

Umeå University
Department of Computing Science

Parallel Programming 7.5 p
5DV152

Exercises, Chapter/Topic 3

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1 Introduction

This report is part of the mandatory coursework. It describes the solutions for several chosen exercises from the course book [?].

2 3.2 - Generalization of algorithm for trapezoidal rule

Two functions to adapt the *trapezoidal rule* for `calc_local_a` and `calc_local_b` were written and tested with the source code from the book (*mpi_trap.c*).

```
double calc_local_a(int my_rank, double a, double b, int n, int comm_sz){
    double local_a = 0;
    double h = 0;
    int local_n = 0;
    int rest_n = 0;

    h = (b-a)/n;
    local_n = n/comm_sz;

    rest_n = n%comm_sz;

    if(my_rank < rest_n){
        local_a = a + my_rank*local_n*h + my_rank*h;
    } else {
        local_a = a + my_rank*local_n*h + rest_n*h;
        local_a += (my_rank-rest_n) * h;
    }

    return local_a;
}

double calc_local_b(int my_rank, double a, double b, int n, int comm_sz){
    double h;
    int local_n;

    h = (b-a)/n;
    local_n = n/comm_sz;

    if (my_rank == (comm_sz-1)){
        return a + my_rank+1*local_n*h;
    } else {
        return calc_local_a(my_rank+1, a, b, n, comm_sz);
    }
}
```

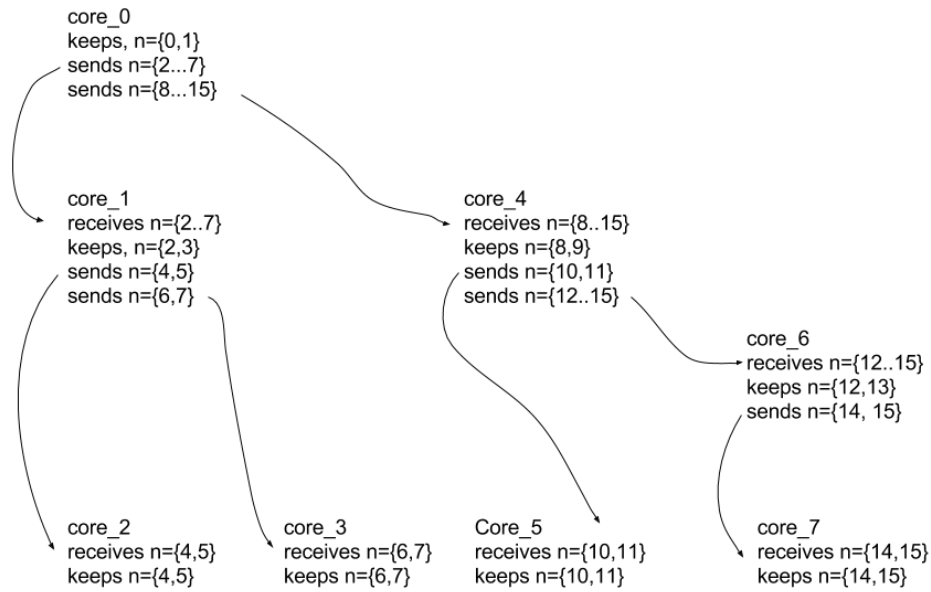


Figure 1: This graph shows a tree based implementation of scatter for $comm_sz = 8$ and $n = 16$.

3 3.6 - Array distributions

Block distribution

Block distribution can be obtained by $b = \lfloor i \div p \rfloor$ where b is the block number, i the index of n and p is the number of processes. This solution is however not fair. An improved, fair expression can be devised using a ternary operator:

$$i < n \bmod p \times \lceil n \div p \rceil ? \lfloor i \div \lceil n \div p \rceil \rfloor : n \bmod p + \lfloor (i - n \bmod p \times \lceil n \div p \rceil) \div \lfloor n \bmod p \rfloor \rfloor$$

Cyclic distribution

Cyclic distribution is described by $b = i \bmod p$ with b as block number i as index of n and p as number of processes.

Block cyclic distribution

Block cyclic distribution can be expressed as $b = \lfloor i \div l \rfloor \bmod p$ where b is block index, i index of n , l block length and p number of processes.

4 3.8 - Tree-structured algorithms for scatter and gather

5 3.9 - Vector scaling and dot product

takes a while to solve, requires programming

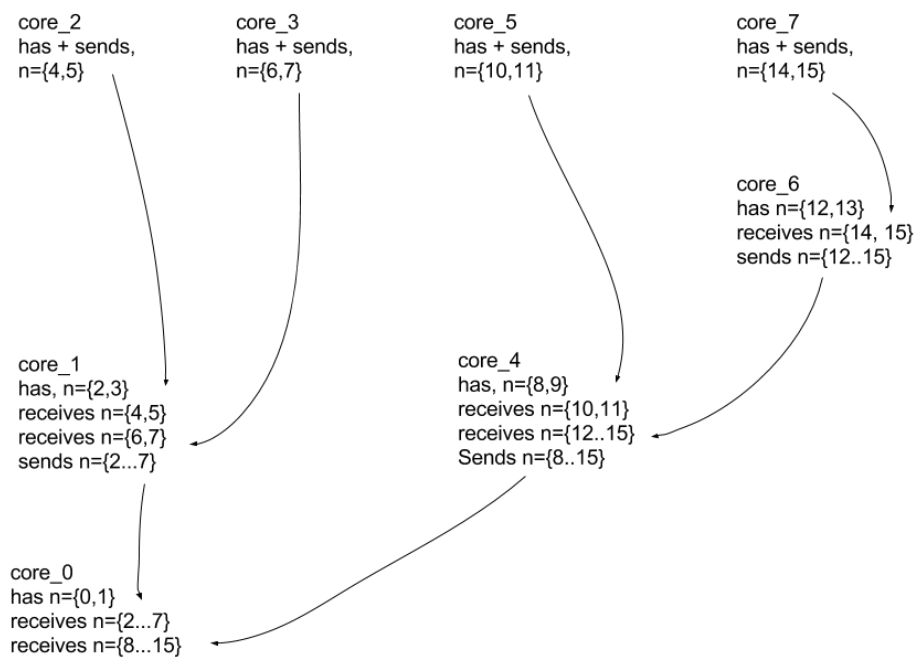


Figure 2: This graph shows a tree based implementation of gather for $comm_sz = 8$ and $n = 16$.

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6 3.11 - Prefix sums

takes a while to solve requires programming

7 3.13 - Generalization of vector scaling and dot product

8 3.16 - Diagram for a butterfly implementation of allgather

9 3.18 - Derived data types

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10 3.20 - Pack and unpack

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11 3.21 - Matrix-vector multiplication

takes a while to solve requires programming requires testing

12 3.22 - Timing the trapezoidal rule

takes a while to solve Requires programming requires testing

13 3.27 - Speedup and efficieniy of odd-even sort