the ideal behavior of a blackbody at the same temperature.
- The definition of the emissivity depends upon one's interest in resolving directional and/or spectral features of the emitted radiation, in contrast to averages over all directions (hemispherical) and/or wavelengths (total).
- The spectral, directional emissivity:

$$\varepsilon_{\lambda,\theta}\left(\lambda,\theta,\phi,T\right) \equiv \frac{I_{\lambda,e}\left(\lambda,\theta,\phi,T\right)}{I_{\lambda,b}\left(\lambda,T\right)}$$



• The spectral, hemispherical emissivity (a directional average):

$$\varepsilon_{\lambda}\left(\lambda,T\right) \equiv \frac{E_{\lambda}\left(\lambda,T\right)}{E_{\lambda,b}\left(\lambda,T\right)} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi/2} I_{\lambda,e}\left(\lambda,\theta,\phi,T\right) \cos\theta \sin\theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi/2} I_{\lambda,b}\left(\lambda,T\right) \cos\theta \sin\theta d\theta d\phi}$$



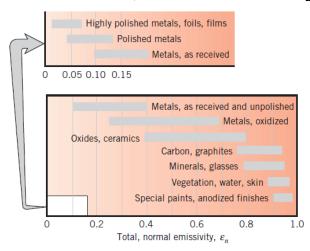
• The total, hemispherical emissivity (a directional and spectral average):

$$\varepsilon(T) \equiv \frac{E(T)}{E_b(T)} = \frac{\int_0^\infty \varepsilon_\lambda(\lambda, T) E_{\lambda, b}(\lambda, T) d, \lambda}{E_b(T)}$$

• To a reasonable approximation, the hemispherical emissivity is equal to the normal emissivity.

$$\varepsilon \approx \varepsilon_n$$

• Representative values of the total, normal emissivity:

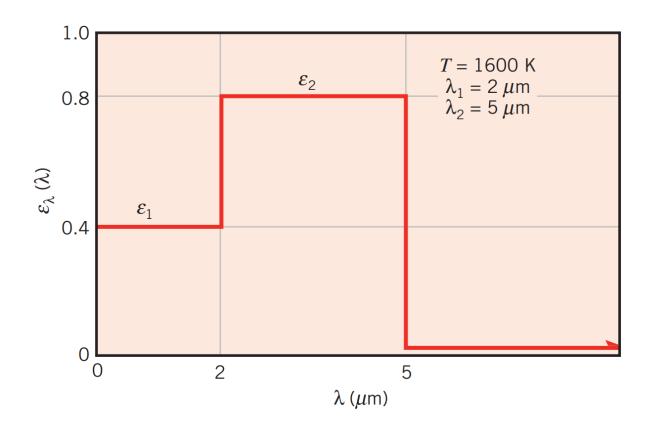


Note:

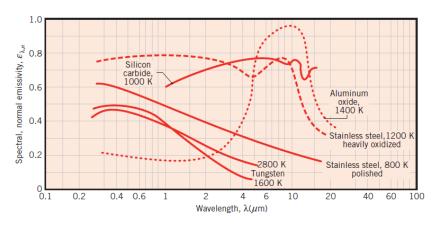
- Low emissivity of polished metals and increasing emissivity for unpolished and oxidized surfaces.
- Comparatively large emissivities of nonconductors.

## Example 1

A diffuse surface at 1600 *K* has the spectral, hemispherical emissivity shown as follows. Determine the total, hemispherical emissivity and the total emissive power.

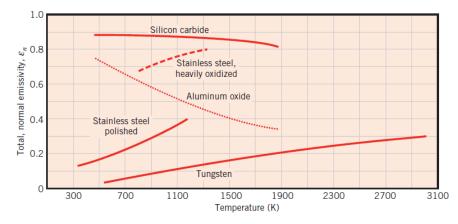


• Representative spectral variations:



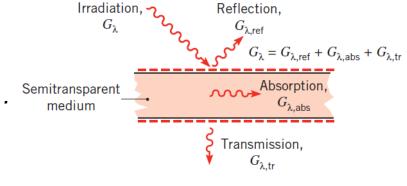
Note decreasing  $\mathcal{E}_{\lambda,n}$  with increasing  $\lambda$  for metals and different behavior for nonmetals.

• Representative temperature variations:



# Response to Surface Irradiation: Absorption, Reflection and Transmission

- There may be three responses of a semitransparent medium to irradiation:
  - $\triangleright$  Reflection from the medium  $(G_{\lambda,\text{ref}})$ .
  - $\triangleright$  Absorption within the medium  $(G_{\lambda,abs})$ .
  - ightharpoonup Transmission through the medium  $(G_{\lambda, \text{tr}})$ .



Radiation balance ----

$$G_{\lambda} = G_{\lambda, \text{ref}} + G_{\lambda, \text{abs}} + G_{\lambda, \text{tr}}$$

• In contrast to the foregoing volumetric effects, the response of an opaque material to irradiation is governed by surface phenomena and  $G_{\lambda,tr} = 0$ .

$$G_{\lambda} = G_{\lambda, \text{ref}} + G_{\lambda, \text{tr}}$$

• The wavelength of the incident radiation, as well as the nature of the material, determine whether the material is semitransparent or opaque.

#### Absorptivity of an Opaque Material

• The spectral, directional absorptivity: Assuming negligible temperature dependence,

$$\alpha_{\lambda,\theta}(\lambda,\theta,\phi) \equiv \frac{I_{\lambda,i,abs}(\lambda,\theta,\phi)}{I_{\lambda,i}(\lambda,\theta,\phi)}$$

• The spectral, hemispherical absorptivity:

$$\alpha_{\lambda}(\lambda) \equiv \frac{G_{\lambda,\text{abs}}(\lambda)}{G_{\lambda}(\lambda)} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi/2} \alpha_{\lambda,\theta}(\lambda,\theta,\phi) I_{\lambda,i}(\lambda,\theta,\phi) \cos\theta \sin\theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi/2} I_{\lambda,i}(\lambda,\theta,\phi) \cos\theta \sin\theta d\theta d\phi}$$

• The total, hemispherical absorptivity:

$$\alpha \equiv \frac{G_{\rm abs}}{G} = \frac{\int_{o}^{\infty} \alpha_{\lambda}(\lambda) G_{\lambda}(\lambda) d\lambda}{\int_{0}^{\infty} G_{\lambda}(\lambda) d\lambda}$$

#### Reflectivity of an Opaque Material

• The spectral, directional reflectivity: Assuming negligible temperature dependence:

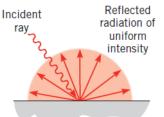
$$\rho_{\lambda,\theta}(\lambda,\theta,\phi) \equiv \frac{I_{\lambda,i,\text{ref}}(\lambda,\theta,\phi)}{I_{\lambda,i}(\lambda,\theta,\phi)}$$

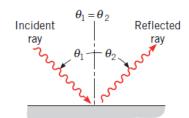
• The spectral, hemispherical reflectivity:

$$\rho_{\lambda} \equiv \frac{G_{\lambda, \text{ref}}\left(\lambda\right)}{G_{\lambda}\left(\lambda\right)} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi/2} \rho_{\lambda, \theta}\left(\lambda, \theta, \phi\right) I_{\lambda, i}\left(\lambda, \theta, \phi\right) \cos\theta \sin\theta d\theta d\phi}{I_{\lambda, i}\left(\lambda, \theta, \phi\right)}$$

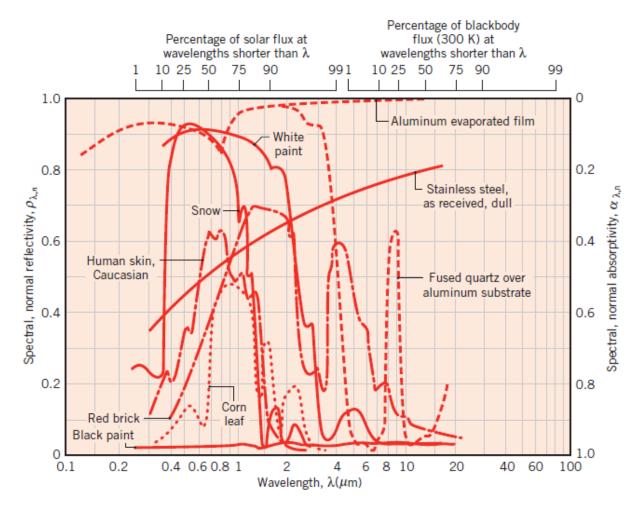
• The total, hemispherical reflectivity:

$$\rho \equiv \frac{G_{\text{ref}}}{G} = \frac{\int_{0}^{\infty} \rho_{\lambda}(\lambda) G_{\lambda}(\lambda) d\lambda}{\int_{0}^{\infty} G_{\lambda}(\lambda) d\lambda}$$





• Limiting conditions of diffuse and specular reflection. Polished and rough surfaces.

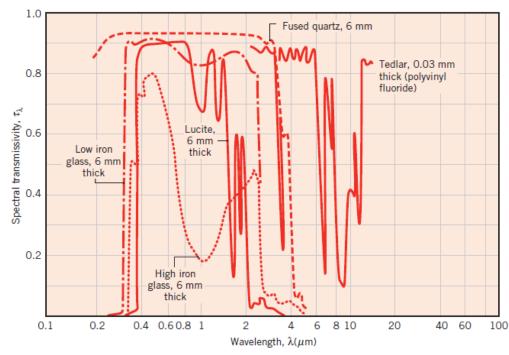


- $\triangleright$  Note strong dependence of  $\rho_{\lambda}$  (and  $\alpha_{\lambda} = 1 \rho_{\lambda}$ ) on  $\lambda$ .
- ➤ Is snow a highly reflective substance? White paint?

#### **Transmissivity**

• The spectral, hemispherical transmissivity: Assuming negligible temperature dependence,

$$au_{\lambda} \equiv \frac{G_{\lambda, \mathrm{tr}}(\lambda)}{G_{\lambda}(\lambda)}$$



Note shift from semitransparent to opaque conditions at large and small wavelengths.

• The total, hemispherical transmissivity:

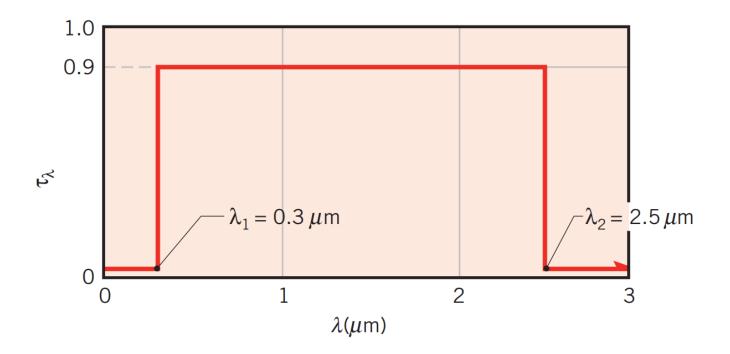
$$\tau \equiv \frac{G_{\rm tr}}{G} = \frac{\int_0^\infty G_{\lambda,\rm tr}(\lambda) d\lambda}{\int_0^\infty G_{\lambda}(\lambda) d\lambda}$$

• For a semitransparent medium,

$$\rho_{\lambda} + \alpha_{\lambda} + \tau_{\lambda} = 1$$
$$\rho + \alpha + \tau + 1$$

### Example 2

The cover glass on a flat-plate solar collector has a low iron content, and its spectral transmissivity may be approximated by the following distribution. What is the total transmissivity of the cover glass to solar radiation?



#### Kirchhoff's Law

• Kirchhoff's law equates the total, hemispherical emissivity of a surface to its total, hemispherical absorptivity:

$$\varepsilon = \alpha$$

However, conditions associated with its derivation are highly restrictive:

Irradiation of the surface corresponds to emission from a blackbody at the same temperature as the surface.

• But, Kirchhoff's law may be applied to the spectral, directional properties without restriction:

$$\varepsilon_{\lambda,\theta} = \alpha_{\lambda,\theta}$$

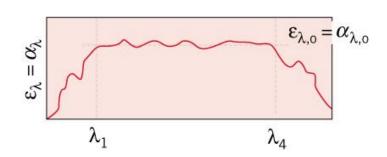
#### Diffuse/Gray Surfaces

• With

$$\varepsilon_{\lambda} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi/2} \varepsilon_{\lambda,\theta} \cos \theta \sin \theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi/2} \cos \theta \sin \theta d\theta d\phi}$$

and

$$\alpha_{\lambda} = \frac{\int_{0}^{2\pi} \int_{0}^{\pi/2} \alpha_{\lambda,\theta} I_{\lambda,i} \cos \theta \sin \theta d\theta d\phi}{\int_{0}^{2\pi} \int_{0}^{\pi/2} I_{\lambda,i} \cos \theta \sin \theta d\theta d\phi}$$

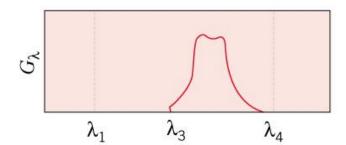


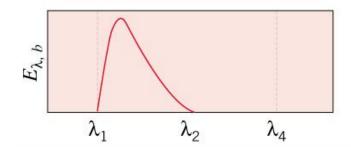
• With

$$\varepsilon = \frac{\int_0^\infty \varepsilon_{\lambda} E_{\lambda,b}(\lambda) d\lambda}{E_b(T)}$$

and

$$\alpha = \frac{\int_0^\infty \alpha_{\lambda} G_{\lambda}(\lambda) d\lambda}{G}$$





## Example 3

A diffuse, fire brick wall of temperature  $T_s = 500K$  has the spectral emissivity shown and is exposed to a bed of coals at 2000 K. Determine the total, hemispherical emissivity and emissive power of the fire brick wall. What is the total absorptivity of the wall to irradiation resulting from emission by the coals?

