

# Physics 230 Notes

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# Chapter 1

## Electric Charge and Electric Field

### 1.1 Electric Charge

**Electromagnetism** (EM) affects only charged particles, mainly electrons and protons. All particles have charges that are integer multiples of the elementary charge  $e$  such that the charge is given by

$$q = ne, \quad (1.1)$$

where  $q$  represents charge (C),  $n$  represents an integer, and  $e = 1.6022 \times 10^{-19}$  C represents the elementary charge.

Electric charge is conserved. This means that the total charge of any isolated system with no charge moving in or out stays the same – charge is never created or destroyed.

**Coulomb's Law** states that charges of the same sign repel and charges of the opposite sign attract. Furthermore, the force  $F$  produced by charges can be calculated via

$$F = k \frac{q_1 q_2}{r^2}, \quad (1.2)$$

where  $k = 9.0 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$ ,  $q_1$  represents the first charge,  $q_2$  represents the second charge, and  $r$  represents the separation distance.

The **principle of superposition of forces** is the vector sum of the individual forces:

$$F = k \frac{q_1 q_2}{(r_{12})^2} r_{12} + k \frac{q_1 q_2}{(r_{13})^2} r_{13} = q_1 \vec{E}. \quad (1.3)$$

## 1.2 Electric Field and Electric Forces

The **electric field of a point charge** is given by

$$\vec{E}(\vec{r}_0) = \frac{kq}{r^2} = \frac{\vec{F}}{q}, \quad (1.4)$$

where  $q$  denotes the charge of the point source (C) and  $r$  denotes the radial distance of the point charge from the origin.

The **electric field of a group of charges** is the superposition of all the electric forces from all the charges. This can be approximated with volume charge density ( $\rho$ ) via

$$\vec{E}(\vec{r}_o) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r})(\vec{r}_0 - \vec{r})}{|\vec{r}_0 - \vec{r}|^3} dx dy dz, \quad (1.5)$$

where  $\epsilon_0 = 8.854 \times 10^{-12} \frac{\text{C}^2}{\text{N}\cdot\text{m}^2}$ ,  $\rho(\vec{r})$  is the surface charge density, and  $\vec{r}$  is the radius.

For a **conductor without current flow**, the charge all resides on the surface. Using the surface charge density  $\sigma(\vec{r})$ , we can approximate the electric field via

$$\vec{E}(\vec{r}_o) = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma(\vec{r})(\vec{r}_0 - \vec{r})}{|\vec{r}_0 - \vec{r}|^3} dA. \quad (1.6)$$

If one has a **thin wire** where all the charge resides, with linear charge density  $\lambda(\vec{r}) = \frac{dq}{dl}$ , where  $dl$  is the element of length along the wire, then

$$\vec{E}(\vec{r}_o) = \frac{1}{4\pi\epsilon_0} \int \frac{\lambda(\vec{r})(\vec{r}_0 - \vec{r})}{|\vec{r}_0 - \vec{r}|^3} dl. \quad (1.7)$$

## 1.3 Electric Field Lines

Electric field lines have tangent vectors parallel to the electric field and begin only on positive charges and end only on negative charges, though they can also go to infinity in either direction.

## 1.4 Electric Dipoles

An **electric dipole** is a pair of point charges of equal magnitude and opposite sign (a positive charge  $q$  and a negative charge  $-q$  separated by a distance  $d$ ).

An **electric dipole moment** is the product of the positive charge  $q$  and the displacement  $d$  it is separated from the negative charge  $-q$ , given by

$$\vec{p} = q\vec{d}. \quad (1.8)$$

Using the volume charge density formula  $\rho(\vec{r}) = \rho(x\vec{i} + y\vec{j} + z\vec{k}) = \rho(x, y, z)$ , we can approximate the electric dipole of a huge number of elementary charges (total charge is neutral) via

$$\vec{P} = \int \rho(\vec{r})\vec{r} \, dx \, dy \, dz. \quad (1.9)$$

The total force on an electric dipole is just the net force from an external electric field (the electric field from all the other charges that are not part of the electric dipole). This is true for the total torque.

If the electric dipole moment  $\vec{P}$  is not parallel to  $\vec{E}$ , then the electric field exerts a torque on the dipole which can be calculated using

$$\vec{\tau} = \vec{P} \times \vec{E}, \quad (1.10)$$

where  $\vec{P}$  is the electric dipole moment,  $\vec{E}$  is the electric field, and the direction of  $\tau$  is perpendicular to both  $\vec{P}$  and  $\vec{E}$ .

To calculate the potential energy of a dipole, we use

$$U = -\vec{P} \cdot \vec{E}. \quad (1.11)$$

To approximate the field of an electric dipole at  $r \gg d$  and using binomial expansion, we use

$$\vec{E}(\vec{r}) = \frac{3(\vec{p} \cdot \vec{r})(\vec{r} - \vec{p})}{4\pi\epsilon_0 r^3}, \quad (1.12)$$

where  $\vec{p} = p \cos(\theta)$  and  $\epsilon_0 = 8.854 \times 10^{-12} \frac{\text{C}^2}{\text{N}\cdot\text{m}^2}$ .

## Chapter 2

# Electric Potential

## Chapter 3

# Electric Potential

### 3.1 Gauss's Law

Gauss's law states that the outward flux of the electric field through a closed surface is equal to the total charge inside the surface divided by the electric constant,  $\epsilon_0$ :

$$\Phi_E \equiv \oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}. \quad (3.1)$$

The total flux through a closed surface and the air mass flux can be calculated using

$$\Phi_E = \oint \rho_m \vec{V} \cdot d\vec{A}, \quad (3.2)$$

where  $\rho_m$  is the mass density and  $\vec{V}$  is the velocity. The **electric flux** is analogous to mass flux, given by

$$\Phi_M = \int \rho_m \vec{v} d\vec{A}. \quad (3.3)$$

When no mass is created or destroyed, we have that

$$\Phi_M = \frac{-dM_{encl}}{dt}. \quad (3.4)$$

and if it is also stationary.  $\Phi_M = 0$

Mass creation is when:

$$\Phi_m + \frac{dM}{dt} > 0 \quad (3.5)$$

Mass destruction is when

$$\Phi_m + \frac{dM}{dt} < 0 \quad (3.6)$$

Conservation of charge

$$\Phi_Q + \frac{dQ}{dt} = 0 \quad (3.7)$$

Second Law of thermodynamics is when

$$\Phi_S + \frac{dS}{dt} \geq 0 \quad (3.8)$$

Gauss's law and spherical symmetry. Using coulomb's law for one charge

$$\vec{E} = \frac{q\vec{r}}{4\pi\epsilon_0 r^2} \quad (3.9)$$

For more than one charge, you need to do superposition

Every region totally inside a conductor is neutral. Excess charge all lies on the surface (static). An interior surface of a conductor, surrounding a cavity, only has charge if there is nonzero charge inside the cavity; the two charges cancel

Spherical symmetry



## Chapter 4

# Capacitance and Dielectrics

## Chapter 5

# Current, Resistance, and Electromotive Force

## Chapter 6

# Direct-Current Circuits

## Chapter 7

# Magnetic Field and Magnetic Forces

## Chapter 8

# Sources of Magnetic Field

## Chapter 9

# Electromagnetic Induction

## Chapter 10

# Inductance

## Chapter 11

# Alternating Current



## Chapter 12

# Electromagnetic Waves