Assignment 2 Spatial Epidemiology

Ferrara Lorenzo, Lucchini Marco

29-11-2022

Description:

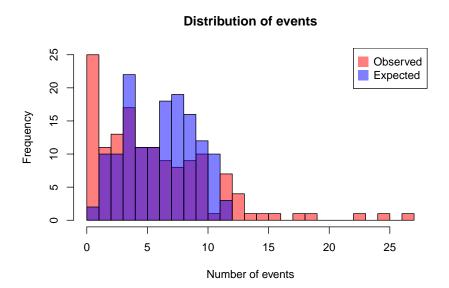
Data of the incidence of larynx cancer diagnosed during 10 years (1982-1991) in the districts of Mersey and West Lancashire in the north-east of England is in the file larynx-dates.odc. They have detected 876 cases in 144 electoral districts. The number of expected cases were calculated using internal standardization, based on the specific rates of sex and age in the zone of study (with the population of the census 1991).

1) Perform an exploratory analysis to study the possible spatial correlation of the larynx incidence (Standardized Mobility Ratio, SMR) (considering neighbors those regions that share geographic limits and the matrix of weights as the matrix standardized by rows)

The data available to as are the following:

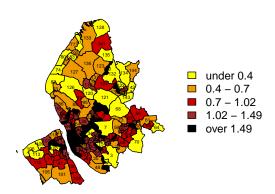
- O: Number of observed events
- E: Number of Expected events

In the observed regions 0 to 27 events were registered and the median number of observations is 5. The expected value of the cases was between 0.710 and 11.700 with median 6.365. The two distribution of the data are the following:



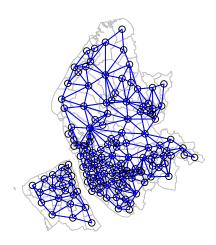
We also visualize the distribution of the data on the map of the regions:

Standardized Mortality Rate (SMR) during 1982-1991



We notice that in the center of the district there's a cluster of regions with high values of SMR, which slowly lower as we get away from the center.

Now we'll analyse the lattice structure of the data: let's consider neighbors those regions that share geographic limits:



After establishing the neighbors we compute the weights (weights standardized by row). The weights corresponding to the first four regions are:

```
## [[1]]
## [1] 0.3333333 0.3333333 0.3333333
##
## [[2]]
## [1] 0.1666667 0.1666667 0.1666667 0.1666667 0.1666667
##
## [[3]]
## [1] 0.1428571 0.1428571 0.1428571 0.1428571 0.1428571 0.1428571
##
## [[4]]
## [1] 0.2 0.2 0.2 0.2 0.2
```

Now we can perform a Moran test to prove or disprove the presence of spatial autocorrelation:

• We do it first using Moran's I statistic:

```
##
##
   Moran I test under randomisation
## data: NW.dataset$SMR
## weights: weight.object
##
## Moran I statistic standard deviate = 6.2244, p-value = 2.417e-10
## alternative hypothesis: greater
## sample estimates:
## Moran I statistic
                           Expectation
                                                 Variance
                          -0.006993007
##
         0.313393219
                                             0.002649439
```

The I statistic is 0.313, which is quite different from the expected value (-0.0069), indeed the p-value is very low $(p = 2.4 \cdot 10^{-10})$, so we reject the null hypothesis.

• We also do it through a Monte Carlo approach:

```
##
## Monte-Carlo simulation of Moran I
##
## data: NW.dataset$SMR
## weights: weight.object
## number of simulations + 1: 9001
##
## statistic = 0.31339, observed rank = 9001, p-value = 0.0001111
## alternative hypothesis: greater
```

and the p-value is p = 0.000111, therefore also in this case we reject the null hypothesis.

Both methods lead us to the conclusion that spatial correlation is present.

2) If we consider that the number of cases of Larynx are a Poisson distribution, are data overdispersed?

We try to fit the data with a Poisson model:

If the Poisson model fits the data reasonably, we would expect the residual deviance to be roughly equal to the degrees of freedom (n - p = 143).

```
##
## Call:
  glm(formula = 0 ~ 1, family = quasipoisson(link = "log"), data = data,
##
       offset = E)
##
## Deviance Residuals:
                         Median
                                       3Q
##
        Min
                   10
                                                Max
  -12.7956
              -0.0396
                         3.0419
                                   5.3649
                                            15.1299
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -7.0356
                            0.5893 -11.94
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for quasipoisson family taken to be 304.254)
##
##
       Null deviance: 3557.1 on 143 degrees of freedom
## Residual deviance: 3557.1 on 143 degrees of freedom
## AIC: NA
##
## Number of Fisher Scoring iterations: 7
```

But we can notice that the residual deviance is very large (3557.1) and that the dispersion parameter is 304.254. Therefore we can conclude that the data are overdispersed.

3) Fit the SMR taking into account the over-dispersion of the data using a heterogeneity model, a spatial (CAR intrinsic) and the convolution model. Estimate the models using Bayesian inference (Gibbs Sampling). Use three chains of initial values.

(for the sake of clarity we didn't show the estimates of RR, the Relative Risk)

• Heterogeneity model: unstructured overdispersion

```
## Inference for Bugs model at "C:/Users/lofer/OneDrive/Documenti/GitHub/Epidemiology_2nd_Assignment/la
   3 chains, each with 10000 iterations (first 1000 discarded), n.thin = 10
   n.sims = 2700 iterations saved
                        2.5%
                                25%
                                      50%
                                            75% 97.5% Rhat n.eff
             mean
                        -0.2
             -0.1
                               -0.2
                                     -0.1
                                           -0.1
                                                  0.0
                                                            2700
## alpha0
                   0.1
              3.7
                   0.8
                         2.5
                                3.2
                                      3.7
                                            4.2
                                                   5.5
                                                             2700
## tau.h
## sigma.h
              0.5 0.1
                         0.4
                                0.5
                                      0.5
                                            0.6
                                                   0.6
                                                          1
                                                             2700
## deviance 616.5 16.0 586.8 605.2 615.8 627.2 649.8
                                                             2700
```

For each parameter, n.eff is a crude measure of effective sample size,
and Rhat is the potential scale reduction factor (at convergence, Rhat=1).

```
##
## DIC info (using the rule, pD = Dbar-Dhat)
## pD = 80.6 and DIC = 697.1
## DIC is an estimate of expected predictive error (lower deviance is better).
```

• Spatial model: we model a structured overdispersion, using the spatial structure we have created above (the neighbors, the weights and the corresponding adjacency matrix)

```
## Inference for Bugs model at "C:/Users/lofer/OneDrive/Documenti/GitHub/Epidemiology_2nd_Assignment//L
   3 chains, each with 7000 iterations (first 1000 discarded), n.thin = 8
   n.sims = 2250 iterations saved
                    sd 2.5%
##
             mean
                               25%
                                      50%
                                            75% 97.5% Rhat n.eff
             -0.2
                  0.0
                        -0.3
                              -0.2
                                    -0.2
                                                 -0.1
## alpha0
                                           -0.1
## tau.s
              2.1
                                            2.4
                                                  3.4
                                                            1700
                   0.6
                         1.2
                               1.7
                                      2.0
                                      0.7
                                            0.8
                                                  0.9
                                                            1700
## sigma.s
              0.7
                   0.1
                         0.5
                               0.6
## deviance 619.2 13.9 593.6 609.7 618.8 628.4 647.7
                                                            2200
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
## DIC info (using the rule, pD = Dbar-Dhat)
## pD = 56.6 and DIC = 675.9
## DIC is an estimate of expected predictive error (lower deviance is better).
```

• Convolution model: we create a model which takes into account both a structured (spatial) overdispersion and an unstructured (heterogeneity) one

```
## Inference for Bugs model at "C:/Users/lofer/OneDrive/Documenti/GitHub/Epidemiology_2nd_Assignment//L
    3 chains, each with 10000 iterations (first 1000 discarded), n.thin = 8
    n.sims = 3375 iterations saved
                     sd
                         2.5%
                                 25%
                                       50%
                                             75%
                                                  97.5% Rhat n.eff
             mean
## alpha0
             -0.2
                    0.0
                         -0.3
                                -0.2
                                      -0.2
                                            -0.1
                                                   -0.1
                                                            1
                                                                770
              2.5
                           1.3
                                 1.9
                                       2.3
                                             2.9
                                                     4.7
                                                                870
## tau.s
                    0.9
                                                            1
## sigma.s
              0.7
                    0.1
                           0.5
                                 0.6
                                       0.7
                                             0.7
                                                     0.9
                                                                870
            217.4 420.8
                           9.8
                               27.8
                                     71.2 207.7 1369.8
                                                                570
## tau.h
                                                            1
## sigma.h
              0.1
                    0.1
                           0.0
                                 0.1
                                       0.1
                                             0.2
                                                     0.3
                                                            1
                                                                570
## deviance 615.3 14.2 588.3 605.9 615.1 624.6 643.5
##
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
##
## DIC info (using the rule, pD = Dbar-Dhat)
## pD = 59.1 and DIC = 674.5
## DIC is an estimate of expected predictive error (lower deviance is better).
```

4) Check the convergence and study the autocorrelation of the chain. Decide which model fit better the data.

To study the convergence we look both at the traceplots of the fitted parameters (the 3 chains should stabilize after some time around the same value) and at the \hat{R} coefficient of the parameters of the models (we'll assume that convergence is reached if $\hat{R} < 1.05$)

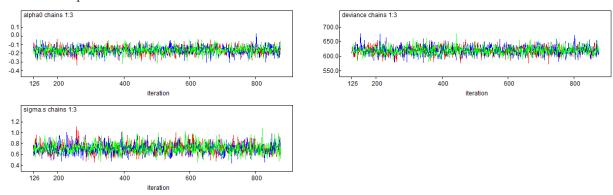
To study the autocorrelation of the chain we look at the autocorrelation plots which WinBugs gives us.

• Spatial:

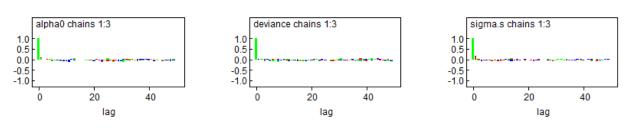
All the \hat{R} coefficients are below 1.05, indeed the maximum value we get is:

[1] 1.004156

and the traceplots are:



The autocorrelation plots are:

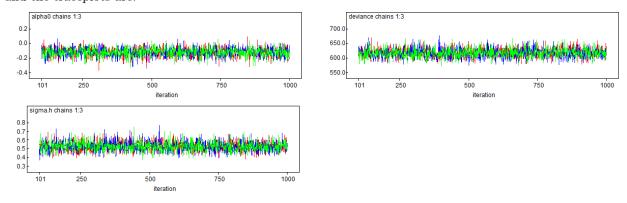


• Heterogeneity:

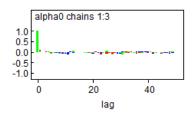
All the \hat{R} coefficients are below 1.05, indeed the maximum value we get is:

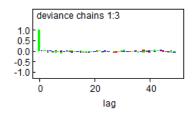
[1] 1.004661

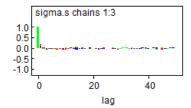
and the traceplots are:



The autocorrelation plots are:





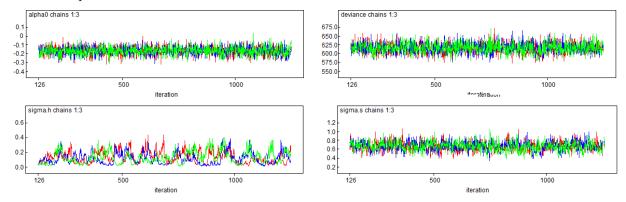


• Convolutional:

All the \hat{R} coefficients are below 1.05, indeed the maximum value we get is:

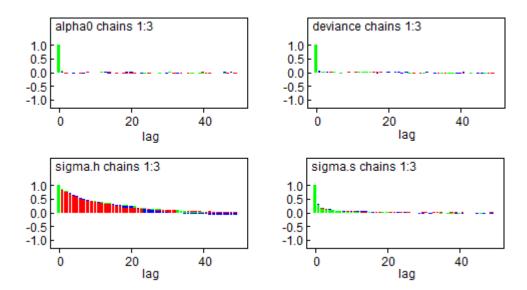
[1] 1.016474

and the traceplots are:



Since there are more than one random effect, the convergence of the parameters is harder to reach because the Monte Carlo Markov Chain struggles to find a stable value of sigma_h to converge to.

The autocorrelation plot is



We also have issues with the autocorrelation of the chains for sigma_h: even using a high value for the thin parameter it's difficult to find a chain with no or little autocorrelation. So we'll avoid choosing the Convolutional model.

We can also evaluate the DIC (Deviance Information Criterion):

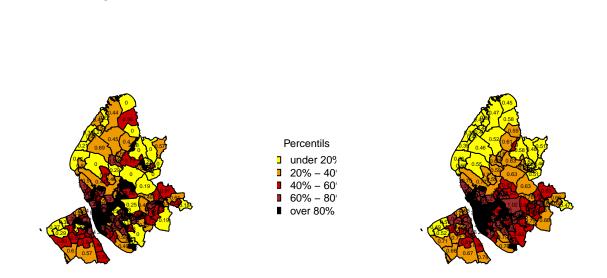
```
## type DIC
## 1 spatial 675.889
## 2 heterogeneity 697.117
## 3 convolutional 674.470
```

SMR

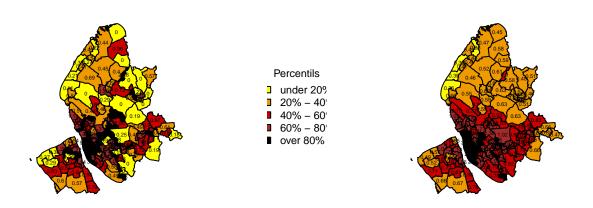
The DIC index is an estimate of expected predictive error, so we'll choose the model with the lowest DIC. The Spatial model and the Convolutional model are almost comparable, but even though the Convolutional has a slightly lower DIC we'll choose the Spatial, due to the two considerations we have made above.

5.1) Using the model that better fit the data: Make a plot of the observed SMRs and Relative Risk estimated by the model (mean posterior of SMR), using the percentiles of the values. Compare them and discuss the differences.

RR



SMR RR

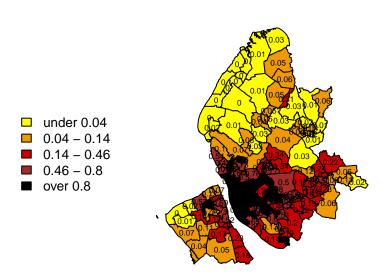


The values of RR estimated by the model follow a radial pattern - with higher values in the center and gradually lower values far from the center. Its pattern is smoother than the one followed by the observed values of SMR, which present many low-value hotspots in the center and some high-value clusters in the north

We could say that the SMR has two main clusters (center and north), of which only one is recognized by the model (center), but from a qualitative point of view the chosen model can describe well the phenomenon, even though just in a rough way and not so in detail.

5.2) Make a plot showing the posterior probability of relative risk of the electoral districts that exceed 1. What do you observe?





Let's analyse the meaning of the SMR: a ratio greater than 1 indicates that more mortality has occurred with respect to the expected values, which means that we can state with pretty high probability that the black and brown regions have an increase in the value of the observed cases (p > 46% for the brown regions and p > 80% for the black ones).

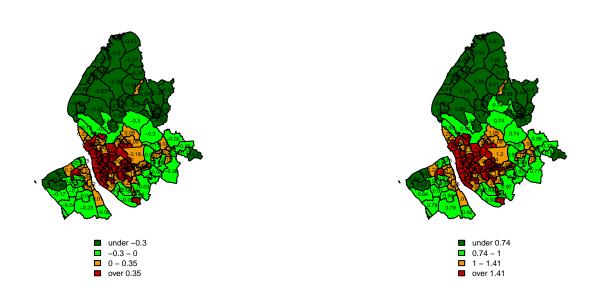
We may suppose the presence of an underlying phenomenon which is causing this increase of the mortality due to larynx cancer. It may be linked to some change of the environmental-working conditions in the areas under investigation.

5.3) Make a plot showing the random effects for each districts (exponential scale) and another with the significance of this parameters. What do you observe?

The random effect is the spatial effect $s[i], \forall i \in \{1, ..., 144\}$. If we want to see it in exponential scale, we'll use $resid[i] = e^{s[i]}$.

Notice that the formula is $RR[i] = e^{\alpha_0 + s[i]} = e^{\alpha_0} \cdot e^{s[i]}$ and the multiplying factor is exactly $e^{s[i]}$.

Random Effect resid



These plots show how the spatial effect affects the values of the RR estimated by the model:

- In the regions where s[i] > 0, so $e^{s[i]} > 1$, RR is positively influenced by the spatial effect, leading to a higher number of deaths than expected
- Viceversa in the regions where s[i] < 0, so $e^{s[i]} < 1$, RR is negatively influenced by the spatial effect, leading to a lower number of deaths than expected.