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— Module MCSequential -
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EXTENDS Sequential, Sequences, Naturals, TLC

Variables h

CONSTANTS Hmax

$$TypeOk \triangleq \land op \in \{\text{"r"}, \text{"w"}\} \\ \land arg \in Obj \cup Obj \times Val \\ \land rval \in Val \cup \{Ok\} \cup \text{SUBSET } Obj \\ \land env \in [Obj \rightarrow Val] \\ \land ff \in \{Flip, Flop\}$$

$$TypeOkH \triangleq \land TypeOk \land h \in Seq([op : \{ \text{"r"}, \text{"w"} \}, obj : Obj, val : Val])$$

$$\begin{array}{ccc} \mathit{InitH} & \stackrel{\triangle}{=} & \land \mathit{Init} \\ & \land h = \langle \rangle \end{array}$$

$$\begin{array}{ccc} ReadH(obj, \, val) & \triangleq & \land \, Read(obj, \, val) \\ & & \land \, h' = Append(h, \, [op \mapsto \text{``r''}, \, obj \mapsto obj, \, val \mapsto val]) \end{array}$$

$$WriteH(obj, val) \triangleq \land Write(obj, val) \\ \land h' = Append(h, [op \mapsto \text{``w''}, obj \mapsto obj, val \mapsto val])$$

$$NextH \triangleq \forall \exists obj \in Obj, val \in Val : ReadH(obj, val) \lor WriteH(obj, val)$$

$$vh \stackrel{\triangle}{=} \langle op, arg, rval, env, ff, h \rangle$$

 $SpecH \stackrel{\triangle}{=} InitH \wedge \Box [NextH]_{vh}$

The set of writes to *obj*

$$Wr(obj) \triangleq \text{LET } evt \triangleq \{h[i] : i \in \text{DOMAIN } h\}$$

IN $\{e \in evt : e.op = \text{``w''} \land e.obj = obj\}$

Most recent value written to *obj*

$$\begin{array}{l} \mathit{MRW}(\mathit{obj}) \ \stackrel{\triangle}{=} \\ \text{LET } i \ \stackrel{\triangle}{=} \ \mathsf{CHOOSE} \ i \in \mathsf{DOMAIN} \ h : \\ & \land h[i].\mathit{op} = \text{``w''} \\ & \land h[i].\mathit{obj} = \mathit{obj} \\ & \land \neg \exists \ j \in \mathsf{DOMAIN} \ h : \land h[j].\mathit{op} = \text{``w''} \\ & \land h[j].\mathit{obj} = \mathit{obj} \\ & \land j > i \end{array}$$

IN h[i].val

If an object was previously written, the read should correspond to the most recent write

$$ReadLastWrite \stackrel{\triangle}{=} op = \text{``r''} \Rightarrow$$

$$LET \ obj \stackrel{\triangle}{=} arg$$

$$val \stackrel{\triangle}{=} rval$$

IN
$$Wr(obj) \neq \{\} \Rightarrow MRW(obj) = val$$

Successive reads without intervening writes should return the same value

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Successive reads without intervening writes should return the same value Successive Reads \triangleq \text{LET } obj \triangleq arg \\ val \triangleq rval \\ IsRd(k, o) \triangleq h[k].op = \text{"r"} \land h[k].obj = o \\ IsWr(k, o) \triangleq h[k].op = \text{"w"} \land h[k].obj = o \\ NoWrRd(i, o) \triangleq IsRd(i, o) \land \neg \exists j \in i+1 \dots Len(h)-1 : IsWr(j, o) \\ j \triangleq \text{CHOOSE } j \in 1 \dots Len(h)-1 : NoWrRd(j, obj) \\ \text{IN } (op = \text{"r"} \land \exists i \in 1 \dots Len(h)-1 : NoWrRd(i, obj)) \Rightarrow rval = h[j].val
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 $Symmetry \triangleq Permutations(Obj) \cup Permutations(Val)$

 $MaxHistory \triangleq Len(h) \leq Hmax$