Project documentation

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May 11, 2023

1 Introduction

The aim of this project is the study of Yao's protocol [3] and an useful application of it. More precisely, we will implement Secure multi-party computation; this field has the goal of creating methods for parties to jointly compute a function over their inputs while keeping those inputs private [2]. In this project, the function we decided to implement is the 8 bit sum.

2 Analysis

We can focus on the sum computed by two parties, say Alice and Bob. The goal is to use MPC to calculate the result while avoiding each member to know the others values; to do that we need an external component, called OT.

This protocol allows two parties, Alice who knows x and Bob who knows y, to compute jointly the value of f(x, y) in a way that does not reveal to each side more information than can be deduced from f(x, y) [1]. As already written, f is the 8-bit sum.

Both Alice and Bob have a set of integers and need to compute the sum of everything. Two new roles are introduced: Alice is the *garbler* and has the responsibility of creating the garbled circuit, while Bob is the *evaluator*. They will behave as follows:

- 1. Alice creates the garbled circuit and the tables and send them to Bob.
- 2. Alice select her set, via input.
- 3. Bob select his set, via input.
- 4. Both interact with each other using OT.
- 5. Bob evaluate the function result and sends it to Alice.
- 6. Alice checks the correctness of the result, and sends it to Bob (in clear).

3 Implementation

We will present how to implement the *circuit* and how to make Alice and Bob comunicate securely.

3.1 Circuit

1

We will present briefly the 8-bit sum circuit. There are two basic components in this construction:

- Half Adder: used to sum the right-most digit;
- Full adder: used to sum a generic digit in the number, ranging from position 1 to 8. It receives in input also carry of the previous sum.

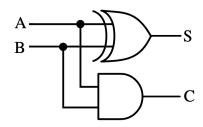


Figure 1: Half Adder

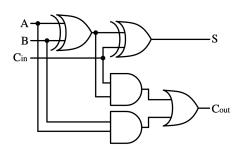


Figure 2: Full Adder

We then proceede creating the circuit by wiring 7 full adders and an half adder together, as represented in Figure 3.

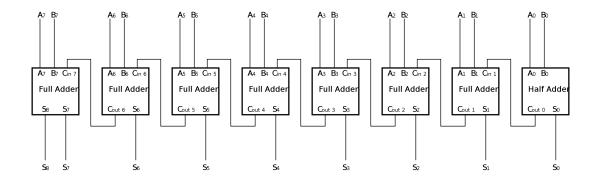


Figure 3: 8-bit Adder

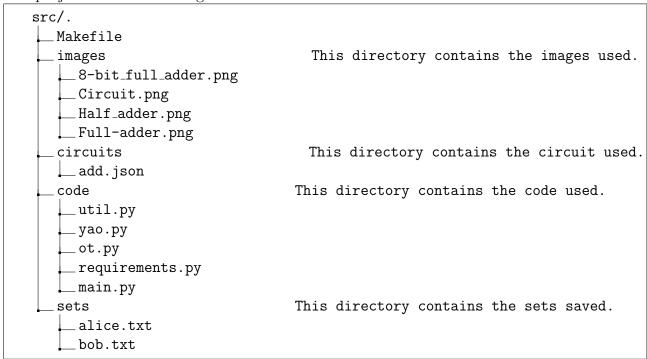
 $^{^{1}1~\}rm was~taken~over~https://upload.wikimedia.org/wikipedia/commons/1/14/Half-adder.svg <math display="inline">2~\rm was~taken~over~https://upload.wikimedia.org/wikipedia/commons/a/a9/Full-adder.svg.$

3.1.1 Project structure

The project will be developed using *Python 3.9.10* and we will use functions provided in the GitHub repo https://github.com/ojroques/garbled-circuit.

There is also a dedicated GitHub page related to this project at https://github.com/lorenzozanolin/garbledCircuit.

The project has the following structure:



The code folder contains all the file that we will utilize for the secure communication. ot.py, util.py, yao.py are utilities taken from Ojroques repo.

3.1.2 Coding

First thing first, we need to represent the circuit; we decided to create the add.json file to code the circuit. Each wire is mapped to a number and linked with the other following the structure represented in Figure 3.

We then created class Alice, class Bob in main.py to represent their behaviour. It was decided that both parties have command line user interaction with the user, so we developed askForInput in requirements.py. In the same file we can also find two functions saveSet, readSet used to write in two external files sets/alice.txt and sets/bob.txt the input values; this will be useful when we want to check the correctness of the computed result, using verifyOperation.

Since the communication is encrypted, we decided to use AES-CBC as technique; we can see that in the file yao.py, more precisely in the two functions encrypt, decrypt. As written in the code, we opted to prepend the IV at the cyphertext to avoid reusing

the same IV for all the communications.

We can represent the pseudocode that represents the behaviour listed before.

Algorithm 1 Alice's behaviour	Algorithm 2 Bob's behaviour
1: dataProcessing (dataset)	1: dataProcessing (dataset)
2: $unitToDrop \leftarrow 25\%$	2: $unitToDrop \leftarrow 25\%$
3: text	3: text
4: text	4: text
5: repeat	5: repeat
6: /*text*/	6: /*text*/
7: for $i \leftarrow 1, rows$ do	7: for $i \leftarrow 1, rows$ do
8: text	8: text
9: text	9: text
10: text	10: text
11: text	11: text
12: text	12: text
13: end for	13: end for
14: until text	14: until text
15: text	15: text
16: repeat	16: repeat
17: text	17: text
18: for $i \leftarrow 1, rows$ do	18: for $i \leftarrow 1, rows$ do
19: text	19: text
20: V	20: v
21: end for	21: end for
22: until text	22: until text
23: Return text, text	23: Return text, text

4 Usage

4.1 Installation

4.2 Communication

4.2.1 Example

References

[1] Moni Naor and Benny Pinkas. Computationally secure oblivious transfer. *Journal of Cryptology*, 18, 2005.

- [2] Wikipedia contributors. Secure multi-party computation Wikipedia, the free encyclopedia, 2023. [Online; accessed 10-May-2023].
- [3] Andrew C. Yao. Protocols for secure computations. In 23rd Annual Symposium on Foundations of Computer Science (sfcs 1982), pages 160–164, 1982.