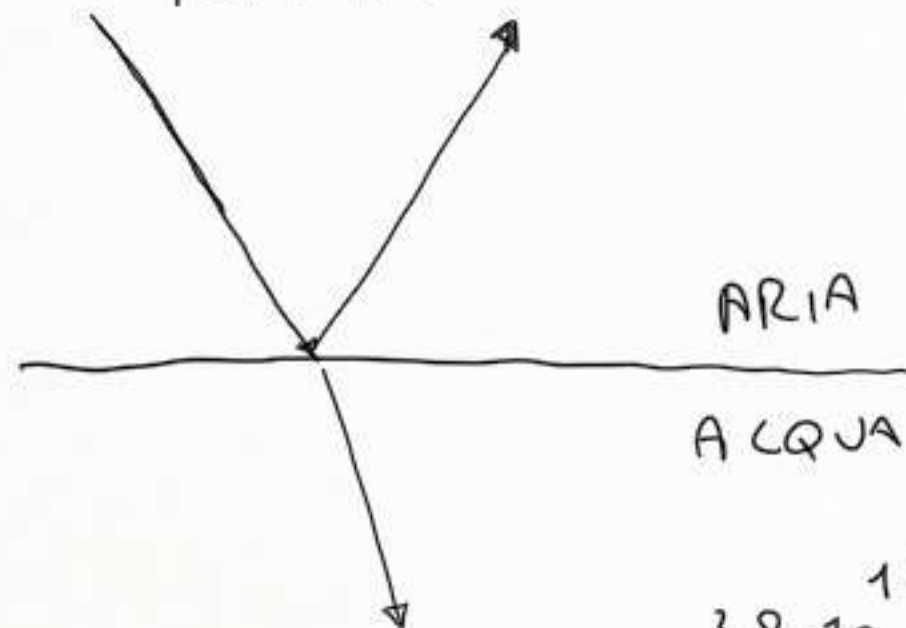
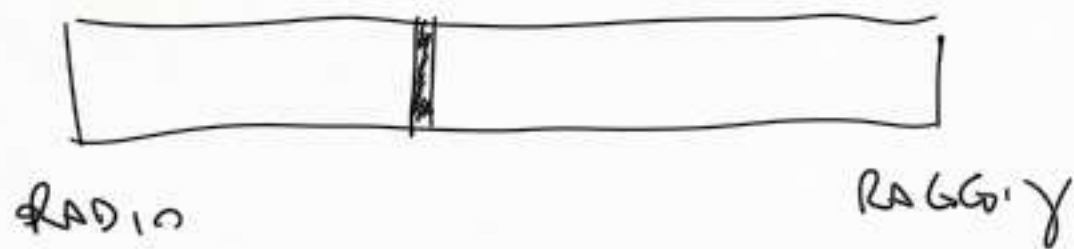


# RIFRAZIONE E RIFLESSIONE



$3.8 \cdot 10^{14} \leq \nu \leq 7.9 \cdot 10^{14} \text{ Hz}$   
 $0.78 \cdot 10^{-6} \geq \lambda \geq 0.38 \cdot 10^{-6} \text{ m}$



le onde nel vuoto hanno  $c$   
 " nel mezzo hanno  $v$

$$\frac{c}{v} \equiv n \quad \text{INDICE DI RIFRAZIONE}$$

$$n \geq 1$$

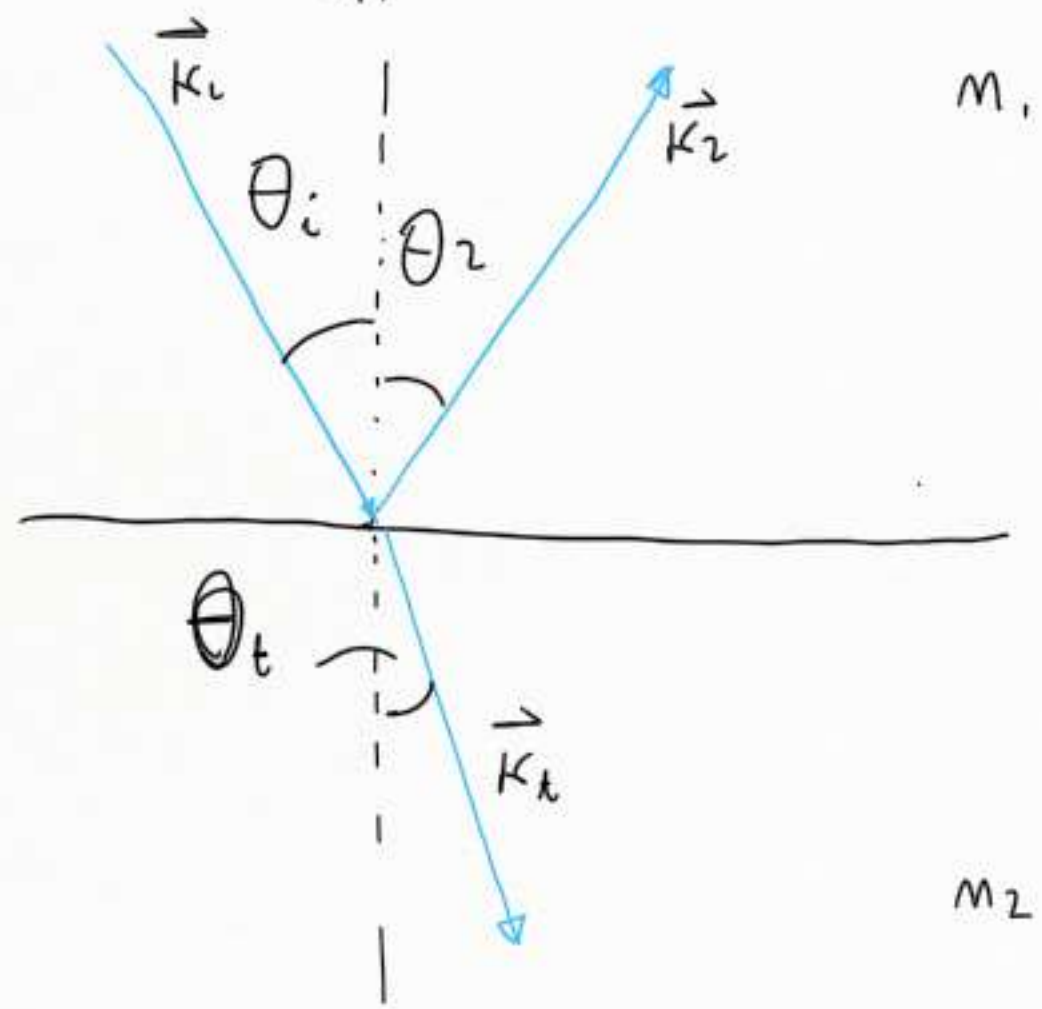
$$n \approx 1 \quad \text{ARIA}$$

$$1.33 \quad \text{ACQUA}$$

$$1.5 - 2 \quad \text{VETRO}$$

$$v = \lambda \nu, \quad c = \lambda_0 \nu \Rightarrow$$

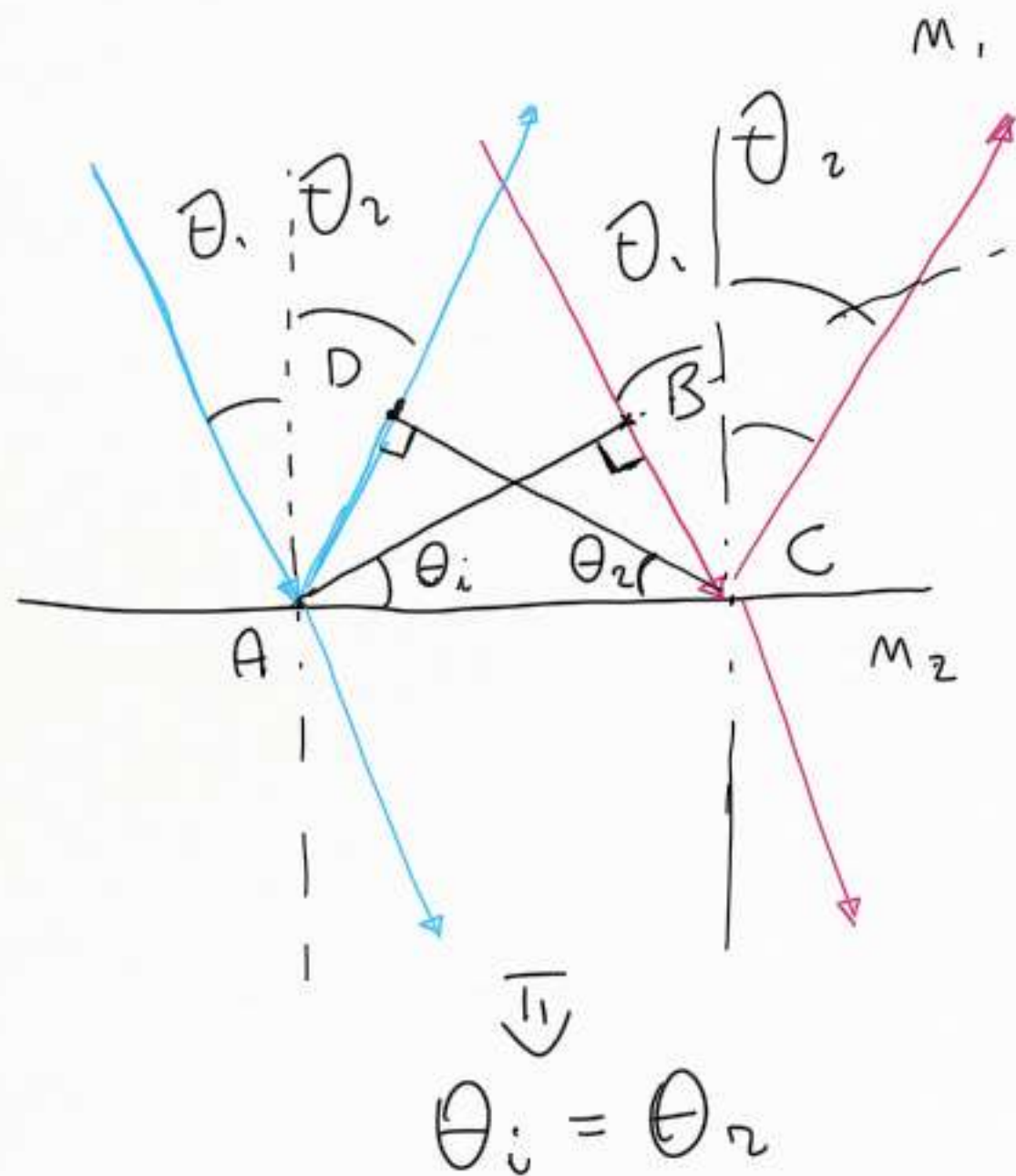
$$\lambda = \frac{\lambda_0}{n} \Rightarrow k = n k_0$$



- piano di incidenza :  
 il piano formato da  $\vec{k}_i$  e dalla normale

- superficie speculare

$\downarrow$   
 $\vec{k}_r, \vec{k}_t$  giacciono sul piano d'incidenza



$$\overline{AD} = \overline{BC}$$

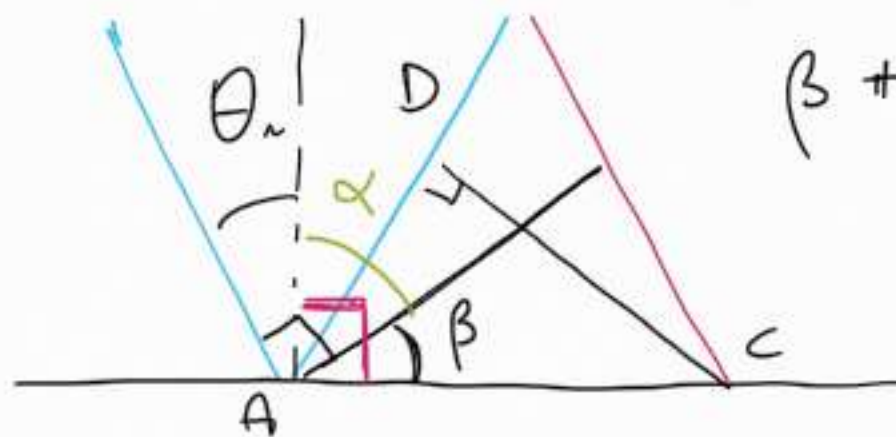
consideriamo  $ACD$  e  $ABC$

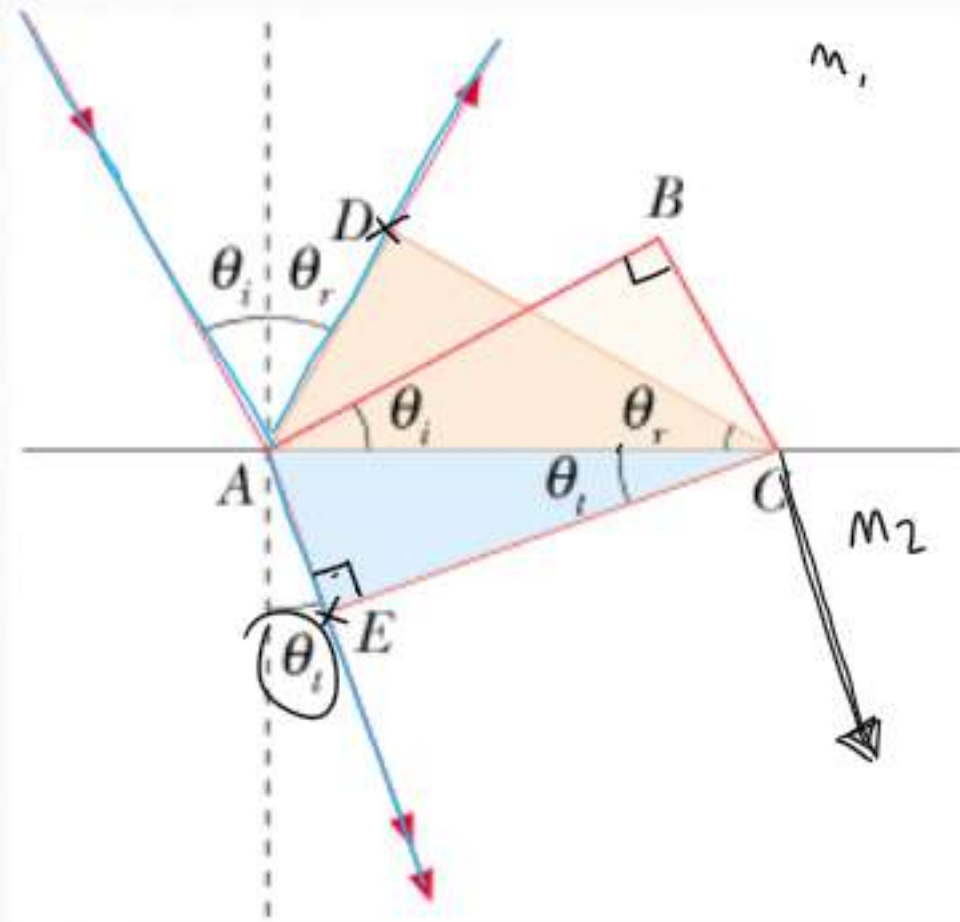
- hanno  $AC$  in comune
- hanno un altro lato uguale ( $\overline{AD} = \overline{BC}$ )
- hanno un angolo retto

$\Downarrow$

i due triangoli hanno tutti i lati e angoli uguali

$$\left. \begin{array}{l} \theta_i + \alpha = \frac{\pi}{2} \\ \beta + \alpha = \frac{\pi}{2} \end{array} \right\} \Rightarrow \beta = \theta_i$$





Consideriamo  $ABC$  e  $ACE$

↳ hanno un lato in comune ( $AC$ ): l'ipotenusa

$$\overline{AE} = v_2 \Delta t = \frac{c}{n_2} \Delta t = \overline{AC} \sin \theta_t \Rightarrow$$

$$\overline{AC} = \frac{c \Delta t}{n_2 \sin \theta_t}$$

$$\overline{BC} = v_1 \Delta t = \frac{c}{n_1} \Delta t = \overline{AC} \sin \theta_i \Rightarrow$$

$$\overline{AC} = \frac{c \Delta t}{n_1 \sin \theta_i} \Rightarrow$$

$$\frac{c \Delta t}{n_2 \sin \theta_t} = \frac{c \Delta t}{n_1 \sin \theta_i} \Rightarrow n_1 \sin \theta_i = n_2 \sin \theta_t$$

LEGGE DI SNELL

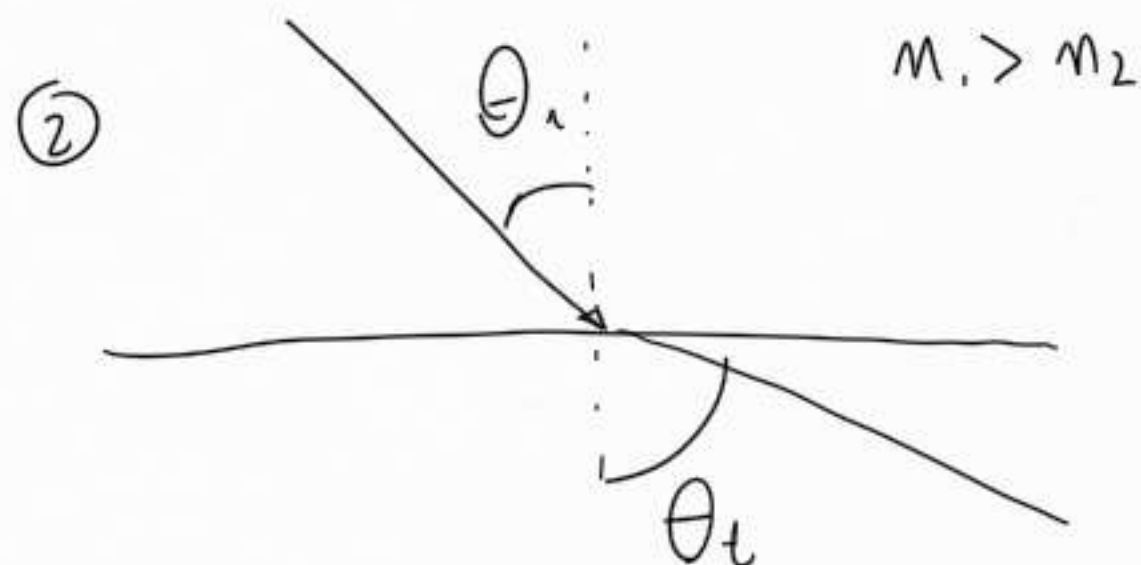
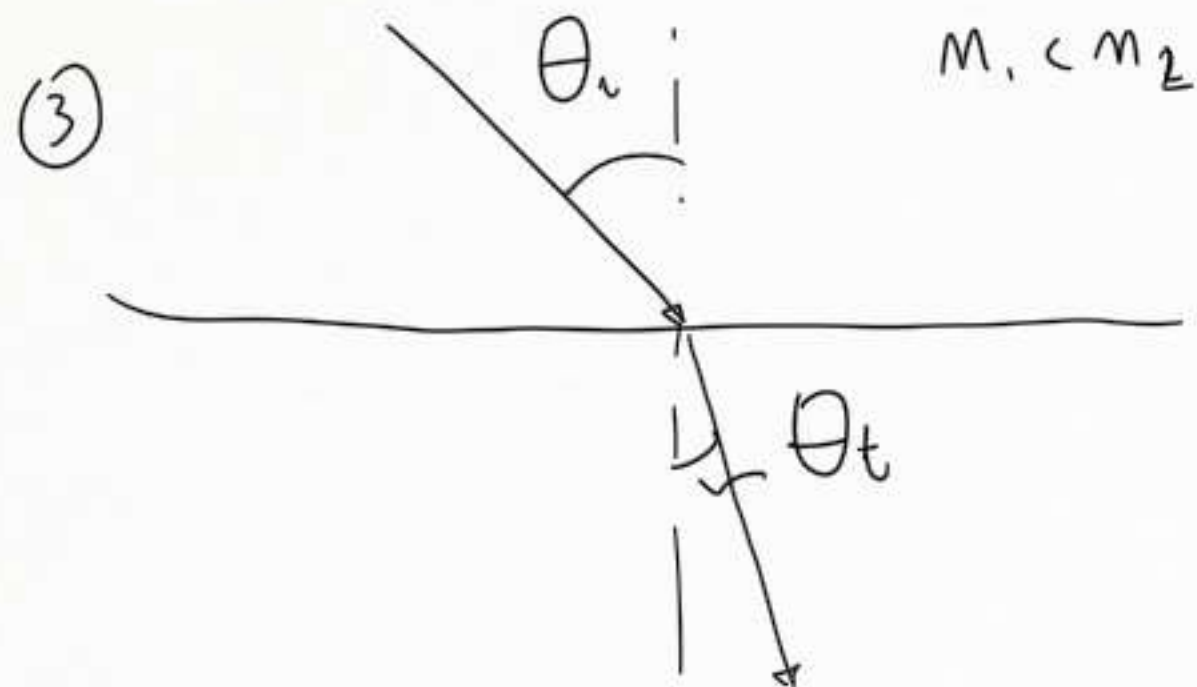


$$\sin \theta_t = \frac{n_1}{n_2} \sin \theta_i$$

↓  
 ① se  $\theta_i = 0$ ,  $\theta_t = 0$

② se  $n_1 > n_2$ ,  $\theta_t > \theta_i$

③ se  $n_2 > n_1$ ,  $\theta_i > \theta_t$

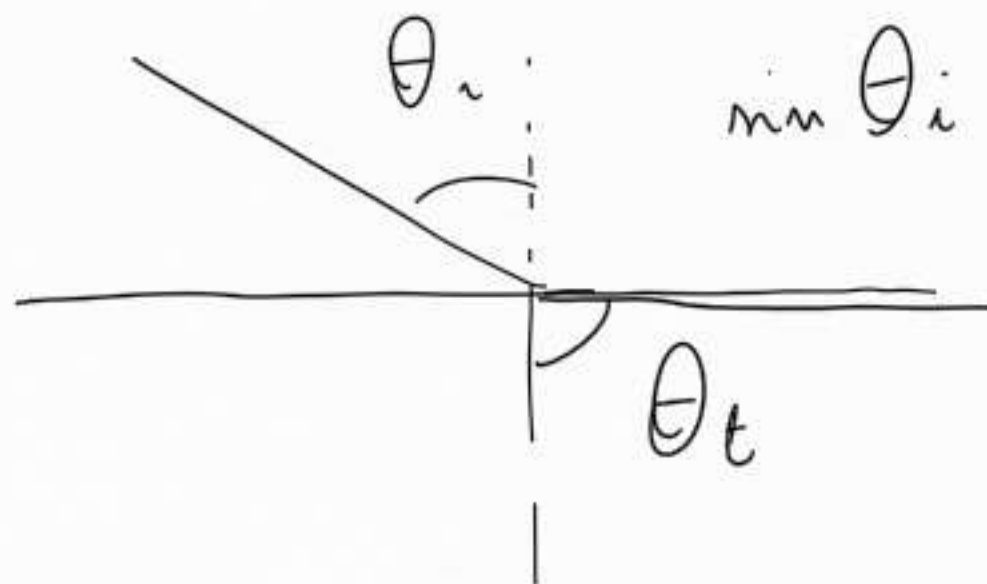


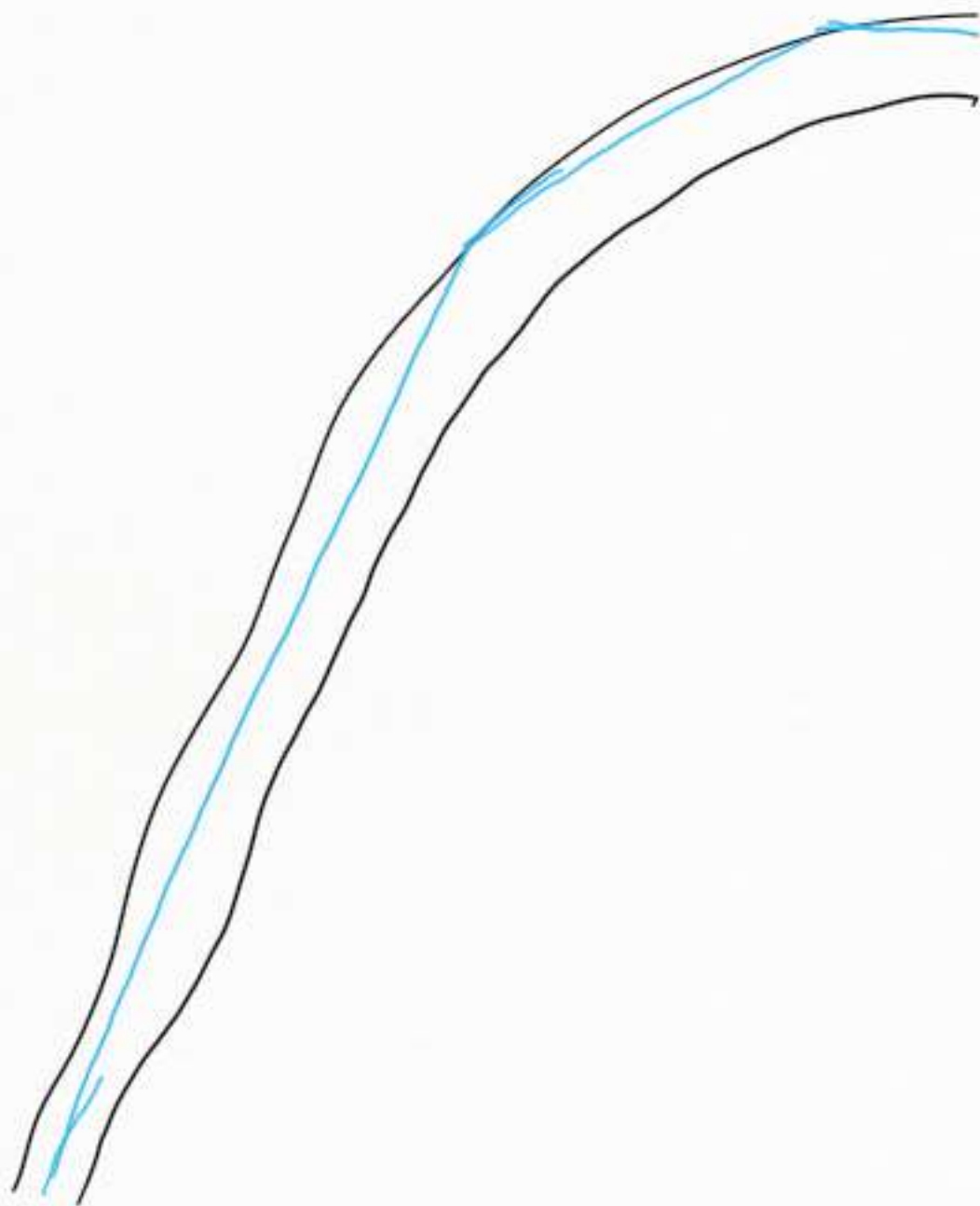
$$\sin \theta_t = 1 = \frac{n_1}{n_2} \sin \theta_i \Rightarrow$$

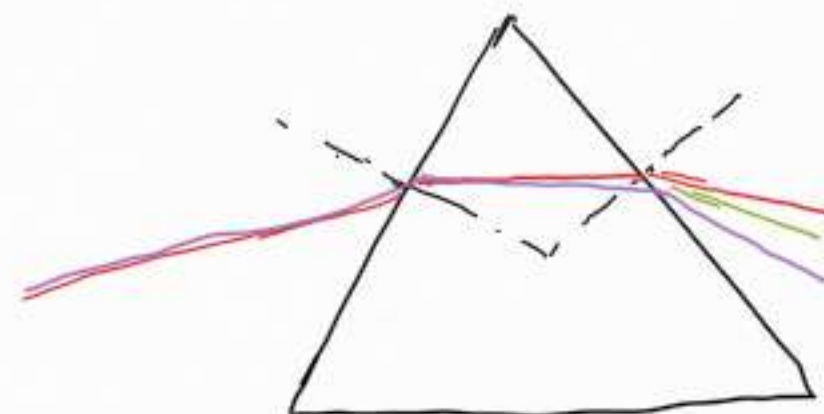
$$\sin \theta_i = \frac{n_2}{n_1} \equiv \sin \theta_0$$

ANGOLO LIMITE

per  $\theta_i > \theta_0$

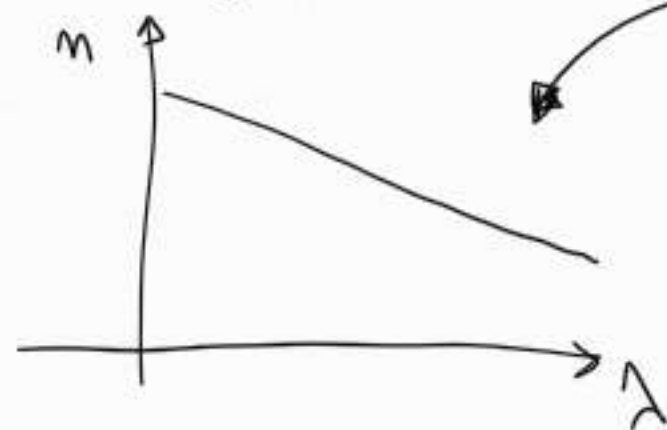






DISPERSIONE  
DELLA LUCE

$$n = n(\lambda)$$



$$E(r, t) = E_0(r) \cos(kr - \omega t)$$

$$P_m(r) = I(r) 4\pi r^2 = \frac{1}{2} c \epsilon_0 E_0^2(r) 4\pi r^2 = \omega r \quad \Rightarrow$$

$$E_0^2(r) r^2 = \omega r \quad \Rightarrow \quad E_0(r) \sim \frac{1}{r} \quad \Rightarrow$$

$$\begin{cases} E(r, t) = \frac{E_0}{r} \cos(kr - \omega t) \\ B(r, t) = \frac{E_0}{cr} \cos(kr - \omega t) \end{cases} \quad \text{ONDA E.M. SFERICA}$$





stesse  $\lambda$  e  $\omega$

$$\bar{E}_1 = \frac{\bar{E}_0}{2} \cos(\kappa r_1 - \omega t + \phi_1)$$

$$\bar{E}_2 = \frac{\bar{E}_0}{2} \cos(\kappa r_2 - \omega t + \phi_2)$$

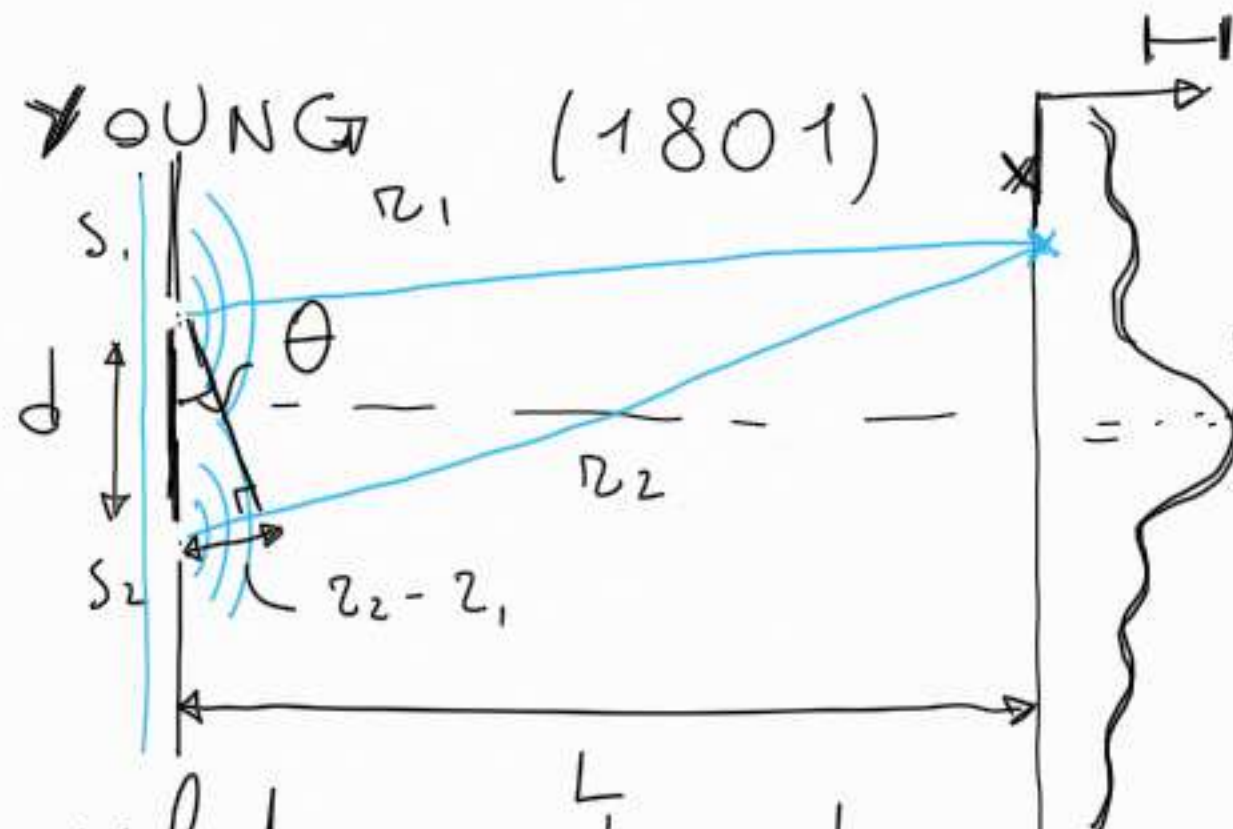
difference di  
fase

$$\begin{aligned} \Delta \phi &= (\kappa r_2 - \omega t + \phi_2) - (\kappa r_1 - \omega t + \phi_1) = \\ &= \boxed{\kappa (r_2 - r_1)} + \phi_2 - \phi_1 = \kappa (r_2 - r_1) + \Delta \phi \end{aligned}$$

difference di  
fase intrinseca  
possono dare  
interferenza

$\Delta \phi$  non dipende dal tempo  $\rightarrow$  le sorgenti sono coerenti  
se  $\Delta \phi = 0 \rightarrow$  le sorgenti sono in fase

# ESPERIMENTO DI YOUNG (1801)



PATERN DI  
INTERFERENZA

$$\delta = k(r_2 - r_1) \approx kd \sin \theta \quad \text{valida per } L \gg d$$

$$kd \sin \theta = \boxed{\frac{2\pi}{\lambda} \sin \theta}$$

$$I(\theta) = 4I_0 \cos^2\left(\frac{\pi d \sin \theta}{\lambda}\right), \quad I_0 \text{ è l'intensità della singola onda}$$

$$I(\theta) = 4I_0 \cos^2 \left( \frac{\pi d \sin \theta}{\lambda} \right)$$

maxima se

$$\frac{\pi d \sin \theta}{\lambda} = m\pi$$

$$\Rightarrow$$

$$\boxed{d \sin \theta = m\lambda}$$

con  $m$  intero

minima se

$$\frac{\pi d \sin \theta}{\lambda} = \pi \left( m + \frac{1}{2} \right)$$

$$\Rightarrow$$

$$\boxed{d \sin \theta = \left( m + \frac{1}{2} \right) \lambda}$$

$m$  intero

