Umeå University
Institution för Datavetenskap

DV2: Algorithms and Problemsolving 7.5 p
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OU5 Automaton

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Author: Lorenz Gerber (dv15lgr@cs.umu.se)
Instructor: Lena Kallin Westin / Erik Moström / Jonathan Westin

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1 Introduction

The subject of this assignment was to design and construct Push Down Automaton (PDA) as a general datatype and apply it to implement a specific PDA that can process input according to *reverse polish notation* (RPN).

1.1 Push Down Automata Implementation

The lab assignment proposed to use either a representation as table or as a graph. It was also communicated that the implementation shall be finite and non-deterministic.

The PDA was implemented as a struct with the fields **current state**, **current input**, **stack**, **table of states**

2 Program Structure

The program was implemented using a conventional C structure with a lean main function that first defines and initializes variables, then calls for a function that creates and configures the push down automaton and finally the applying the command line argument to the configured pda.

2.1 Own Datatypes

pda - Push Down Automaton

A generic implementation of a push down automaton according to Sipser [2, pp 112-125].

- current state
- current input
- register
- input alphabet dlist with function pointers
- stack
- stack alphabet, dlist with function pointers
- states table
- create
- add input alphabet character
- add stack alphabet character
- add state
- add transition
- run automaton

The datatype *pda* is constructed from a struct. It contains a table (from course datatypes [1], constructed from dynamic list) with *states*, a stack (from course datatypes [1], *stack_1cell*). The *states* table contains the transitions.

Alphabets

The alphabets could be implemented as single chars. Then it is however difficult to define a more generic group of chars such as number or operator. To provide this possibility an alphabet character could also be as a list or an array of unsigned chars. A more elegant way to solve this issue would be to define a character by a function, implemented through function pointers. This opens up for very flexible definition of alphabet characters. For the current implementation it was decided to define the alphabet by function pointers and functions.

States and Transitions

The representation of *state* and *transition* for a table based pda can be done in various ways and the distinction between *state* and *transition* is less clear than in a graph based model. Here two different ways were considered: Either states constructed only as a container for transitions, without any reference to the alphabet. This would require a more complex transition datatype. Also the datatype transition becomes less generic as it fits just for one specified pair of input and stack values.

Alternatively, *states* could also be implemented according to the example 2.14 in Sipser [2, p. 114]: The state is represented by triple nested table or an aggregated array where there is a multi column for each letter in the input alphabet with subgroups as the individual column for each letter of the stack alphabet. Implementing a representation for this model could be done with a nested table, an array, where the logic for accessing the different levels is integrated in the code or a tree structure. Such a representation has the advantage that it is directly visible whether a transition for a certain state is already defined or not as it has a unique location in the data structure. When choosing a representation with states as mere containers for transitions, a control mechanism to prevent assignment of duplicate transitions is needed.

A state has an numeric *id* and a table with *id's* of possible transitions to proceed along.

- id
- description
- table with allowed transitions

struct contains a table constructed from *dynamic list*. The table keys are integers with *structs* as data container.

Transition

A transition needs to know whether it matches the current state, it needs to define how to modify the current state and the id of the new state. *struct table* constructed from *dynamic list*.

pseudo example: create automata set input alphabet as list of unsigned chars set stack alphabet as list of unsigned chars set

3 Discussion

4 Conclusions

References

[1] DV169VT16, cambro course homepage, ‘datatypes’. https://www8.cs.umu.se/kurser/5DV169/datatypes/index.html, 2016. accessed: 2016-02-28.

[2] Michael Sipser. *Introduction to the Theory of Computation*. Cengage Learning, Boston, USA, 2012.