# Project documentation

## Lorenzo Zanolin

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## 1 Introduction

The aim of this project is the study of Yao's protocol [3] and it's useful application. More precisely, we will implement secure multi-party computation; this field has the goal of creating methods for parties to jointly compute a function over their inputs while keeping those inputs private [2]. In this project, the function we decided to implement is the 8 bit sum.

# 2 Analysis

We can focus on the sum computed by two parties, say Alice and Bob. The goal is to use MPC to calculate the result while avoiding each member knowing the others values; to do that, we need an external component called OT.

This protocol allows two parties, Alice who knows x and Bob who knows y, to jointly compute the value of f(x, y) in a way that does not reveal to each side more information than can be deduced from f(x, y) [1]. As already written, f is the 8-bit sum.

Both Alice and Bob have a set of integers and need to compute the sum of everything. Two new roles are introduced: Alice is the *garbler* and has the responsibility of creating the garbled circuit, while Bob is the *evaluator*. They will behave as follows:

- 1. Alice creates the garbled circuit and the tables and sends them to Bob.
- 2. Alice selects her set, via input.
- 3. Bob selects his set, via input.
- 4. Both interact with each other using OT.
- 5. Bob evaluates the function result and sends it to Alice.
- 6. Alice checks the correctness of the result, and sends it to Bob (in clear).

# 3 Implementation

We will present how to implement the *circuit* and how to make Alice and Bob comunicate securely.

### 3.1 Circuit

We will briefly present the 8-bit sum circuit. There are three basic components in this construction:

- *Half Adder*: used to sum the right-most digit;
- Full adder: used to sum a generic digit in the number, ranging from position 1 to 8. It receives in input also a carry of the previous sum.
- If then else: there could be situations, called overflow, in which you sum two numbers with the same sign and obtain a number with the opposite sign; to avoid this scenario, this construct is employed by examining the signs of the two numbers and the sign of the calculated result. If the two input numbers have the same sign, the output sign is set to be the same as the inputs. Instead, if the two input numbers have different signs, the sign of the result is determined according to the previous circuit.



Figure 1: Half Adder

Figure 2: Full Adder

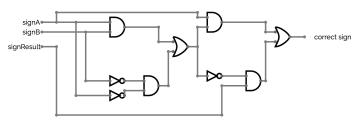


Figure 3: If then else

1

We then proceeded to create the circuit by wiring seven full adders, a half adder and the if-then-else together, as represented in Figure 4.

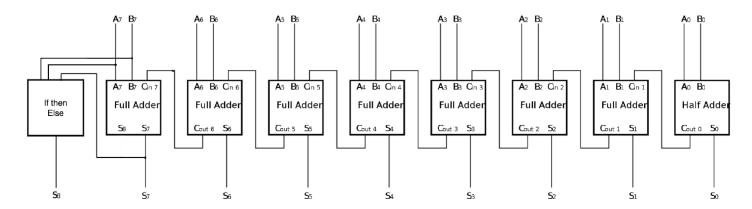


Figure 4: 8-bit adder

Since we are using 8 bits to represent the sum of each set, it immediately follows that the sum of each set must be smaller than 256. In this case, we are dealing with *integers*, so we also need to consider negative numbers; to do that we are using 2-complement. In this case we are considering numbers that belong to [-128, 127]. The final sum has a 9 bits representation, thus the result that we can obtain belongs to [-256, 254].

#### 3.1.1 Project structure

The project will be developed using Python~3.9.10 and we will use functions provided in the GitHub repo: https://github.com/ojroques/garbled-circuit.

There is also a dedicated GitHub page related to this project at https://github.com/lorenzozanolin/garbledCircuit.

The project has the following structure:

The code folder contains all the files that we will utilize for secure communication. ot.py, util.py, yao.py are utilities taken from the Ojroques repo.

The images folder contains all images used in the report and documentation.

The circuits folder contains the used circuit, in this case only add. json

The sets folder contains the two files used to store sets of Alice and Bob.

<sup>&</sup>lt;sup>1</sup>1 was taken over https://upload.wikimedia.org/wikipedia/commons/1/14/Half-adder.svg 2 was taken over https://upload.wikimedia.org/wikipedia/commons/a/a9/Full-adder.svg.

```
src/.
  _Makefile
                                      This directory contains the images used.
   images
   <u>∟</u> . . .
   circuits
                                      This directory contains the circuit used.
    __add.json
                                    This directory contains the code used.
   code
     _util.py
     _yao.py
     _ot.py
     \_ requirements.py
     _{\mathtt{main.py}}
                                    This directory contains the sets saved.
   sets
     _alice.txt
     _bob.txt
```

### 3.1.2 Coding part

First things first, we need to represent the *circuit*; we decided to create the add.json file to code the circuit. Each wire is mapped to a number and linked with the others following the structure represented in Figure 4.

Each gate that appears in figure 4 is represented by a single JSON line.

The syntax is:

```
"id" : <gateId>, "type" : "<TYPE>", "in": [<gateIdInput1>, <gateIdInput2>]
```

In this case the circuit is represented as follows:

```
\{"name":"adder",
1
        "circuits":[
2
3
           "id": "8 bit adder",
4
           "alice": [47,40,33,26,19,12,5,1],
5
           "bob": [48,41,34,27,20,13,6,2],
6
           "out": [62,50,43,36,29,22,15,8,3],
7
           "gates":[
8
                {"id":3,"type":"XOR","in":[1,2]},
9
                {"id":4,"type":"AND","in":[1,2]},
10
11
                {"id":7,"type":"XOR","in":[5,6]},
12
                 "id":8,"type":"XOR","in":[4,7]},
13
                 "id":9,"type":"AND","in":[4,7]},
14
```

```
{"id":10,"type":"AND","in":[5,6]},
15
                {"id":11,"type":"OR","in":[9,10]},
16
17
                {"id":14,"type":"XOR","in":[12,13]},
18
                "id":15,"type":"XOR","in":[11,14]},
19
                "id":16,"type":"AND","in":[11,14]},
20
                {"id":17,"type":"AND","in":[12,13]},
21
                {"id":18,"type":"OR","in":[16,17]},
22
23
                {"id":21,"type":"XOR","in":[19,20]},
24
                "id":22, "type": "XOR", "in": [18,21]},
25
                "id":23,"type":"AND","in":[18,21]},
26
                {"id":24,"type":"AND","in":[19,20]},
27
                {"id":25,"type":"OR","in":[23,24]},
28
29
                {"id":28,"type":"XOR","in":[26,27]},
30
                {"id":29,"type":"XOR","in":[25,28]},
31
                "id":30,"type":"AND","in":[25,28]},
32
                {"id":31,"type":"AND","in":[26,27]},
33
                {"id":32,"type":"OR","in":[30,31]},
34
35
                {"id":35,"type":"XOR","in":[33,34]},
36
                {"id":36,"type":"XOR","in":[32,35]},
37
                "id":37,"type":"AND","in":[32,35]},
38
                "id":38,"type":"AND","in":[33,34]},
39
                {"id":39,"type":"OR","in":[37,38]},
40
41
                {"id":42,"type":"XOR","in":[40,41]},
42
                "id":43,"type":"XOR","in":[39,42]},
43
                \{ 	t "id" : 44, 	t ype" : 	t AND", 	t in" : [39,42] \},
44
                {"id":45,"type":"AND","in":[40,41]},
45
                {"id":46,"type":"OR","in":[44,45]},
46
47
                {"id":49,"type":"XOR","in":[47,48]},
48
                "id":50,"type":"XOR","in":[46,49]},
49
                "id":51,"type":"AND","in":[46,49]},
50
                "id":52, "type": "AND", "in": [47,48]},
51
                {"id":53,"type":"OR","in":[51,52]},
52
53
                {"id":54,"type":"AND","in":[47,48]},
54
                "id":55,"type":"NOT","in":[47]},
55
                "id":56,"type":"NOT","in":[48]},
56
                 "id":57,"type":"AND","in":[55,56]},
57
```

We then created class Alice, class Bob in main.py to represent their behavior (illustrated below). It was decided that both parties have command line user interaction with the user, so we developed askForInput in requirements.py. In the same file, we can also find two functions, saveSet, readSet used to write the input values to two external files sets/alice.txt and sets/bob.txt; this will be useful when we want to check the correctness of the computed result using verifyOperation.

Since we are dealing with negative numbers, we decided to create two functions, intToBin and binToInt to convert numbers. Since the communication is encrypted, we decided to use AES-CBC as a technique; we can see that in the file yao.py, more precisely in the two functions encrypt, decrypt. As written in the code, we opted to prepend the IV to the ciphertext to avoid reusing the same IV for all the communications.

We can represent the pseudocode that represents the behavior (of the two parties) listed before.

## Algorithm 1 Alice's behaviour

```
1: send(circuit)

2: aliceSet \leftarrow askForInput()

3: saveSet(aliceSet)

4: aliceSet \leftarrow intToBin(aliceSet)

5:

6: aliceValue \leftarrow sum(aliceSet)

7: aliceE \leftarrow encrypt(aliceValue)

8:

9: r \leftarrow OT.getResult(aliceE, bKeys)

10:

11: result \leftarrow binToInt(r)

12: msg \leftarrow verifyOperation(result)

13: sendToBob(msg)

14: printResult(result, msg)
```

## Algorithm 2 Bob's behaviour

```
1: receive(circuit)

2: bobSet \leftarrow askForInput()

3: saveSet(bobSet)

4: bobSet \leftarrow intToBin(bobSet)

5:

6: bobValue \leftarrow sum(bobSet)

7:

8: OT.sendResult(bobValue)

9:

10: msg \leftarrow receive()

11: printResult(msg)
```

# 4 Usage

We will briefly explain how to install the program and how it works. In my repo, there is also a graphical visualization of the executing program.

### 4.1 Installation

To run the program, you need some packages:

- ZeroMQ used in util.py to implement communication;
- SymPy to use prime numbers;
- AES from encryption;
- Bits from bitstring, to do conversions from 2-complement to integers.

Simply run: \$ pip3 install bitstring pyzmq sympy cryptography You can also find specific versions that I used in the file requirements.txt.

#### 4.2 Execution

As already written, there are two parties: Alice and Bob. You must run on two different terminals. For simplicity, we assume that we are positioned inside /src/. From Alice's Terminal, simply run make alice, while for Bob's Terminal run make bob. Note that in the Makefile I use python3 compiler.

Now the connection will be established and the program will ask the user to give the input set, for each party. Once done, the result will be computed and printed on each terminal.

### **4.2.1** Example

A practical example will follow, we will show the output of each terminal.

#### Alice' side:

```
$ make alice
python3 code/main.py alice    -c circuits/add.json
Enter the list of integers of Alice's set: 1 2 -5
[1, 1, 1, 1, 1, 1, 1, 1]

===== 8 bit adder ======

Values of the computation

Syntax: parties/result: [list of bits] = [correspective values]

Alice: [8, 7, 6, 5, 4, 3, 2, 1] = 1 1 1 1 1 1 1 0
Computed result by circuit: [53, 51, 46, 41, 36, 31, 26, 21, 17] = 1 1 1 1 1 1 1 0 0 0
The sum has been done correctly, result is -8.
```

### Bob's side:

```
$ make bob python3 code/main.py bob Enter the list of integers of Bob's set: 4\ 6\ -16 Received 8 bit adder [1,\ 1,\ 1,\ 1,\ 1,\ 0,\ 1,\ 0] Syntax: parties/result [list of bits] = [correspective values] Bob [16,\ 15,\ 14,\ 13,\ 12,\ 11,\ 10,\ 9] = 1\ 1\ 1\ 1\ 1\ 0\ 1\ 0 The sum has been done correctly, result is -8.
```

Interpretation: As already written in the output, the syntax is
parties/result: [list of bits] = [correlated values].

The numbers on the left represent the bits in the circuit add.json, while the right ones represent the respective values. The last line is the output of the function verifyOperation.

## References

- [1] Moni Naor and Benny Pinkas. Computationally secure oblivious transfer. *Journal of Cryptology*, 18, 2005.
- [2] Wikipedia contributors. Secure multi-party computation Wikipedia, the free encyclopedia, 2023. [Online; accessed 10-May-2023].
- [3] Andrew C. Yao. Protocols for secure computations. In 23rd Annual Symposium on Foundations of Computer Science (sfcs 1982), pages 160–164, 1982.