$$\begin{split} m &= \rho \forall \\ & \dot{\forall} = \frac{\forall}{t} \\ q &= mc_p \Delta T \\ q &= -kA\frac{dT}{dt} & \frac{1}{r^2}\frac{\partial}{\partial t} \\ q &= hA\left(T_s - T_\infty\right) & \frac{1}{r^2}\frac{\partial}{\partial t} \\ q &= \delta A\left(T_s^4 - T_{sur}^4\right) & \frac{\partial}{\partial t} \\ \sigma &= 5.67 \times 10^{-8}\frac{W}{m^2K^4} \\ \Delta E_{sys} &= \Sigma E_{in} - \Sigma E_{out} & \frac{1}{r^2\sin\theta}\frac{\partial}{\partial t} \\ q'' &= -k_x\frac{\partial T}{\partial t}\hat{i} - k_y\frac{\partial T}{\partial y}\hat{j} - k_z\frac{\partial T}{\partial z}\hat{k} & \frac{1}{r^2\sin\theta}\frac{\partial}{\partial t} \\ k &= \frac{9\gamma - 5}{4}\frac{c}{\pi d^2}\sqrt{\frac{M_{wk}B^T}{N_A\pi}} & \frac{1}{r^2\sin\theta}\frac{\partial}{\partial t} \\ k_B &= 1.381 \times 10^{-23}\frac{J}{K} \\ N_A &= 6.022 \times 10^{23} & \frac{1}{r^2\sin\theta}\frac{\partial}{\partial t} \\ q_{x+dx} &= q_x + \frac{\partial q_x}{\partial x}dx & \frac{1}{r^2\sin\theta}\frac{\partial}{\partial t} \\ q_{x+dz} &= q_z + \frac{\partial q_z}{\partial z}dz & \frac{1}{r^2\sin\theta}\frac{\partial}{\partial t} \\ \frac{\partial}{\partial x}\left(k\frac{\partial T}{\partial x}\right) + \frac{\partial}{\partial y}\left(k\frac{\partial T}{\partial y}\right) + \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right) + \\ \dot{q} &= \rho c_p\frac{\partial T}{\partial t} & -k\frac{\partial T}{\partial z} \\ \frac{\partial}{\partial x}\left(k\frac{\partial T}{\partial x}\right) + \frac{\partial}{\partial y}\left(k\frac{\partial T}{\partial y}\right) + \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right) + \\ \dot{q} &= 0 & q = \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial x}\right) + \dot{q} &= \rho c_p\frac{\partial T}{\partial t} \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial$$

$$\begin{array}{c} \frac{1}{r}\frac{\partial}{\partial r}\left(kr\frac{\partial T}{\partial r}\right)+\frac{1}{r^2}\frac{\partial}{\partial \phi}\left(k\frac{\partial T}{\partial \phi}\right)+\\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right)+\dot{q}=0 \\ \\ \frac{1}{r}\frac{\partial}{\partial r}\left(kr\frac{\partial T}{\partial r}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t} \\ \\ \frac{1}{r^2}\frac{\partial}{\partial \phi}\left(k\frac{\partial T}{\partial \phi}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t} \\ \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t} \\ \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t} \\ \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t} \\ \\ \frac{\partial}{\partial z}\left(k\frac{\partial T}{\partial z}\right)+\frac{1}{r^2}\frac{1}{\sin^2\theta}\frac{\partial}{\partial \phi}\left(k\frac{\partial T}{\partial \phi}\right)+\\ \\ \frac{1}{r^2}\frac{\partial}{\partial r}\left(kr^2\frac{\partial T}{\partial r}\right)+\frac{1}{r^2\sin^2\theta}\frac{\partial}{\partial \phi}\left(k\frac{\partial T}{\partial \phi}\right)+\\ \\ \frac{1}{r^2}\frac{\partial}{\partial r}\left(kr^2\frac{\partial T}{\partial r}\right)+\frac{1}{r^2\sin^2\theta}\frac{\partial^2 C}{\partial \phi}+\\ \\ \frac{1}{r^2}\frac{\partial}{\partial r}\left(kr^2\frac{\partial T}{\partial r}\right)+\frac{1}{r^2\sin^2\theta}\frac{\partial}{\partial \phi}\left(k\frac{\partial T}{\partial \phi}\right)+\\ \\ \frac{1}{r^2}\frac{\partial}{\partial r}\left(kr^2\frac{\partial T}{\partial r}\right)+\frac{1}{r^2\sin^2\theta}\frac{\partial}{\partial \phi}\left(k\frac{\partial T}{\partial \phi}\right)+\\ \\ \frac{1}{r^2\sin\theta}\frac{\partial}{\partial \theta}\left(k\sin\theta\frac{\partial T}{\partial \theta}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t}\\ \\ \frac{\partial T}{\partial \phi}\left(k\sin\theta\frac{\partial T}{\partial \theta}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t}\\ \\ \frac{\partial T}{\partial \phi}\left(k\sin\theta\frac{\partial T}{\partial \theta}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t}\\ \\ \frac{\partial T}{\partial \phi}\left(k\sin\theta\frac{\partial T}{\partial \theta}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t}\\ \\ \frac{\partial T}{\partial \phi}\left(k\sin\theta\frac{\partial T}{\partial \theta}\right)+\dot{q}=\rho c_p\frac{\partial T}{\partial t}\\ \\ \frac{\partial T}{\partial \phi}\left(k\sin\theta\frac{\partial T}{$$

$$\eta_{o} = 1 - \frac{NA_{f}}{A_{t}} (1 - \eta_{f})$$

$$R_{t,o} = \frac{\theta_{b}}{q_{t}} = \frac{1}{\eta_{o}hA_{t}}$$

$$\frac{u(y)}{u_{\infty}} = 0.99$$

$$C_{f} = \frac{\tau_{s}}{\rho u_{\infty}^{2}/2}$$

$$\tau_{s} = \mu \frac{\partial u}{\partial y} \Big|_{y=0}$$

$$\frac{T_{s}-T(y)}{T_{s}-T_{\infty}} = 0.99$$

$$q_{s}'' = -k \frac{\partial T}{\partial y} \Big|_{y=0}$$

$$q_{s}'' = h (T_{s} - T_{\infty})$$

$$h = \frac{-k \frac{\partial T}{\partial y}}{T_{s}-T_{\infty}}$$

$$q = \int_{A_{s}} q'' dA_{s} = (T_{s} - T_{\infty}) \int_{A_{s}} h dA_{s}$$

$$\bar{q}'' = \bar{h} (T_{s} - T_{\infty})$$

$$\bar{q} = \bar{q}'' A_{s} = \bar{h} A_{s} (T_{s} - T_{\infty})$$

$$\bar{h} = \frac{1}{A_{s}} \int_{A_{s}} h dA_{s}$$

$$\bar{h} = \frac{1}{L} \int_{0}^{L} h dx$$

$$Re_{x} = \frac{\rho u_{\infty} x}{\mu}$$

$$x^{*} = \frac{x}{L}$$

$$y^{*} = \frac{y}{L}$$

$$u^{*} = \frac{u}{V}$$

$$V^{*} = \frac{V}{V}$$

$$T^{*} = \frac{T - T_{s}}{T_{\infty} - T_{s}}$$

$$p^{*} = \frac{\rho \infty}{\rho V^{2}}$$

$$u^{*} \frac{\partial u^{*}}{\partial x^{*}} + v^{*} \frac{\partial u^{*}}{\partial y^{*}} = -\frac{dp^{*}}{dx^{*}} + \frac{1}{Re_{L}} \frac{\partial^{2} u^{*}}{\partial y^{*2}}$$

$$Re_{L} = \frac{VL}{\nu}$$

$$\nu = \frac{\mu}{\rho}$$

$$u^{*} \frac{\partial T^{*}}{\partial x^{*}} + v^{*} \frac{\partial T^{*}}{\partial y^{*}} = \frac{1}{Re_{L} Pr} \frac{\partial^{2} T^{*}}{\partial y^{*2}}$$

$$Pr = \frac{\nu}{\alpha}$$

$$Nu = \frac{hL}{k} = \frac{\partial T^{*}}{\partial y^{*}}|_{y^{*}=0}$$

$$\overline{Nu} = \frac{\overline{hL}}{k}$$

$$T_{f} = \frac{T_{s} + T_{\infty}}{2}$$

$$C_{f,x} = \frac{\tau_{s,x}}{\frac{\rho u_{\infty}^2}{2}} = 0.664 Re_x^{-1/2}$$

$$Nu_x = \frac{h_x x}{k} = 0.332 Re_x^{1/2} Pr^{1/3}$$

$$(Pr \gtrsim 0.6)$$

$$\overline{C}_{f,x} = 1.328 Re_x^{-1/2}$$

$$\overline{Nu}_x = \frac{\overline{h}_x x}{k} = 0.664 Re_x^{1/2} Pr^{1/3}$$

$$(Pr \gtrsim 0.6)$$

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$$\overline{Nu}_x = \frac{\overline{h}_x x}{k} = 0.664Re_x^{1/2}Pr^{1/3}$$

$$(Pr \gtrsim 0.6)$$
Turbulent:
$$\delta = 0.37xRe_x^{-1/2}$$

$$C_{f,x} = 0.0592Re_x^{-1/5}$$

$$(Re_{x,c} \lesssim Re_x \lesssim 10^8)$$

$$Nu_x = 0.0296Re_x^{4/5}Pr^{1/3}$$

$$(0.6 \lesssim Pr \lesssim 60)$$

$$A = 0.037Re_{x,c}^{4/5} - 0.664Re_{x,c}^{1/2}$$

$$\overline{C}_{f,L} = 0.074Re_L^{-1/5} - \frac{2A}{Re_L}$$

$$(Re_{x,c} \lesssim Re_L \lesssim 10^8)$$

$$\overline{Nu}_L = \begin{pmatrix} 0.037Re_L^{4/5} - A \end{pmatrix} Pr^{1/3}$$

$$(0.6 \lesssim Pr \lesssim 60)$$

$$(Re_{x,c} \lesssim Re_L \lesssim 10^8)$$

$$Re_D = \frac{\rho VD}{\mu} = \frac{VD}{\nu}$$

$$C_D = \frac{F_D}{A_f \left(\frac{\rho V^2}{2}\right)}$$

$$Re_D = \frac{\rho VD}{\mu} = \frac{VD}{\nu}$$

$$C_D = \frac{F_D}{A_f\left(\frac{\rho V^2}{2}\right)}$$

Cylinder $\overline{Nu}_D = \frac{\overline{h}D}{k} = CRe_D^m Pr^{1/3}$ $(Pr \gtrsim 0.7)$ See Table 4

<u>Isothermal Flat Plate</u>

$$\frac{\delta}{\delta_t} \approx P r^{1/3}$$

Laminar:

$$\delta = \frac{5}{\sqrt{\frac{u_{\infty}}{v_{x}}}} = \frac{5x}{\sqrt{Re_{x}}}$$

Various Geometries

$$\overline{Nu}_D = \frac{\overline{h}D}{k} = CRe_D^m P r^{1/3}$$

$$(Pr \gtrsim 0.7)$$
See Table 5

Sphere

$$A_s = \pi D^2$$

$$C_D = \frac{25}{Re_D}$$

$$(Re_D \lesssim 0.5)$$

$$\overline{Nu}_{D} = 2 + \left(0.4Re_{D}^{1/2} + 0.06Re_{D}^{2/3}\right)Pr^{0.4}\left(\frac{\mu}{\mu_{s}}\right)^{1/4}$$

$$(0.71 \lesssim Pr \lesssim 380)$$

$$\left(3.5 \lesssim Re_{D} \lesssim 7.6 \times 10^{4}\right)$$

$$\left(1.0 \lesssim \frac{\mu}{\mu_{s}} \lesssim 3.2\right)$$

$$m = \rho u_m A_c$$

$$Re_D = \frac{\rho u_m D}{\mu} = \frac{u_m D}{\nu}$$

$$\left(\frac{x_{fd,t}}{D}\right) \approx 0.05 Re_D Pr$$

$$f = \frac{-\frac{dP}{dx}D}{\rho \frac{u_m^2}{2}}$$

$$f = \frac{6^2}{Re_D}$$

$$\frac{1}{\sqrt{f}} = -2.0 \log \left[\frac{e/D}{3.7} + \frac{2.51}{Re_D \sqrt{f}}\right]$$

$$dq_{conv} = mc_p \left[(T_m + dT_m) - T_m \right] =$$

$$mc_p dT_m$$

$$dq_{conv} = q_s'' P dx$$

$$\frac{dT_m}{dx} = \frac{q_s'' P}{mc_p} = \frac{P}{mc_p} h \left(T_s - T_m \right)$$

$$T_m \left(x \right) = T_{m,i} + \frac{q_s'' P}{mc_p} x$$

$$\Delta T = T_s - T_m$$

$$\frac{dT_m}{dx} = -\frac{d(\Delta T)}{dx} = \frac{P}{mc_p} h \Delta T$$

$$\frac{T_s - T_m(x)}{T_s - T_{m,i}} = e^{-\frac{Px}{mc_p} h}$$

$$\Delta T_{lm} = \frac{\Delta T_o - \Delta T_i}{\ln\left(\frac{\Delta T_o}{\Delta T_i}\right)}$$

$$\Delta T_o = T_s - T_{m,o}$$

$$\Delta T_i = T_s - T_{m,i}$$
$$q_{conv} = \overline{h} A_s \Delta T_{lm}$$

Circular Tubes

Fully dev. lam. w/
$$q^{''}=\mathbb{C}$$
:
$$Nu_D=4.36$$

Fully dev. lam. w/
$$T_s = \mathbb{C}$$
:
$$Nu_D = 3.66$$

Fully dev. turb. w/ small ΔT :

$$Nu_D = 0.023 Re_D^{4/5} Pr^n$$

 $n = 0.4, \quad T_s > T_m$
 $n = 0.3, \quad T_s < T_m$
 $(0.6 \lesssim Pr \lesssim 160)$
 $(Re_D \gtrsim 10,000)$
 $(L/D \gtrsim 10)$

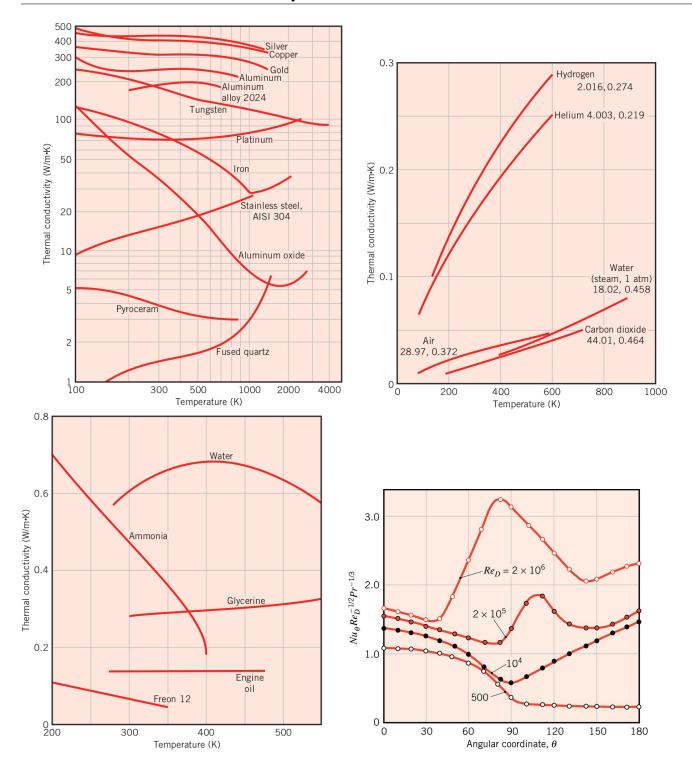
Fully dev. turb. w/ large ΔT : $Nu_D = 0.027 Re_D^{4/5} P r^{1/3} \left(\frac{\mu}{\mu_s}\right)^{0.14}$ $(0.7 \lesssim Pr \lesssim 16,700)$ $(Re_D \gtrsim 10,000)$ $(L/D \gtrsim 10)$

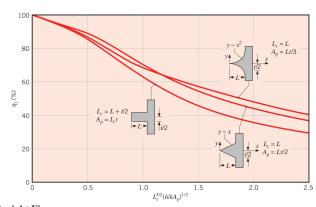
.....

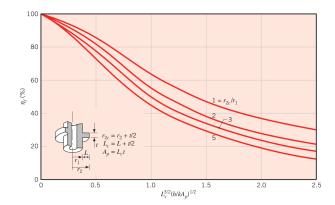
Noncircular Tubes

$$D_h = \frac{4A_c}{P}$$

$$Nu_D = \frac{hD_h}{k}$$
See Table 6







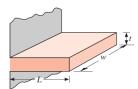
Straight Fins

Rectangular

$$A_f = 2wL_c$$

$$L_c = L + (t/2)$$

 $A_p = tL$

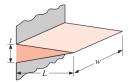


$$\eta_f = \frac{\tanh mL_c}{mL_c}$$

Triangular

$$A_f = 2w[L^2 + (t/2)^2]^{1/2}$$

 $A_p = (t/2)L$



$$\eta_f = \frac{1}{mL} \frac{I_1(2mL)}{I_0(2mL)}$$

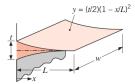
Parabolic

$$A_f = w[C_1L +$$

$$(L^2/t)\ln(t/L + C_1)$$

$$C_1 = [1 + (t/L)^2]^{1/2}$$

 $A_p = (t/3)L$



$$\eta_f = \frac{2}{[4(mL)^2 + 1]^{1/2} + 1}$$

Pin Fins

Rectangular

$$A_f = \pi D L_c$$

$$L_c = L + (D/4)$$

 $V = (\pi D^2/4)L$



$$\eta_f = \frac{\tanh mL_c}{mL_c}$$

Triangular

$$A_f = \frac{\pi D}{2} \left[L^2 + (D/2)^2 \right]^{1/2}$$

 $V=(\pi/12)D^2L$



$$\eta_f = \frac{2}{mL} \frac{I_2(2mL)}{I_1(2mL)}$$

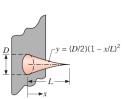
Parabolic

$$\begin{split} A_f &= \frac{\pi L^3}{8D} \left\{ C_3 C_4 - \frac{L}{2D} \ln \left[(2DC_4/L) + C_3 \right] \right\} \end{split}$$

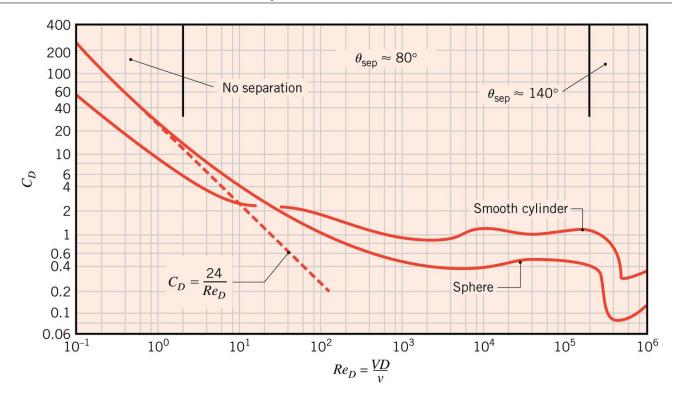
$$C_3 = 1 + 2(D/L)^2$$

$$C_4 = [1 + (D/L)^2]^{1/2}$$

 $V = (\pi/20)D^2 L$



$$\eta_f = \frac{2}{[4/9(mL)^2 + 1]^{1/2} + 1}$$



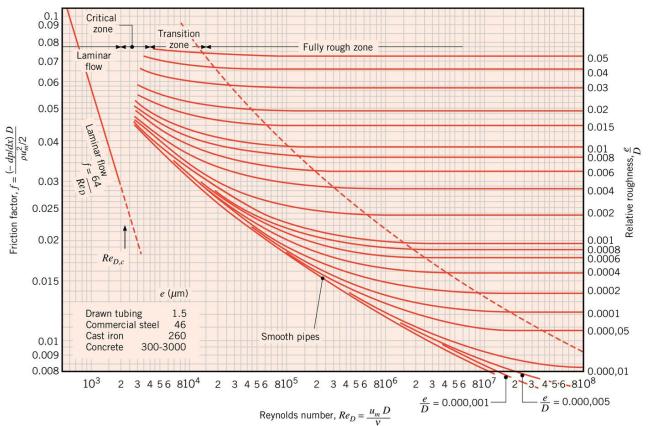


Table 1: Contact Resistance for vacuum interfaces, $R_{t,c}^{''}\times 10^4\left(\frac{m^2K}{W}\right)$

Material	100 (kPa)	10,000 (kPa)
Stainless Steel	6-25	0.7-4.0
Copper	1-10	0.1 - 0.5
Magnesium	1.5 - 3.5	0.2-0.4
Aluminum	1.5 - 5.0	0.2-0.4

Table 2: Contact Resistance for aluminum ($10\mu m$ surface roughness, 10kPa contact pressure)

Interfacial Fluid	$R_{t,c}^{"} \times 10^4 \left(\frac{m^2 K}{W}\right)$
Air	2.75
Helium	1.05
Hydrogen	0.720
Silicone Oil	0.525
Glycerine	0.265

Table 3: Fin Tip Conditions

Case	Tip Condition	Temperature Distribution $\frac{\theta}{\theta_b}$	Fin Heat Transfer Rate q_f
A	Convection	$\frac{\cosh m(L-x) + \left(\frac{h}{mk}\right) \sinh m(L-x)}{\cosh mL + \left(\frac{h}{mK}\right) \sinh mL}$	$M \frac{\sinh mL + \left(\frac{h}{mk}\right) \cosh mL}{\cosh mL + \left(\frac{h}{mk}\right) \sinh mL}$
В	Adiabatic	$\frac{\cosh m(L-x)}{\cosh mL}$	M anh mL
C	Constant Temperature	$\frac{\left(\frac{\theta_L}{\theta_b}\right)\sinh mx + \sinh m(L-x)}{\sinh mL}$	$M \frac{\cosh mL - \frac{\theta_L}{\theta_b}}{\sinh mL}$
D	Infinite Fin $(L \to \infty)$	e^{-mx}	M

Table 4: Cylinder In Cross Flow

Re_D	C	m
0.4 - 4	0.989	0.330
4 - 40	0.911	0.385
40 - 4000	0.683	0.466
4000 - 40,000	0.193	0.618
40,000 - 400,000	0.027	0.805

Table 5: Various Geometries In Cross Flow

Geometry	Re_D	C	m
$V \rightarrow \bigcirc \qquad \stackrel{\uparrow}{D} \qquad \qquad \downarrow$	6000 - 60,000	0.304	0.59
$V \rightarrow $	5000 - 60,000	0.158	0.66
$V \rightarrow \bigcirc \qquad \stackrel{\uparrow}{\downarrow}$	5200 - 20,400 20,400 - 105,000	0.164 0.039	0.638 0.78
$V \longrightarrow \qquad \qquad \downarrow \qquad \qquad \downarrow$	4500 - 90,700	0.150	0.638
$V \longrightarrow \begin{bmatrix} & & \\ D & & \\ & & \\ & & \\ & & \\ \end{bmatrix} $ Front	10,000 - 50,000 7,000 - 80,000	$0.667 \\ 0.191$	$0.500 \\ 0.667$

Table 6: Noncircular Tubes

Cross Section	$\frac{b}{a}$	Uniform $q_s^{''}$	Uniform T_s	fRe_{D_h}
		4.36	3.66	64
a	1.0	3.61	2.98	57
<i>ab</i>	1.43	3.73	3.08	59
<i>a b</i>	2.0	4.12	3.39	62
<i>a b</i>	3.0	4.79	3.96	69
<i>ab</i>	4.0	5.33	4.44	73
Heated	∞	8.23	7.54	96
CASSA ASSA ASSA Insulated	∞	5.39	4.86	96
		3.11	2.49	53