

GV300 - Quantitative Political Analysis

University of Essex - Department of Government

Lorenzo Crippa

Week 23 – 2 March, 2020



**WHAT
DO YOU
THINK?**

Department of Government

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Today's activity

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- Consider only the first 100 workers, get rid of the rest of the data

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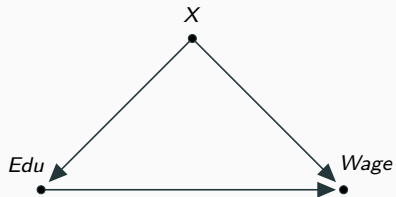
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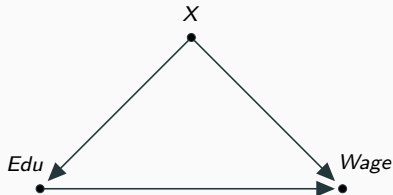
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 - (c) Compare the results and discuss which model best fits data based on point 2(b).

1. Causal identification

1(a) and (b) – Causal model

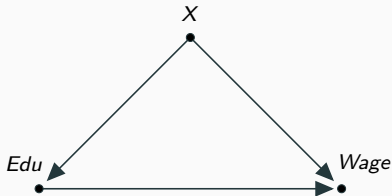


1(a) and (b) – Causal model



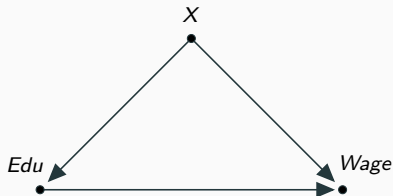
- Suppose X is a set of confounders that make each specific unit *idiosyncratic* both in treatment and outcome variables

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- Suppose X is a set of confounders that make each specific unit *idiosyncratic* both in treatment and outcome variables
- Then panel data help us identify the causal effect of Edu on $Wage$ because they allow us to include a fixed (random) effect and control for it.
- **BUT** fixed/random effects are no solution for all other types of confounders (non-idiosyncratic)!

2. Data description

2(a) – Summary statistics

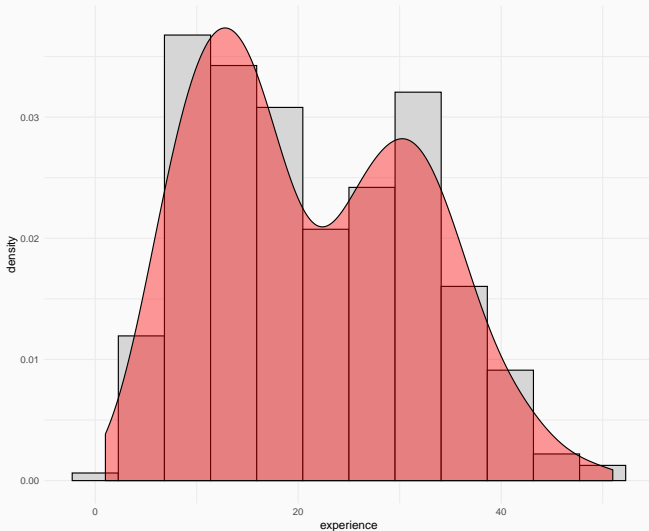
Variable	N	Mean	St. Dev.	Min	Pctl(25)	Pctl(75)	Max
id	700	50.500	28.887	1	25.8	75.2	100
t	700	4.000	2.001	1	2	6	7
occ	700	0.486	0.500	0	0	1	1
lwage	700	6.704	0.492	5.165	6.397	7.003	8.049
ed	700	13.040	2.995	4	12	16	17
exp	700	21.280	10.788	1	12	30	51
exp2	700	569.060	508.066	1	144	900	2,601
south	700	0.327	0.470	0	0	1	1
smsa	700	0.627	0.484	0	0	1	1
fem	700	0.130	0.337	0	0	0	1
union	700	0.321	0.467	0	0	1	1

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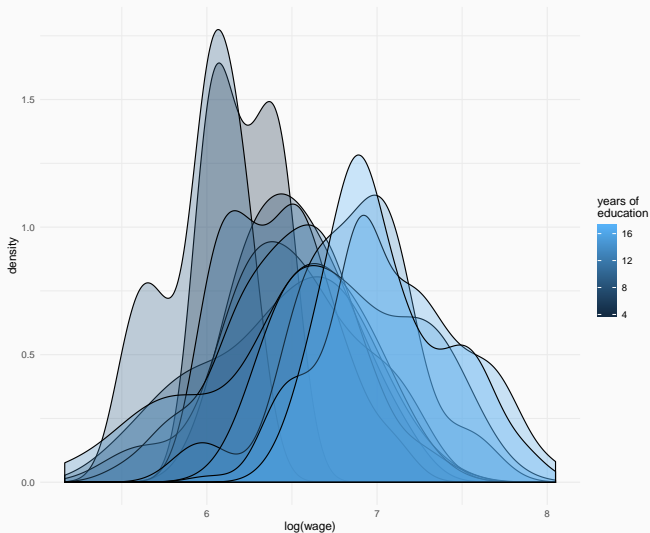


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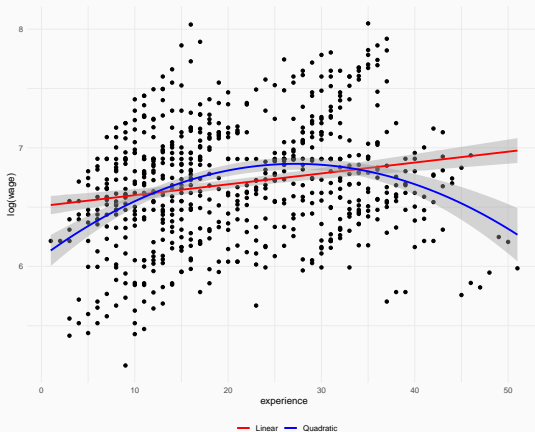
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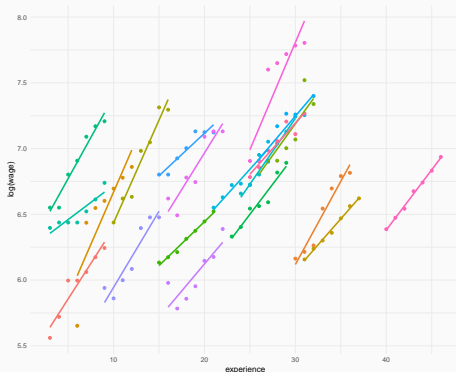
What does the following scatterplot tell you?



Our usual linear model doesn't really seem to fit this cloud. Why?

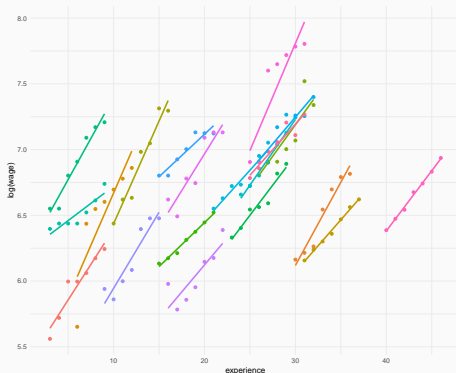
2(b) – Fixed effect

Take a look at this graph (only first 20 individuals). What does it suggest about the relationship we are studying?



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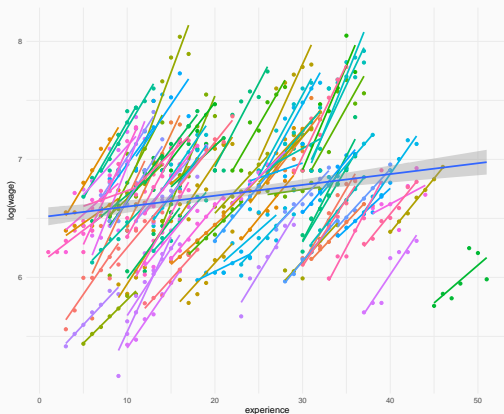
Take a look at this graph (only first 20 individuals). What does it suggest about the relationship we are studying?



The slopes of the regression lines by individual seem similar, only between-units intercepts are different!

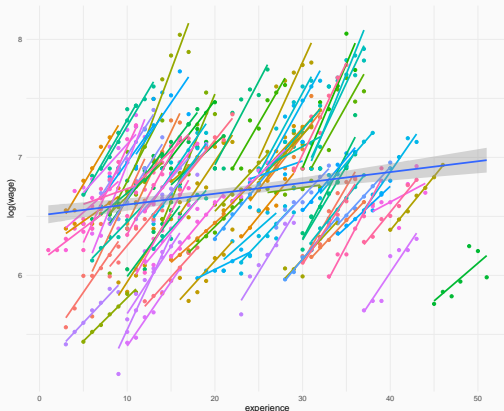
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Now look at the following (all 100 individuals, plus pooled):



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A typical example of a fixed effect: slopes and intercepts of lines by individuals are different from those of pooled line.

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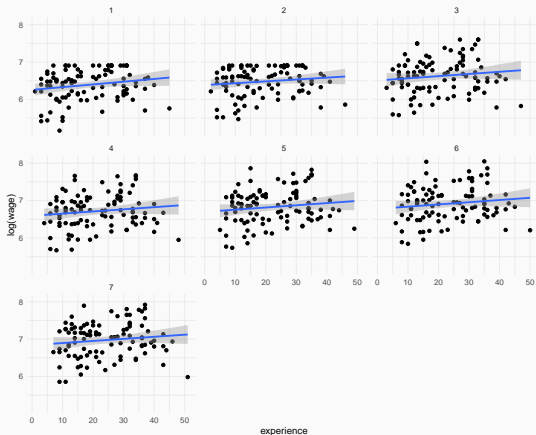
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- Intuitively: you include a fixed effect in a pooled model \rightarrow you have no clue of what's the difference between units, so you get rid of it. Random effect \rightarrow you can explain part of it.

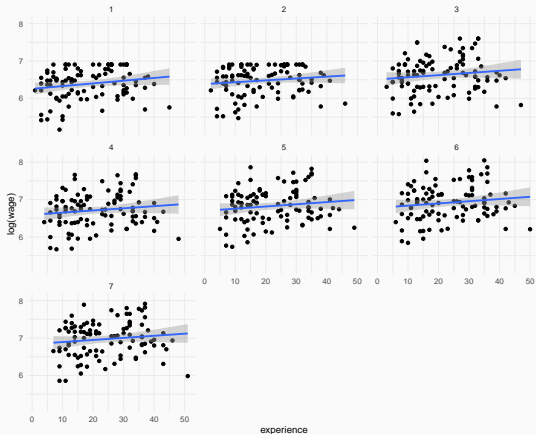
2(b) – What about time?

Are the time-points we have absolutely different from each others?



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In R we can even animate our graphs using `gganimate`!

2(b) – Time fixed effect?

Look at the following lines: is a time-fixed effect appropriate here?



2(b) – Within, between and overall variation

We can get statistics about within, between and overall variation of a selected number of variables (see R script):

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within.variation

t	lwage	ed	exp	exp2	wks
2.00	0.235	0	2.00	95.2	3.85

between.variation

t	lwage	ed	exp	exp2	wks
0	0.434	3.01	10.6	501.	3.24

overall.variation

t	lwage	ed	exp	exp2	wks
2.00	0.492	3.00	10.8	508.	5.02

3. Data analysis

Fixed effect: dummies

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$$Y_{it} = a_0 + \mathbf{X}'_{it}\mathbf{b} + a_1D_1 + a_2D_2 + \dots + a_{k-1}D_{k-1} + e_{it}$$

$$\mathbf{D} = D_1, D_2, \dots, D_k = \begin{bmatrix} 1 & 0 & \dots & 0 \\ 1 & 0 & \dots & 0 \\ 0 & 1 & \dots & 0 \\ 0 & 1 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & 1 \\ 0 & 0 & \dots & 1 \end{bmatrix}$$

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The matrix has size $N \times k$. Your software will exclude one dummy (thus $k - 1$) or the intercept a_0 to avoid multicollinearity

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We can now do the group demeaning:

$$(Y_{it} - \bar{Y}_i) = (\mathbf{X}'_{it} - \bar{\mathbf{X}}'_i)\mathbf{b} + (a_i - a_i) + (e_{it} - \bar{e}_i)$$

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Thus we get rid of between-unit variation ($a_i - a_i = 0$)

Random effect:

$$(Y_{it} - \hat{\theta}_i \bar{Y}_i) = (1 - \hat{\theta}_i) a_0 + (\mathbf{X}_{it} - \hat{\theta}_i \bar{\mathbf{X}}_i)' \mathbf{b} + [(1 - \hat{\theta}_i) a_i + (e_{it} - \hat{\theta}_i \bar{e}_i)]$$

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where $\hat{\theta}_i$ is an estimate of

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Notice that, for each covariate in \mathbf{X}_{it} , you have a (slightly) different slope for each unit i , depending on $\hat{\theta}_i$!

From random effect to fixed effect and pooled model

Now, consider:

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Your software will usually provide to you an estimate of θ_i (or of the variance of slopes) and related tests. Check the output!

3(c) – Model comparison

	Pooled	Pooled (clustered SE)	Fixed Effect	Random Effect
(Intercept)	4.72*** (0.15)	4.72*** (0.24)		3.20*** (0.33)
exp	0.06*** (0.01)	0.06*** (0.01)	0.11*** (0.01)	0.09*** (0.01)
exp2	−0.00*** (0.00)	−0.00*** (0.00)	−0.00 (0.00)	−0.00* (0.00)
wks	−0.00 (0.00)	−0.00 (0.00)	0.00* (0.00)	0.00 (0.00)
ed	0.10*** (0.01)	0.10*** (0.01)		0.14*** (0.02)
Adj. R ²	0.43	0.43	0.70	0.52
Num. obs.	700	700	700	700

*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

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In R (Stata is very similar, see script):

```
1 phtest(fe, re)
2
3 #####
4 #   Hausman Test
5 #
6 # data:  lwage ~ exp + exp2 + wks + ed
7 # chisq = 3805.5, df = 3, p-value < 2.2e-16
8 # alternative hypothesis: one model is inconsistent
9 #####
```

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- We should use **clustered** SEs (on our units) when we have panel data, otherwise we are not fixing serial correlation between units
- These SEs will **also** be robust to heteroskedasticity
- Look at the education variable. Why is it omitted from the fixed effect model?
- Because for each respondent (within unit) education does not change! Thus there is no within-variation, and the within-variation is the only thing a fixed-effect looks at.

All clear? More questions?
Thanks and see you next week!