STAT 812: Computational Statistics

Introduction to R Programming

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1	Vector	
a <	<- 1	
a		
	[1] 1	
	<- 2:10	
b		
	[1] 2 3 4 5 6 7 8 9 10	
	oncatenate two vectors <- c(a,b)	
С		
##	[1] 1 2 3 4 5 6 7 8 9 10	
#ve	ector arithmetics	

```
## [1] 1.0000000 0.5000000 0.3333333 0.2500000 0.2000000 0.1666667 0.1428571
## [8] 0.1250000 0.1111111 0.1000000
       1 4 9 16 25 36 49 64 81 100
## [1]
c^2 + 1
## [1] 2 5 10 17 26 37 50 65 82 101
#apply a function to each element
log(c)
## [1] 0.0000000 0.6931472 1.0986123 1.3862944 1.6094379 1.7917595 1.9459101
## [8] 2.0794415 2.1972246 2.3025851
sapply(c,log)
## [1] 0.0000000 0.6931472 1.0986123 1.3862944 1.6094379 1.7917595 1.9459101
## [8] 2.0794415 2.1972246 2.3025851
#operation on two vectors
d <- (1:10)*10
d
## [1] 10 20 30 40 50 60 70 80 90 100
c + d
## [1] 11 22 33 44 55 66 77 88 99 110
                  90 160 250 360 490 640 810 1000
## [1]
         10
              40
d ^ c
## [1] 1.000000e+01 4.000000e+02 2.700000e+04 2.560000e+06 3.125000e+08
## [6] 4.665600e+10 8.235430e+12 1.677722e+15 3.874205e+17 1.000000e+20
#more concrete example: computing variance of 'c'
sum((c - mean(c))^2)/(length(c)-1)
## [1] 9.166667
#of course, there is build-in function for computing variance:
var(c)
## [1] 9.166667
#subsetting vector
## [1] 1 2 3 4 5 6 7 8 9 10
c[2]
## [1] 2
c[c(2,3)]
## [1] 2 3
```

```
c[c(3,2)]
## [1] 3 2
c[c > 5]
## [1] 6 7 8 9 10
#let's see what is "c > 5"
c > 5
## [1] FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE TRUE
c[c > 5 \& c < 10]
## [1] 6 7 8 9
c[as.logical((c > 8) + (c < 3))]
## [1] 1 2 9 10
log(c)
## [1] 0.0000000 0.6931472 1.0986123 1.3862944 1.6094379 1.7917595 1.9459101
## [8] 2.0794415 2.1972246 2.3025851
c[log(c) < 2]
## [1] 1 2 3 4 5 6 7
#modifying subset of vector
c[log(c) < 2] <- 3
С
## [1] 3 3 3 3 3 3 3 8 9 10
#introduce a function ``seq''
seq(0,10,by=1)
## [1] 0 1 2 3 4 5 6 7 8 9 10
seq(0,10,length=20)
## [1] 0.0000000 0.5263158 1.0526316 1.5789474 2.1052632 2.6315789
## [7] 3.1578947 3.6842105 4.2105263 4.7368421 5.2631579 5.7894737
## [13] 6.3157895 6.8421053 7.3684211 7.8947368 8.4210526 8.9473684
## [19] 9.4736842 10.0000000
1:10
## [1] 1 2 3 4 5 6 7 8 9 10
#seq is more reliable than ":"
n <- 0
1:n
## [1] 1 0
\#seq(1, n, by=1)
\#Error\ in\ seq.default(1,\ n,\ by\ =\ 1)\ :\ wrong\ sign\ in\ 'by'\ argument
#Execution halted
```

```
#function ``rep''
c<- 1:5
## [1] 1 2 3 4 5
rep(c,5)
## [1] 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5 1 2 3 4 5
rep(c,each=5)
## [1] 1 1 1 1 1 2 2 2 2 2 3 3 3 3 3 4 4 4 4 4 5 5 5 5 5
2
    Strings
A <- c("a","b","c")
## [1] "a" "b" "c"
paste("a","b",sep="")
## [1] "ab"
paste0("a","b",sep="")
## [1] "ab"
paste(A,c("d","e"))
## [1] "a d" "b e" "c d"
paste(A, 10)
## [1] "a 10" "b 10" "c 10"
paste(A,10,sep="")
## [1] "a10" "b10" "c10"
paste0(A,10)
## [1] "a10" "b10" "c10"
paste0(A,1:10)
## [1] "a1" "b2" "c3" "a4" "b5" "c6" "a7" "b8" "c9" "a10"
sprintf("unit%g.pdf", 1:10)
  [1] "unit1.pdf" "unit2.pdf" "unit3.pdf" "unit4.pdf" "unit5.pdf"
   [6] "unit6.pdf" "unit7.pdf" "unit8.pdf" "unit9.pdf" "unit10.pdf"
sprintf("unit%g.%s", 1:10, "html")
## [1] "unit1.html" "unit2.html"
                                   "unit3.html" "unit4.html" "unit5.html"
## [6] "unit6.html" "unit7.html" "unit8.html" "unit9.html" "unit10.html"
```

```
filelist <- list.files(); filelist</pre>
                                             "css"
    [1] "cauchyNR.R"
##
    [3] "images"
                                            "js"
##
   [5] "mixmodel.bug"
                                            "mixmodel.jags"
  [7] "mtcars.csv"
                                             "mtcars.RData"
##
##
   [9] "mtcars2.csv"
                                             "normmodel.bug"
## [11] "nr-cauchy1.html"
                                            "nr-cauchy2.html"
## [13] "nr-cauchy3.html"
                                             "numbers.txt"
## [15] "oldRcode"
                                             "opsnr.stt"
## [17] "rdemo.Rproj"
                                             "regmodel.bug"
## [19] "s348.fld"
                                             "unit01_introduction_longer.html"
## [21] "unit01_introduction_longer.Rmd"
                                             "unit02_comparith.docx"
## [23] "unit02_comparith.html"
                                             "unit02_comparith.pdf"
## [25] "unit02_comparith.Rmd"
                                             "unit03_sampling_basics.html"
## [27] "unit03_sampling_basics.Rmd"
                                             "unit04_simulation_cache"
## [29] "unit04_simulation_files"
                                             "unit04_simulation.html"
## [31] "unit04_simulation.Rmd"
                                             "unit05_MLE1_cache"
## [33] "unit05_MLE1_files"
                                             "unit05_MLE1.html"
## [35] "unit05_MLE1.Rmd"
                                             "unit06_MLEm_cache"
## [37] "unit06_MLEm_files"
                                             "unit06 MLEm.html"
## [39] "unit06 MLEm.Rmd"
                                             "unit07 em cache"
## [41] "unit07_em_files"
                                            "unit07_em.html"
## [43] "unit07 em.Rmd"
                                             "unit08 integral.html"
## [45] "unit08_integral.pdf"
                                             "unit08_integral.Rmd"
## [47] "unit09_laplace_cache"
                                             "unit09_laplace.html"
## [49] "unit09 laplace.pdf"
                                            "unit09 laplace.Rmd"
## [51] "unit10 rejection sampling.Rmd"
                                             "unit10 rejection sampling cache"
## [53] "unit10_rejection_sampling_files"
                                             "unit10_rejection_sampling.html"
## [55] "unit11_importance_sampling_cache"
                                            "unit11_importance_sampling_files"
## [57] "unit11_importance_sampling.html"
                                            "unit11_importance_sampling.Rmd"
## [59] "unit11_mcmc_intro.html"
                                             "unit11_mcmc_intro.Rmd"
## [61] "unit12_gibbs_cache"
                                             "unit12_gibbs_files"
## [63] "unit12_gibbs.html"
                                             "unit12_gibbs.Rmd"
## [65] "unit14_MHsampling.html"
                                             "unit14_MHsampling.Rmd"
## [67] "unit15_jags_cache"
                                             "unit15_jags_files"
## [69] "unit15_jags.html"
                                             "unit15_jags.Rmd"
## [71] "unit16_stan_cache"
                                            "unit16_stan_files"
## [73] "unit16 stan.html"
                                            "unit16 stan.Rmd"
## [75] "y.txt"
# selecting strings
filelist[grep( "*.pdf",filelist)]
## [1] "unit02_comparith.pdf" "unit08_integral.pdf" "unit09_laplace.pdf"
filelist[grep( "*.Rmd",filelist)]
    [1] "unit01_introduction_longer.Rmd"
                                          "unit02_comparith.Rmd"
##
    [3] "unit03_sampling_basics.Rmd"
                                          "unit04_simulation.Rmd"
##
    [5] "unit05_MLE1.Rmd"
                                          "unit06_MLEm.Rmd"
##
   [7] "unit07_em.Rmd"
                                          "unit08_integral.Rmd"
   [9] "unit09_laplace.Rmd"
                                          "unit10_rejection sampling.Rmd"
## [11] "unit11_importance_sampling.Rmd"
                                          "unit11_mcmc_intro.Rmd"
## [13] "unit12_gibbs.Rmd"
                                          "unit14_MHsampling.Rmd"
```

```
## [15] "unit15_jags.Rmd"
                                          "unit16_stan.Rmd"
unit.files <- filelist[grep( "^unit",filelist)]; unit.files</pre>
    [1] "unit01_introduction_longer.html"
                                            "unit01_introduction_longer.Rmd"
##
    [3] "unit02_comparith.docx"
                                            "unit02_comparith.html"
##
    [5] "unit02_comparith.pdf"
                                            "unit02_comparith.Rmd"
##
   [7] "unit03_sampling_basics.html"
                                            "unit03_sampling_basics.Rmd"
  [9] "unit04_simulation_cache"
                                            "unit04_simulation_files"
## [11] "unit04_simulation.html"
                                            "unit04 simulation.Rmd"
## [13] "unit05 MLE1 cache"
                                            "unit05 MLE1 files"
## [15] "unit05_MLE1.html"
                                            "unit05_MLE1.Rmd"
## [17] "unit06_MLEm_cache"
                                            "unit06 MLEm files"
## [19] "unit06_MLEm.html"
                                            "unit06_MLEm.Rmd"
## [21] "unit07_em_cache"
                                            "unit07_em_files"
## [23] "unit07_em.html"
                                            "unit07_em.Rmd"
## [25] "unit08_integral.html"
                                            "unit08_integral.pdf"
## [27] "unit08_integral.Rmd"
                                            "unit09_laplace_cache"
## [29] "unit09_laplace.html"
                                            "unit09_laplace.pdf"
## [31] "unit09_laplace.Rmd"
                                            "unit10_rejection sampling.Rmd"
## [33] "unit10_rejection_sampling_cache"
                                            "unit10_rejection_sampling_files"
## [35] "unit10_rejection_sampling.html"
                                            "unit11_importance_sampling_cache"
## [37] "unit11_importance_sampling_files"
                                            "unit11_importance_sampling.html"
## [39] "unit11_importance_sampling.Rmd"
                                            "unit11_mcmc_intro.html"
## [41] "unit11_mcmc_intro.Rmd"
                                            "unit12_gibbs_cache"
## [43] "unit12_gibbs_files"
                                            "unit12_gibbs.html"
## [45] "unit12_gibbs.Rmd"
                                            "unit14_MHsampling.html"
## [47] "unit14 MHsampling.Rmd"
                                            "unit15 jags cache"
## [49] "unit15_jags_files"
                                            "unit15_jags.html"
## [51] "unit15_jags.Rmd"
                                            "unit16 stan cache"
## [53] "unit16_stan_files"
                                            "unit16_stan.html"
## [55] "unit16_stan.Rmd"
unit.pdf.files <- unit.files[grep("*.pdf", unit.files)]; unit.pdf.files
## [1] "unit02_comparith.pdf" "unit08_integral.pdf" "unit09_laplace.pdf"
unit.html.files <- unit.files[grep("*.html", unit.files)]; unit.html.files
    [1] "unit01_introduction_longer.html" "unit02_comparith.html"
##
   [3] "unit03_sampling_basics.html"
                                           "unit04_simulation.html"
##
   [5] "unit05_MLE1.html"
                                           "unit06_MLEm.html"
  [7] "unit07_em.html"
                                           "unit08_integral.html"
  [9] "unit09_laplace.html"
                                           "unit10_rejection_sampling.html"
## [11] "unit11_importance_sampling.html"
                                           "unit11_mcmc_intro.html"
                                           "unit14_MHsampling.html"
## [13] "unit12_gibbs.html"
  [15] "unit15_jags.html"
                                           "unit16_stan.html"
```

3 Special Values

```
a <- 0/0
a
```

[1] NaN

```
is.nan(a)
## [1] TRUE
b <- log(0)
## [1] -Inf
is.finite(b)
## [1] FALSE
c <- c(0:4,NA)
## [1] 0 1 2 3 4 NA
is.na(c)
## [1] FALSE FALSE FALSE FALSE TRUE
    Matrices
A \leftarrow matrix(0,4,5)
      [,1] [,2] [,3] [,4] [,5]
## [1,]
## [2,] 0
                0
                      0
                                0
## [3,]
## [4,]
A <- matrix(1:20,4,5)
B \leftarrow matrix(1:20,4,5,byrow = T)
#subsectioning and modifying subsection
D \leftarrow A[c(1,4),c(2,3)]
A[c(1,4),c(2,3)] \leftarrow 1
A[c(1,4),c(2,3)] \leftarrow 101:104
A[c(1,4),c(2,3)] \leftarrow matrix (1001:1004, 2,2)
a < - A[4,]
b<- A[3:4,]
A[1,1]
```

```
## [1] 1
a2 < A[4,, drop = FALSE]
#combining two matrices
#create another matrix using another way
A2 \leftarrow array(1:20,dim=c(4,5))
A2
      [,1] [,2] [,3] [,4] [,5]
## [1,] 1
           5
               9
                        17
                    13
## [2,]
      2
           6 10
                        18
                    14
## [3,]
      3 7 11
                    15
                        19
       4 8 12
## [4,]
                   16
                        20
cbind(A,A2)
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
      1 1001 1003 13 17
## [1,]
                           1 5 9
                                        13
                                            17
           6 10
## [2,]
       2
                        18
                             2
                                 6 10
                                        14
                    14
                                              18
       3 7 11
## [3,]
                           3 7 11
                   15
                        19
                                        15
                                             19
## [4,]
       4 1002 1004
                   16
                        20
                           4 8 12 16
                                              20
rbind(A,A2)
    [,1] [,2] [,3] [,4] [,5]
## [1,]
      1 1001 1003
                       17
## [2,]
       2
            6 10
                    14
                        18
      3 7
## [3,]
                        19
                11
                    15
## [4,]
      4 1002 1004
                   16
                        20
## [5,]
      1 5
               9
                   13
                        17
      2
               10
## [6,]
            6
                   14
                        18
## [7,]
      3 7
                11
                   15
                        19
## [8,]
      4 8 12 16
#operating matrice
\#transpose\ matrix
t(A)
##
      [,1] [,2] [,3] [,4]
## [1,]
      1 2 3
## [2,] 1001
               7 1002
           6
## [3,] 1003
           10 11 1004
## [4,]
            14 15 16
      13
## [5,]
      17
           18 19
Α
## [,1] [,2] [,3] [,4] [,5]
## [1,]
      1 1001 1003
                   13
                        17
## [2,]
         2 6 10
                    14
                        18
      3 7 11
## [3,]
                    15
                        19
## [4,]
      4 1002 1004
                        20
A + 1
```

```
[,1] [,2] [,3] [,4] [,5]
           2 1002 1004
## [1,]
                         14
                              18
                              19
## [2,]
           3
               7
                    11
                         15
## [3,]
                  12
                              20
           4
                         16
                8
## [4,]
           5 1003 1005
                              21
x <- 1:5
A*x
        [,1] [,2] [,3] [,4] [,5]
## [1,]
          1 5005 4012
                              54
## [2,]
           4
               6
                  50
                         56
## [3,]
          9
                    11
                              76
               14
                         75
## [4,]
        16 3006 2008
                         16 100
#the logical here is coercing the matrix "A" into a vector by joining the column
#and repeat the shorter vector, x, as many times as making it have the same
#length as the vector coerced from "A"
#see another example
x < -1:3
A*x
## Warning in A * x: longer object length is not a multiple of shorter object
## length
        [,1] [,2] [,3] [,4] [,5]
           1 2002 3009
## [1,]
                         13
## [2,]
              18
                  10
                         28
                              54
## [3,]
                    22
                              19
               7
                         45
           9
## [4,]
           4 2004 3012
                              40
A^2
                        [,3] [,4] [,5]
##
        [,1]
                [,2]
## [1,]
           1 1002001 1006009
                             169 289
## [2,]
                         100 196
                                   324
           4
                  36
## [3,]
           9
                  49
                         121
                              225
                                   361
         16 1004004 1008016
                                   400
## [4,]
                              256
A <- matrix(sample(1:20),4,5)
        [,1] [,2] [,3] [,4] [,5]
##
## [1,]
           3
               13
                     6
                          2
## [2,]
                         17
                              16
          10
               19
                     8
## [3,]
          20
               15
                     9
                         12
                               5
## [4,]
           4
                     7
               11
                         14
B <- matrix(sample(1:20),5,4)</pre>
В
        [,1] [,2] [,3] [,4]
## [1,] 3 8
```

```
## [2,] 16 18 6 14
## [3,] 12 19 17 7
            20 5 13
## [4,] 10
## [5,] 11
                  2 1
C <- A %*% B
## [,1] [,2] [,3] [,4]
## [1,] 507 484 253 313
## [2,] 776 978 457 709
## [3,] 583 861 493 734
## [4,] 423 647 293 446
solve(C)
               [,1]
                           [,2]
##
                                      [,3]
## [1,] 1.322652e-03 0.005653140 -0.001207281 -0.007928078
## [2,] 7.086392e-05 -0.004322597 -0.003824803 0.013116473
## [3,] 1.519669e-02 -0.022344154 0.007772377 0.012063938
## [4,] -1.134072e-02 0.015588070 0.001587491 -0.017191737
#solving linear equation
x < -1:4
d <- C %*% x
solve(C,d)
## [,1]
## [1,] 1
## [2,]
         2
## [3,]
## [4,]
#altenative way (but not recommended)
solve(C) %*% d
## [,1]
## [1,] 1
## [2,]
       2
## [3,]
## [4,]
\#SVD (C = UDV') and determinant
svd.C <- svd(C)</pre>
svd.C
## [1] 2372.17247 189.21650 72.06705 24.33562
##
## $u
                   [,2] [,3]
           [,1]
## [1,] -0.3354912  0.7266184 -0.4172467  0.43055380
```

```
## [2,] -0.6347357 0.2599097 0.2627143 -0.67863002
## [3,] -0.5730231 -0.6220683 -0.5251285 0.09442239
## [4,] -0.3952224 -0.1323015 0.6936328 0.58751096
##
## $v
##
                          [,2]
                                     [,3]
                                                [,4]
              [,1]
## [1,] -0.4906475  0.80043820 -0.2833610 -0.1956279
## [2,] -0.6459189 -0.08099123 0.7164439 0.2508730
## [3,] -0.3259687 -0.22635879 -0.5710919 0.7185821
## [4,] -0.4855905 -0.54909090 -0.2833174 -0.6184111
#calculating determinant of C
prod(svd.C$d)
```

[1] 787198914

5 Data frame

```
name <- c("john","peter","jennifer")</pre>
gender <- factor(c("m", "m", "f"))</pre>
hw1 < -c(60,60,80)
hw2 < -c(40,50,30)
grades <- data.frame(name,gender,hw1,hw2)</pre>
grades[,"gender"]
## [1] m m f
## Levels: f m
grades[,2]
## [1] m m f
## Levels: f m
#subsectioning a data frame
grades[1,2]
## [1] m
## Levels: f m
grades[,"name"]
## [1] "john"
                               "jennifer"
                    "peter"
grades$name
## [1] "john"
                    "peter"
                               "jennifer"
grades[grades$gender=="m",]
##
      name gender hw1 hw2
```

```
## 1 john m 60 40
## 2 peter m 60 50
subset (grades, hw1 >60)
       name gender hw1 hw2
## 3 jennifer
               f 80 30
grades[,"hw1"]
## [1] 60 60 80
#divide the subjects by "gender", and calculating means in each group
tapply(grades[,"hw1"], grades[,"gender"],mean)
## f m
## 80 60
6
   \operatorname{List}
a <- 1:10
b <- matrix(1:10,2,5)
c <- c("name1","name2")</pre>
alst <- list(aa=a,b=b,c=c)</pre>
names (alst)
## [1] "aa" "b" "c"
str(alst)
## List of 3
## $ aa: int [1:10] 1 2 3 4 5 6 7 8 9 10
## $ b : int [1:2, 1:5] 1 2 3 4 5 6 7 8 9 10
## $ c : chr [1:2] "name1" "name2"
#refering to component of a list
alst$aa
## [1] 1 2 3 4 5 6 7 8 9 10
alst[[2]]
## [,1] [,2] [,3] [,4] [,5]
## [1,] 1 3 5 7
## [2,]
        2
             4 6 8
                            10
blst <- list(d=2:10*10)
#concatenating list
ablst <- c(alst,blst)</pre>
ablst
## $aa
```

```
## [1] 1 2 3 4 5 6 7 8 9 10
##
## $b
       [,1] [,2] [,3] [,4] [,5]
##
## [1,]
          1
              3
                   5
                        7
## [2,]
          2
               4
                        8
                            10
##
## $c
## [1] "name1" "name2"
##
## $d
      20 30 40 50 60 70 80 90 100
## [1]
```

7 Reading and saving data to harddrive

```
a < - scan (text = "3 4 5.3 3")
numbers <- scan (file="numbers.txt")</pre>
mtcars <- read.csv ("mtcars.csv")</pre>
## save objects
save (mtcars, numbers, file = "mtcars.RData")
load ("mtcars.RData")
## note that load will override the objects with the same in .RData file
## output numbers to a text file
cat (numbers, file = "numbers.txt")
## save data frame as csv or other types of file
write.csv(mtcars, file = "mtcars2.csv")
## save an object into an RDS file
alist \leftarrow list (A = rnorm (100), B = letters[1:10])
saveRDS(alist, file = "alist.RDS")
blist <- readRDS("alist.RDS")</pre>
## note that a list is not erased by readRDS
identical(alist, blist)
```

[1] TRUE

8 Function

```
#looking for the maximum value of a numeric vector x
find.max <- function(x)
{
    n <- length(x)

    x.m <- x[1]
    ix.m <- 1

    if(n > 1)
    {
```

```
for( i in seq(2,n,by=1) )
         if(x[i] > x.m)
             x.m \leftarrow x[i]
             ix.m <- i
      }
   }
   #return the maximum value and the index
   list(max=x.m,index.max=ix.m)
}
# To use this function
a <- rnorm (5); a
## [1] 0.5683147 0.8759119 0.6311846 0.7874359 -1.2718505
find.max(a)
## $max
## [1] 0.8759119
## $index.max
## [1] 2
# Some relevant R built-in functions
## [1] 0.8759119
which.max(a)
## [1] 2
order (a)
## [1] 5 1 3 4 2
sort (a)
sort(a, index.return=TRUE)
## $x
##
## $ix
## [1] 5 1 3 4 2
   Graphics
```

```
demofun1 <- function(x)
{
    (1 + 2*x^2 + 3*x^3 + exp(x)) / x^2</pre>
```

```
}
demofun2 <- function(x)</pre>
{
    (1 + 2*(10-x)^2 + 3*(10-x)^3 + exp(10-x)) / (10-x)^2
}
# plot in R windows (for quick look)
#specify plotting parameters
par(mfrow=c(1,2), mar = c(4,4,3,1))
x \leftarrow seq(0,10,by=0.1)
#make "Plot 1"
plot(x, demofun1(x), type="p", pch = 1, ylab="y", main="Plot 1")
#add another line to "Plot 1"
points(x, demofun2(x), type="1", lty = 1)
#make "plot 2"
plot(x, demofun1(x), type="b", pch = 3, lty=1, ylab="y", main="Plot 2")
#add another line to "Plot 2"
points(x, demofun2(x), type="b", pch = 4, lty = 2)
```

Plot 1 Plot 2 250 250 0 0 0 0 200 200 0 0 0 0 20 150 0 00 100 20 50 Commission of the Commission o 0 0 2 8 10 0 2 6 8 10 Х Х

```
# save plot in a file (for publication)
pdf ("afig.pdf", height=4.8, width=10)
#specify plotting parameters
par(mfrow=c(1,2), mar = c(4,4,3,1))
x <- seq(0,10,by=0.1)
#make "Plot 1"
plot(x, demofun1(x), type="p", pch = 1, ylab="y", main="Plot 1")
#add another line to "Plot 1"
points(x, demofun2(x), type="l", lty = 1)
#make "plot 2"
plot(x, demofun1(x), type="b", pch = 3, lty=1, ylab="y", main="Plot 2")</pre>
```

```
#add another line to "Plot 2"
points(x, demofun2(x), type="b", pch = 4, lty = 2)

dev.off()

## pdf
## 2
```