

Input:  $y_t, \hat{y}_{t|t-1} \in \mathbb{R}^p$  for  $t=1, \dots, T$   
 window size  $n$ , set  $\Lambda$  (or step  $x$ )

$$\hat{e}_{t|t-1} = y_t - \hat{y}_t \quad \text{for } t=1, \dots, T$$

for  $i = n : T-1$  do

$$j = i - n + 1$$

$$\hat{W}_j = \frac{1}{n} \sum_{t=j}^i \hat{e}_{t|t-1} \hat{e}_{t|t-1}'$$

$$\hat{R}_j = \hat{D}_j^{-1/2} \hat{W}_j \hat{D}_j^{-1/2}$$

$\Lambda = \text{sequence}(\text{from} = 0, \text{to} = 1, \text{step} = x)$

for  $s \in \Lambda$

Compute  $\hat{R}_{j,s}$  using Eq (1)

Compute  $\hat{\lambda}_{j,s}$  using Eq (2)

$$\hat{R}_{j,s}^N = \hat{\lambda}_{j,s} \hat{R}_{j,s} + (1 - \hat{\lambda}_{j,s}) \hat{R}_j$$

$$\hat{W}_{j,s}^N = \hat{D}_j^{1/2} \hat{R}_{j,s}^N \hat{D}_j^{1/2}$$

$$P_{j,s} = (S' \hat{W}_{j,s}^{N-1} S)^{-1} S' \hat{W}_{j,s}^{N-1}$$

$$\tilde{y}_{i+1|i,s} = S P_{j,s} \hat{y}_{i+1}$$

$$\tilde{e}_{i+1|i,s} = y_{i+1} - \tilde{y}_{i+1|i,s}$$

end

end

$$MSE_s = MSE(\tilde{e}_{i+1|i,s} \text{ for } i = n, n+1, \dots, T-1)$$

$$\hat{s}^* = \underset{s \in \Lambda}{\operatorname{argmin}} MSE_s$$

Compute  $\hat{\lambda}^*$  on  $\hat{e}_{t|t-1}$  for  $t=1, \dots, T$  using  $\hat{s}^*$  by Eq (1)

Compute  $\hat{W}_1^*$  using  $\hat{s}^*, \lambda^*$  by Eq (3)

Return  $\hat{s}^*, \hat{\lambda}^*, \hat{W}_1^*$