### ALDA\_HW3\_EH

## Elizabeth Hawkey 9/24/2017

```
library(lme4)
## Loading required package: Matrix
library(tidyverse)
## Loading tidyverse: ggplot2
## Loading tidyverse: tibble
## Loading tidyverse: tidyr
## Loading tidyverse: readr
## Loading tidyverse: purrr
## Loading tidyverse: dplyr
## Conflicts with tidy packages ------
## expand(): tidyr, Matrix
## filter(): dplyr, stats
## lag():
            dplyr, stats
library(broom)
library(tidyr)
library(merTools)
## Loading required package: arm
## Loading required package: MASS
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
##
## arm (Version 1.9-3, built: 2016-11-21)
## Working directory is /Users/elizabethhawkey/ejhawkey
PDS_data_2 <- read.csv(file = "~/Documents/PDS_project/Longitudinal_project/datasets/PDS_long_final.cs
PDS_data_2$AGEMOSCAN <- as.numeric(PDS_data_2$AGEMOSCAN)
PDS_data_2$ADHDsum <- as.numeric(PDS_data_2$ADHDsum)</pre>
PDS_data_2$ADHD_INsum <- as.numeric(PDS_data_2$ADHD_INsum)
PDS_data_2$ADHD_HYIMsum<- as.numeric(PDS_data_2$ADHD_HYIMsum)
```

1. Run a series of models using a time-invariant nominal covariate.
a) where the covariate only predicts the intercept b) predicts both intercept and slope c) is rescaled eg centering. For all models, how does your model change from model to model. What is your final

model?

```
#nominal covariate = sex
#a) where the covariate only predicts the intercept
mod.1 <- lmer(ADHDsum ~ agemo_converted + sex + (1|Subid_fMRI), data=PDS_data_2)</pre>
summary(mod.1)
## Linear mixed model fit by REML ['lmerMod']
## Formula: ADHDsum ~ agemo_converted + sex + (1 | Subid_fMRI)
##
     Data: PDS_data_2
## REML criterion at convergence: 2732
##
## Scaled residuals:
              1Q Median
                               3Q
      Min
                                      Max
## -3.4032 -0.4035 -0.1066 0.2421 4.6492
##
## Random effects:
## Groups
             Name Variance Std.Dev.
## Subid_fMRI (Intercept) 8.908
                                   2.985
## Residual
                          3.959
                                   1.990
## Number of obs: 554, groups: Subid_fMRI, 209
## Fixed effects:
                  Estimate Std. Error t value
## (Intercept) 8.5212 1.0937 7.791
## agemo_converted -3.3747
                               0.5892 -5.727
## sex
                   -1.1163
                               0.4490 - 2.486
##
## Correlation of Fixed Effects:
             (Intr) agm_cn
## agem_cnvrtd -0.766
## sex
              -0.640 0.040
#b) predicts both intercept and slope
mod.2 <- lmer(ADHDsum ~ agemo_converted + sex + (agemo_converted|Subid_fMRI), data=PDS_data_2)</pre>
summary(mod.2)
## Linear mixed model fit by REML ['lmerMod']
## Formula: ADHDsum ~ agemo_converted + sex + (agemo_converted | Subid_fMRI)
##
     Data: PDS_data_2
## REML criterion at convergence: 2702.9
## Scaled residuals:
      Min 1Q Median
                               3Q
                                      Max
## -3.5203 -0.3163 -0.1150 0.2092 3.7891
```

```
##
## Random effects:
## Groups
                               Variance Std.Dev. Corr
## Subid_fMRI (Intercept)
                               65.158
                                       8.072
               agemo_converted 14.427
                                        3.798
                                                 -0.98
## Residual
                                3.468
                                        1.862
## Number of obs: 554, groups: Subid_fMRI, 209
## Fixed effects:
##
                   Estimate Std. Error t value
## (Intercept)
                    8.7777
                               1.1559
                                        7.594
## agemo_converted -3.4633
                                0.6146 -5.635
                    -1.1862
                                0.4201 - 2.823
##
## Correlation of Fixed Effects:
##
               (Intr) agm_cn
## agem_cnvrtd -0.825
## sex
               -0.558 0.027
#c) is rescaled eq centering
sex_c <- scale(PDS_data_2$sex, center = T, scale = F)</pre>
PDS_data_2$sex_c <- as.numeric(sex_c)
mod.3 <- lmer(ADHDsum ~ agemo_converted + sex_c + (agemo_converted|Subid_fMRI), data=PDS_data_2)</pre>
summary(mod.3)
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## ADHDsum ~ agemo_converted + sex_c + (agemo_converted | Subid_fMRI)
##
     Data: PDS_data_2
##
## REML criterion at convergence: 2702.9
##
## Scaled residuals:
      Min
              1Q Median
                                3Q
## -3.5203 -0.3163 -0.1150 0.2092 3.7891
##
## Random effects:
## Groups
                               Variance Std.Dev. Corr
               Name
## Subid fMRI (Intercept)
                               65.158
                                        8.072
               agemo_converted 14.427
                                        3.798
                                                 -0.98
## Residual
                                3.468
                                        1.862
## Number of obs: 554, groups: Subid_fMRI, 209
##
## Fixed effects:
                   Estimate Std. Error t value
##
                                       7.317
## (Intercept)
                    7.0189
                                0.9592
## agemo_converted -3.4633
                                0.6146 -5.635
## sex_c
                    -1.1862
                                0.4201 -2.823
##
## Correlation of Fixed Effects:
               (Intr) agm_cn
## agem_cnvrtd -0.976
              -0.023 0.027
## sex_c
```

The model fit improves (explains more of the variance) when a time variable is added, showing that sex is a more useful predictor of ADHD symptoms when the slopes are allowed to vary by subject. Centering sex does not improve the model.

## 2. Introduce a time-invariant continuous covariate and run models a-c from #1.

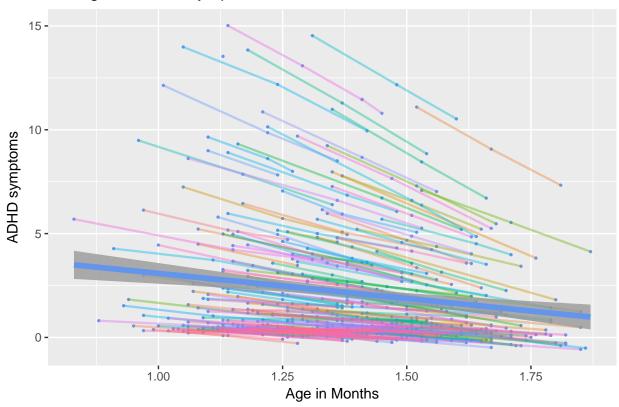
```
#continuous covariate = SES (Income_to_Need_Scan)
#a) where the covariate only predicts the intercept
mod.4 <- lmer(ADHDsum ~ Income_to_Need_Scan + (1|Subid_fMRI), data=PDS_data_2)</pre>
summary(mod.4)
## Linear mixed model fit by REML ['lmerMod']
## Formula: ADHDsum ~ Income_to_Need_Scan + (1 | Subid_fMRI)
     Data: PDS_data_2
##
## REML criterion at convergence: 2758.8
##
## Scaled residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -3.5855 -0.3508 -0.1653 0.2227 4.6363
##
## Random effects:
## Groups
                           Variance Std.Dev.
              Name
## Subid_fMRI (Intercept) 8.423
                                    2.902
## Residual
                           4.314
                                    2.077
## Number of obs: 554, groups: Subid_fMRI, 209
##
## Fixed effects:
##
                      Estimate Std. Error t value
## (Intercept)
                        3.1860 0.3462 9.203
## Income_to_Need_Scan -0.5099
                                    0.1407 - 3.624
##
## Correlation of Fixed Effects:
##
              (Intr)
## Incm_t_Nd_S -0.771
#b) predicts both intercept and slope
mod.5 <- lmer(ADHDsum ~ agemo_converted + Income_to_Need_Scan + (agemo_converted|Subid_fMRI), data=PDS_
summary(mod.5)
## Linear mixed model fit by REML ['lmerMod']
## ADHDsum ~ agemo_converted + Income_to_Need_Scan + (agemo_converted |
##
      Subid_fMRI)
##
      Data: PDS_data_2
##
## REML criterion at convergence: 2709.9
## Scaled residuals:
```

```
##
                1Q Median
                                3Q
## -3.5957 -0.3202 -0.1196 0.2055 3.7449
##
## Random effects:
##
  Groups
               Name
                               Variance Std.Dev. Corr
   Subid_fMRI (Intercept)
                               66.683
                                        8.166
##
               agemo_converted 16.112
                                         4.014
                                                  -0.98
##
  Residual
                                3.476
                                         1.864
## Number of obs: 554, groups: Subid_fMRI, 209
##
## Fixed effects:
##
                       Estimate Std. Error t value
## (Intercept)
                         7.0188
                                    0.9670 7.258
                                    0.6459 -4.849
## agemo_converted
                        -3.1322
## Income_to_Need_Scan -0.2420
                                    0.1295 -1.869
##
## Correlation of Fixed Effects:
##
               (Intr) agm_cn
## agem_cnvrtd -0.939
## Incm_t_Nd_S -0.018 -0.254
#c) is rescaled eq centering
Income_to_Need_Scan_c <- scale(PDS_data_2$ Income_to_Need_Scan , center = T, scale = F)</pre>
PDS_data_2$ Income_to_Need_Scan_c <- as.numeric(Income_to_Need_Scan_c)
mod.6 <- lmer(ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + (agemo_converted|Subid_fMRI), data=PD</pre>
summary(mod.6)
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + (agemo_converted |
##
       Subid_fMRI)
##
      Data: PDS_data_2
##
## REML criterion at convergence: 2709.9
##
## Scaled residuals:
##
                1Q Median
       Min
                                3Q
                                        Max
## -3.5957 -0.3202 -0.1196 0.2055 3.7449
##
## Random effects:
## Groups
               Name
                               Variance Std.Dev. Corr
##
   Subid_fMRI (Intercept)
                               66.683
                                        8.166
                                         4.014
##
               agemo_converted 16.112
                                                  -0.98
## Residual
                                3.476
                                         1.864
## Number of obs: 554, groups: Subid_fMRI, 209
##
## Fixed effects:
##
                         Estimate Std. Error t value
## (Intercept)
                           6.5596
                                      0.9934
                                                6.603
## agemo_converted
                          -3.1322
                                       0.6459 -4.849
## Income_to_Need_Scan_c -0.2420
                                       0.1295 - 1.869
##
## Correlation of Fixed Effects:
##
               (Intr) agm_cn
## agem_cnvrtd -0.977
```

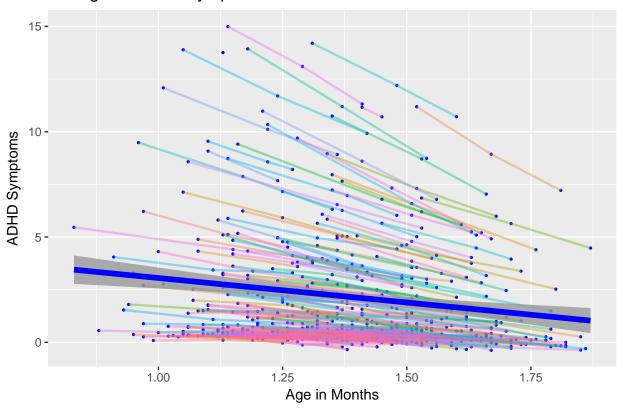
# 3. Graph both of your final models for the continuous and nominal models above.

Calculate confidence intervals around your estimates for your final models

#### Change in ADHD Symptoms Across Time



#### Change in ADHD Symptoms Across Time



```
## Computing profile confidence intervals ...
##
                       2.5 %
                                 97.5 %
## .sig01
                    5.894002 10.6846893
## .sig02
                   -1.000000 -0.9462445
## .sig03
                          NA
                          NA
## .sigma
                                      NA
## (Intercept)
                    5.124051 8.9261166
## agemo_converted -4.695715 -2.2488878
                   -2.009822 -0.3610493
## sex_c
## Computing profile confidence intervals \dots
##
                              2.5 %
                                          97.5 %
                          5.6991115 10.79504166
## .sig01
## .sig02
                         -1.0000000 -0.93767917
## .sig03
                                 NA
                                              NA
## .sigma
                                 NA
## (Intercept)
                          4.5999620 8.52969672
## agemo_converted
                         -4.4152518 -1.85632875
## Income_to_Need_Scan_c -0.5069412  0.02290092
```

## 4. Include both types of covariates in a single model. How does your interpretation of parameters change?

```
mod.7 <- lmer(ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + sex_c + (agemo_converted|Subid_fMRI),
summary(mod.7)
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + sex_c + (agemo_converted |
##
      Subid fMRI)
     Data: PDS_data_2
##
##
## REML criterion at convergence: 2701.8
##
## Scaled residuals:
      Min
               1Q Median
                               3Q
                                       Max
## -3.4792 -0.3210 -0.1312 0.2327
                                   3.8149
##
## Random effects:
## Groups
              Name
                              Variance Std.Dev. Corr
## Subid_fMRI (Intercept)
                              69.497
                                       8.336
##
              agemo_converted 17.398
                                        4.171
                                                 -0.98
                               3.435
                                        1.853
## Number of obs: 554, groups: Subid_fMRI, 209
##
## Fixed effects:
##
                        Estimate Std. Error t value
## (Intercept)
                                   0.9965
                         6.6245
                                             6.648
## agemo_converted
                        -3.1802
                                     0.6476 - 4.911
## Income_to_Need_Scan_c -0.2444
                                     0.1281 -1.907
## sex_c
                         -1.1798
                                     0.4150 -2.843
## Correlation of Fixed Effects:
              (Intr) agm_cn I__N_S
## agem_cnvrtd -0.978
## Incm_t_N_S_ 0.226 -0.250
## sex_c
              -0.025 0.029 -0.007
anova(mod.6, mod.7)
## refitting model(s) with ML (instead of REML)
## Data: PDS_data_2
## Models:
## mod.6: ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + (agemo_converted |
             Subid fMRI)
## mod.7: ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + sex_c + (agemo_converted |
## mod.7:
             Subid_fMRI)
              AIC
                     BIC logLik deviance Chisq Chi Df Pr(>Chisq)
        Df
## mod.6 7 2721.2 2751.4 -1353.6
## mod.7 8 2715.2 2749.8 -1349.6
                                   2699.2 8.0128
                                                      1
                                                          0.004645 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Model 7 (including both covariates) appears to be a better fit since the AIC values are smaller.

#### 5. If you have one available, introduce a time-varying covariate.

```
#time-varying covariate = MDD symptoms at each scan
mod.8 <- lmer(ADHDsum ~ agemo_converted + MDDCorescan + Income_to_Need_Scan_c + sex_c + (agemo_converte
summary(mod.8)
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## ADHDsum ~ agemo_converted + MDDCorescan + Income_to_Need_Scan_c +
      sex_c + (agemo_converted | Subid_fMRI)
##
##
     Data: PDS_data_2
##
## REML criterion at convergence: 2637.8
## Scaled residuals:
##
      Min
               1Q Median
                                       Max
## -3.2387 -0.4358 -0.0725 0.3033 3.4690
##
## Random effects:
  Groups
              Name
                               Variance Std.Dev. Corr
                                        5.899
                               34.80
##
  Subid_fMRI (Intercept)
              agemo_converted 6.54
                                        2.557
                                                 -0.98
##
## Residual
                                3.51
                                        1.874
## Number of obs: 554, groups: Subid_fMRI, 209
##
## Fixed effects:
##
                         Estimate Std. Error t value
## (Intercept)
                         4.18752
                                    0.92356
                                              4.534
## agemo_converted
                         -2.31166
                                     0.59687 - 3.873
## MDDCorescan
                          0.55689
                                     0.06316
                                              8.817
## Income_to_Need_Scan_c -0.25229
                                     0.12145 -2.077
                         -1.04852
                                     0.37086 -2.827
## sex_c
##
## Correlation of Fixed Effects:
               (Intr) agm_cn MDDCrs I__N_S
## agem_cnvrtd -0.969
## MDDCorescan -0.271 0.134
## Incm_t_N_S_ 0.213 -0.244 0.039
## sex_c
              -0.038 0.038 0.029 -0.001
anova(mod.7, mod.8)
## refitting model(s) with ML (instead of REML)
## Data: PDS_data_2
## Models:
## mod.7: ADHDsum ~ agemo_converted + Income_to_Need_Scan_c + sex_c + (agemo_converted |
              Subid fMRI)
## mod.7:
## mod.8: ADHDsum ~ agemo_converted + MDDCorescan + Income_to_Need_Scan_c +
              sex_c + (agemo_converted | Subid_fMRI)
                      BIC logLik deviance Chisq Chi Df Pr(>Chisq)
##
        Df
              AIC
```

```
## mod.7 8 2715.2 2749.8 -1349.6 2699.2
## mod.8 9 2648.7 2687.6 -1315.4 2630.7 68.473 1 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

### 6. Create a density plot of the random effects from your final model.

```
library(merTools)
re.sim <- REsim(mod.7)
head(re.sim)
##
      groupFctr groupID
                                                median
                              term
                                        mean
## 1 Subid fMRI
                  L025 (Intercept) -4.603313 -4.522919 6.634843
## 2 Subid_fMRI
                  L027 (Intercept) 11.400055 12.349789 7.932123
## 3 Subid_fMRI
                  L029 (Intercept) -3.422130 -3.925376 6.926335
## 4 Subid_fMRI
                L032 (Intercept) -4.185303 -3.671231 6.703955
## 5 Subid_fMRI
                  L039 (Intercept) 6.956372 7.017352 6.375679
                  L041 (Intercept) 8.989068 9.532653 7.421615
## 6 Subid_fMRI
p.3 <- re.sim %>%
 filter(term == "(Intercept)")
ggplot(p.3, aes(mean)) +
 geom_density()
```

