Homework 3

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Question 1

```
## Add a nominal covariate into the model (sex)
#Predicting intercept
model1a <- lmer(PPeerScale ~ age + sex_01 + (age | ID), data=data_long)
tidy(model1a)
##
                                estimate std.error statistic
                                                                  group
                 (Intercept) 60.0226065 0.80293062 74.754412
## 1
                                                                  fixed
## 2
                          age 0.1398691 0.07583897
                                                      1.844291
                                                                  fixed
## 3
                      sex_01
                              1.1445315 0.81234532
                                                      1.408922
                                                                  fixed
## 4
           sd_(Intercept).ID 9.3856236
                                                            NA
                                                                     ID
                                                            NΑ
                                                                     ID
## 5
                   sd_age.ID 0.9272482
                                                 NA
    cor_(Intercept).age.ID -0.7219755
                                                 NA
                                                            NA
                                                                     ID
## 7 sd_Observation.Residual 5.5121080
                                                 NA
                                                            NA Residual
#Predicting intercept and slope
model1b <- lmer(PPeerScale ~ age + sex_01 + age:sex_01 + (age | ID), data=data_long)</pre>
tidy(model1b)
##
                                 estimate std.error statistic
                         term
                                                                   group
## 1
                 (Intercept) 60.15626064 0.9734250 61.7985547
                                                                   fixed
## 2
                              0.12212264 0.1052498
                                                     1.1603118
                                                                   fixed
## 3
                      sex_01
                               0.86830675 1.3972050
                                                      0.6214598
                                                                   fixed
## 4
                  age:sex_01
                               0.03706303 0.1521906
                                                      0.2435303
                                                                   fixed
## 5
           sd_(Intercept).ID
                                                             NA
                                                                      ID
                              9.41102333
                                                 NA
## 6
                                                                      ID
                   sd_age.ID 0.93139467
                                                 NA
                                                             NA
## 7 cor_(Intercept).age.ID -0.72388054
                                                                      ID
                                                             NA
                                                 NA
## 8 sd_Observation.Residual 5.51149113
                                                             NA Residual
#Predicting intercept and slope, with sex centerd
model1c <- lmer(PPeerScale ~ age + sex_c + age:sex_c + (age | ID), data=data_long)</pre>
tidy(model1c)
##
                         term
                                 estimate std.error statistic
                                                                    group
## 1
                 (Intercept) 60.57622586 0.69830867 86.7470625
                                                                    fixed
## 2
                              0.14004856 0.07602785
                                                       1.8420692
                                                                    fixed
## 3
                       sex_c 0.86830540 1.39720619
                                                       0.6214583
                                                                    fixed
## 4
                   age:sex_c
                               0.03706321 0.15219071
                                                       0.2435313
                                                                    fixed
## 5
           sd_(Intercept).ID
                                                  NA
                                                              NA
                                                                       ID
                              9.41103774
                                                                       ID
## 6
                   sd_age.ID 0.93139569
                                                  NA
                                                              NA
      cor_(Intercept).age.ID -0.72388126
                                                  NA
                                                              NA
                                                                       ID
## 8 sd_Observation.Residual 5.51148999
                                                  NA
                                                              NA Residual
model1c_t <- lmer(TPeerScale ~ age + sex_c + age:sex_c + (age | ID), data=data_long)</pre>
```

Centering the nominal covariate (sex) affected the fixed effect estimate of age. This makes sense, since, with

the introduction of the interaction term in model b, now means that the fixed effect of age is representative of the predicted change in PPeer (x) for every unit change in age (y), when sex = 0. Prior to centering, this then represented the mean change for males (dummy coded as 0), but after centering indicates the average mean change across both genders.

Question 2

```
## Add a continuous time-invariant covariate into the model (SES=T1Income_to_Need)
#Predicting intercept
model2a <- lmer(PPeerScale ~ age + T1Income to Need + (age | ID), data=data long)
tidy(model2a)
##
                        term
                                estimate std.error statistic
                                                                 group
## 1
                 (Intercept) 57.9969948 1.02198386 56.749423
                                                                 fixed
## 2
                              0.1159405 0.08002175
                                                     1.448863
                                                                 fixed
## 3
                              1.3132346 0.34943302
                                                     3.758187
            T1Income_to_Need
                                                                 fixed
## 4
           sd_(Intercept).ID
                              8.8914954
                                                           NA
                                                                     ID
                                                                     ID
## 5
                   sd_age.ID
                              0.9349945
                                                 NA
                                                           NA
## 6 cor_(Intercept).age.ID -0.7205910
                                                 NA
                                                           NA
                                                                     ID
## 7 sd_Observation.Residual
                                                 NA
                                                           NA Residual
#Predicting intercept and slope
model2b <- lmer(PPeerScale ~ age + T1Income_to_Need + age:T1Income_to_Need + (age | ID), data=data_long
tidy(model2b)
##
                                estimate std.error statistic
                        term
                                                                   group
## 1
                 (Intercept) 56.62454864 1.45236144 38.987918
                                                                   fixed
## 2
                         age 0.30440457 0.16287574 1.868937
                                                                  fixed
## 3
            T1Income_to_Need
                              1.97092892 0.60565796 3.254195
                                                                   fixed
## 4
        age:T1Income_to_Need -0.09058726 0.06819463 -1.328364
                                                                   fixed
## 5
           sd_(Intercept).ID 8.87935104
                                                  NA
                                                            NA
                                                                      ID
## 6
                                                                      ID
                   sd_age.ID 0.93424638
                                                  NA
                                                            NA
      cor_(Intercept).age.ID -0.72009574
                                                  NA
                                                                      ID
                                                            NA
## 8 sd_Observation.Residual 5.58681457
                                                  NA
                                                            NA Residual
#Predicting intercept and slope, with SES centerd
model2c <- lmer(PPeerScale ~ age + T1Income_to_Need_c + age:T1Income_to_Need_c + (age | ID), data=data_
tidy(model2c)
##
                                estimate std.error statistic
                                                                   group
## 1
                 (Intercept) 60.69319059 0.70811194 85.711294
                                                                   fixed
## 2
                         age 0.11740286 0.07999075
                                                                  fixed
## 3
          T1Income_to_Need_c 1.97092901 0.60565808
                                                      3.254194
                                                                  fixed
## 4
      age:T1Income_to_Need_c -0.09058727 0.06819465 -1.328363
                                                                   fixed
## 5
           sd_(Intercept).ID 8.87935358
                                                  NA
                                                            NA
                                                                      ID
## 6
                   sd_age.ID 0.93424691
                                                  NA
                                                            NA
                                                                      ID
     cor_(Intercept).age.ID -0.72009642
## 7
                                                  NA
                                                            NA
                                                                      ID
## 8 sd_Observation.Residual 5.58681503
                                                  NA
                                                            NA Residual
model2c_t <- lmer(TPeerScale ~ age + T1Income_to_Need_c + age:T1Income_to_Need_c + (age | ID),</pre>
                  data=data_long)
```

Centering the covariate affected the Intercept and age fixed effects estimates, since (similar to above), they

go from being interpreted as the average intercept and average change in PPeer with age of the male group to the average intercept and change in PPeer with age of all subjects.

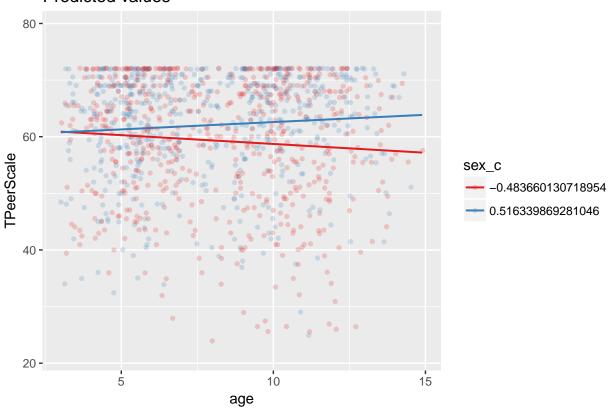
Question 3



Predicted values 80 60 60 -0.483660130718954 -0.516339869281046

```
sjp.lmer(model1c_t, type="pred", facet.grid=F,
    vars = c("age", "sex_c"))
```

Predicted values

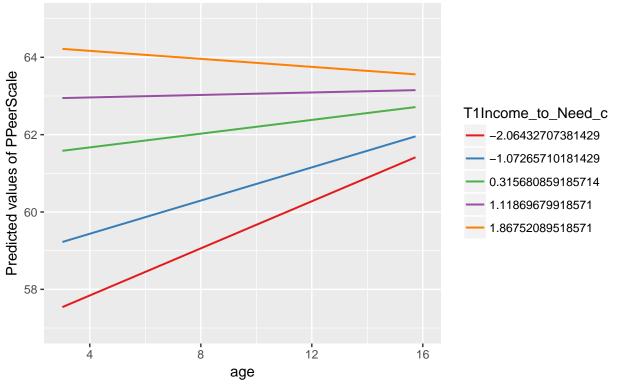


 $\verb|## Note: method with signature 'sparseMatrix \verb|#ANY' chosen for function 'kronecker', \\$

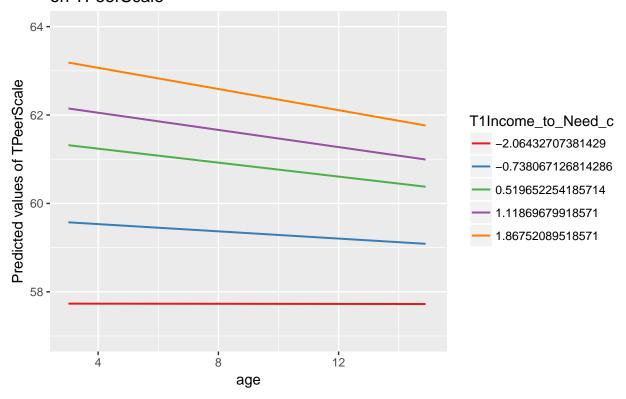
target signature 'dgCMatrix#ngCMatrix'.

"ANY#sparseMatrix" would also be valid

Interaction effect of T1Income_to_Need_c and age on PPeerScale



Interaction effect of T1Income_to_Need_c and age on TPeerScale



Question 4

```
model1c_ci <- confint(model1c, level=.95, oldNames=F, method="boot", nsim=100)</pre>
## Computing bootstrap confidence intervals ...
model1c_ci[c(1,3,5:8),]
                           2.5 %
##
                                      97.5 %
## sd_(Intercept)|ID 8.23561604 10.6522435
## sd_age|ID
                      0.77344713 1.1148318
## (Intercept)
                     59.11656052 61.8841314
## age
                     -0.02172511 0.3063149
## sex c
                     -1.97715027 4.9660375
## age:sex_c
                     -0.33297121 0.3694215
model2c_ci <- confint(model2c, level=.95, oldNames=F, method="boot", nsim=100)</pre>
## Computing bootstrap confidence intervals ...
model2c_ci[c(1,3,5:8),]
                                2.5 %
                                            97.5 %
## sd_(Intercept)|ID
                           7.47905870 10.18743476
## sd_age|ID
                           0.75659256 1.09645878
## (Intercept)
                          59.15845251 62.05091765
                          -0.05420942 0.31596190
## age
```

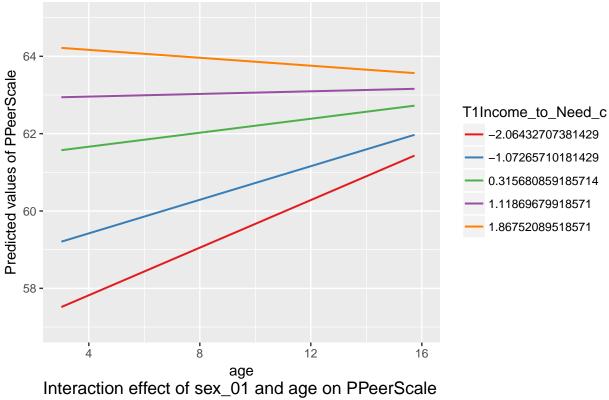
```
## T1Income_to_Need_c 0.88654256 3.18565339
## age:T1Income_to_Need_c -0.23996012 0.03358028
```

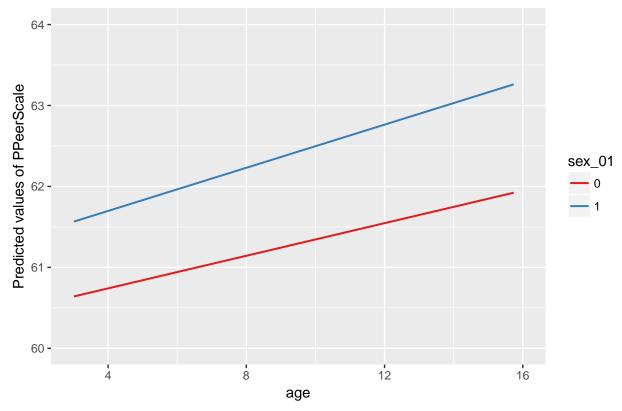
Question 5

```
model5 <- lmer(PPeerScale ~ age*T1Income_to_Need_c + age*sex_01 + (age | ID), data=data_long)</pre>
model5_t <- lmer(TPeerScale ~ age*T1Income_to_Need_c + age*sex_01 + (age | ID), data=data_long)
tidy(model5)
##
                         term
                                 estimate std.error statistic
                                                                    group
## 1
                  (Intercept) 60.27697756 0.99465839 60.6006829
                                                                    fixed
## 2
                          age 0.10353002 0.11137647 0.9295502
                                                                    fixed
## 3
           T1Income_to_Need_c 1.97903445 0.60695547
                                                      3.2605925
                                                                    fixed
## 4
                       sex_01 0.82678254 1.41910153 0.5826099
                                                                    fixed
## 5
       age:T1Income_to_Need_c -0.09128101 0.06840884 -1.3343451
                                                                    fixed
## 6
                   age:sex_01  0.03254273  0.16060463  0.2026263
                                                                    fixed
## 7
            sd_(Intercept).ID 8.90930187
                                                              NA
                                                                       ID
                                                   NA
## 8
                                                              NA
                                                                       ID
                    sd_age.ID 0.93963380
                                                   NA
## 9
       cor_(Intercept).age.ID -0.72419531
                                                   NA
                                                              NA
                                                                       ID
## 10 sd_Observation.Residual 5.58696375
                                                   NA
                                                              NA Residual
tidy(model2c)
##
                        term
                                estimate std.error statistic
                                                                  group
## 1
                 (Intercept) 60.69319059 0.70811194 85.711294
                                                                  fixed
## 2
                         age 0.11740286 0.07999075 1.467705
                                                                  fixed
          T1Income_to_Need_c 1.97092901 0.60565808 3.254194
                                                                  fixed
      age:T1Income_to_Need_c -0.09058727 0.06819465 -1.328363
                                                                  fixed
## 5
           sd_(Intercept).ID 8.87935358
                                                  NA
                                                            NA
                                                                     ID
## 6
                                                            NA
                                                                     ID
                   sd_age.ID 0.93424691
                                                 NA
## 7 cor_(Intercept).age.ID -0.72009642
                                                 NA
                                                            NA
                                                                     ID
## 8 sd Observation.Residual 5.58681503
                                                  NA
                                                            NA Residual
sjp.int(model5,
        type = "eff",
        mdrt.values = "quart",
        swap.pred=T,
        p.value=.05)
```

Could not compute quartiles, too small range of moderator variable. Defaulting `mdrt.values` to `min

Interaction effect of T1Income_to_Need_c and age on PPeerScale

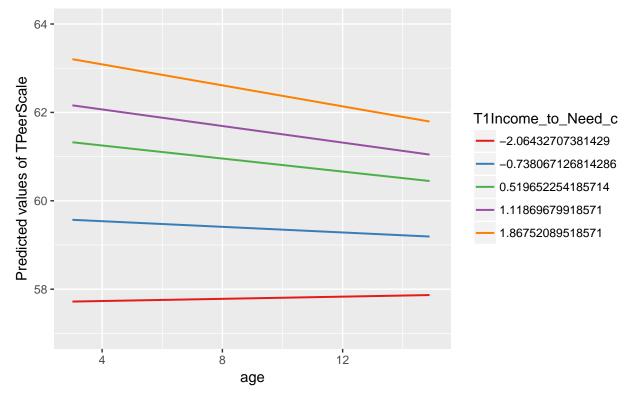




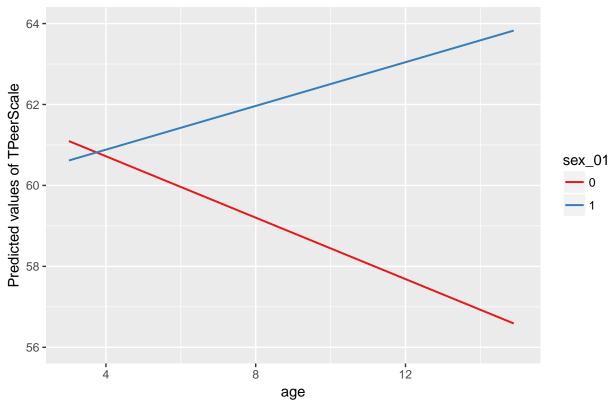
Could not compute quartiles, too small range of moderator variable. Defaulting `mdrt.values` to `min

Interaction effect of T1Income to Need c and age

Interaction effect of T1Income_to_Need_c and age on TPeerScale



Interaction effect of sex_01 and age on TPeerScale



The fixed effect of sex now represents the difference between males and females at average levels of SES (females scored 0.8267825 higher than males). The fixed effect of SES represents the slope (SES and PPeer) of the reference group (males in this case). Age and sex interaction indicates difference of the slope of between males and females, and age and SES interactions represents the change in the slope at different levels of SES(?).