

RISPOSTA A INGRESSI SINUSOIDALI

$$u(t) = \sin(\tilde{\omega} t)$$

$$e(t) = k_d \cdot u(t) - y(t)$$

$$e(s) = W_e(s) \cdot u(s)$$

STESSA PULSAZIONE DELL'INGRESSO

$$\tilde{e}(t) = |W_e(j\tilde{\omega})| \sin(\tilde{\omega} t + \angle W_e(j\tilde{\omega})) \rightarrow |\tilde{e}(t)| \leq |W_e(j\tilde{\omega})|$$

$$d_1(t) = \sin(\tilde{\omega} t)$$

$$\tilde{y}_{d1}(t) = |W_{d1}(j\tilde{\omega})| \sin(\tilde{\omega} t + \angle W_{d1}(j\tilde{\omega}))$$

$$W_{d1}(s) = \frac{1}{1 + \frac{F(s)}{k_d}}$$

$$|W_{d1}(j\omega)| = \frac{1}{|1 + \frac{F(j\omega)}{k_d}|}$$

$$|\tilde{y}_{d1}(t)| \leq \left| \frac{1}{1 + \frac{F(j\omega)}{k_d}} \right|$$

$$W_e(s) = k_d - W(s) = k_d - \frac{F(s)}{1 + \frac{F(s)}{k_d}} =$$

$$= \frac{k_d + \cancel{F(s)} - \cancel{F(s)}}{1 + \frac{F(s)}{k_d}} = \frac{k_d^2}{k_d + F(s)}$$

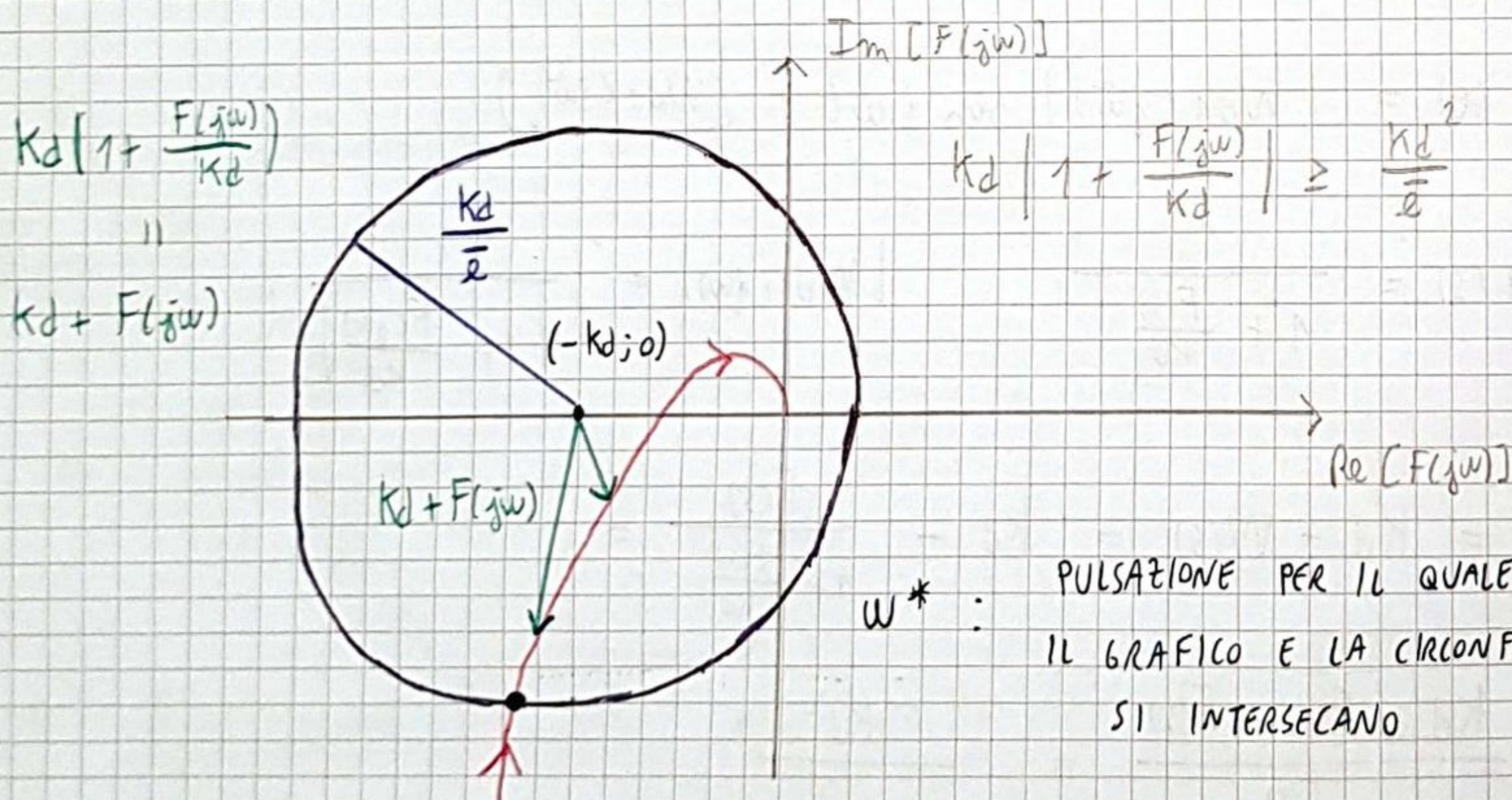
$$|W_e(j\omega)| = \frac{k_d^2}{|k_d + F(j\omega)|} = \frac{k_d}{|1 + \frac{F(j\omega)}{k_d}|}$$

Desidero che l'ampiezza dell'errore a regime permanente sia limitata

$$|\tilde{e}(t)| \leq |W_e(j\omega)| \leq \bar{e}$$

$$|W_e(j\omega)| \leq \bar{e} \iff \frac{K_d}{\left|1 + \frac{F(j\omega)}{K_d}\right|} \leq \bar{e}$$

$$\longrightarrow \left|1 + \frac{F(j\omega)}{K_d}\right| \geq \frac{K_d}{\bar{e}}$$



$$1 + \frac{F(j\omega^*)}{K_d} = \frac{K_d}{\bar{e}}$$

• $\omega < \omega^* \longrightarrow \left|1 + \frac{F(j\omega)}{K_d}\right| \geq \frac{K_d}{\bar{e}} \quad \checkmark$

• $\omega > \omega^* \longrightarrow \left|1 + \frac{F(j\omega)}{K_d}\right| < \frac{K_d}{\bar{e}}$