

8.1.

SOLUTION Suppose the total concentration of the enzyme is  $[E_0]$  and  $[S] = x$ ,

$$V_p = V_o = k_3 [ES]$$

$$V_{ES} = V_{ES} (\text{synthesis}) - V_{ES} (\text{decomposition})$$

$$= k_1 ([E_0] - [ES]) ([S]) - (k_2 + k_3) [ES]$$

Similarly,

$$V_E = k_1 ([E_0] - [ES]) \overset{([S])}{\downarrow} - (k_2 + k_3) [ES]$$

$$V_S = k_1 ([E_0] - [ES]) ([S]) - k_2 [ES]$$

Since the reaction is in steady state, so

$$V_{ES} (\text{synthesis}) = V_{ES} (\text{decomposition})$$

$$\text{i.e. } k_1 ([E_0] - [ES]) [S] = (k_2 + k_3) [ES]$$

Simplifying the equation gives

$$[ES] = \frac{[E_0] [S]}{[S] + (k_2 + k_3) / k_1}$$

Let  $K_m$  (Michaelis Constant) =  $\frac{k_2 + k_3}{k_1}$ , then

$$[ES] = \frac{[E_0] [S]}{K_m + [S]}$$

Since  $V_p = k_3 [ES]$ , so

$$V_p = \frac{k_3 [E_0] [S]}{K_m + [S]} = \frac{k_3 [E_0] x}{K_m + x}, K_m = \frac{k_2 + k_3}{k_1}$$

Summarizing :

$$V_p = k_3 [ES]$$

$$V_{ES} = k_1 ([E_0] - [ES]) [S] - (k_2 + k_3) [ES]$$

$$V_E = k_1 ([E_0] - [ES]) [S] - (k_2 + k_3) [ES]$$

$$V_S = k_1 ([E_0] - [ES]) [S] - k_2 [ES]$$

When the reaction is in steady state, we conclude that

$$[ES] = \frac{[E_0][S]}{K_m + [S]}, \quad K_m = \frac{k_2 + k_3}{k_1}$$

Thus

$$V_p = \frac{k_3 [E_0][S]}{K_m + [S]}$$

$$= \frac{k_3 [E_0]x}{K_m + x}, \quad K_m = \frac{k_2 + k_3}{k_1}$$