Project documentation

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1 Introduction

The aim of this project is the study of Yao's protocol [3] and an useful application of it. More precisely, we will implement Secure multi-party computation; this field has the goal of creating methods for parties to jointly compute a function over their inputs while keeping those inputs private [2]. In this project, the function we decided to implement is the 8 bit sum.

2 Analysis

We can focus on the sum computed by two parties, say Alice and Bob. The goal is to use MPC to calculate the result while avoiding each member to know the others values; to do that we need an external component, called OT.

This protocol allows two parties, Alice who knows x and Bob who knows y, to compute jointly the value of f(x, y) in a way that does not reveal to each side more information than can be deduced from f(x, y) [1]. As already written, f is the 8-bit sum.

Both Alice and Bob have a set of integers and need to compute the sum of everything. Two new roles are introduced: Alice is the *garbler* and has the responsibility of creating the garbled circuit, while Bob is the *evaluator*. They will behave as follows:

- 1. Alice creates the garbled circuit and the tables and send them to Bob.
- 2. Alice select her set, via input.
- 3. Bob select his set, via input.
- 4. Both interact with each other using OT.
- 5. Bob evaluate the function result and sends it to Alice.
- 6. Alice checks the correctness of the result, and sends it to Bob (in clear).

3 Implementation

We will present how to implement the *circuit* and how to make Alice and Bob comunicate securely.

3.1 Circuit

We will present briefly the 8-bit sum circuit. There are three basic components in this construction:

- Half Adder: used to sum the right-most digit;
- Full adder: used to sum a generic digit in the number, ranging from position 1 to 8. It receives in input also carry of the previous sum.
- If then else: there could be situations, called overflow, in which you sum two number with the same sign and obtain a number with opposite sign; to avoid this scenario, this construct is employed by examining the signs of the two numbers and the sign of the calculated result. If the two input numbers have the same sign, the output sign is set to be the same as the inputs. Instead, if the two input numbers have different signs, the sign of the result is determined accordingly to the previous circuit.



Figure 1: Half Adder

Figure 2: Full Adder

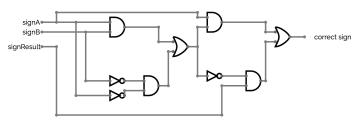


Figure 3: If then else

1

We then proceede creating the circuit by wiring 7 full adders, an half adder and the if-then-else together, as represented in Figure 4.

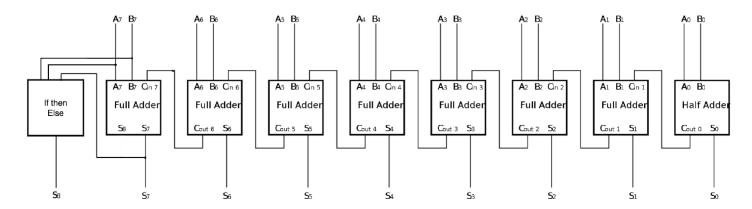


Figure 4: 8-bit Adder

Since we are using 8 bit to represent the sum of each set, it immediatly follows that the sum of each set must be smaller than 256. In this case we are dealing with *integers*, thus we also need to consider negative numbers; to do that we are using 2-complement. In this case we are considering numbers that belong to [-128,127]. The final sum has 9 bit representation, thus the result that we can obtain belongs to [-256,254].

3.1.1 Project structure

The project will be developed using *Python 3.9.10* and we will use functions provided in the GitHub repo https://github.com/ojroques/garbled-circuit.

There is also a dedicated GitHub page related to this project at https://github.com/lorenzozanolin/garbledCircuit.

The project has the following structure:

The code folder contains all the file that we will utilize for the secure communication. ot.py, util.py, yao.py are utilities taken from Ojroques repo.

The images folder contains all images used in the report and documentation.

The circuits folder contains the used circuit, in this case only add. json

The sets folder contains the two files used to store sets of Alice and Bob.

¹1 was taken over https://upload.wikimedia.org/wikipedia/commons/1/14/Half-adder.svg 2 was taken over https://upload.wikimedia.org/wikipedia/commons/a/a9/Full-adder.svg.

```
src/.
  _Makefile
                                      This directory contains the images used.
   images
   <u>∟</u> . . .
   circuits
                                      This directory contains the circuit used.
    __add.json
                                    This directory contains the code used.
   code
     _util.py
     _yao.py
     _ot.py
     \_ requirements.py
     _{\mathtt{main.py}}
                                    This directory contains the sets saved.
   sets
     _alice.txt
     _bob.txt
```

3.1.2 Coding part

First thing first, we need to represent the *circuit*; we decided to create the add.json file to code the circuit. Each wire is mapped to a number and linked with the other following the structure represented in Figure 4.

Each gate that appears in figure 4 is represented in a single JSON line.

The syntax is:

```
"id" : <gateId>, "type" : "<TYPE>", "in": [<gateIdInput1>, <gateIdInput2>]
```

In this case the circuit is represented as follows:

```
\{"name":"adder",
1
        "circuits":[
2
3
           "id": "8 bit adder",
4
           "alice": [47,40,33,26,19,12,5,1],
5
           "bob": [48,41,34,27,20,13,6,2],
6
           "out": [62,50,43,36,29,22,15,8,3],
7
           "gates":[
8
                {"id":3,"type":"XOR","in":[1,2]},
9
                {"id":4,"type":"AND","in":[1,2]},
10
11
                {"id":7,"type":"XOR","in":[5,6]},
12
                 "id":8,"type":"XOR","in":[4,7]},
13
                 "id":9,"type":"AND","in":[4,7]},
14
```

```
{"id":10,"type":"AND","in":[5,6]},
15
                {"id":11,"type":"OR","in":[9,10]},
16
17
                {"id":14,"type":"XOR","in":[12,13]},
18
                "id":15,"type":"XOR","in":[11,14]},
19
                "id":16,"type":"AND","in":[11,14]},
20
                {"id":17,"type":"AND","in":[12,13]},
21
                {"id":18,"type":"OR","in":[16,17]},
22
23
                {"id":21,"type":"XOR","in":[19,20]},
24
                "id":22, "type": "XOR", "in": [18,21]},
25
                "id":23,"type":"AND","in":[18,21]},
26
                {"id":24,"type":"AND","in":[19,20]},
27
                {"id":25,"type":"OR","in":[23,24]},
28
29
                {"id":28,"type":"XOR","in":[26,27]},
30
                {"id":29,"type":"XOR","in":[25,28]},
31
                "id":30,"type":"AND","in":[25,28]},
32
                {"id":31,"type":"AND","in":[26,27]},
33
                {"id":32,"type":"OR","in":[30,31]},
34
35
                {"id":35,"type":"XOR","in":[33,34]},
36
                {"id":36,"type":"XOR","in":[32,35]},
37
                "id":37,"type":"AND","in":[32,35]},
38
                "id":38,"type":"AND","in":[33,34]},
39
                {"id":39,"type":"OR","in":[37,38]},
40
41
                {"id":42,"type":"XOR","in":[40,41]},
42
                "id":43,"type":"XOR","in":[39,42]},
43
                \{ 	t "id" : 44, 	t ype" : 	t AND", 	t in" : [39,42] \},
44
                {"id":45,"type":"AND","in":[40,41]},
45
                {"id":46,"type":"OR","in":[44,45]},
46
47
                {"id":49,"type":"XOR","in":[47,48]},
48
                "id":50,"type":"XOR","in":[46,49]},
49
                "id":51,"type":"AND","in":[46,49]},
50
                "id":52, "type": "AND", "in": [47,48]},
51
                {"id":53,"type":"OR","in":[51,52]},
52
53
                {"id":54,"type":"AND","in":[47,48]},
54
                "id":55,"type":"NOT","in":[47]},
55
                "id":56,"type":"NOT","in":[48]},
56
                 "id":57,"type":"AND","in":[55,56]},
57
```

We then created class Alice, class Bob in main.py to represent their behaviour (illustrated below). It was decided that both parties have command line user interaction with the user, so we developed askForInput in requirements.py. In the same file we can also find two functions saveSet, readSet used to write in two external files sets/alice.txt and sets/bob.txt the input values; this will be useful when we want to check the correctness of the computed result, using verifyOperation.

Since we are dealing with negative numbers, we decided to create two functions, intToBin and binToInt to convert numbers. Since the communication is encrypted, we decided to use AES-CBC as technique; we can see that in the file yao.py, more precisely in the two functions encrypt, decrypt. As written in the code, we opted to prepend the IV at the cyphertext to avoid reusing the same IV for all the communications.

We can represent the pseudocode that represents the behaviour (of the two parties) listed before.

Algorithm 1 Alice's behaviour

```
1: send(circuit)

2: aliceSet \leftarrow askForInput()

3: saveSet(aliceSet)

4: aliceSet \leftarrow intToBin(aliceSet)

5:

6: aliceValue \leftarrow sum(aliceSet)

7: aliceE \leftarrow encrypt(aliceValue)

8:

9: r \leftarrow OT.getResult(aliceE,bKeys)

10:

11: result \leftarrow binToInt(r)

12: msg \leftarrow verifyOperation(result)

13: sendToBob(msg)

14: printResult(result, msg)
```

Algorithm 2 Bob's behaviour

```
1: receive(circuit)

2: bobSet \leftarrow askForInput()

3: saveSet(bobSet)

4: bobSet \leftarrow intToBin(bobSet)

5:

6: bobValue \leftarrow sum(bobSet)

7:

8: OT.sendResult(bobValue)

9:

10: msg \leftarrow receive()

11: printResult(msg)
```

4 Usage

We will briefly explain how to install the program and how it works. In my repo there is also a graphical visualization of the executing program.

4.1 Installation

To run the program you need some packages:

- ZeroMQ used in util.py to implement communication;
- SymPy to use prime numbers;
- AES from encryption;
- Bits from bitstring, to do conversions from 2-complement to integers.

Simply run: \$ pip3 install bitstring pyzmq sympy cryptography bitstring You can also find specific versions that I used in the file requirements.txt.

4.2 Execution

As already writte, there are two parties: Alice and Bob. You must run on two different terminals them. From now, for simplicity, we assume that we are positioned inside /src/. From Alice's Terminal, simply run make alice, while for Bob's Terminal run run make bob. Note that in the Makefile I use python3 compiler.

Now the connection will be established and the program will ask the user to give the input set, for each party. Once done, the result will be computed and printed in each terminal.

4.2.1 Example

A practical example will follow, we will show the output of each terminal.

Alice' side:

Bob's side:

```
$ make bob python3 code/main.py bob Enter the list of integers of Bob's set: 4\ 6\ -16 Received 8 bit adder [1,\ 1,\ 1,\ 1,\ 1,\ 0,\ 1,\ 0] Syntax: parties/result [list of bits] = [correspective values] Bob [16,\ 15,\ 14,\ 13,\ 12,\ 11,\ 10,\ 9] = 1\ 1\ 1\ 1\ 1\ 0\ 1\ 0 The sum has been done correctly, result is -8.
```

Interpretation: As already written in the output, the syntax is
parties/result: [list of bits] = [correspective values].

The numbers on the left represent the bits in the circuit add.json, while the right ones represent the corrispective values. The last line is the output of the function verifyOperation.

References

- [1] Moni Naor and Benny Pinkas. Computationally secure oblivious transfer. *Journal of Cryptology*, 18, 2005.
- [2] Wikipedia contributors. Secure multi-party computation Wikipedia, the free encyclopedia, 2023. [Online; accessed 10-May-2023].
- [3] Andrew C. Yao. Protocols for secure computations. In 23rd Annual Symposium on Foundations of Computer Science (sfcs 1982), pages 160–164, 1982.