Introduction to Vector Processing

- Motivation: Why vector Processing?
- Paper: VEC-1
- Limits to Conventional Exploitation of ILP
- Flynn's 1972 Classification of Computer Architecture
- Data Parallelism and Architectures
- Vector Processing Fundamentals

Paper: VEC-1

- Vectorizable Applications
- Loop Level Parallelism (LLP) Review (From 551)
- Vector vs. Single-Issue and Superscalar Processors
- Properties of Vector Processors/ISAs
- Vector MIPS (VMIPS) ISA
- Vector Memory Operations Basic Addressing Modes
- Vectorizing Example: DAXPY
- Vector Execution Time Evaluation
- Vector Load/Store Units (LSUs) and Multi-Banked Memory
- Vector Loops (n > MVL): Strip Mining
- More on Vector Memory Addressing Modes: Vector Stride Memory Access
- Vector Operations Chaining | Vector element data forwarding

vector element data forwarding

- Vector Conditional Execution & Gather-Scatter Operations
- Vector Example with Dependency: Vectorizing Matrix Multiplication
- Common Vector Performance Metrics & Examples
- Limited Vector Processing: SIMD/vector or Multimedia Extensions to Scalar ISA
- Summary: Vector Processing Advantages & Pitfalls
- Vector Processing & VLSI: Vector Intelligent RAM (VIRAM)

Papers: VEC-2, VEC-3

- Potential Advantages
- VIRAM Architecture
- Overview of VIRAM Prototype Generations: VIRAM-1, VIRAM-2

Papers: VEC-1, VEC-2, VEC-3

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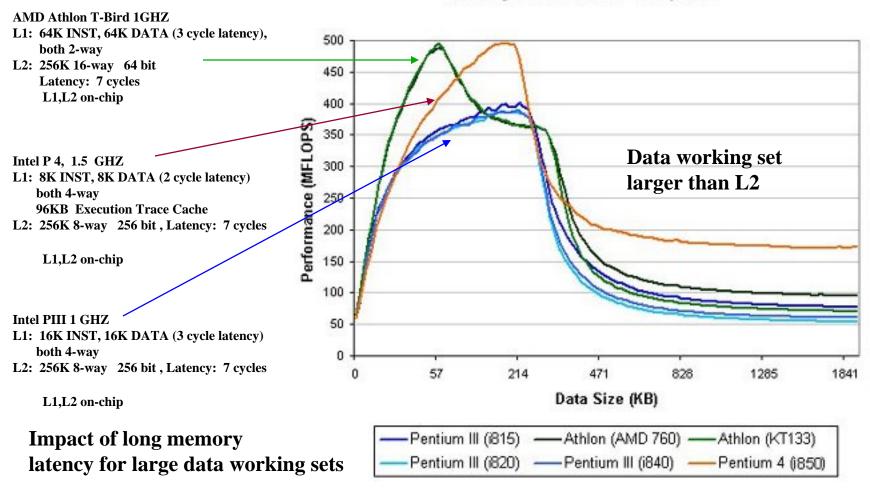
#1 lec # 7 Fall 2012 10-1-2012

Problems with Superscalar approach

- Limits to conventional exploitation of ILP:
- 1) <u>Pipelined clock rate</u>: Increasing clock rate requires deeper pipelines with longer pipeline latency which increases the CPI increase (longer branch penalty, other hazards).
- 2) <u>Instruction Issue Rate</u>: Limited instruction level parallelism (ILP) reduces actual instruction issue/completion rate. (vertical & horizontal waste) **SMT** fixes this one?
- 3) <u>Cache hit rate</u>: Data-intensive scientific programs <u>have very large</u> <u>data working sets</u> accessed with poor locality; others have continuous data streams (multimedia) and hence poor locality. (poor memory latency hiding).
- 4) <u>Data Parallelism</u>: Poor exploitation of data parallelism present in many scientific and multimedia applications, where similar independent computations are performed on large arrays of data (Limited ISA, hardware support).
- As a result, actual achieved performance is much less than peak potential performance and low computational energy efficiency (computations/watt)

X86 CPU Cache/Memory Performance Example: AMD Athlon T-Bird Vs. Intel PIII, Vs. P4

Memory Performance - Linpack



Source: http://www1.anandtech.com/showdoc.html?i=1360&p=15

Flynn's 1972 Classification of Computer **Architecture**

i.e single-threaded Uniprocessor

SISD

Single Instruction stream over a Single Data stream (SÍSD): Conventional sequential machines (Superscalar, VLIW).

SIMD

Single Instruction stream over Multiple Data streams (SIMD): Vector computers, array of synchronized processing elements. (exploit data parallelism) AKA Data Parallel or Data Streaming

Architectures

MISD

Multiple Instruction streams and a Single Data stream (MISD): Systolic arrays for pipelined execution.

MIMD

Multiple Instruction streams over Multiple Data streams (MIMD): Parallel computers:

Parallel Processor Systems: Exploit Thread Level Parallelism (TLP)

- Shared memory multiprocessors (e.g. SMP, CMP, NUMA, SMT)
- Multicomputers: Unshared distributed memory, message-passing used instead (Clusters)

Instruction stream = Hardware context or thread

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From 756 Lecture 1

Data Parallel Systems SIMD in Flynn taxonomy

• Programming model: Data Parallel

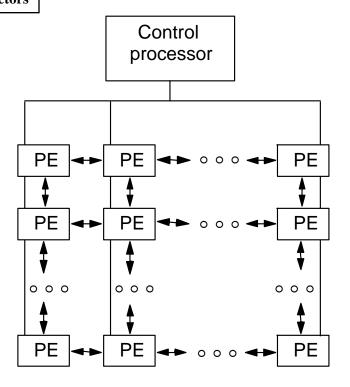
- Operations performed in parallel on each element of data structure i.e elements of arrays or vectors
- Logically single thread of control, performs sequential or parallel steps
- Conceptually, a processing element (PE) or processor is associated with each data element

Architectural model

- Array of many simple, cheap processors each with little memory
 - Processors don't sequence through instructions Control processor does that
- Attached to a control processor that issues instructions
- Specialized and general communication, cheap global synchronization

• Example machines:

- Thinking Machines CM-1, CM-2 (and CM-5)
- Maspar MP-1 and MP-2,
- Current Variations: IBM's Cell Architecture, Graphics Processor Units (GPUs)
 - Difference: PE's are full processors optimized for data parallel computations.



PE = Processing Element

SIMD (array) Machine

Alternative Model:Vector Processing

- <u>Vector processing exploits data parallelism</u> by performing the same computation on linear arrays of numbers "vectors" using one instruction.

Per scalar SCALAR instruction (1 operation) Scalar ISA (RISC or CISC) Add.d F3, F1, F2

VECTOR Per vector instruction (N operations) (Vector-vector instruction shown) Vector ISA Up to Maximum lenath Vector Add vector **Vector Registers** Length addv.d v3, v1, v2 (MVL) $\mathbf{v} = \mathbf{vector}$

VEC-1

Typical MVL = 64 (Cray)

Vector (Vectorizable) Applications

Applications with <u>high degree of data parallelism</u> (loop-level parallelism), thus suitable for vector processing. <u>Not Limited to scientific computing</u>

- Astrophysics
- Atmospheric and Ocean Modeling
- Bioinformatics
- Biomolecular simulation: Protein folding
- Computational Chemistry
- Computational Fluid Dynamics
- Computational Physics
- Computer vision and image understanding
- Data Mining and Data-intensive Computing
- Engineering analysis (CAD/CAM)
- Global climate modeling and forecasting
- Material Sciences
- Military applications
- Quantum chemistry
- VLSI design
- Multimedia Processing (compress., graphics, audio synth, image proc.)
- Standard benchmark kernels (Matrix Multiply, FFT, Convolution, Sort)
- Lossy Compression (JPEG, MPEG video and audio)
- Lossless Compression (Zero removal, RLE, Differencing, LZW)
- Cryptography (RSA, DES/IDEA, SHA/MD5)
- Speech and handwriting recognition
- Operating systems/Networking (memcpy, memset, parity, checksum)
- Databases (hash/join, data mining, image/video serving)
- Language run-time support (stdlib, garbage collection)

Data Parallelism & Loop Level Parallelism (LLP)

- <u>Data Parallelism</u>: Similar independent/parallel computations on different elements of arrays that usually result in <u>independent (or parallel) loop iterations</u> when such computations are implemented as sequential programs.
- - One method covered earlier to accomplish this is by <u>unrolling the loop</u> either statically by the compiler, or dynamically by hardware, which <u>increases the size of the basic block</u> present. This resulting larger basic block provides <u>more instructions</u> that can be <u>scheduled</u> or re-ordered by the compiler/hardware to eliminate more stall cycles.
- The following loop has parallel loop iterations since computations in each iterations are data parallel and are performed on different elements of the arrays.

Scalar Code

4 vector instructions:

LV
LV
LV
ADDV
SV

Load Vector X
Load Vector Y
Add Vector X, X, Y
Store Vector X

Vector
Code

- In supercomputing applications, data parallelism/LLP has been traditionally exploited by <u>vector ISAs/processors</u>, utilizing vector instructions
 - Vector instructions operate on a number of data items (vectors) producing \
 a vector of elements not just a single result value. The above loop might require just four such instructions.

Assuming Maximum Vector Length(MVL) = 1000 is supported otherwise a vector loop (i.e strip mining) is needed, more on this later

Loop-Level Parallelism (LLP) Analysis

Loop-Level Parallelism (LLP) analysis focuses on whether data accesses in later iterations of a loop are data dependent on data values produced in earlier iterations and possibly making loop iterations independent (parallel).

e.g. in for (i=1; i<=1000; i++) Iteration #
$$\rightarrow$$
 1 2 3 1000
Usually: Data Parallelism \rightarrow LLP \times [i] = \times [i] + \times ; \leftarrow S1 (Body of Loop) \times S1 \times S1 \times

the computation in each iteration is <u>independent</u> of the <u>previous iterations</u> and the loop is thus parallel. The use of X[i] twice is within a single iteration.

 \Rightarrow Thus loop iterations are parallel (or independent from each other).

Classification of Date Dependencies in Loops:

- **Loop-carried Data Dependence:** A data dependence between different loop iterations (data produced in an earlier iteration used in a later one).
- Not Loop-carried Data Dependence: Data dependence within the same loop iteration.
- LLP analysis is important in software optimizations such as loop unrolling since it usually requires <u>loop iterations</u> to be <u>independent (and in vector processing)</u>.
- LLP analysis is normally done at the source code level or close to it since assembly language and target machine code generation introduces loop-carried name dependence in the registers used in the loop.
 - Instruction level parallelism (ILP) analysis, on the other hand, is usually done when instructions are generated by the compiler.

LLP Analysis Example 1

In the loop:

```
for (i=1; i<=100; i=i+1) {  A[i+1] = A[i] + C[i]; \text{ } /* \text{ } S1 \text{ } */ \\ B[i+1] = B[i] + A[i+1]; \} \text{ } /* \text{ } S2 \text{ } */ \\ \}
```

Loop-carried Dependence

Iteration # i i+1Not Loop Carried Dependence (within the same iteration)

S1 A_{i+1} A_{i+1

(Where A, B, C are distinct non-overlapping arrays)

Dependency Graph

- S2 uses the value A[i+1], computed by S1 in the same iteration. This data dependence is within the same iteration (not a loop-carried dependence).
 - \Rightarrow does not prevent loop iteration parallelism.

i.e.
$$S1 \rightarrow S2$$
 on A[i+1] Not loop-carried dependence

S1 uses a value computed by S1 in the earlier iteration, since iteration i computes A[i+1] read in iteration i+1 (loop-carried dependence, prevents parallelism). The same applies for S2 for B[i] and B[i+1]

i.e.
$$S1 \rightarrow S1$$
 on A[i] Loop-carried dependence $S2 \rightarrow S2$ on B[i] Loop-carried dependence

⇒ These two data dependencies are loop-carried spanning more than one iteration (two iterations) preventing loop parallelism.

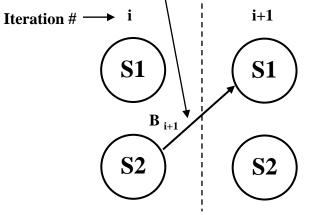
In this example the loop carried dependencies form two dependency chains starting from the very first iteration and ending at the last iteration

From 551

LLP Analysis Example 2

Dependency Graph Loop-carried Dependence

• In the loop:

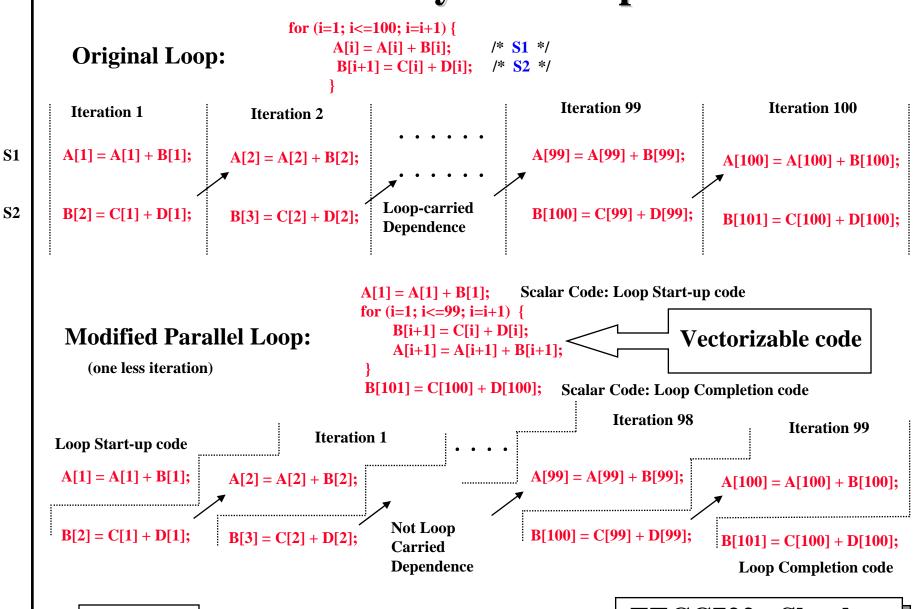


- S1 uses the value B[i] computed by S2 in the previous iteration (loop-carried dependence)
 i.e. S2 → S1 on B[i] Loop-carried dependence
- This dependence is not circular:
 - S1 depends on S2 but S2 does not depend on S1.
- Can be made parallel by replacing the code with the following:

```
A[1] = A[1] + B[1]; \qquad \text{Scalar Code: Loop Start-up code} for \ (i=1; \ i <= 99; \ i=i+1) \ \{ B[i+1] = C[i] + D[i]; \qquad \qquad code \qquad Parallel \ loop \ iterations \ (data \ parallelism \ in \ computation \ exposed \ in \ loop \ code) B[101] = C[100] + D[100]; \qquad \text{Scalar Code: Loop Completion code}
```

From 551

LLP Analysis Example 2



From 551

Properties of Vector Processors/ISAs

- <u>Each result (element) in a vector operation is independent</u> of previous results (Data Parallelism, LLP exploited)
 - => Multiple pipelined Functional units (lanes) usually used, vector compiler ensures <u>no dependencies between computations on elements of a single vector instruction</u>
 - => Higher clock rate (less complexity)
- Vector instructions access memory with known patterns:
 - => Highly interleaved memory with multiple banks used to provide the high bandwidth needed and hide memory latency.
 - => Amortize memory latency of over many vector elements.
 - => No (data) caches usually used. (Do use instruction cache)

i.e. lower effective impact of memory latency

Thus more predictable performance

Up to MVL computations

- A single vector instruction implies a large number of computations (replacing loops or reducing number of iterations needed) By a factor of MVL
 - => Fewer instructions fetched/executed, TLB look-ups....
 - => Reduces branches and branch problems (control hazards) in pipelines.

As if loop-unrolling by default MVL times?

Vector vs. Single-Issue Scalar Processor

Single-issue Scalar

- One instruction fetch, decode, dispatch per operation
- Arbitrary register accesses, adds area and power
- Loop unrolling and software pipelining for high performance increases instruction cache footprint
- All data passes through cache; waste power if no temporal locality
- One TLB lookup per load or store
- Off-chip access in whole cache lines

Vector

- One instruction fetch, decode, dispatch per vector (up to MVL elements)
- Structured register accesses
- Smaller code for high performance, less power in instruction cache misses
- Bypass cache (for data)
- One TLB lookup per group of loads or stores
- Move only necessary data across chip boundary

Vector vs. Superscalar Processors

Superscalar

- Control logic grows quad-ratically with issue width
- Control logic consumes energy regardless of available parallelism
 - Low Computational power efficiency (computations/watt)
- Dynamic nature makes real-time performance less predictable
- Speculation to increase visible parallelism wastes energy and adds complexity

Vector

- Control logic grows linearly with issue width
- Vector unit switches off when not in use
 - Higher energy efficiency
- More predictable real-time performance
- Vector instructions expose data parallelism without speculation
- Software control of speculation when desired:
 - Whether to use vector mask or compress/expand for conditionals

The above differences are <u>in addition</u> to the "Vector vs. Single-Issue Scalar Processor" differences (from last slide)

Changes to Scalar Processor to Run Vector Instructions

- A vector processor typically consists of:
 1- <u>a pipelined scalar unit plus</u>
 2- <u>a vector unit.</u>
- The scalar unit is basically not different than advanced pipelined CPUs, commercial vector machines have included both out-of-order scalar units (NEC SX/5) and VLIW scalar units (Fujitsu VPP5000).
 - Computations that don't run in vector mode don't have high ILP, so can make scalar CPU simple.
- The vector unit supports a vector ISA including decoding of vector instructions which includes:
 - Vector functional units.

Multiple Pipelined Functional Units (FUs) or lanes

ISA vector register bank.

Each has MVL elements

- **3** Vector control registers
 - e,.g Vector Length Register (VLR), Vector Mask (VM)

1 1 1 0 0 0 1

Vector Mask (VM) Register

- MVL Bits

- **4** − Vector memory Load-Store Units (LSUs).
- 5 Multi-banked main memory To provide the very high data bandwidth needed
- Send scalar registers to vector unit (for vector-scalar ops).
- Synchronization for results back from vector register, including exceptions.

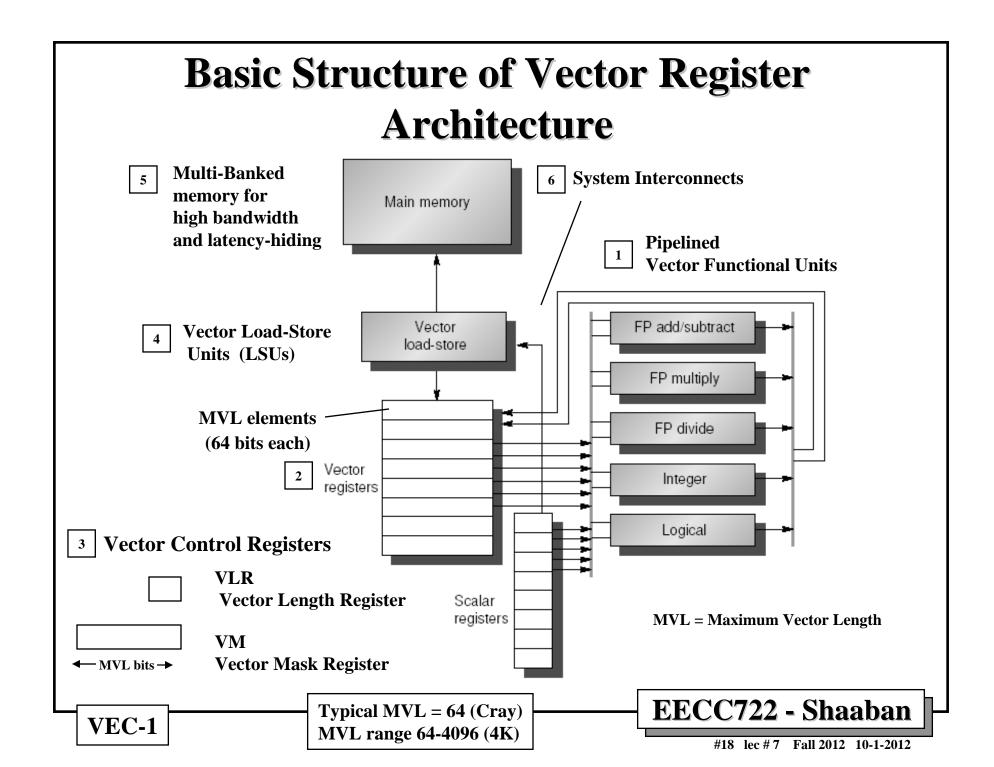
6 + System component interconnects

Basic Types of Vector Architecture/ISAs

- Types of architecture/ISA for vector processors:
 - Memory-memory Vector ISAs/Processors:
 All vector operations are memory to memory
 (No vector ISA registers)
 - <u>Vector-register ISAs/Processors:</u>

All vector operations between vector registers (except vector load and store)

- Vector equivalent of load-store scalar GPR architectures (ISAs)
- Includes all vector machines since the late 1980 (Cray, Convex, Fujitsu, Hitachi, NEC)
- We assume vector-register for rest of the lecture.



Components of Vector Processor

- <u>Vector Functional Units (FUs):</u> Fully pipelined, start new operation every clock
 - Typically 4 to 8 Fus (or lanes): FP add, FP mult, FP reciprocal (1/X), integer add, logical, shift; may have multiple of same unit (multiple lanes of the same type)

More on lanes later

- ISA Vector Register Bank: Fixed length bank holding vector ISA registers
 - Has at least 2 read and 1 write ports
 - Typically 8-32 vector registers, each holding MVL = 64-128 elements (typical, up to 4K possible) 64-bit elements.
 - ISA Scalar registers: single element for FP scalar or address.
- **Vector Control Registers:** Vector Length Register (VLR), Vector Mask Register (VM).
- <u>Vector Load-Store Units (LSUs):</u> fully pipelined unit to load or store a vector; may have multiple LSUs.
- Multi-Banked memory: Multi-Banked memory for high throughput (bandwidth) and long latency-hiding.
- System Interconnects: Cross-bar to connect FUs, LSUs, registers, memory.

Vector ISA Issues:

How To Pick Maximum Vector Length (MVL)?

- Longer good because:
 - 1) Hide vector startup time
 - 2) Lower instruction bandwidth

Vector Instruction Processing Time (or latency):

Startup Time

Vector elements computation time

Pipelined vector functional unit (FU) startup latency (fill cycles)

One cycle per result vector element (up to MVL cycles)

Fewer instructions fetched for a given computation

- 3) Tiled access to memory reduce scalar processor memory bandwidth needs
- 4) If known maximum length of app. is < MVL, no strip mining (vector loop) overhead is needed.
- 5) Better spatial locality for memory access
- Longer not much help because:
 - 1) Diminishing returns on overhead savings as keep doubling number of elements.
 - 2) Need natural application vector length to match physical vector register length, or no help

i.e MVL

Media-Processing: Vectorizable? Vector Lengths?

MVL?

Computational Kernel

- Matrix transpose/multiply
- DCT (video, communication)
- FFT (audio)
- Motion estimation (video)
- Gamma correction (video)
- Haar transform (media mining)
- Median filter (image processing)
- Separable convolution (img. proc.)

Natural Application Vector length

vertices at once image width 256-1024 image width, iw/16 image width image width image width image width image width image width

(from Pradeep Dubey - IBM,

http://www.research.ibm.com/people/p/pradeep/tutor.html)

Vector Implementation

- Vector register file:
 - Each register is an array of MVL elements.
 - Size of each register is determined by the maximum vector length (MVL) supported by the implemented vector ISA.

Vector Control Registers

- Vector Length Register (VLR) determines the actual vector length used for a particular vector operation or instruction.
- Vector Mask Register (VM) determines which elements of a vector will be computed.
 ✓ MVL Bits →

Vector Lanes

- Multiple parallel execution units = "lanes" (sometimes called "pipelines" or "pipes") of the same type:
 - Multiples pipelined functional units (lanes) are each assigned a number of computations of a single vector instruction.

→ Vector Instruction Latency = Vector Startup Time + $\left[\frac{MVL}{N}\right]$

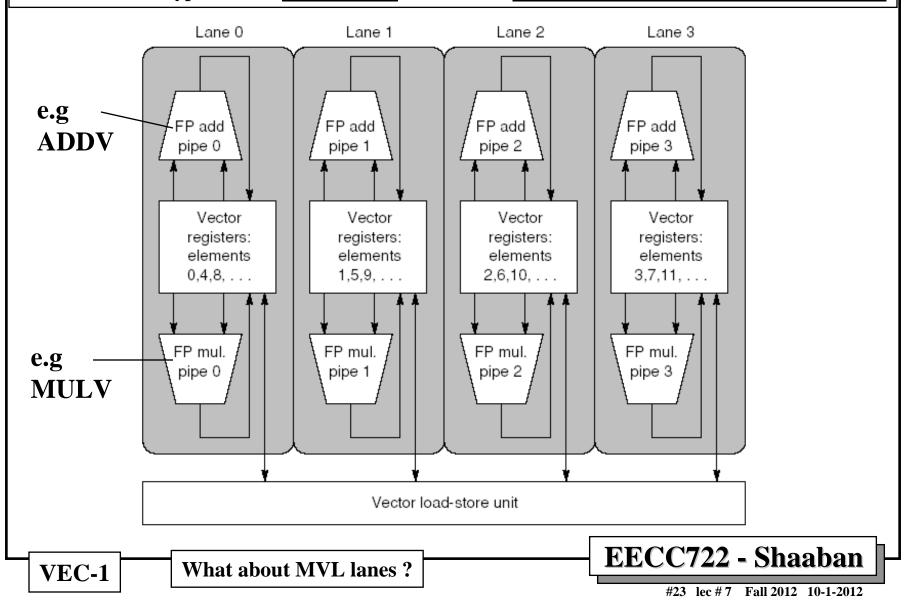
Where N is the number of lanes supported by the vector processor

- Thus, supporting <u>multiple lanes</u> in a vector processor reduces vector instruction latency by producing multiple elements of the result vector per cycle (after fill cycles).
- Having multiple lanes, however, does not reduce vector startup time (vector unit fill cycles).

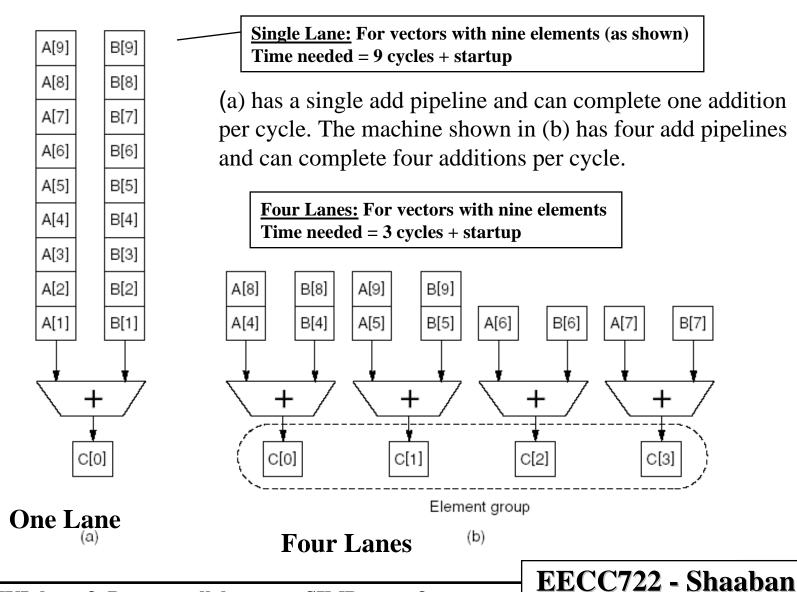
Processing time for a vector instruction in cycles

Structure of a Vector Unit Containing Four Lanes

<u>Number of Lanes in a vector unit (processor):</u> The number of vector functional units of the same type that are <u>each assigned</u> a number of <u>computations</u> of the same vector instruction



Using Multiple Lanes (Vector Functional Units) to Improve Performance of A Single Vector Add Instruction



MVL lanes? Data parallel system, SIMD array?

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Example Vector-Register Architectures

	Processor (year)	Clock rate (MHz)	Vector registers	Elements pe register (64-bit elements)	(MVL) Vector arithmetic units	(LSUs) Vector load-store units	Lanes
Peak 133 MFLOPS	Cray-1 (1976)	80	8	64	FP add, FP multiply, FP reciprocal, integer add, logical, shift	1	1
	Cray X-MP (1983) Cray Y-MP (1988)	118 166	8	64	8: FP add, FP multiply, FP reciprocal, integer add, 2 logical, shift, population count/parity	2 loads 1 store	1
	Cray-2 (1985)	244	8	64	5: FP add, FP multiply, FP reciprocal/ sqrt, integer add/shift/population count, logical	1	1
	Fujitsu VP100/ VP200 (1982)	133	8–256	32-1024	FP or integer add/logical, multiply, divide	2	1 (VP100) 2 (VP200)
	Hitachi S810/ S820 (1983)	71	32	256	4: FP multiply-add, FP multiply/ divide-add unit, 2 integer add/logical	3 loads 1 store	1 (S810) 2 (S820)
	Convex C-1 (1985)	10	8	128	2: FP or integer multiply/divide, add/ logical	1	1 (64 bit) 2 (32 bit)
	NEC SX/2 (1985)	167	8 + 32	256	 FP multiply/divide, FP add, integer add/logical, shift 	1	4
	Cray C90 (1991) Cray T90 (1995)	240 460	8	128	 FP add, FP multiply, FP reciprocal, integer add, 2 logical, shift, population count/parity 	2 loads 1 store	2
Vector processor family Used in Earth Simulator	NEC SX/5 (1998)	312	8 + 64	512	4: FP or integer add/shift, multiply, divide, logical	1	16
	Fujitsu VPP5000 (1999)	300	8–256	128–4096	FP or integer multiply, add/logical, divide	1 load 1 store	16
	Cray SV1 (1998) SV1ex (2001)	300 500	8	64	8: FP add, FP multiply, FP reciprocal, integer add, 2 logical, shift, population count/parity	1 load-store 1 load	2 8 (MSP)
	VMIPS (2001)	500	8	64	5: FP multiply, FP divide, FP add, integer add/shift, logical	1 load-store	1
						1700	71 1

VEC-1

VMIPS = **Vector MIPS**

8 Vector Registers V0-V7 MVL = 64(Similar to Cray)

The VMIPS Vector FP Instructions

L = 64	Instruct	tion Operands	Function			
ilar to Cray)	ADDV.D ADDVS.I	V1,V2,V3 V1,V2,F0	Add elements of V2 and V3, then put each result in V1. Add F0 to each element of V2, then put each result in V1.			
Vector ?	FP SUBV.D SUBVS.I		Subtract elements of V3 from V2, then put each result in V1. Subtract F0 from elements of V2, then put each result in V1. Subtract elements of V2 from F0, then put each result in V1.			
	MULV.D MULVS.I	V1,V2,V3 V1,V2,F0	Multiply elements of V2 and V3, then put each result in V1. Multiply each element of V2 by F0, then put each result in V1.	Vector I	Memory Access	
DIVVS.D V1,			Divide elements of V2 by V3, then put each result in V1. Divide elements of V2 by F0, then put each result in V1. Divide F0 by elements of V2, then put each result in V1.		Addressing Modes	
	LV	V1,R1	Load vector register V1 from memory starting at address R1.	1- Unit Stride		
Vector	SV	R1,V1	Store vector register V1 into memory starting at address R1.	Access		
Memor	LVWS	V1,(R1,R2)	Load V1 from address at R1 with stride in R2, i.e., R1+1 \times R2.	2- Constant S	Stride	
111011101	SVWS	(R1,R2),V1	Store V1 from address at R1 with stride in R2, i.e., R1+1 \times R2.	Access	/_ I	
	LVI	V1,(R1+V2)	Load V1 with vector whose elements are at R1+V2(1), i.e., V2	is an index.	3- Variable Stride	
	SVI	(R1+V2),V1	Store V1 to vector whose elements are at R1+V2(1), i.e., V2 is a	an index.	Access (indexed)	
Vector Ind	ex cvi	V1,R1	Create an index vector by storing the values 0 , $1 \times R1$, $2 \times R1$,,63×R	₹1 into ¥1.	
Vector Mas	SV.D SVS.I	V1,V2 V1,F0	Compare the elements (EQ, NE, GT, LT, GE, LE) in V1 and V2. If a 1 in the corresponding bit vector; otherwise put 0. Put resulti mask register (VM). The instruction SVS.D performs the same scalar value as one operand.	ing bit vector	r in vector-	
	POP	R1,VM	Count the 1s in the vector-mask register and store count in R1.			
	CVM		Set the vector-mask register to all 1s.			
Vector Lex (VLR)	ngth MTC1 MFC1	VLR,R1 R1,VLR	Move contents of R1 to the vector-length register. Move the contents of the vector-length register to R1.			
(121)	MVTM MVFM	VM,F0 FO,VM	Move contents of F0 to the vector-mask register. Move contents of vector-mask register to F0.			
					—— I	

VEC-1

Vector Control Registers: VM = Vector Mask

VLR = **Vector Length Register**

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Basic Vector Memory Access Addressing Modes

- Load/store operations move groups of data between registers and memory
- Three types of addressing:
- 1 <u>Unit stride</u> Fastest memory access Sequential element access, i.e Stride = 1

LV (Load Vector), SV (Store Vector):

LV V1, R1 Load vector register V1 from memory starting at address R1 SV R1, V1 Store vector register V1 into memory starting at address R1.

2 – <u>Non-unit</u> (constant) <u>stride</u>

LVWS (Load Vector With Stride), SVWS (Store Vector With Stride):

LVWS V1,(R1,R2) Load V1 from address at R1 with stride in R2, i.e., R1+i \times R2. SVWS (R1,R2),V1 Store V1 from address at R1 with stride in R2, i.e., R1+i \times R2.

- 3 <u>Indexed</u> (gather-scatter) Or Variable stride (i size of element)
 - Vector equivalent of register indirect
 - Good for sparse arrays of data
 - Increases number of programs that vectorize

LVI (Load Vector Indexed or Gather), SVI (Store Vector Indexed or Scatter):

LVI V1,(R1+V2) Load V1 with vector whose elements are at R1+V2(i), i.e., V2 is an index. SVI (R1+V2),V1 Store V1 to vector whose elements are at R1+V2(i), i.e., V2 is an index.

Stride = Distance in elements between **consecutive** vector elements loaded or stored by a vector memory access instruction

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VEC-1

Scalar Vs. Vector **Code Example**

DAXPY $(Y = \underline{a} * \underline{X + Y})$

	y vectors X, Y gth 64 =MVL	L.D LV	F0,a V1,Rx	;load scalar a ;load vector X
Scalar vs.	Vector ——	MULVS.D	V2,V1,F0	;vector-scalar mult.
		LV	V3,Ry	;load vector Y
	VLR = 64	ADDV.D	V4,V2,V3	;add
\	VM = (1,1,1,11)	SV	Ry,V4	;store the result
L.D	F0,a			f the scalar loop code was unrolled MVL = 64 times: ry vector instruction replaces 64 scalar instructions.
DADDIU	R4,Rx,#512	;last addres	•	Scalar Vs. Vector Code
loop: L.D	$\mathbf{F2}, 0(\mathbf{Rx})$;load X(i)		578 (2+9*64) vs.
MUL.D	$\overrightarrow{F2}$, $\overrightarrow{F2}$;a*X(i)		321 (1+5*64) ops (1.8X)
L.D	F4 , 0(Ry)	;load Y(i)		578 (2+9*64) vs.
ADD.D	F4,F2, <u>F4</u>	a*X(i) + Y	(i)	6 instructions (96X)
S.D	$\sqrt{F4}$,0(Ry)	;store into	` '	64 operation vectors +
DADDIU	Rx,Rx,#8	;increment		no loop overhead
DADDIU	Ry,Ry,#8	;increment	index to Y	also 64X fewer pipeline
DSUBU	R20,R4,Rx	;compute b	ound	hazards
BNEZ	R20,loop	;check if do	one	
VEC-1	Unroll scalar loop code? What does loop unrolling a	ccomplish?	E	#28 lec # 7 Fall 2012 10-1-2012

In seconds or cycles

Vector Execution Time/Performance

- Time = f(vector length, data dependencies, struct. hazards, C)
- **<u>Initiation rate:</u>** rate that FU consumes vector elements. (= number of lanes; usually 1 or 2 on Cray T-90)
- **Convoy:** a set of vector instructions that can begin execution in approximately the same clock cycle (no structural or data hazards).
- **Chime:** approx. time in cycles to produce a vector element result (usually = number of convoys in vector code). Assuming one lane is used/ignore startup
- <u>m convoys take $T_{chime} = m$ cycles (or 1 chime)</u>; if each vector length is n, then they take approx. $m \times n$ clock cycles (ignores overhead; one lane; good approximation for long vectors) i.e vector functional unit

Convoy

```
Assuming vector length, n \leq MVL
1: LV
            V1,Rx
```

;load vector X

2: MULV <u>V2</u>,F0,<u>V1</u> ;vector-scalar mult.

LV V3,Ry ;load vector Y

3: ADDV <u>V4, V2</u>, V3 ;add

4: SV Ry, **V4** store the result 4 conveys, 1 lane, VL= n = 64 $=> 4 \times 64 = 256$ cycles (or m= 4 cycles per result vector element)

Ignoring vector startup time, n <= MVL

DAXPY

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VEC-1

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startup time etc.

DAXPY $(Y = \underline{a} * \underline{X} + \underline{Y})$ Timing

(One LSU, One Lane, No Vector Chaining, Ignoring Startup) n ≤ MVL

From Last Slide: Time in Cycles = Number of Convoys x Vector Length = $\mathbf{T}_{\text{chime}}$ x n = m x n

Convoy :load vector X V1,Rx m= 4 conveys, 1 lane, 2: MULV <u>V2</u>,F0,<u>V1</u> VL = n = 64:vector-scalar mult. => 4 x 64 = 256 cycles V3,Ry ;load vector Y LV (or T_{chime}= 4 cycles per 3: ADDV <u>V4, V2, V3</u> ;add result vector element) 4: SV Ry,<u>V4</u> store the result m = 4 Convoys or $T_{chime} = 4$ cycles per element mxn n elements take = $m \times n = 4 n$ cycles For n = VL = MVL = 64 it takes 4x64 = 256 cycles n LV <u>V1</u>,Rx $T_{chime} = m = 4$ 2n MULV <u>V2</u>,F0,<u>V1</u> 4 convoys x n V3.Rv n $= 4 \times 64 = 256$ cycles 3n 3 ADDV <u>V4, V2, V3</u> 4n n = vector length = VL = number of elements in vector $m or T_{chime} = Number of convoys$ EECC722 - Shaaban What if multiple lanes are used? VEC-1 #30 lec # 7 Fall 2012 10-1-2012

Accounting For Vector FU Start-up Time

i.e Pipelined Vector Functional Unit Fill Cycles

- <u>Start-up time</u>: pipeline latency time (depth of FU pipeline); another sources of overhead
- Operation Start-up penalty (from CRAY-1)
 - Vector load/store 12
 - Vector multiply7
 - Vector add6

Time to get first result element

(To account for pipeline fill cycles)

Assume convoys don't overlap (no vector chaining); vector length = n:

Accounting For Startup Time (for one lane):

 $n \leq MVL$

 $Time\ in\ Cycles = Total\ Startup + Number\ of\ Convoys\ x\ Vector\ Length = = Total\ Startup + m\ x\ n$

Convoy	Start	1st result	last result
1. LV	0	12	11+n (12+n-1)
2. MULV, LV	12+n	12+n+12	23+2n Load start-up
3. ADDV	24+2n	24+2n+6	29+3n Wait convoy 2
4. SV	30+3n	30+3n+12	41+4n Wait convoy 3
	DAXPY	Total Startup cycl	es 4 Convoys
VEC 1		E	ECC722 - Shaaban

VEC-1

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DAXPY $(Y = \underline{a} * \underline{X + Y})$ Timing

(One LSU, One Lane, One LSU, No Vector Chaining, Including Startup)

Time in Cycles = Total Startup + Number of Convoys x Vector Length = = Total Startup + m x n Time to get first Convoy result element ;load vector X **Operation Start-up penalty** 2: MULV <u>V2</u>,F0,<u>V1</u> ;vector-scalar mult. (from CRAY-1) -Vector load/store 12 LV ;load vector Y -Vector multiply -Vector add 3: ADDV <u>V4, V2</u>, V3 ;add 4: SV ;store the result Ry, *V4* m = 4 Convoys or $T_{chime} = 4$ cycles per element 297 cycles Vs. 256 cycles n elements take = Startup + $m \times n = 41 + 4 n$ cycles when ignoring startup time (slide 30) For n = VL = MVL = 64 it takes 41 + 4x64 = 297 cycles 11+n 1 | LV <u>V1</u>,Rx Here Total Startup Time = 41 cycles n-1 MULV <u>V2,F0,V1</u> 23 + 2nn-1 V3.Rv 29 + 3nn-1 3 ADDV <u>V4, V2, V3</u> 41 + 4n4 SV Ry,<u>V4</u> n = vector length = VL = number of elements in vector $m or T_{chime} = Number of convoys$ EECC722 - Shaaban What if multiple lanes are used? VEC-1 #32 lec # 7 Fall 2012 10-1-2012

Vector Load/Store Units (LSUs) & Memories

- Start-up overheads usually longer for LSUs
- CPU
- Memory system must sustain (# lanes x word) /clock cycle
- Many Vector Procs. use banks (vs. simple interleaving):
 - 1) support multiple loads/stores per cycle
 - => multiple banks & address banks independently
 - 2) support non-sequential accesses (non unit stride)
- Note: No. memory banks > memory latency to avoid stalls
 - -m banks => m words per memory lantecy l clocks
 - -if m < l, then gap in memory pipeline:

i.e to hide memory latency

clock: 0 ... l l+1 l+2 ... l+m-1 1+m ... 2 l

word: -- ... 0 1 2 ... m-1 -- ... m

may have 1024 banks in SRAM

i.e a large number of memory banks maybe needed

Vector Memory Requirements Example

- The Cray T90 has a CPU clock cycle of 2.167 ns (460 MHz) and in its largest configuration (Cray T932) has 32 processors each capable of generating four loads and two stores per CPU clock cycle. i.e Each processor has 6 LSUs
- The CPU clock cycle is 2.167 ns, while the cycle time of the SRAMs used in the memory system is 15 ns.
- Calculate the minimum number of memory banks required to allow all CPUs to run at full memory bandwidth.
- Answer:
- The maximum number of memory references each cycle is 192 (32 CPUs times 6 references per CPU).
- Each SRAM bank is busy for 15/2.167 = 6.92 clock cycles, which we round up to 7 CPU clock cycles. Therefore we require a minimum of $192 \times 7 = 1344$ memory banks!
- The Cray T932 actually has 1024 memory banks, and so the early models could not sustain full bandwidth to all CPUs simultaneously. A subsequent memory upgrade replaced the 15 ns asynchronous SRAMs with pipelined synchronous SRAMs that more than halved the memory cycle time, thereby providing sufficient bandwidth/latency.

Note: No Data cache is used

Vector Memory Access Pattern Example

MVL

- Suppose we want to fetch a vector of 64 elements (each element 8 bytes) starting at byte address 136, and a memory access takes 6 CPU clock cycles.
 - How many memory banks must we have to support one fetch per clock cycle?
 - With what addresses are the banks accessed?
 - When will the various elements arrive at the CPU?

Assuming stride distance = 1 element = 8 bytes (sequential element access)

Answer

• Six clocks per access require at least six banks, but because we want the number of banks to be a power of two, we choose to have eight banks as shown on next slide Not a require

More than minimum number of memory banks needed to hide individual memory bank latency

Not a requirement just assumed In this example

Vector Memory Access Pattern Example

Unit Access Stride Shown (Access Stride = 1 element = 8 bytes)

U 20 12	_
	М.

LSU or memory bank startup latency (6 cycles)

Cycle no.	0	1	2	3	4	5	6	7
0	Γ	136						
		busy	144					
2		busy	busy	152				
3		busy	busy	busy	160			
4		busy	busy	busy	busy	168		
5		- busy	busy	busy	busy	busy	176	
6			busy	busy	busy	busy	busy	184
7	192			busy	busy	busy	busy	busy
8	busy	200			busy	busy	busy	busy
9	busy	busy	208			busy	busy	busy
10	busy	busy	busy	216			busy	busy
11	busy	busy	busy	busy	224			busy
12	busy	busy	busy	busy	busy	232		
13		busy	busy	busy	busy	busy	240	
14			busy	busy	busy	busy	busy	248
15	256			busy	busy	busy	busy	busy
16	busy	264			busy	busy	busy	busy

8 Banks

What if access stride = 8 elements (which equals number of banks)?

Vector Length (VL or n) Needed Not Equal to MVL

- What to do when vector length is not exactly 64?
- vector-length register (VLR) controls the length of any vector operation, including a vector load or store. (cannot be > MVL = the length of vector registers)

do 10
$$i = 1, n$$

10
$$Y(i) = a * X(i) + Y(i)$$

Vector length = n

Don't know n until runtime!

n > MVL What if n > Max. Vector Length (MVL)?

Vector Loop (Strip Mining)

What if n > MVL?

Vector Loop: Strip Mining

- **Suppose Vector Length > Max. Vector Length (MVL)?**
- **Strip mining:** generation of code such that each vector operation is done for a size Š to the MVL Vector
 - 1st loop do short piece (n mod MVL), reset VL = MVL

```
(For other iterations)
            low = 1
VL=Vector
   Length
            VL = (n \mod MVL) /*find the odd size piece*/
                                                                          First iteration: < MVL elements
  Control
            do 1 j = 0,(n / MVL) /*outer loop*/
  Register
                do 10 i = low,low+VL-1 /*runs for length VL*/
                           Y(i) = a*X(i) + Y(i) /*main operation*/
          10
                continue
                low = low+VL /*start of next vector*/
                VL = MVL /*reset the length to max*/
                                                                    Other iterations: MVL elements
                continue
                                                                          Number of Convoys = m
                                                 Startup Time
Time for Vector Loop: T_n = \left\lceil \frac{n}{\text{MVL}} \right\rceil \times (T_{\text{loop}} + T_{\text{start}}) + n \times T_{\text{chime}}
                                                                   Number of elements (i.e vector length)
      Vector loop iterations needed
                                               Loop Overhead
```

VEC-1

Loop

VL = **Vector Length Control Register**

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Strip Mining Illustration

1st iteration
n MOD MVL elements
(odd size piece)

2nd iteration

MVL

MVL

2nd iteration MVL elements

3rd iteration MVL elements

For First Iteration (shorter vector)
Set VL = n MOD MVL

For MVL = 64 VL = 1 - 63

For second Iteration onwards Set VL = MVL

(e.g. VL = MVL = 64)

Number of Vector loop iterations:

n/MVL vector loop iterations needed

n= Number of elements (i.e vector length)

VEC-1

VL = **Vector Length Control Register**

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Strip Mining Example

MVL =64 n = 200

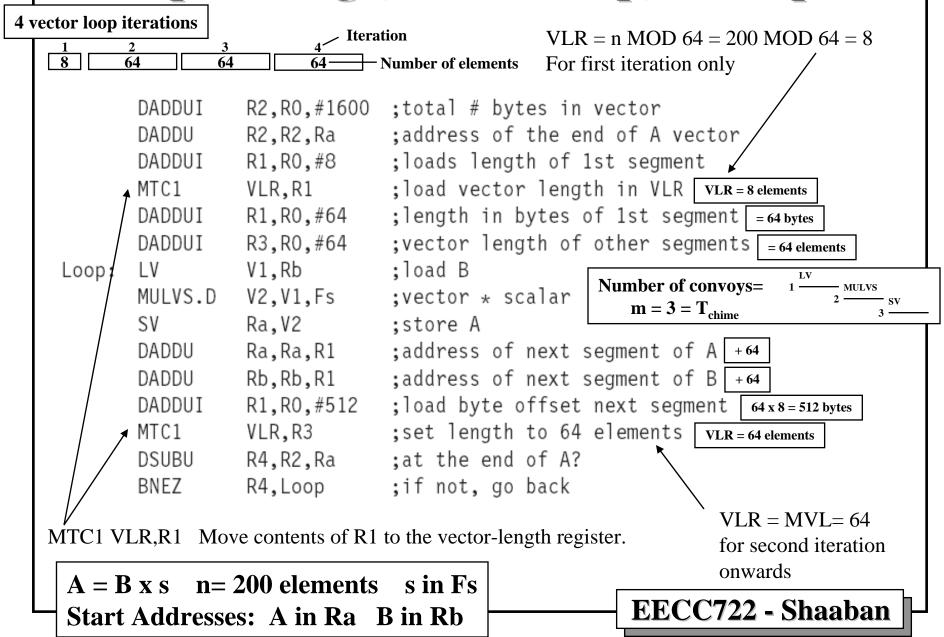
• What is the execution time on VMIPS for the vector operation $A = B \times s$, where s is a scalar and the length of the vectors A and B is 200 (MVL supported =64)? Each element is 8 bytes

Answer



- Assume the addresses of A and B are initially in Ra and Rb, s is in Fs, and recall that for MIPS (and VMIPS) R0 always holds 0.
- Since (200 mod 64) = 8, the first iteration of the strip-mined loop will execute for a vector length of VL = 8 elements, and the following iterations will execute for a vector length = MVL = 64 elements.
- The starting byte addresses of the next segment of each vector is eight times the vector length. Since the vector length is either 8 or 64, we increment the address registers by $8 \times 8 = 64$ after the first segment and $8 \times 64 = 512$ for later segments.
- The total number of bytes in the vector is $8 \times 200 = 1600$, and we test for completion by comparing the address of the next vector segment to the initial address plus 1600.
- Here is the actual code follows: (next) ----

Strip Mining (Vector Loop) Example



$A = B \times s$

Strip Mining Example

Cycles Needed

m=3

The three vector instructions in the loop are dependent and must go into three convoys, hence $T_{chime} = 3$. Let's use our basic formula:

n = 200MVL = 64

$$T_n = \left\lceil \frac{n}{\text{MVL}} \right\rceil \times (T_{\text{loop}} + T_{\text{start}}) + n \times T_{\text{chime}}$$

$$T_{200} = 4 \times (15 + T_{\text{start}}) + 200 \times 3$$

 $T_{200} = 60 + (4 \times T_{start}) + 600 = 660 + (4 \times T_{start})$

 $T_{loop} = loop overhead = 15 cycles$

(assumed/given)

The value of T_{start} is the sum of | Startup time calculation

- The vector load start-up of 12 clock cycles
- A 7-clock-cycle start-up for the multiply
- A 12-clock-cycle start-up for the store

Thus, the value of T_{start} is given by

$$T_{\text{start}} = 12 + 7 + 12 = 31$$

So, the overall value becomes

$$T_{200} = 660 + 4 \times 31 = 784$$

784 cycles / 200 elements = 3.9 cycles/element

3.9 vs. m = 3

The execution time per element with all start-up costs is then 784/200 = 3.9, compared with a chime approximation of three. m=3

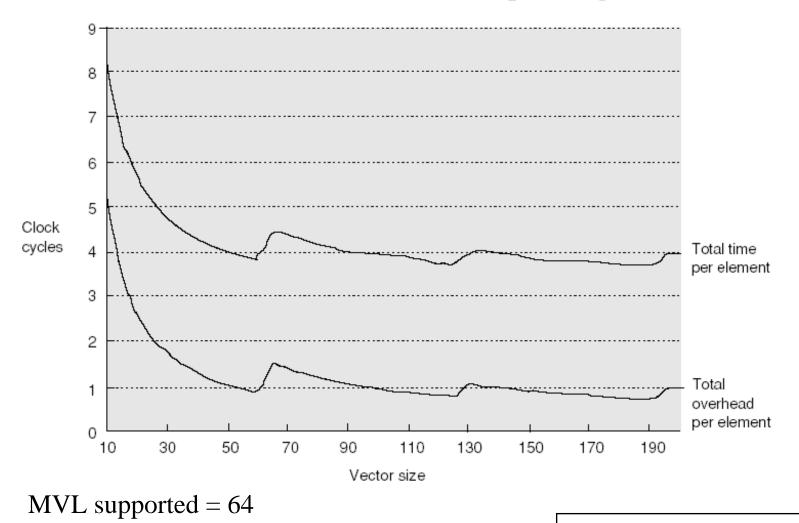
VEC-1

Ideally 3.9/3 = 1.3 times faster (ignoring loop/startup overheads) EECC722 - Shaaban

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Strip Mining Example

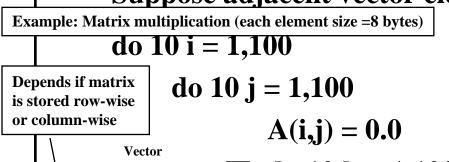
The total execution time per element and the total overhead time per element versus the vector length for the strip mining example



Vector Memory Access Addressing:

Constant Vector Stride

• Suppose adjacent vector elements not sequential in memory



do 10 k = 1,100 A(i,i) = A(i,i)+B(i,i)

 $A(\mathbf{i},\mathbf{j}) = A(\mathbf{i},\mathbf{j}) + B(\mathbf{i},\mathbf{k}) * C(\mathbf{k},\mathbf{j})$

Or 100 elements = stride

- Either B or C accesses not adjacent (800 bytes between)
- <u>stride</u>: distance separating elements that are to be merged into a single vector (caches do <u>unit stride</u>)

In number of elements or in bytes

=> LVWS (load vector with stride) instruction

LVWS V1,(R1,R2) Load V1 from address at R1 with stride in R2, i.e., R1+i \times R2.

=> **SVWS** (store vector with stride) instruction

i = element size

SVWS (R1,R2),V1 Store V1 from address at R1 with stride in R2, i.e., R1+i \times R2.

• Strides => can cause bank conflicts and stalls may occur.

Here stride is constant > 1 element (100 elements)

Vector Stride Memory Access Example

• Suppose we have 8 memory banks with a bank busy time of 6 clocks and a total memory latency of 12 cycles. How long will it take to complete a 64-element vector load with a stride of 1? With a stride of 32?

element

Answer

Note: Multiple of memory banks number $(32 = 4 \times 8)$

- Since the number of banks is larger than the bank busy time, for a stride of 1, the load will take 12 + 64 = 76 clock cycles, or 1.2 clocks per element. Startup latency
- The worst possible stride is a value that is a multiple of the number of memory banks, as in this case with a stride of 32 and 8 memory banks.

Memory Bank Conflicts (collisions)

- Every access to memory (after the first one) will collide with the previous access and will have to wait for the 6-clock-cycle bank busy time.
- The total time will be 12 + 1 + 6 * 63 = 391 clock cycles, or 6.1 clocks per element.

Stride = Multiple the number of banks --- Bank Conflicts

Vector Operations Chaining

(AKA <u>Vector Data Forwarding or Convoy Overlap</u>)

Suppose:

 $\mathbf{MULV.D} \quad \mathbf{\underline{V1}}, \mathbf{V2}, \mathbf{V3}$

ADDV.D V4,V1,V5 ; separate convoys?

Vector version of result data forwarding

- <u>chaining</u>: vector register (V1) is not treated as a single entity but as a group of individual registers, then pipeline forwarding can work on individual elements of a vector
- Flexible chaining: allow vector to chain to any other active And reduces number of vector operation => more read/write ports $convoys = T_{chime} = m$
- As long as enough HW is available, increases convoy size
- With chaining, the above sequence is treated as <u>a single</u> convoy and the total running time becomes:

Overlap convovs

Vector length + Start-up time_{ADDV} + Start-up time_{MULV}

Assuming $n \le MVL$ i.e no strip mining (vector loop) is needed and also assuming one lane is used

Vector Chaining Example

For one lane

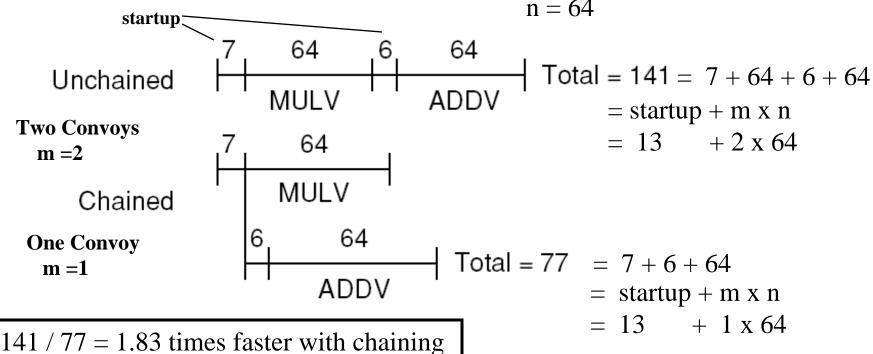
• Timings for a sequence of dependent vector operations

MULV.D <u>V1</u>,V2,V3 ADDV.D V4,*V1*,V5

m convoys with n elements take: startup + m x n cycles

both unchained and chained.

Here startup = 7 + 6 = 13 cycles n = 64



Assuming $n \le MVL$ i.e no strip mining (vector loop) is needed and also assuming one lane is used

DAXPY $(Y = \underline{a} * \underline{X + Y})$ Timing

With One LSU

(One Lane, One LSU, With Vector Chaining, Including Startup)

:load vector X LV V1,Rx **Operation Start-up penalty** (from CRAY-1) ;vector-scalar mult. MULV -Vector load/store LV :load vector Y -Vector multiply **ADDV** :add -Vector add SV ;store the result

DAXPY With Chaining and One LSU (Load/Store Unit)

Was 4 convoys without chaining

228 cycles vs. 297 (no chaining slide 32)

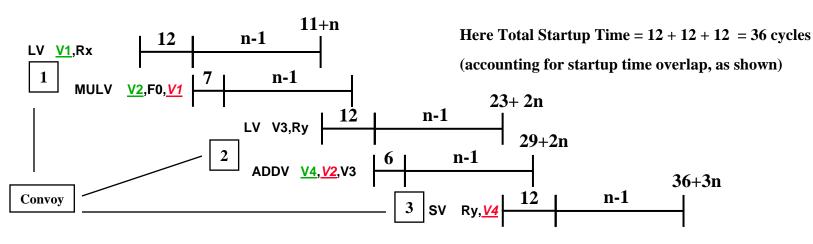
VEC-1

m = 3 Convoys or $T_{chime} = 3$ cycles per element n elements take = Startup + m x n = 36 + 3 n cycles For n = VL = MVL = 64 it takes 36 + 3x64 = 228 cycles

3 Convoys:

 $m = T_{chime} = 3$

12



n = vector length = VL = number of elements in vector

 $| Time = Startup + m \times n |$

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DAXPY $(Y = \underline{a} * \underline{X + Y})$ Timing

With Three LSUs

(One Lane, With Vector Chaining, Including Startup)

LV V1,Rx ;load vector X

MULV V2,F0,V1 ;vector-scalar mult.

LV V3,Ry ;load vector Y

ADDV V4,V2,V3 ;add

SV Ry,V4 ;store the result

Operation Start-up penalty
(from CRAY-1)

-Vector load/store 12

-Vector multiply 7

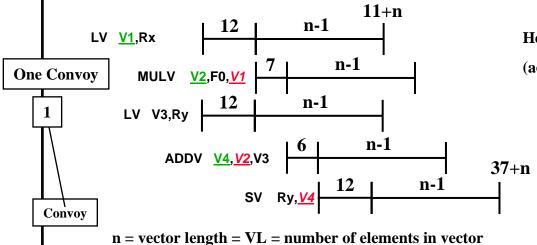
-Vector add 6

DAXPY With Chaining and Three LSUs (Load/Store Units)

Still one lane

m = 1 Convoy or $T_{chime} = 1$ cycle per element n elements take = Startup + m x n = 37 + n cycles For n = VL = MVL = 64 it takes 37 + 1 x64 = 101 cycles

One Convoy: $m = T_{chime} = 1$



VEC-1

Here Total Startup Time = 12 + 7 + 6 + 12 = 37 cycles (accounting for startup time overlap, as shown)

101 cycles vs. 228 cycles For one LSU (228/101 = 2.57 times faster)

Why not 3 times faster?

 $Time = Startup + m \times n$

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Vector Conditional Execution Using Vector Mask (VM)

Or Vector Element Masking

• Suppose:

do 100 i = 1, 64

if (A(i) .né. 0) then

A(i) = A(i) - B(i)

Vector Element test

VM(i) =
1 = compute element i
0 = mask element i
(i.e do not compute element i)

endif

100 continue

VM = Vector Mask Control Register → MVL Bits →

- vector-mask control takes a Boolean vector: when vector-mask (VM) register is loaded from vector test, vector instructions operate only on vector elements whose corresponding entries in the vector-mask register are 1.

 i.e vector mask, VM bits = 1
- Still requires a clock cycle or more per element even if result not stored or computed.

VEC-1

VM = Vector Mask Control Register

Vector Conditional Execution Example

V1,Ra LV ;load vector A into V1 **Unit Stride** ; load vector B into V2 V2,Rb ΙV **Vector Load** Set mask. F0,#0 ;load FP zero into FO L.D SNEVS.D ;sets VM(i) to 1 if V1(i)!=F0 V1,F0 Set Mask Clear V1,V1,V2 SUBV.D ;subtract under vector mask mask ;set the vector mask to all 1s Clear Mask CVM SV Ra,V1 ;store the result in A

S--V.D V1. V2 S--VS.D V1, F0

scalar

100

Compare the elements (EQ, NE, GT, LT, GE, LE) in V1 and V2. If condition is true, put a 1 in the corresponding bit vector; otherwise put 0. Here in F0

Put resulting bit vector in vector mask register (VM).

The instruction S--VS.D performs the same compare but using a scalar value as one operand.

Vector element test and set Vector Mask (VM) instructions

LV, SV Load/Store vector with stride 1 VM = Vector Mask Control Register

Vector Memory Operations/Addressing: Gather, Scatter

• Suppose:

Variable Stride Vector Memory Access (or Indexed LVI, SVI)

do 100 i = 1,n

$$A(K(i)) = A(K(i)) + C(M(i))$$

• gather (LVI, load vector indexed), operation takes an index vector and fetches the vector whose elements are at the addresses given by adding a base address to the offsets given in the index vector => a nonsparse vector in a vector register

LVI V1,(R1+V2) Load V1 with vector whose elements are at R1+V2(i), i.e., V2 is an index.

• After these elements are operated on in dense form, the sparse vector can be stored in expanded form by a *scatter* store (SVI, store vector indexed), using the same or different index vector

SVI (R1+V2),V1 Store V1 to vector whose elements are at R1+V2(i), i.e., V2 is an index.

- Can't be done by compiler since can't know K(i), M(i) elements
- Use CVI (create vector index) to create index 0, 1xm, 2xm,

..., 63xm

Very useful for sparse matrix operations (few non-zero elements to be computed)

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VEC-1

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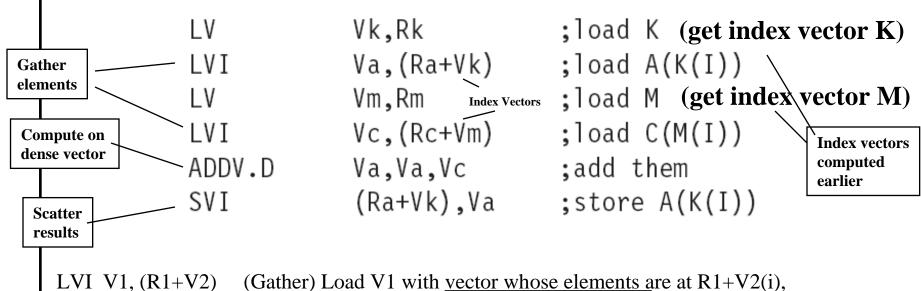
Gather, Scatter Example

do 100 i = 1,n
100
$$A(K(i)) = A(K(i)) + C(M(i))$$

For data vectors

For Index vectors

Assuming that Ra, Rc, Rk, and Rm contain the starting addresses of the vectors in the previous sequence, the inner loop of the sequence can be coded with vector instructions such as:



LVI = Load vector indexed i.e., V2 is an index.

SVI (R1+V2), V1 (Scatter) Store V1 to vector whose elements are at R1+V2(i),

i.e., V2 is an index.

SVI = **Store vector indexed**

Assuming Index vectors Vk Vm already initialized

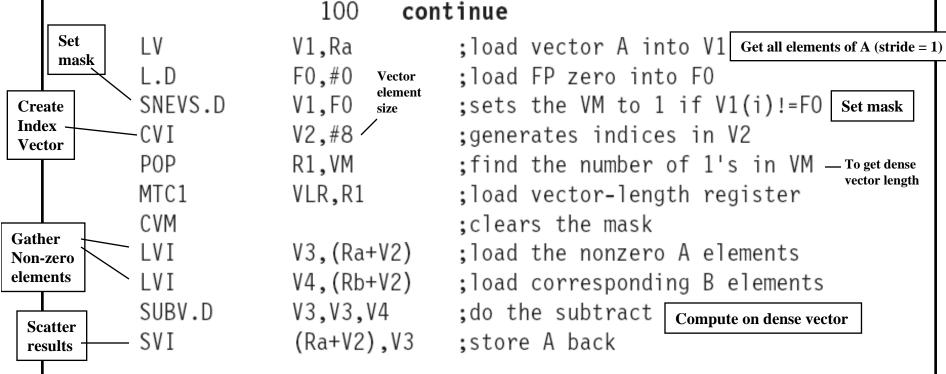
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Vector Conditional Execution Using Masking + Gather, Scatter

• The <u>indexed loads-stores</u> and the <u>create an index vector CVI</u> instruction provide <u>an alternative method to support conditional vector execution</u>.

do 100 j = 1, 64



CVI V1,R1 Create an index vector by storing the values 0, $1 \times R1$, $2 \times R1$,..., $63 \times R1$ into V1.

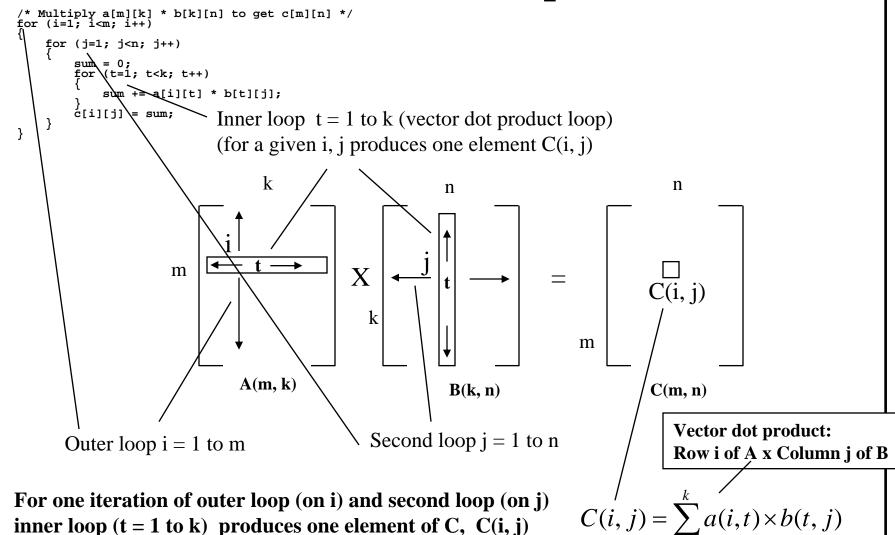
VEC-1

R1 has Vector element size

Vector Example with Dependency: Matrix Multiplication

```
/* Multiply a[m][k] * b[k][n] to get c[m][n] */
for (i=1; i<m; i++)
                                    C_{mxn} = A_{mxk} X B_{kxn}
    for (j=1; j<n; j++)
         sum = 0:
         for (t=1; t<k; t++) _____ Dot product
                                             (two vectors of size k)
              sum += a[i][t] * b[t][j];
         c[i][j] = sum;
```





inner loop (t = 1 to k) produces one element of C, C(i, j)

Inner loop (one element of C, C(i, j) produced)

Vectorize inner loop "t"?

Straightforward Solution

Produce Partial Product Terms (vectorized)

Accumulate

(Not vectorized)

Partial

Product Terms

Vectorize most inner loop t (dot product) ?

- MULV.D V1, V2, V3 | Produce partial product terms

- Must sum of all the elements of a vector to produce dot product besides grabbing one element at a time from a vector register and putting it in the scalar unit?
- e.g., shift all elements left 32 elements or collapse into a compact vector all elements not masked
- In T0, the vector extract instruction, vext.v. This shifts elements within a vector
- Called a "reduction"

$$C(i,j) = \sum_{t=1}^{k} a(i,t) \times b(t,j)$$

Assuming k = 32

Vectorized: Partial product terms using MULV.D V1, V2, V3

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A More Optimal Vector Matrix Multiplication Solution

- You don't need to do reductions for vector matrix multiplication.
- You can calculate multiple independent sums within one vector register

 / Instead on most inner loop t
- You can vectorize the j loop to perform 32 dot-products at the same time
- Or you can think of each 32 Virtual Processor doing one of the dot products each.

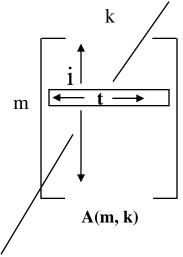
 Or MVL
- (Assume Maximum Vector Length MVL = 32 and n is a multiple of MVL)
- Shown in "vector" C source code, but can create the assembly vector instructions from it.

```
/* Multiply a[m][k] * b[k][n] to get c[m][n] */
    for (i=1; i<m; i++)
                                                             Each iteration of j
     for (j=1; j<n; j+=32)/* Step j 32 at a time. */
                                                             Loop produces
                                                             MVL result elements
             sum[0:31] = 0; /* Initialize a vector
                                                             (here MVL = 32)
                   register to zeros. */
             for (t=1; t<k; t++)
Vectorize j
Loop
              a scalar = a[i][t]; /* Get scalar from
(how many
                                     a matrix. */
Iterations?)
              b_vector[0:31] = b[t][j:j+31];
                                                  /* Get vector from
                                              b matrix. */
Vector Scalar
              prod[0:31] = b_vector[0:31]*a_scalar;
                /* Do a vector-scalar multiply. */
Multiply
MULVS
                 /* Vector-vector add into results. */
                 sum[0:31] += prod[0:31];
Vector Add ADDV
                                                    Work on MVL elements
                                                    (here MVL = 32)
             /* Unit-stride store of vector of
      results. */
                                                   32 = MVL elements done
             c[i][j:j+31] = sum[0:31];
                                                   (one j loop iteration)
             Optimized Vector Solution
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         Here we assume MVL = 32
                                                       #59 lec # 7 Fall 2012 10-1-2012
```

Optimal Vector Matrix Multiplication

Inner loop t = 1 to k (vector dot product loop for MVL = 32 elements) (for a given i, j produces a 32-element vector C(i, j: j+31)

Each iteration of j **Loop produces MVL** result elements (here MVL = 32)



to j+31. X k B(k, n)

n C(m, n)32 = MVLelement vector

n

to j

C(i, j: j+31)

Outer loop i = 1 to m Not vectorized

Second loop j = 1 to n/32(vectorized in steps of 32)

For one iteration of outer loop (on i) and vectorized second loop (on j) inner loop (t = 1 to k) produces 32 elements of C, C(i, j : j+31)

MULVS

Assume MVL =32 and n multiple of 32 (no odd size vector)

$$C(i, j: j+31) = \sum_{t=1}^{\infty} a(i,t) \times b(t, j: j+31)$$

ADDV

Inner loop (32 element vector of C produced)

Common Vector Performance Metrics

For a given benchmark or program running on a given vector machine:

- \mathbf{R}_{∞} : MFLOPS rate on an infinite-length vector for this benchmark
 - Vector "speed of light" or peak vector performance. For the given benchmark
 - Real problems do not have unlimited vector lengths, and the effective startup penalties encountered in real problems will be larger
 - $(R_n \text{ is the MFLOPS rate for a vector of length } n)$
- $N_{1/2}$: The vector length needed to reach one-half of R_{∞}

Half power point?

- a good measure of the impact of start-up + other overheads
- $oldsymbol{N_V}$: The vector length needed to make vector mode performance equal to scalar mode
 - Break-even vector length, i.e:

Break Even Vector Length N_V

- For vector length = Nv
 - Vector performance = Scalar performance
- For Vector length > Nv
 - $-\quad Vector\ performance > Scalar\ performance$
- Measures both start-up and speed of scalars relative to vectors, quality of connection of scalar unit to vector unit, etc.

The Peak Performance R of VMIPS for DAXPY

With vector chaining and one LSU

$$T_{\text{start}} = 12 + 7 + 12 + 6 + 12 = 49$$

See slide 48

Using MVL = 64, T_{loop} = 15, T_{start} = 49, and T_{chime} = 3 in the performance equation, and assuming that n is not an exact multiple of 64, the time for an nelement operation is Loop Overhead = 15

From vector loop (strip mining) cycles equation (slide 38)

Coop Overhead = 15 Startup Time = 49

Number of Convoys = m = 3

$$T_n = \left\lceil \frac{n}{64} \right\rceil \times (15 + 49) + 3n$$

$$\leq (n + 64) + 3n$$
Number of elements n (i.e vector length)
$$= 4n + 64$$

See slide 48

The <u>sustained</u> rate is actually over 4 clock cycles per iteration, rather than the theoretical rate of 3 chimes, which ignores overhead. The major part of the difference is the cost of the start-up overhead for each block of 64 elements (49 cycles versus 15 for the loop overhead).

We can now compute R_∞ for a 500 MHz clock as

64x2

$$R_{\infty} = \lim_{n \to \infty} \left(\frac{\text{Operations per iteration} \times \text{Clock rate}}{\text{Clock cycles per iteration}} \right)$$

The numerator is independent of n, hence

2 FP operations per result element

$$R_{\infty} = \frac{\text{Operations per iteration} \times \text{Clock rate}}{\lim_{n \to \infty} (\text{Clock cycles per iteration})}$$

$$\lim_{n \to \infty} (\text{Clock cycles per iteration}) = \lim_{n \to \infty} \left(\frac{T_n}{n} \right) = \lim_{n \to \infty} \left(\frac{4n + 64}{n} \right) = 4$$
Cycles per result element

2 FP operations every 4 cycles
$$R_{\infty} = \frac{2 \times 500 \text{ MHz}}{4} = 250 \text{ MFLOPS}$$

One LSU thus needs 3 convoys $T_{chime} = m = 3$

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Sustained Performance of VMIPS on the Linpack Benchmark

The Linpack benchmark is a Gaussian elimination on a 100×100 matrix. Thus, the vector element lengths range from 99 down to 1. A vector of length k is used k times. Thus, the average vector length is given by

Note: DAXPY is the core computation of Linpack with vector length 99 down to 1

$$\sum_{i=1}^{99} i^{2}$$
Average Vector Length
$$\sum_{i=1}^{99} i$$

$$\sum_{i=1}^{99} i$$

Now we can obtain an accurate estimate of the performance of DAXPY using a vector length of 66. $T_n = \left\lceil \frac{n}{64} \right\rceil \times (15 + 49) + 3n$ From last slide

$$T_{66} = 2 \times (15 + 49) + 66 \times 3 = 128 + 198 = 326$$
 cycles

$$R_{66} = \frac{2 \times 66 \times 500}{326} \text{ MFLOPS} = 202 \text{ MFLOPS}$$

$$R_{66}/=202 \text{ MFLOPS}$$
 vs. $R_{\infty}=250 \text{ MFLOPS}$

$$R_{66}/R_{\infty} = 202/250 = 0.808 = 80.8 \%$$

VMIPS DAXPY N_{1/2}

Example What is $N_{1/2}$ for just the inner loop of DAXPY for VMIPS with a 500 MHz

clock? 250 MFLOPS

 $N_{1/2}$ = vector length needed to reach half of R_{∞}

Answer Using R_{∞} as the peak rate, we want to know the vector length that will achieve about 125 MFLOPS. We start with the formula for MFLOPS assuming that the measurement is made for $N_{1/2}$ elements:

MFLOPS =
$$\frac{\text{FLOPS executed in N}_{1/2} \text{ iterations}}{\text{Clock cycles to execute N}_{1/2} \text{ iterations}} \times \frac{\text{Clock cycles}}{\text{Second}} \times 10^{-6}$$

$$125 = \frac{2 \times \text{N}_{1/2}}{\text{Ty}} \times 500$$

Simplifying this and then assuming $N_{1/2} \le 64$, so that $T_{n \le 64} = 1 \times 64 + 3 \times n$, yields

i.e. 125 MFLOPS = 8 cycles per result element (2 FP operations) $T_{N_{1/2}} = 8 \times N_{1/2}$ $1 \times 64 + 3 \times N_{1/2} = 8 \times N_{1/2}$

$$5 \times N_{1/2} = 64$$

$$N_{1/2} = 12.8$$

Thus: $N_{1/2} = 13$

So $N_{1/2} = 13$; that is, a vector of length 13 gives approximately one-half the peak performance for the DAXPY loop on VMIPS.

VMIPS DAXPY N_v—Break-even Vector Length

 N_v = Vector length needed to make vector mode performance equal to scalar performance or break-even vector length (For n > N_v vector mode is faster)

Example

What is the vector length, N_v , such that the vector operation runs faster than the scalar?

One element

Answer

Scalar Processor: 59 cycles per result (element)

Again, we know that $N_v < 64$. The time to do one iteration in scalar mode can be estimated as 10 + 12 + 12 + 7 + 6 + 12 = 59 clocks, where 10 is the estimate of the loop overhead, known to be somewhat less than the strip-mining loop overhead. In the last problem, we showed that this vector loop runs in vector mode in time $T_{n < 64} = 64 + 3 \times n$ clock cycles. Therefore,

$$64 + 3N_{v} = 59N_{v}$$

$$N_{v} = \left\lceil \frac{64}{56} \right\rceil$$

$$N_{v} = 2$$

For the DAXPY loop, vector mode is faster than scalar as long as the vector has at least two elements. This number is surprisingly small,

i.e for vector length = VL = n > 2 vector is faster than scalar mode

Is MVL = 4 potentially useful?

DAXPY Performance on an Enhanced VMIPS

Vector Chained DAXPY
With 3 LSUs

See slide 49

Here 3 LSUs

DAXPY, like many vector problems, is memory limited. Consequently, performance could be improved by adding more memory access pipelines. This is the major architectural difference between the Cray X-MP (and later processors) and the Cray-1. The Cray X-MP has three memory pipelines, compared with the Cray-1's single memory pipeline, and the X-MP has more flexible chaining. How does this affect performance?

See slide 49

For chained DAXPY with 3 LSUs number of convoys = $m = T_{chime} = 1$ (as opposed to 3 with one LSU)

Example What would be the value of T₆₆ for DAXPY on VMIPS if we added two more memory pipelines? 3 LSUs total

Answer With three memory pipelines all the instructions fit in one convoy and take one chime. The start-up overheads are the same, so

m = 1 convoy Not 3

$$T_{66} = \left\lceil \frac{66}{64} \right\rceil \times (T_{loop} + T_{start}) + 66 \times T_{chime}$$

$$T_{66} = 2 \times (15 + 49) + 66 \times 1 = 194$$
194 cycles vs 326 with one LSU

With three memory pipelines, we have reduced the clock cycle count for sustained performance from 326 to 194, a factor of 1.7. Note the effect of Amdahl's Law: We improved the theoretical peak rate as measured by the number of chimes by a factor of 3, but only achieved an overall improvement of a factor of 1.7 in sustained performance.

Speedup = 1.7 (going from m=3 to m=1) Not 3 (Why?)

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Vector or Multimedia ISA Extensions: Limited vector instructions added to scalar RISC/CISC ISAs with MVL = 2-8

Why? Improved exploitation of data parallelism in scalar ISAs/processors

- Example: Intel MMX: 57 new x86 instructions (1st since 386)
 - similar to Intel 860, Mot. 88110, HP PA-71000LC, UltraSPARC
 - 3 integer vector element types: 8 8-bit (MVL =8), 4 16-bit (MVL =4), 2 32bit (MVL =2) in packed in 64 bit registers
 - reuse 8 FP registers (FP and MMX cannot mix)

MVL = 8for byte elements

- short vector: load, add, store 8 8-bit operands

MMX

- Claim: overall speedup 1.5 to 2X for multimedia applications (2D/3D) graphics, audio, video, speech ...)
- Intel SSE (Streaming SIMD Extensions) adds support for FP with MVL =2 to MMX
- SSE2 Adds support of FP with MVL = 4 (4 single FP in 128 bit registers), 2 double FP MVL = 2, to SSE

Major Issue: Efficiently meeting the increased data memory bandwidth requirements of such instructions

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MMX Instructions

- Move 32b, 64b
- Add, Subtract in parallel: 8 8b, 4 16b, 2 32b
 - opt. signed/unsigned saturate (set to max) if overflow
- Shifts (sll,srl, sra), And, And Not, Or, Xor in parallel: 8 8b, 4 16b, 2 32b
- Multiply, Multiply-Add in parallel: 4 16b
- Compare = , > in parallel: 8 8b, 4 16b, 2 32b
 - sets field to 0s (false) or 1s (true); removes branches
- Pack/Unpack
 - Convert 32b<-> 16b, 16b <-> 8b
 - Pack saturates (set to max) if number is too large

Vector Processing Advantages

- Easy to get high-performance; N operations:
 - are independent Data parallel within a vector instruction
 - use same functional unit (similar operations)
 - access disjoint registers
 - access registers in same order as previous instructions
 - access contiguous memory words or known patterns (normally)
 - can exploit large memory bandwidth
 - hide memory latency (and any other latency)
- <u>Scalable</u> get higher performance as more HW resources available (e.g. more vector lanes/FUs)
- Compact: Describe N operations with 1 short instruction (v. VLIW)
- Predictable (real-time) performance vs. statistical performance (cache)
- Multimedia ready: choose N * 64b, 2N * 32b, 4N * 16b, 8N * 8b
- Mature, developed <u>vectorizing compiler technology</u>

Vector Processing Pitfalls

- Pitfall: Concentrating on peak performance and ignoring start-up/strip mining/other overheads: N_V (length faster than scalar) > 100!
- Pitfall: Increasing vector performance, without comparable increases in scalar (strip mining overhead ..) performance (Amdahl's Law).
- Pitfall: High-cost of traditional vector processor implementations (Supercomputers).
- Pitfall: Adding vector instruction support without providing the needed memory bandwidth/low latency
 - MMX? Other vector media extensions, SSE, SSE2, SSE3..?
- One More Vector Disadvantage: Out of fashion in high performance computing due to rise of lower-cost commodity supercomputing/clusters utilizing multiple off-the-shelf GPPs.

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Vector Processing & VLSI: Vector Intelligent RAM (VIRAM) Proc **Effort towards a full-vector Capitalize on increasing** a **VLSI** chip density processor on a chip: Bus b Bus How to meet vector processing high memory bandwidth and low latency requirements? R **Full Vector Microprocessor & DRAM** on a single chip: I/C On-chip memory latency One 5-10X lower, bandwidth 50-100X Chip Why? **Proc** higher Improve energy efficiency Bus 2X-4X (no off-chip bus) - Serial I/O 5-10X v. buses **Memory** Smaller board area/volume **Banks** R A M D Adjustable memory size/width Much lower cost/power than Vector Processor with memory on a single chip traditional vector supercomputers EECC722 - Shaaban VEC-2, VEC-3

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Potential VIRAM Latency Reduction: 5 - 10X

- No parallel DRAMs, memory controller, bus to turn around, SIMM module, pins...
- New focus: Latency oriented DRAM?
 - Dominant delay = RC of the word lines
 - keep wire length short & block sizes small?
- 10-30 ns for 64b-256b IRAM "RAS/CAS"?
- AlphaSta. 600: 180 ns=128b, 270 ns= 512b Next generation (21264): 180 ns for 512b?

Now about 70 ns

Potential VIRAM Bandwidth Increase: 100X

- 1024 1Mbit modules(1Gb), each 256b wide
 - 20% @ 20 ns RAS/CAS = 320 GBytes/sec
- If cross bar switch delivers 1/3 to 2/3 of BW of 20% of modules
 - \Rightarrow 100 200 GBytes/sec
- FYI: AlphaServer 8400 = 1.2 GBytes/sec (now ~ 6.4 GB/sec)
 - 75 MHz, 256-bit memory bus, 4 banks

Characterizing V-IRAM Cost/Performance

- Low Cost VMIPS vector processor + memory banks/interconnects integrated on one chip
- Small memory on-chip (25 100 MB)
- High vector performance (2 -16 GFLOPS)
- High multimedia performance (4 64 GOPS)
- Low latency main memory (15 30ns)

~ 5-10X Lower latency

• High BW main memory (50 - 200 GB/sec)

~ 100X Higher Bandwidth

Cray 1

Peak

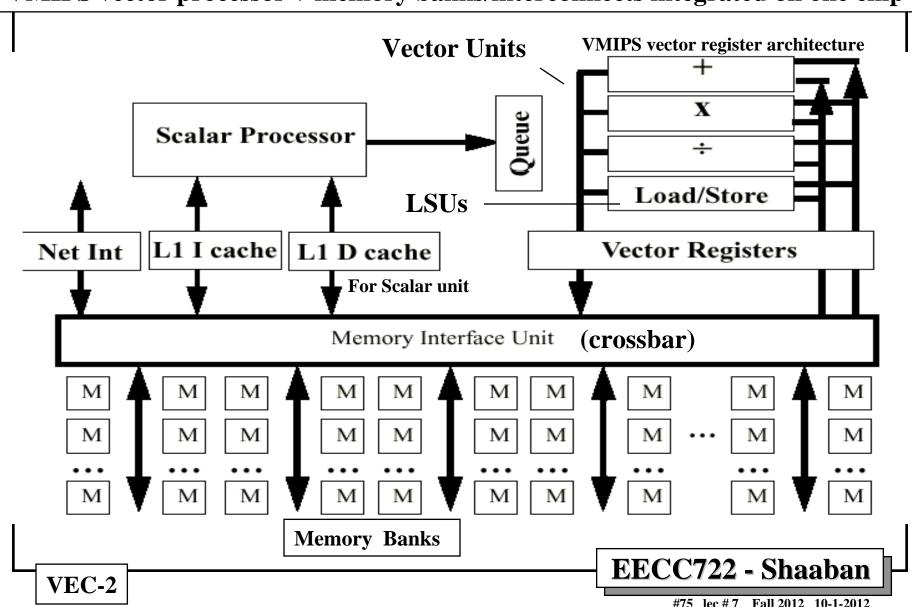
133 MFLOPS

- High BW I/O (0.5 2 GB/sec via N serial lines)
 - Integrated CPU/cache/memory with high memory BW ideal for fast serial I/O

Estimated power ~ 2 watts

Vector IRAM Organization

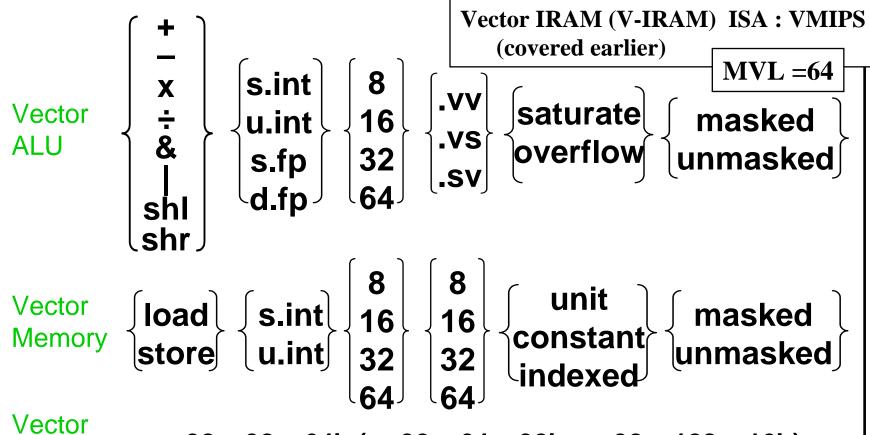
VMIPS vector processor + memory banks/interconnects integrated on one chip



V-IRAM1 Instruction Set (VMIPS)

Scalar

Standard scalar instruction set (e.g., ARM, MIPS)



Vector Registers

32 x 32 x 64b (or 32 x 64 x 32b or 32 x 128 x 16b) + 32 x128 x 1b flag

Plus: flag, convert, DSP, and transfer operations

Goal for Vector IRAM Generations

- V-IRAM-1 (-2000)
- 256 Mbit generation (0.20)
- Die size = 1.5X 256 Mb die
- 1.5 2.0 v logic, 2-10 watts
- 100 500 MHz
- 4 64-bit pipes/lanes
- 1-4 GFLOPS(64b)/6-16G (16b)
- 30 50 GB/sec Mem. BW
- 32 MB capacity + DRAM bus
- Several fast serial I/O
- 16 memory banks

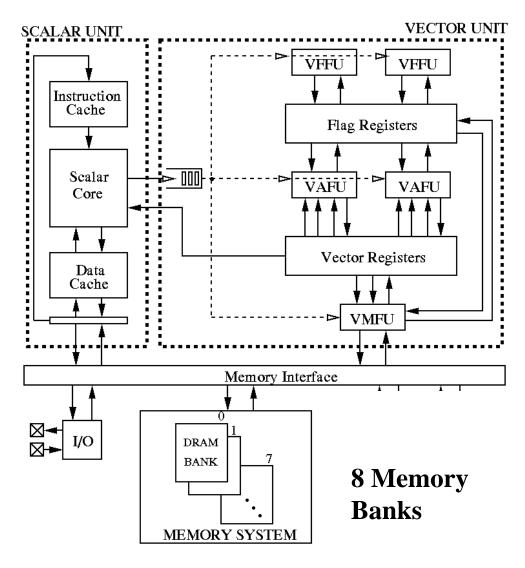
- V-IRAM-2 (-2005???)
- 1 Gbit generation (0.13)
- **Die size = 1.5X 1 Gb die**
- 1.0 1.5 v logic, 2-10 watts
- 200 1000 MHz
- 8 64-bit pipes/lanes
- 2-16 GFLOPS/24-64G
- 100 200 GB/sec Mem. BW
- 128 MB cap. + DRAM bus
- Many fast serial I/O
- 32 memory banks

VIRAM-1 Microarchitecture

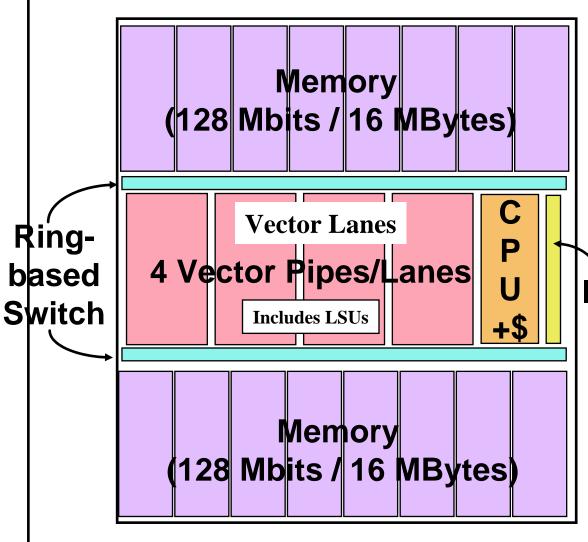
- 2 arithmetic units
 - both execute integer operations
 - one executes FP operations
 - 4 64-bit datapaths (lanes) per unit
- 2 flag processing units
 - for conditional execution and speculation support
- 1 load-store unit
 - optimized for strides 1,2,3,and 4
 - 4 addresses/cycle for indexed and strided operations
 - decoupled indexed and strided stores

- Memory system
 - 8 DRAM banks
 - 256-bit synchronous interface
 - 1 sub-bank per bank
 - 16 Mbytes total capacity
- Peak performance
 - 3.2 GOPS₆₄, 12.8 GOPS₁₆ (w. madd)
 - 1.6 GOPS₆₄, 6.4 GOPS₁₆ (wo. madd)
 - 0.8 GFLOPS₆₄, 1.6 GFLOPS₃₂
 - 6.4 Gbyte/s memory bandwidth comsumed byVU

VIRAM-1 block diagram



VIRAM-1 Floorplan



0.18 µm DRAM32 MB in 16 banksbanks x 256b, 128 subbanks

- 0.25 μm,5 Metal Logic
- 200 MHz MIPS, 16K I\$, 16K D\$
- 4 200 MHzFP/int. vector units

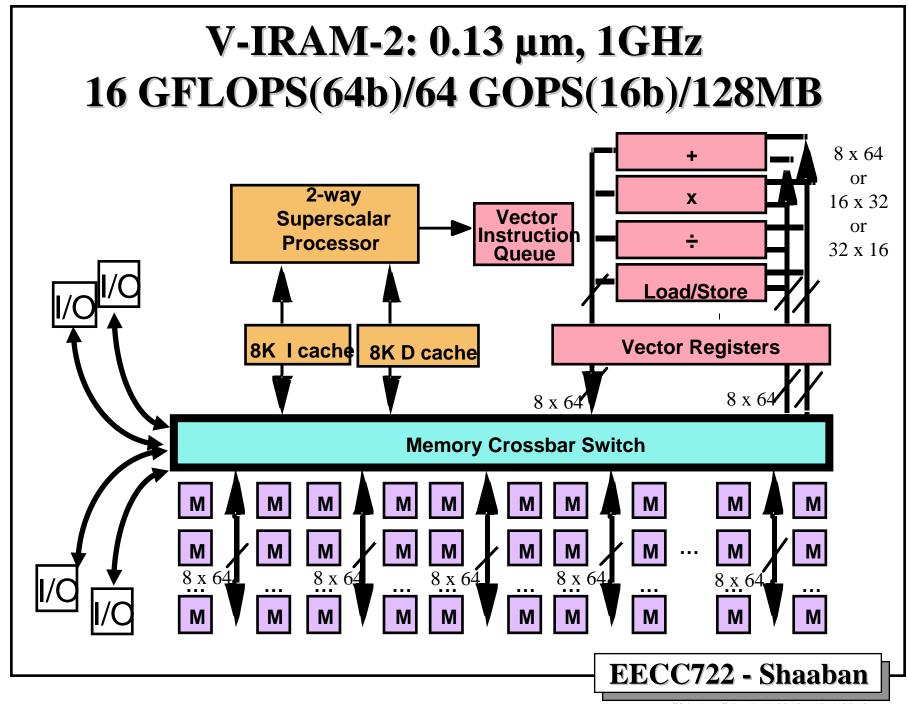
die: - 16x16 mm

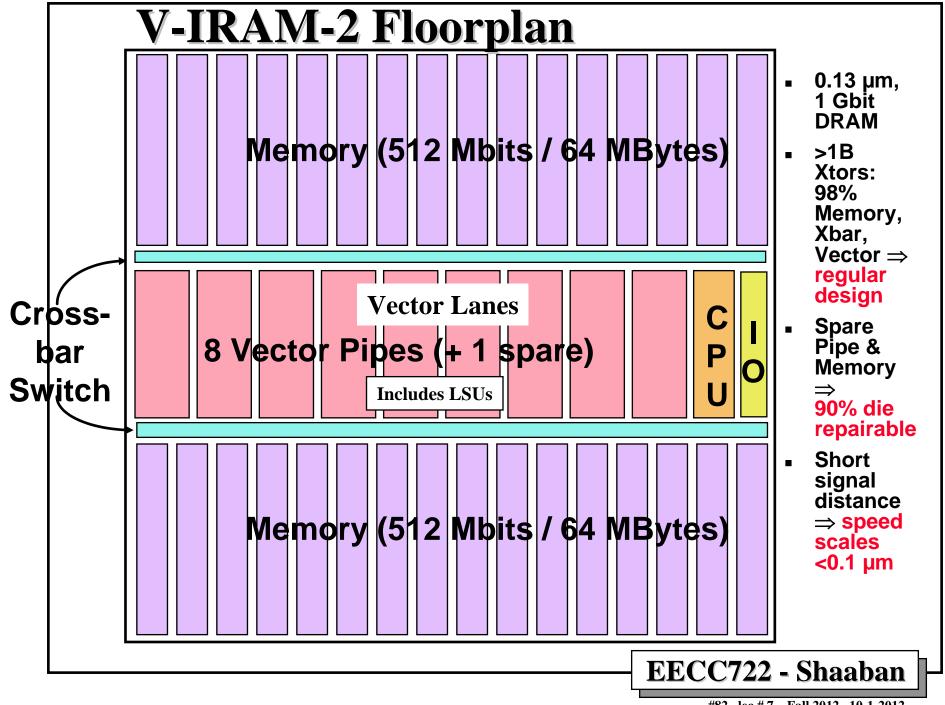
Transistors: - 270M

power: -2 Watts

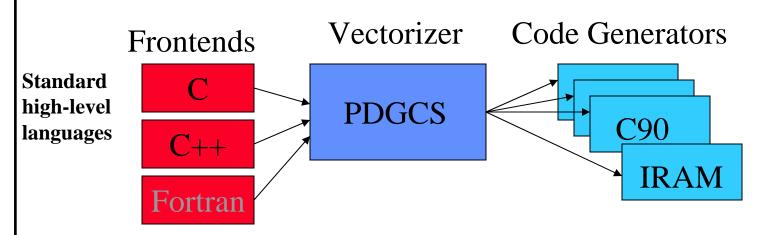
Performance:

1-4 GFLOPS





VIRAM Compiler



- Retargeted Cray compiler to VMIPS
- Steps in compiler development
 - Build MIPS backend (done)
 - Build VIRAM backend for vectorized loops (done)
 - Instruction scheduling for VIRAM-1 (done)
 - Insertion of memory barriers (using Cray strategy, improving)
 - Additional optimizations (ongoing)
 - Feedback results to Cray, new version from Cray (ongoing)