

# Towards an Incremental Unified Multimodal Anomaly Detection: Augmenting Multimodal Denoising From an Information Bottleneck Perspective (Supplementary Material)

Kaifang Long<sup>1</sup>, Lianbo Ma<sup>1\*</sup>, Jiaqi Liu<sup>2</sup>, Liming Liu<sup>1</sup>, Guoyang Xie<sup>3</sup>,

<sup>1</sup>Software College, Northeastern University, China, <sup>2</sup>UBC, Canada, <sup>3</sup>CATL, China

longkf@stumail.neu.edu.cn, malb@swc.neu.edu.cn, guoyang.xie@ieee.org

## 1. Overview

This supplementary material includes:

- Detailed theoretical analysis and proof related to information bottleneck regularization in our denoising framework of incremental unified multimodal anomaly detection. (Appendix A).
- P-AUROC and AUPRO scores on MVTEC 3D-AD dataset (Appendix B).
- P-AUROC and AUPRO scores on Eyecndies dataset (Appendix C).
- A detailed description of the IB-IUMAD algorithm (see Algorithms 1 and Appendix D).

## 2. Appendix A: Theoretical Proofs

Let  $F_{fu}$ ,  $F_{fu}^g$ , and  $Y$  be continuous random variables with corresponding support sets  $\mathcal{F}$ ,  $\mathcal{F}_g$ , and  $\mathcal{Y}$ , as well as probability distributions  $P_{F_{fu}}$ ,  $P_{F_{fu}^g}$ , and  $P_Y$ . The mutual information between  $P_{F_{fu}^g}$  and  $Y$ , along with its relationship to information entropy [3, 7], is defined as:

$$\begin{aligned} I(F_{fu}^g; Y) &\equiv \mathbb{E} \left[ \log \frac{P_{F_{fu}^g, Y}(F_{fu}^g, Y)}{P_{F_{fu}^g}(F_{fu}^g)P_Y(Y)} \right] = -\mathbb{E}[\log P_Y(Y)] \\ &\quad + \mathbb{E}[\log P_{F_{fu}^g, Y}(F_{fu}^g, Y)] - \mathbb{E}[\log P_{F_{fu}^g}(F_{fu}^g)] \\ &= -H(F_{fu}^g, Y) + H(F_{fu}^g) + H(Y) \\ &= H(F_{fu}^g) - H(F_{fu}^g|Y). \end{aligned}$$

Additionally, given  $Y$ , the conditional mutual information of  $P_{F_{fu}}$  and  $P_{F_{fu}^g}$  is defined as:

$$\begin{aligned} I(F_{fu}; F_{fu}^g|Y) &\equiv \mathbb{E} \left[ \log \frac{P_{F_{fu}, F_{fu}^g|Y}(F_{fu}, F_{fu}^g|Y)}{P_{F_{fu}, Y}(F_{fu}, Y)P_{F_{fu}^g|Y}(F_{fu}^g|Y)} \right] \\ &= \int_{\mathcal{F}, \mathcal{F}_g, \mathcal{Y}} P_{F_{fu}, F_{fu}^g|Y}(F_{fu}, F_{fu}^g|Y) P_Y(Y) \\ &\quad \log \frac{P_{F_{fu}, F_{fu}^g|Y}(F_{fu}, F_{fu}^g|Y)}{P_{F_{fu}, Y}(F_{fu}, Y)P_{F_{fu}^g|Y}(F_{fu}^g|Y)} dF_{fu} dF_{fu}^g dY. \end{aligned}$$

Based on the aforementioned definitions of mutual information, conditional mutual information, and entropy [4–6], we derive the following corollaries:

**Corollary 1.** Given a random variable  $Y$ , the mutual information between features  $F_{fu}$  and  $F_{fu}^g$ , can be equivalently rewritten as  $I(F_{fu}; F_{fu}^g) = I(F_{fu}; F_{fu}^g|Y) + I(F_{fu}^g; Y)$  according to the chain rule.

**Proof.** Based on mutual information theory, we first know that  $I(F_{fu}^g; Y) = -\mathbb{E}[\log P_Y(Y)] + \mathbb{E}[\log P_{F_{fu}^g, Y}(F_{fu}^g, Y)] - \mathbb{E}[\log P_{F_{fu}^g}(F_{fu}^g)] = H(F_{fu}^g) - H(F_{fu}^g|Y)$ . Then, since  $F_{fu}^g$  is derived from  $F_{fu}$ , it follows that  $P_{F_{fu}, F_{fu}^g}(F_{fu}, F_{fu}^g) = P_{F_{fu}}(F_{fu})$ , implying  $I(F_{fu}; F_{fu}^g) = \mathbb{E}[-\log P_{F_{fu}^g}(F_{fu}^g)] = [\log \frac{P_{F_{fu}, F_{fu}^g}(F_{fu}, F_{fu}^g)}{P_{F_{fu}^g}(F_{fu}^g)P_{F_{fu}}(F_{fu})}] = H(F_{fu}^g)$ . Similarly, we can deduce that  $I(F_{fu}, F_{fu}^g|Y) = H(F_{fu}^g|Y)$ . Notably, given that mutual information is symmetric, it follows that  $I(F_{fu}; Y) = I(Y; F_{fu})$  and  $I(F_{fu}^g; Y) = I(Y; F_{fu}^g)$ . Combining these relations, we can prove that  $I(F_{fu}; F_{fu}^g) = I(F_{fu}; F_{fu}^g|Y) + I(F_{fu}^g; Y)$ .

**Corollary 2.** If the KL divergence between  $p(Y|F_{fu})$  and  $p(Y|F_{fu}^g)$  is 0, that is,  $\text{KL}[P(Y|F_{fu})||P(Y|F_{fu}^g)] = 0$ , we have  $I(Y; F_{fu}) - I(Y; F_{fu}^g) = I(F_{fu}; Y) - I(F_{fu}^g; Y) = 0$ .

\*Corresponding author.

Table 1. AUPRO scores on MVTec 3D-AD dataset (10-0 with 0 step). The red / blue indicates the best/second-best results.

	Method	Year	Bagel	Cable Gland	Carrot	Cookie	Dowel	Foam	Peach	Potato	Rope	Tire	Mean
RGB	UniAD	NIPS22	84.4	96.3	93.4	88.7	96.1	55.8	90.4	91.1	94.3	90.6	88.1
	SimpleNet	CVPR23	70.4	86.8	84.4	66.6	83.0	66.7	74.8	72.8	92.8	77.9	77.6
	DeSTSeg	CVPR23	77.6	64.1	14.2	40.9	31.2	63.6	48.2	6.2	90.4	27.3	46.4
	DiAD	AAAI24	93.8	94.5	94.6	83.5	89.6	69.1	94.2	93.9	96.5	68.8	87.8
	IUF	ECCV24	85.8	93.4	93.8	86.5	93.7	68.4	89.6	88.6	93.4	92.2	88.5
	CDAD	CVPR25	87.1	95.2	88.3	77.3	95.8	72.0	88.9	88.2	92.4	90.0	87.5
	IB-IUMAD	-	89.1	97.0	91.8	91.3	95.9	64.3	89.9	92.5	93.5	87.6	89.3
3D	DiAD	AAAI24	61.5	62.8	70.4	63.7	76.5	35.7	68.8	76.7	65.7	55.6	63.7
	IUF	ECCV24	64.6	64.2	81.3	60.6	76.5	26.8	71.7	76.8	68.8	62.6	65.4
	CDAD	CVPR25	39.2	48.7	36.8	33.7	45.2	40.4	39.8	36.1	44.9	40.7	40.6
	IB-IUMAD	-	68.9	63.6	81.1	58.3	82.9	39.1	66.8	83.0	69.4	62.5	67.6
RGB+3D	DiAD	AAAI24	95.2	94.8	92.9	85.6	90.7	65.3	93.5	94.6	95.1	71.2	87.9
	IUF	ECCV24	87.5	96.6	95.3	90.3	96.2	64.5	89.8	88.7	97.3	85.4	89.2
	CDAD	CVPR25	87.8	96.1	87.6	79.4	96.1	74.3	87.2	86.9	94.3	91.2	88.1
	IB-IUMAD	-	92.6	90.7	95.4	90.5	95.3	68.9	92.5	92.2	97.4	88.7	90.4

**Proof.**

$$\begin{aligned}
I(F_{fu}; Y) - I(F_{fu}^g; Y) &= I(Y; F_{fu}) - I(Y; F_{fu}^g) \\
&= - \iint P(F_{fu}^g) P(Y|F_{fu}^g) \log P(Y|F_{fu}^g) dF_{fu}^g dY \\
&\quad + \iint P(F_{fu}) P(Y|F_{fu}) \log P(Y|F_{fu}) dF_{fu} dY \\
&= \iint P(F_{fu}) P(Y|F_{fu}) \log \left[ \frac{P(Y|F_{fu})}{P(Y|F_{fu}^g)} P(Y|F_{fu}^g) \right] \\
&\quad dF_{fu} dY \\
&\quad - \iint P(F_{fu}^g) P(Y|F_{fu}^g) \log \left[ \frac{P(Y|F_{fu}^g)}{P(Y|F_{fu})} P(Y|F_{fu}) \right] \\
&\quad dF_{fu}^g dY \\
&= - \int P(F_{fu}) \text{KL} [P(Y|F_{fu}^g) || P(Y|F_{fu})] dF_{fu}^g \\
&\quad - \iint P(F_{fu}^g) P(Y|F_{fu}^g) \log P(Y|F_{fu}^g) dF_{fu}^g dY \\
&\quad + \int P(F_{fu}) \text{KL} [P(Y|F_{fu}) || P(Y|F_{fu}^g)] dF_{fu} \\
&\quad - \iint P(F_{fu}) P(Y|F_{fu}) \log P(Y|F_{fu}^g) dF_{fu} dY \\
&= \mathbb{E}_{F_{fu}} [\text{KL}[P(Y|F_{fu}) || P(Y|F_{fu}^g)]] \\
&\quad - \mathbb{E}_{F_{fu}^g} [\text{KL}[P(Y|F_{fu}^g) || P(Y|F_{fu})]] \\
&\quad + \int P(Y) \log \frac{P(Y|F_{fu}^g)}{p(Y|F_{fu})} dY \\
&\leq \mathbb{E}_{F_{fu}} [\text{KL}[P(Y|F_{fu}) || P(Y|F_{fu}^g)]] \\
&\quad + \int P(Y) \log \frac{P(Y|F_{fu}^g)}{p(Y|F_{fu})} dY
\end{aligned}$$

By Jensen's inequality and the strict convexity of

$-\log$ , we conclude that the KL divergence is non-negative [3]. When  $\text{KL}[P(Y|F_{fu}) || P(Y|F_{fu}^g)] = 0$ , it follows that  $P(Y|F_{fu}^g) = P(Y|F_{fu})$  almost everywhere, which means that  $\int P(Y) \log \frac{P(Y|F_{fu}^g)}{p(Y|F_{fu}^g)} dY = 0$ , and we have  $I(Y|F_{fu}) - I(Y|F_{fu}^g) \leq 0$ . Therefore, combining these, we prove that when the KL divergence between  $p(Y|F_{fu})$  and  $p(Y|F_{fu}^g)$  is 0, i.e.,  $\text{KL}[P(Y|F_{fu}) || P(Y|F_{fu}^g)] = 0$ , we have  $I(Y; F_{fu}) - I(Y; F_{fu}^g) = 0$ .

To this end, based on **Corollary 1** and **Corollary 2**, we conclude that using KL divergence as the target loss function between  $F_{fu}$  and  $F_{fu}^g$  effectively eliminates redundant information from the fused multimodal features.

### 3. Appendix B: AUPRO and P-AUROC on MVTec 3D-AD

To validate the effectiveness of the proposed method, we report the P-AUROC and AUPRO metrics of IB-IUMAD under the setting of 10-0 with 0 step. As shown in Tables 1 and 2, on the MVTec 3D-AD dataset [1], IB-IUMAD consistently outperforms the state-of-the-art unified multimodal anomaly detection approaches in most test cases. Specifically, when trained solely with RGB images, IB-IUMAD achieves improvements of 3.3% and 11.7% over SimpleNet in terms of P-AUROC and AUPRO metrics, respectively (0.4% and 1.2% higher than UniAD, and 0.5% and 0.8% higher than IUF, respectively). When both RGB and 3D depth images are used for training, IB-IUMAD achieves 0.6% and 1.2% higher than IUF in terms of P-AUROC and AUPRO metrics, respectively (0.4% and 2.5% higher than DiAD, and 0.4% and 2.3% higher than CDAD, respectively). In fact, the abovementioned performance enhancements exceed state-of-the-art (SOTA) methods. These experimental results validate the critical role of eliminating spurious and redundant features in improving the perfor-

Table 2. P-AUROC scores on MVTec 3D-AD dataset (10-0 with 0 step). The red / blue indicates the best/second-best results.

	Method	Year	Bagel	Cable Gland	Carrot	Cookie	Dowel	Foam	Peach	Potato	Rope	Tire	Mean
RGB	UniAD	NIPS22	97.6	<span style="background-color: #f8d7da;">98.9</span>	98.0	<span style="background-color: #f8d7da;">97.5</span>	<span style="background-color: #f8d7da;">99.1</span>	82.2	<span style="background-color: #d1ecf1;">97.4</span>	97.6	99.0	98.0	96.5
	SimpleNet	CVPR23	93.2	95.2	96.4	90.5	95.3	87.8	92.9	91.0	<span style="background-color: #d1ecf1;">99.3</span>	93.8	93.6
	DeSTSeg	CVPR23	<span style="background-color: #f8d7da;">98.7</span>	97.8	86.9	93.3	97.3	<span style="background-color: #f8d7da;">95.7</span>	95.9	89.2	98.8	97.0	95.1
	DiAD	AAAI24	<span style="background-color: #d1ecf1;">98.5</span>	<span style="background-color: #d1ecf1;">98.4</span>	<span style="background-color: #f8d7da;">98.6</span>	94.3	97.2	89.8	<span style="background-color: #f8d7da;">98.4</span>	<span style="background-color: #d1ecf1;">98.0</span>	<span style="background-color: #d1ecf1;">99.3</span>	91.8	96.4
	IUF	ECCV24	97.9	98.2	<span style="background-color: #d1ecf1;">98.5</span>	<span style="background-color: #d1ecf1;">97.0</span>	<span style="background-color: #d1ecf1;">98.9</span>	81.8	<span style="background-color: #d1ecf1;">97.4</span>	96.6	<span style="background-color: #f8d7da;">99.4</span>	<span style="background-color: #d1ecf1;">98.1</span>	96.4
	CDAD	CVPR25	97.5	<span style="background-color: #f8d7da;">98.9</span>	95.8	95.1	<span style="background-color: #f8d7da;">99.1</span>	<span style="background-color: #d1ecf1;">92.3</span>	96.9	96.0	99.0	97.7	<span style="background-color: #d1ecf1;">96.8</span>
	IB-IUMAD	-	97.4	97.1	97.4	<span style="background-color: #f8d7da;">97.5</span>	98.6	88.7	96.6	<span style="background-color: #f8d7da;">98.1</span>	99.2	<span style="background-color: #f8d7da;">98.5</span>	<span style="background-color: #f8d7da;">96.9</span>
3D	DiAD	AAAI24	88.3	<span style="background-color: #d1ecf1;">90.6</span>	<span style="background-color: #d1ecf1;">94.4</span>	84.9	<span style="background-color: #f8d7da;">95.1</span>	62.8	<span style="background-color: #d1ecf1;">91.3</span>	<span style="background-color: #f8d7da;">94.5</span>	<span style="background-color: #d1ecf1;">91.6</span>	<span style="background-color: #f8d7da;">88.5</span>	<span style="background-color: #d1ecf1;">88.2</span>
	IUF	ECCV24	<span style="background-color: #f8d7da;">90.3</span>	90.0	94.3	<span style="background-color: #d1ecf1;">86.8</span>	93.1	60.1	90.2	<span style="background-color: #d1ecf1;">93.6</span>	90.8	84.5	87.4
	CDAD	CVPR25	70.6	75.8	71.4	71.6	76.0	<span style="background-color: #f8d7da;">77.7</span>	75.8	73.1	75.0	76.8	74.4
	IB-IUMAD	-	<span style="background-color: #d1ecf1;">89.3</span>	<span style="background-color: #f8d7da;">90.8</span>	<span style="background-color: #f8d7da;">94.7</span>	<span style="background-color: #f8d7da;">87.4</span>	<span style="background-color: #d1ecf1;">93.8</span>	<span style="background-color: #d1ecf1;">64.1</span>	<span style="background-color: #f8d7da;">91.7</span>	93.4	<span style="background-color: #f8d7da;">91.9</span>	<span style="background-color: #f8d7da;">87.8</span>	<span style="background-color: #f8d7da;">88.5</span>
RGB+3D	DiAD	AAAI24	97.6	96.8	<span style="background-color: #d1ecf1;">98.1</span>	<span style="background-color: #f8d7da;">97.4</span>	98.6	90.4	<span style="background-color: #f8d7da;">97.7</span>	<span style="background-color: #d1ecf1;">97.6</span>	<span style="background-color: #f8d7da;">99.5</span>	<span style="background-color: #d1ecf1;">97.8</span>	<span style="background-color: #d1ecf1;">97.2</span>
	IUF	ECCV24	97.8	<span style="background-color: #d1ecf1;">97.8</span>	97.7	<span style="background-color: #d1ecf1;">96.7</span>	<span style="background-color: #f8d7da;">99.3</span>	90.1	97.5	96.7	<span style="background-color: #d1ecf1;">99.4</span>	97.2	97.0
	CDAD	CVPR25	<span style="background-color: #f8d7da;">98.4</span>	<span style="background-color: #f8d7da;">98.8</span>	96.1	95.5	99.1	<span style="background-color: #d1ecf1;">93.4</span>	97.1	96.6	98.7	<span style="background-color: #f8d7da;">97.9</span>	<span style="background-color: #d1ecf1;">97.2</span>
	IB-IUMAD	-	<span style="background-color: #d1ecf1;">97.9</span>	97.6	<span style="background-color: #f8d7da;">99.0</span>	<span style="background-color: #f8d7da;">97.4</span>	<span style="background-color: #d1ecf1;">99.2</span>	<span style="background-color: #f8d7da;">93.5</span>	<span style="background-color: #d1ecf1;">97.6</span>	<span style="background-color: #f8d7da;">97.7</span>	<span style="background-color: #d1ecf1;">99.4</span>	96.4	<span style="background-color: #d1ecf1;">97.6</span>

Table 3. AUPRO scores on Eyecandies dataset (10-0 with 0 step). The red / blue indicates the best/second-best results.

	Method	Year	Candy Cane	Chocolate Cookie	Chocolate Praline	Confetto	Gummy Bear	Hazelnut Truffle	Licorice Sandwich	Lollipop	Marsh-mallow	Peppermint Candy	Mean
RGB	DiAD	AAAI24	86.8	83.8	76.7	96.5	70.5	<span style="background-color: #d1ecf1;">53.2</span>	85.1	88.7	93.1	93.8	82.8
	IUF	ECCV24	<span style="background-color: #d1ecf1;">87.8</span>	<span style="background-color: #d1ecf1;">87.9</span>	<span style="background-color: #d1ecf1;">77.8</span>	<span style="background-color: #d1ecf1;">96.6</span>	72.0	52.7	<span style="background-color: #d1ecf1;">86.7</span>	89.2	<span style="background-color: #d1ecf1;">94.6</span>	<span style="background-color: #d1ecf1;">94.3</span>	<span style="background-color: #d1ecf1;">84.0</span>
	CDAD	CVPR25	80.7	86.2	69.8	96.4	<span style="background-color: #f8d7da;">72.8</span>	<span style="background-color: #f8d7da;">66.4</span>	79.9	<span style="background-color: #f8d7da;">91.4</span>	86.4	91.3	82.1
	IB-IUMAD	-	<span style="background-color: #f8d7da;">89.8</span>	<span style="background-color: #f8d7da;">89.5</span>	<span style="background-color: #f8d7da;">80.3</span>	<span style="background-color: #f8d7da;">97.5</span>	<span style="background-color: #f8d7da;">74.5</span>	<span style="background-color: #d1ecf1;">53.2</span>	<span style="background-color: #f8d7da;">88.2</span>	<span style="background-color: #d1ecf1;">90.3</span>	<span style="background-color: #f8d7da;">95.0</span>	<span style="background-color: #f8d7da;">95.0</span>	<span style="background-color: #f8d7da;">85.3</span>
3D	DiAD	AAAI24	62.1	<span style="background-color: #d1ecf1;">29.3</span>	<span style="background-color: #d1ecf1;">34.9</span>	<span style="background-color: #f8d7da;">50.3</span>	<span style="background-color: #d1ecf1;">22.4</span>	<span style="background-color: #f8d7da;">21.3</span>	<span style="background-color: #f8d7da;">43.2</span>	<span style="background-color: #d1ecf1;">56.6</span>	39.8	<span style="background-color: #d1ecf1;">54.3</span>	<span style="background-color: #d1ecf1;">41.4</span>
	IUF	ECCV24	<span style="background-color: #d1ecf1;">79.6</span>	28.7	26.7	44.9	18.3	3.2	41.9	54.2	<span style="background-color: #d1ecf1;">42.8</span>	53.8	39.4
	CDAD	CVPR25	48.3	13.6	<span style="background-color: #f8d7da;">38.3</span>	20.1	7.2	<span style="background-color: #d1ecf1;">17.8</span>	32.6	51.2	40.1	33.2	30.2
	IB-IUMAD	-	<span style="background-color: #f8d7da;">82.5</span>	<span style="background-color: #f8d7da;">30.9</span>	31.8	<span style="background-color: #d1ecf1;">49.6</span>	<span style="background-color: #f8d7da;">25.7</span>	10.4	<span style="background-color: #d1ecf1;">42.5</span>	<span style="background-color: #f8d7da;">59.8</span>	<span style="background-color: #f8d7da;">46.3</span>	<span style="background-color: #f8d7da;">57.7</span>	<span style="background-color: #f8d7da;">43.7</span>
RGB + 3D	DiAD	AAAI24	88.7	85.1	75.6	94.3	73.8	56.2	<span style="background-color: #f8d7da;">89.2</span>	<span style="background-color: #d1ecf1;">92.3</span>	93.4	<span style="background-color: #f8d7da;">95.7</span>	84.4
	IUF	ECCV24	<span style="background-color: #f8d7da;">90.1</span>	<span style="background-color: #d1ecf1;">89.7</span>	<span style="background-color: #f8d7da;">81.2</span>	96.4	<span style="background-color: #d1ecf1;">74.7</span>	54.5	<span style="background-color: #d1ecf1;">88.6</span>	90.1	<span style="background-color: #f8d7da;">94.9</span>	<span style="background-color: #d1ecf1;">95.2</span>	<span style="background-color: #d1ecf1;">85.5</span>
	CDAD	CVPR25	86.9	85.4	69.7	<span style="background-color: #d1ecf1;">96.6</span>	69.5	<span style="background-color: #f8d7da;">68.6</span>	83.7	<span style="background-color: #f8d7da;">92.8</span>	90.1	93.2	83.7
	IB-IUMAD	-	<span style="background-color: #d1ecf1;">89.5</span>	<span style="background-color: #f8d7da;">90.4</span>	<span style="background-color: #d1ecf1;">80.9</span>	<span style="background-color: #f8d7da;">97.4</span>	<span style="background-color: #f8d7da;">75.2</span>	<span style="background-color: #d1ecf1;">58.7</span>	87.9	91.1	<span style="background-color: #d1ecf1;">94.6</span>	<span style="background-color: #f8d7da;">95.7</span>	<span style="background-color: #f8d7da;">86.1</span>

Table 4. P-AUROC scores on Eyecandies dataset (10-0 with 0 step). The red / blue indicates the best/second-best results.

	Method	Year	Candy Cane	Chocolate Cookie	Chocolate Praline	Confetto	Gummy Bear	Hazelnut Truffle	Licorice Sandwich	Lollipop	Marsh-mallow	Peppermint Candy	Mean
RGB	DiAD	AAAI24	95.8	<span style="background-color: #d1ecf1;">96.2</span>	91.4	97.9	89.5	<span style="background-color: #d1ecf1;">87.8</span>	95.5	<span style="background-color: #d1ecf1;">97.3</span>	<span style="background-color: #d1ecf1;">98.9</span>	96.7	94.7
	IUF	ECCV24	<span style="background-color: #d1ecf1;">96.1</span>	95.8	<span style="background-color: #f8d7da;">92.8</span>	98.6	<span style="background-color: #f8d7da;">91.1</span>	86.4	<span style="background-color: #d1ecf1;">95.7</span>	96.9	98.8	97.5	<span style="background-color: #d1ecf1;">95.0</span>
	CDAD	CVPR25	94.8	95.6	92.0	<span style="background-color: #d1ecf1;">99.3</span>	87.1	<span style="background-color: #f8d7da;">88.9</span>	94.6	96.6	97.6	<span style="background-color: #f8d7da;">98.5</span>	94.5
	IB-IUMAD	-	<span style="background-color: #f8d7da;">96.2</span>	<span style="background-color: #f8d7da;">97.7</span>	<span style="background-color: #d1ecf1;">92.5</span>	<span style="background-color: #f8d7da;">99.4</span>	<span style="background-color: #d1ecf1;">89.8</span>	86.1	<span style="background-color: #f8d7da;">96.4</span>	<span style="background-color: #f8d7da;">97.4</span>	<span style="background-color: #f8d7da;">99.3</span>	<span style="background-color: #d1ecf1;">98.1</span>	<span style="background-color: #f8d7da;">95.3</span>
3D	DiAD	AAAI24	<span style="background-color: #d1ecf1;">94.9</span>	65.1	<span style="background-color: #d1ecf1;">60.5</span>	<span style="background-color: #d1ecf1;">78.8</span>	56.8	60.6	80.1	85.1	74.8	79.2	73.6
	IUF	ECCV24	<span style="background-color: #f8d7da;">95.0</span>	<span style="background-color: #f8d7da;">69.2</span>	59.8	<span style="background-color: #f8d7da;">81.8</span>	56.2	59.4	<span style="background-color: #d1ecf1;">80.7</span>	<span style="background-color: #f8d7da;">87.6</span>	<span style="background-color: #d1ecf1;">76.0</span>	<span style="background-color: #d1ecf1;">80.7</span>	<span style="background-color: #d1ecf1;">74.6</span>
	CDAD	CVPR25	78.9	54.5	56.9	60.4	<span style="background-color: #d1ecf1;">58.3</span>	<span style="background-color: #d1ecf1;">61.4</span>	62.3	74.1	58.7	56.8	62.2
	IB-IUMAD	-	<span style="background-color: #f8d7da;">95.0</span>	<span style="background-color: #d1ecf1;">65.8</span>	<span style="background-color: #f8d7da;">64.7</span>	78.6	<span style="background-color: #f8d7da;">62.3</span>	<span style="background-color: #f8d7da;">62.7</span>	<span style="background-color: #f8d7da;">81.9</span>	<span style="background-color: #d1ecf1;">85.5</span>	<span style="background-color: #f8d7da;">76.7</span>	<span style="background-color: #f8d7da;">81.6</span>	<span style="background-color: #f8d7da;">75.5</span>
RGB + 3D	DiAD	AAAI24	<span style="background-color: #f8d7da;">98.6</span>	<span style="background-color: #f8d7da;">97.9</span>	92.3	<span style="background-color: #d1ecf1;">99.3</span>	89.6	85.7	95.8	<span style="background-color: #f8d7da;">98.1</span>	<span style="background-color: #f8d7da;">97.8</span>	97.1	95.2
	IUF	ECCV24	96.5	97.3	<span style="background-color: #d1ecf1;">92.7</span>	<span style="background-color: #d1ecf1;">99.3</span>	<span style="background-color: #d1ecf1;">90.8</span>	<span style="background-color: #d1ecf1;">88.0</span>	<span style="background-color: #d1ecf1;">96.3</span>	97.1	<span style="background-color: #d1ecf1;">99.2</span>	<span style="background-color: #d1ecf1;">98.3</span>	<span style="background-color: #d1ecf1;">95.6</span>
	CDAD	CVPR25	94.6	96.5	92.4	<span style="background-color: #f8d7da;">99.5</span>	90.1	<span style="background-color: #f8d7da;">89.1</span>	94.2	<span style="background-color: #d1ecf1;">97.3</span>	97.2	97.6	94.9
	IB-IUMAD	-	<span style="background-color: #d1ecf1;">97.1</span>	<span style="background-color: #d1ecf1;">97.6</span>	<span style="background-color: #f8d7da;">94.7</span>	<span style="background-color: #f8d7da;">99.5</span>	<span style="background-color: #f8d7da;">93.8</span>	87.9	<span style="background-color: #f8d7da;">96.6</span>	96.7	<span style="background-color: #d1ecf1;">99.2</span>	<span style="background-color: #f8d7da;">98.6</span>	<span style="background-color: #f8d7da;">96.2</span>

mance of incremental unified anomaly detection tasks.

#### 4. Appendix C: AUPRO and P-AUROC on Eyecandies.

Tables 3 and 4 demonstrate the AUPRO and P-AUPRO scores under the setting of 10-0 with 0 step on the Eye-

candies dataset [2]. It is clear that IB-IUMAD consistently outperforms the baselines in most cases. In particular, when trained with both RGB and depth images, IB-IUMAD achieves 0.6% and 0.6% improvements compared to IUF in terms of P-AUROC and AUPRO scores, respectively (1.0% and 1.7% higher than DiAD, and 1.3% and 2.4% superior to CDAD, respectively). These experimen-

tal results again demonstrate that the proposed denoising framework not only effectively eliminates inter-object spurious feature interference, but also filters out redundant information from the fused multimodal features.

## 5. Appendix D: Algorithms

We provide a detailed description of the IB-IUMAD implementation algorithm. Taking the MVTEC 3D-AD dataset as an example, the training process primarily consists of two stages: first, we train a base model across six object categories; then, the remaining four objects are introduced sequentially through four incremental learning steps (i.e., 6-1 with 4 steps).

For the basic model training stage, we first employ the multimodal feature extraction network ( $\Phi_{MFEM}$ ) to extract the features of RGB ( $I_{rgb}$ ) and depth ( $I_{depth}$ ) images, respectively, and then generate abnormal RGB ( $A_{rgb}$ ) and depth ( $A_{depth}$ ) features through feature jitter. Subsequently, the Mamba decoder is used to extract fine-grained features (i.e.,  $M_{rgb}$  and  $M_{depth}$ ) from  $I_{rgb}$  and  $I_{depth}$ , aiming to introduce label information of the object category to mitigate interference from inter-object features. Next, the extracted features  $A_{rgb}$ ,  $A_{depth}$ ,  $M_{rgb}$ , and  $M_{depth}$  are fed into the multimodal reconstruction network ( $\Phi_{MRN}$ ) for feature reconstruction. Finally, we utilize the cross-attention mechanism to fuse the reconstructed features  $R_r$  and  $R_d$ , and adopt information bottleneck regularization to filter out noise features in  $F_{fusion}$ , thereby obtaining the final multimodal fusion feature  $F_{fusion}^g$ . The obtained  $F_{fusion}^g$  is fed into the discriminator ( $\Phi_{dis}$ ) for anomaly score discrimination. For the incremental training phase, the training process is similar to the basic model training. Notably, in Algorithm 1,  $I \in [0, 4]$  represents the incremental step,  $M_{ask}$  indicates the ground-truth anomaly segmentation images, and  $Y$  denotes the ground-truth label of objects.

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### Algorithm 1 IB-IUMAD pseudo-code.

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1: Input: Basic training data ( $\mathcal{D}_{trian}^B$ ), Incremental training data ( $\mathcal{D}_{trian}^I$ ), Test data ( $\mathcal{D}_{test}$ ).
2: Output: Trained IUMAD model.
3: /*Basic model training stage*/
4: for  $e \leftarrow 0$  to Epochs do
5:   for  $I_{rgb}, I_{depth}, M_{ask} \leftarrow \mathcal{D}_{trian}^B$  do
6:      $A_{rgb}, A_{depth} = \Phi_{MFEM}(I_{rgb}, I_{depth})$ 
7:      $M_{rgb}, M_{depth} = \Phi_{Mamba}(I_{rgb}, I_{depth})$ 
8:      $R_r, R_d = \Phi_{MRN}(A_{rgb}, M_{rgb}, A_{depth}, M_{depth})$ 
9:      $F_{fusion} = Cross\_attention(R_r, R_d)$ 
10:     $F_{fusion}^g = \Phi_{IB}(F_{fusion})$ 
11:     $M = \Phi_{Dis}(I_{rgb}, F_{fusion}^g)$ 
12:     $\mathcal{L}_{rgb} = \Phi_{CE\_loss}(M_{rgb}, Y)$ 
13:     $\mathcal{L}_{Depth} = \Phi_{CE\_loss}(M_{Depth}, Y)$ 
14:     $\mathcal{L}_{IB} = \Phi_{KL\_loss}(Y_{F_{fusion}^g}, Y_{F_{fusion}})$ 
15:     $\mathcal{L}_{fusion} = \Phi_{MSE\_loss}(I_{rgb}, F_{fusion}^g, M_{ask})$ 
16:     $\mathcal{L}_{total} = \mathcal{L}_{rgb} + \mathcal{L}_{Depth} + \mathcal{L}_{IB} + \mathcal{L}_{fusion}$ 
17:  end for
18: end for
19: /*Incremental model training phase*/
20: for  $I \leftarrow 0$  to Epochs do
21:   for  $e \leftarrow 0$  to Epochs do
22:     for  $I_{rgb}, I_{depth}, M_{ask} \leftarrow \mathcal{D}_{trian}^I$  do
23:        $A_{rgb}, A_{depth} = \Phi_{MFEM}(I_{rgb}, I_{depth})$ 
24:        $M_{rgb}, M_{depth} = \Phi_{Mamba}(I_{rgb}, I_{depth})$ 
25:        $R_r, R_d = \Phi_{MRN}(A_{rgb}, M_{rgb}, A_{depth}, M_{depth})$ 
26:        $F_{fusion} = Cross\_attention(R_r, R_d)$ 
27:        $F_{fusion}^g = \Phi_{IB}(F_{fusion})$ 
28:        $M = \Phi_{Dis}(I_{rgb}, F_{fusion}^g)$ 
29:        $\mathcal{L}_{rgb} = \Phi_{CE\_loss}(M_{rgb}, Y)$ 
30:        $\mathcal{L}_{Depth} = \Phi_{CE\_loss}(M_{Depth}, Y)$ 
31:        $\mathcal{L}_{IB} = \Phi_{KL\_loss}(Y_{F_{fusion}^g}, Y_{F_{fusion}})$ 
32:        $\mathcal{L}_{fusion} = \Phi_{MSE\_loss}(I_{rgb}, F_{fusion}^g, M_{ask})$ 
33:        $\mathcal{L}_{total} = \mathcal{L}_{rgb} + \mathcal{L}_{Depth} + \mathcal{L}_{IB} + \mathcal{L}_{fusion}$ 
34:     end for
35:   end for
36: end for

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