Lecture 4 Biasing Enumerative Search

Plan for this week

Today:

Search space prioritization/biasing

Next lecture:

- Discuss the Euphony paper
- Synthesis frameworks + suggested projects

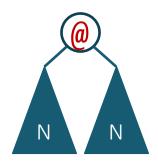
Project:

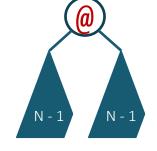
- Proposals due soon
- Talk to me about the topic

Scaling enumerative search

Prune

Discard useless subprograms





$$m * N^2$$

$$m * (N - 1)^2$$

Prioritize

Explore more promising candidates first

Order of search

Enumerative search explores programs by depth / size

- Good default bias: small solution is likely to generalize
- But far from perfect

Result:

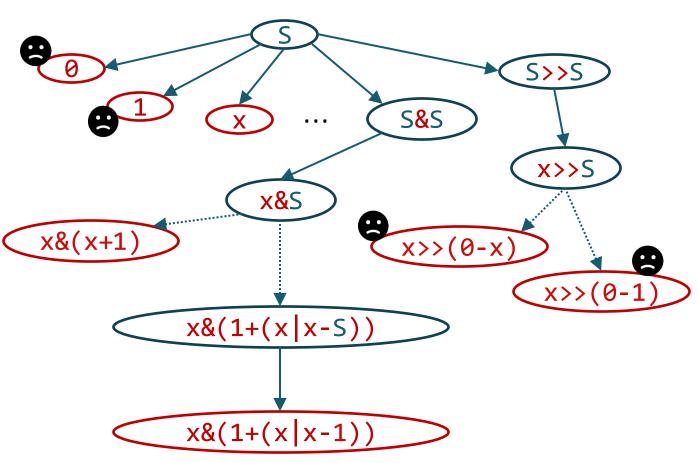
• Scales poorly with the size of the smallest solution to a given spec

Top-down search (revisited)

Turn off the rightmost sequence of **1**s:

```
00101 \rightarrow 00100
01010 \rightarrow 01000
10110 \rightarrow 10000
```

Explores many unlikely programs!



Biasing the search

Idea: explore programs in the order of likelihood, not size

Q1: how do we know which programs are likely?

- hard-code domain knowledge
- learn from a corpus of programs

Q2: how do we use this information to guide search?

our focus today!

Weighted enumerative search

DeepCoder

Balog et al. DeepCoder: Learning to Write Programs. ICLR'17

Weighted top-down search

Lee, et al: Accelerating Search-Based Program Synthesis using Learned Probabilistic Models. PLDI'18

Weighted bottom-up search

Barke, Peleg, Polikarpova. Just-in-Time Learning for Bottom-Up Enumerative Synthesis. OOPSLA'20

Shi, Bieber, Singh. TF-Coder: Program Synthesis for Tensor Manipulations. TOPLAS

DeepCoder

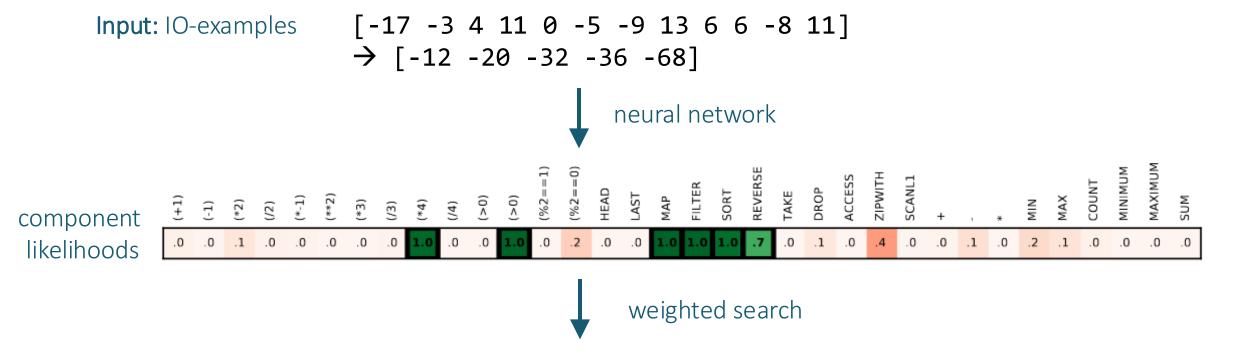
Input: IO-examples
$$[-17 -3 \ 4 \ 11 \ 0 \ -5 \ -9 \ 13 \ 6 \ 6 \ -8 \ 11]$$

$$\rightarrow [-12 \ -20 \ -32 \ -36 \ -68]$$



Output: Program in a list DSL

DeepCoder



Output: Program in a list DSL

DeepCoder: search strategies

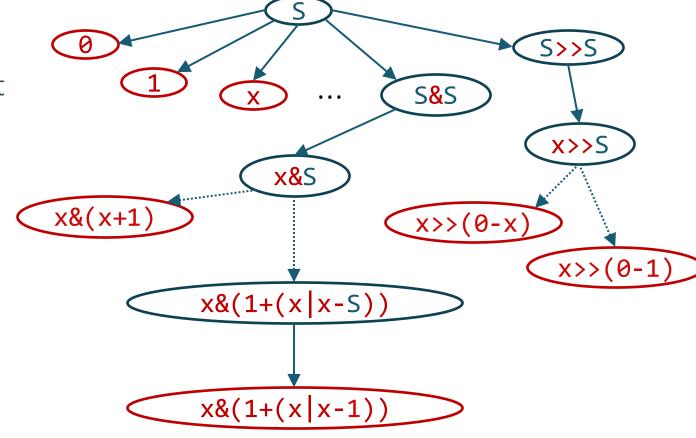
Top-down DFS

 Picks expansions for the current non-terminal in the order of probability

Sort-and-add

- start with N most probable functions
- when search fails, add next N functions

Pros and cons?



Recall: we want to explore programs in the order of likelihood!

Probabilistic Language Models

Originated in Natural Language Processing

In general: a probability distribution over sentences in a language

• P(s) for $s \in L$

In practice:

- must be in a form that can be used to guide search
- for enumerative search: grammar-based (PCFG, PHOG)

Probabilistic CFG (PCFG)

		$\wp(R)$
S ->	0	0.13
S ->	1	0.13
S ->	X	0.18
S ->	S + S	0.11
S ->	S - S	0.11
S ->	S & S	0.12
S ->	S S	0.12
S ->	S << S	0.05
S ->	S >> S	0.05

Encodes the popularity of each operation (terminal)

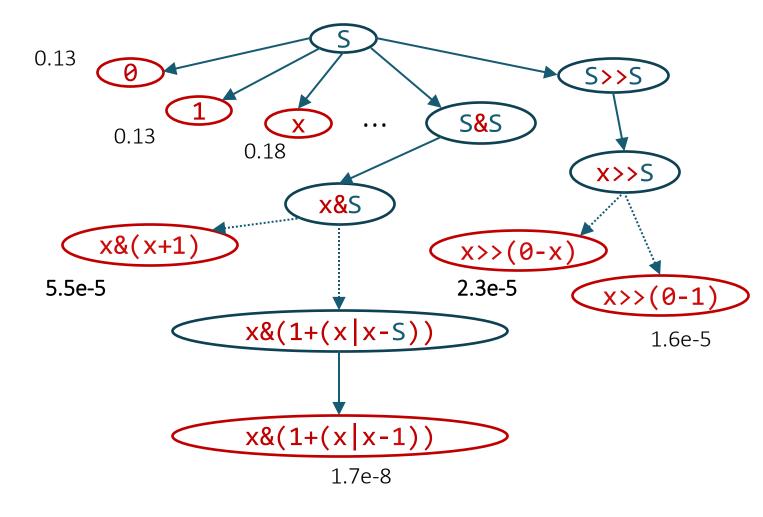
 here: variable more likely than constant, plus more likely than shift

More useful if specific to a spec

Probabilistic CFG (PCFG)

			$\wp(R)$
S	->	0	0.13
S	->	1	0.13
S	->	X	0.18
S	->	S + S	0.11
S	->	S - S	0.11
S	->	S & S	0.12
S	->	SS	0.12
S	->	S << S	0.05
S	->	S >> S	0.05

$$\wp(\mathbf{p}) = \prod_{R \in S \to^* \mathbf{p}} \wp(R)$$



Probabilistic Higher-Order Grammar (PHOG)

[Bielik, Raychev, Vechev '16]

```
N[context] -> rhs
```

```
S[x,-] -> 1 0.72

S[x,-] -> x 0.02

S[x,-] -> S + S 0.12

S[x,-] -> S - S 0.12

...

S[1,+] -> 1 0.26

S[1,+] -> x 0.25

S[1,+] -> S + S 0.19

S[1,+] -> S - S 0.08
```

Encodes context-specific likelihood

here: x is not likely in x - ?
but likely in 1 + ?

Probabilistic Higher-Order Grammar (PHOG)

[Bielik, Raychev, Vechev '16]

S>>S

x>>S

x >> (0-1)

9.8e-9

N[context] -> rhs		3e-5
	\wp	3e-2
$S[x,-] \rightarrow 1$	0.72	x&S
$S[x,-] \rightarrow x$	0.02	(x&(x+1)) $(x>>(0-1)$
$S[x,-] \rightarrow S + S$	0.12	0.25 9.8e-9
$S[x,-] \rightarrow S - S$	0.12	U.25 ÷ 9.8e-9
• • •		(x&(1+(x x-S)))
S[1,+] -> 1	0.26	
$S[1,+] \rightarrow X$	0.25	
$S[1,+] \rightarrow S + S$	0.19	(x&(1+(x x-1)))
$S[1,+] \rightarrow S - S$	0.08	2e-4
		2 C-4

Weighted enumerative search

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Weighted top-down search

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Shi, Bieber, Singh. TF-Coder: Program Synthesis for Tensor Manipulations. arXiv

Weighted top-down search

Wanted: explore programs in the order of likelihood

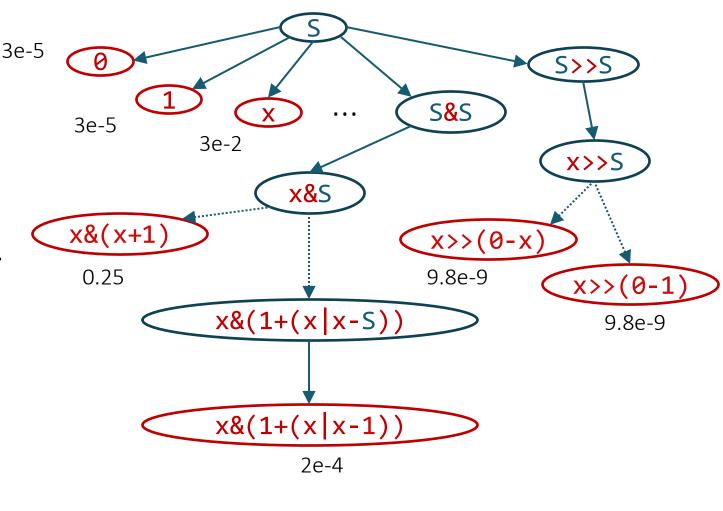
$$\mathscr{D}(\mathbf{p}) = \prod_{R \in S \to^* \mathbf{p}} \mathscr{D}(R)$$

Hard to maximize multiplicative cost... but easy to minimize additive cost!

= shortest path

$$cost(p) = \sum_{R \in S \to *p} cost(R)$$

$$-\log_2 \wp(p) = \sum_{R \in S \to p} -\log_2 \wp(R)$$



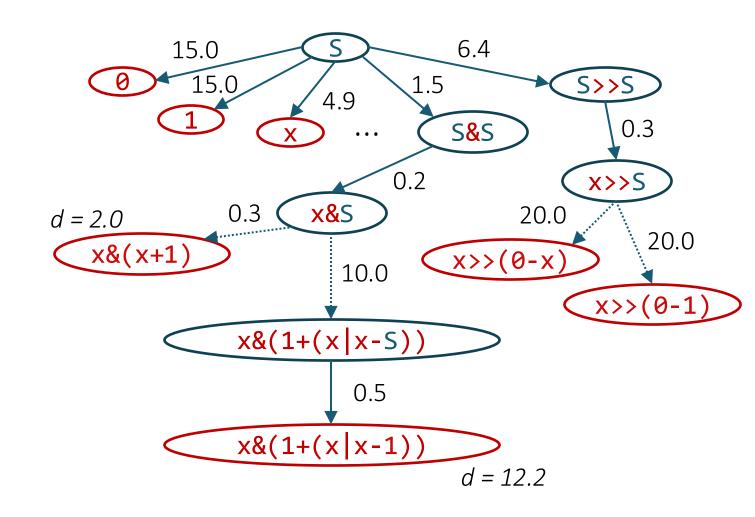
Weighted top-down search

Assigns costs to edges:

$$cost(R) = -\log_2 \wp(R)$$

Now cost(p) < cost(p')iff p is more likely than p'!

We can use shortest path algo (e.g. Dijkstra) to search by cost!



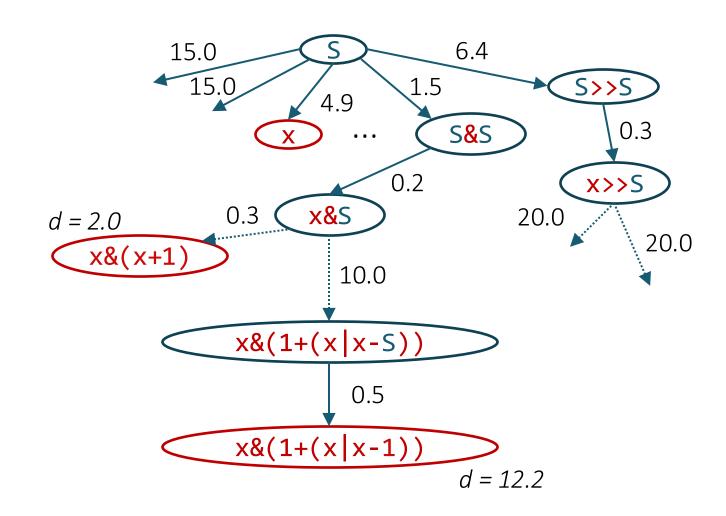
Weighted top-down search (Dijkstra)

```
top-down(\langle \Sigma, N, R, S \rangle, [i \rightarrow o]) {
                                               w1 now stores candidates (nodes)
  wl := [<5,0>] ←
                                              together with their costs
  while (wl != [])
    <p,c> := wl.dequeue_min(c);
                                               Dequeue the node with minimal cost
    if (ground(p) \& p([i]) = [o])
       return p;
    wl.enqueue(unroll(p,c));
unroll(p,c) {
  wl' := []
                                                Distance to a new node: add the w(R)
  A := left-most nonterminal in p
  forall (A \rightarrow rhs) in R:
    wl' += \langle p[A -> rhs], c + w(A \rightarrow rhs) \rangle
  return wl';
```

Can we do better?

Dijkstra: explores a lot of intermediate nodes that don't lead to any cheap leaves

A*: introduce heuristic function h(p) that estimates how close we are to the closest leaf



Weighted top-down search (A*)

```
top-down(\langle \Sigma, N, R, S \rangle, [i \rightarrow o]) {
  w1 := [\langle S, 0, h(S) \rangle]
  while (wl != [])
     <p,c,h> := wl.dequeue_min(c + h);
     if (ground(p) \& p([i]) = [o])
       return p;
     wl.enqueue(unroll(p,c));
unroll(p,c) {
  wl' := []
  A := leftmost nonterminal in p
  forall (A \rightarrow rhs) in R:
    wl' += \langle p[A \rightarrow rhs], c + w(A \rightarrow rhs),
                               h(p[A -> rhs])>
  return wl';
```

Roughly how close is this program to the closest leaf

Weighted enumerative search

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Bottom-up search (revisited)

```
bottom-up (\langle \Sigma, N, R, S \rangle, [i \rightarrow o]):
  bank[A,d] := \{\} forall A, d
  for d in [0..]:
     forall (A \rightarrow rhs) in R:
        forall p in new-terms(A \rightarrowrhs, d, bank):
                                                                           Search by depth
           if (A = S \land p([i]) = [o]):
              return p
           bank[A,d] += p;
new-terms(A \rightarrow \sigma(A_1...A_n), d, bank):
 if (d = 0 \land n = 0) yield \sigma
 else forall \{d_1,...,d_n\} in [0...d-1]^n s.t. \max(d_1,...,d_n) = d-1:
         forall \langle p_1, ..., p_n \rangle in bank [A_1, d_1] \times ... \times bank [A_n, d_n]:
            yield \sigma(p_1,...,p_n)
```

Bottom-up variations

```
new-terms(A \rightarrow \sigma(A_1...A_n), d, bank):
 if (d = 0 \land n = 0) yield \sigma
 else forall \{d_1,...,d_n\} in [0...d-1]^n s.t. \max(d_1,...,d_n) = d-1:
                                                                                                             by depth
          forall \langle p_1, ..., p_n \rangle in bank [A_1, d_1] \times ... \times bank [A_n, d_n]:
             yield \sigma(p_1,...,p_n)
new-terms(A \rightarrow \sigma(A_1...A_n), s, bank):
 if (s = 1 \land n = 0) yield \sigma
 else forall (s_1,...,s_n) in [0...s-1]^n s.t. sum(s_1,...,s_n) = s-1:
                                                                                                              by size
          forall \langle p_1, ..., p_n \rangle in bank [A_1, s_1] \times ... \times bank [A_n, s_n]:
             yield \sigma(p_1,...,p_n)
new-terms(A \rightarrow \sigma(A_1...A_n), c, bank):
 budget = c - w(A \rightarrow \sigma(A_1...A_n))
 if (budget = 0 \land n = 0) yield \sigma
                                                                                                             by cost!
 else forall \langle c_1,...,c_n \rangle in [0... budget]<sup>n</sup> s.t. sum(c_1,...,c_n) = budget:
          forall \langle p_1, ..., p_n \rangle in bank [A_1, c_1] \times ... \times bank [A_n, c_n]:
             yield \sigma(p_1,...,p_n)
```

Bottom-up by cost: discussion

What kind of cost functions are supported?

- positive
- integer
- compositional: $cost(\sigma(p_1,...,p_n)) = C + cost(p_1) + ... + cost(p_n)$

Bottom-up: example

by depth d= 0: x sort(x) d = 1: X + Xd = 2: sort(sort(x)) sort(x + x)x + sort(x)sort(x) + xx + (x + x)(x + x) + xd = 3: ...

by size s= 1: **x** s = 2: sort(x) s = 3: x + xsort(sort(x)) s = 4: sort(x + x)sort(sort(x))) x + sort(x)sort(x) + x

s = 5: ...

cost 10 L ::= sort(L) L + LX by cost c= 1: **x** c = 2, 3, 4: c = 5: x + xc = 6,7,8: c = 9: x + (x + x)(x + x) + xc = 10: c = 11: sort(x)c = 12: c = 13: x + (x + (x + x))(x + x) + (x + x)

(x + (x + x)) + x

Weighted search

[Barke, Peleg, Polikarpova. OOPSLA'20]

Q: can we guide bottom-up search by a PCFG? by a PHOG?

Weighted search

Top-down

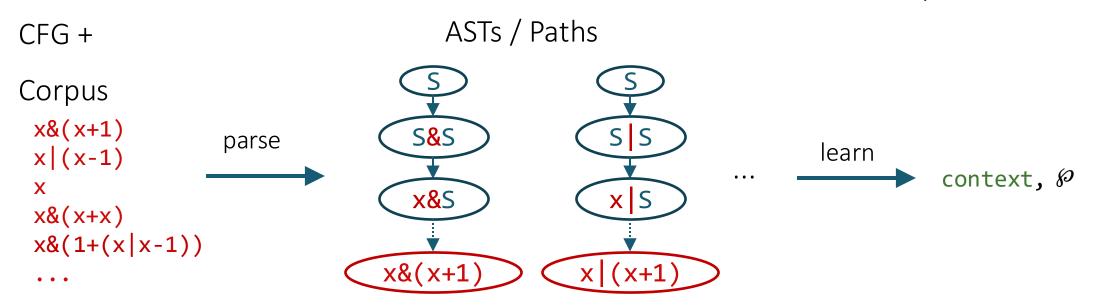
- + Supports real-valued weights: optimal enumeration order
- + Supports context-dependent weights

Bottom-up

+ Inherits benefits of bottom up: fast, supports OE

Learning PHOGs

[Bielik, Raychev, Vechev '16]



Q1: What does Euphony use as behavioral constraints? Structural constraint? Search strategy?

- IO Examples (or first-order formula via CEGIS)
- PHOG
- Weighted enumerative search via A*

Q2: What would these productions look like if we replaced the PHOG with a PCFG? With 3-grams?

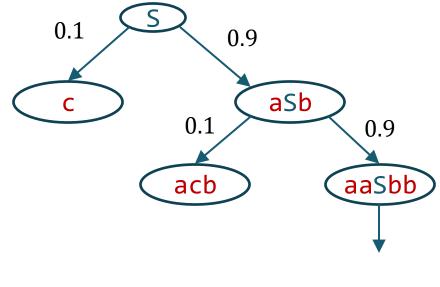
```
PHOG:

S["-",Rep] -> "." 0.72 S -> "." 0.2 S[x,"-"] -> "." 0.72 S["-",Rep] -> "-" 0.001 S -> "-" 0.2 S[x,"-"] -> "-" 0.001 S["-",Rep] -> x 0.12 S -> x 0.3 S[x,"-"] -> x 0.12 S["-",Rep] -> S + S 0.02 S -> S + S 0.2 S[x,"-"] -> S + S 0.02 ... ... ...
```

Do you think these other probabilistic models would work as well as a PHOG?

Q3: What does h(S) = 0.1 mean? Why is it the case?

```
S -> a S b 0.9
S -> c 0.1
```



. . .

Q4: Give an example of sentential forms n_i , n_j and set of points pts such that n_i and n_j are equivalent on pts but not weakly equivalent

```
pts = []

n1 = x + "-" n2 = "-" + x

pts = ["-", "--"]
```

n1 = Rep(x,x,S) n2 = S

$$n1 = Rep(S+x,".","-") n2 = Rep(S,".","-") + Rep(x,".","-")$$

Euphony: strengths

Efficient way to guide search by a probabilistic grammar

- Much better than DeepCoder's sort-and-add
- First to use A* and propose a sound heuristic

Transfer learning for PHOGs

Abstraction is key to learning models of code!

Extend observational equivalence to top-down search

Euphony: weaknesses

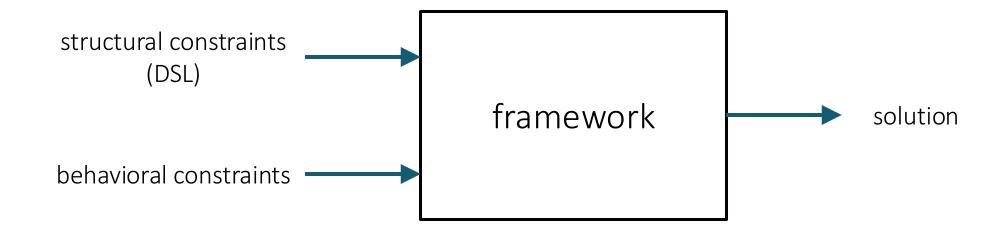
Requires high-quality training data

for each problem domain!

Transfer learning requires manually designed features

Synthesis frameworks

synthesis framework = a highly-configurable synthesizer



Synthesis frameworks

Sketch (https://people.csail.mit.edu/asolar/)

Rosette (https://emina.github.io/rosette/)

• see also: https://www.cs.utexas.edu/~bornholt/post/building-synthesizer.html

PROSE (https://www.microsoft.com/en-us/research/project/prose-framework/)

SemGuS (https://www.semgus.org/)

Sketch

Problem: isolate the least significant zero bit in a word

• example: 0010 0101 → 0000 0010

Easy to implement with a loop

Can this be done more efficiently with bit manipulation?

- Trick: adding 1 to a string of ones turns the next zero to a 1
- i.e. 000111 + 1 = 001000

Sketch: space of possible implementations

```
/**
 * Generate the set of all bit-vector expressions
 * involving +, &, xor and bitwise negation (~).
*/
generator bit[W] gen(bit[W] x){
    if(??) return x;
    if(??) return ??;
    if(??) return ~gen(x);
    if(??){
        return {| gen(x) (+ | & | ^) gen(x) |};
```

Sketch: synthesis goal

```
generator bit[W] gen(bit[W] x, int depth){
    assert depth > 0;
    if(??) return x;
    if(??) return ??;
    if(??) return ~gen(x, depth-1);
    if(??){
        return {| gen(x, depth-1) (+ | & | ^) gen(x, depth-1) |};
bit[W] isolate0fast (bit[W] x) implements isolate0 {
     return gen(x, 3);
```

Sketch: output

```
bit[W] isolate0fast (bit[W] x) {
  return (~x) & (x + 1);
}
```

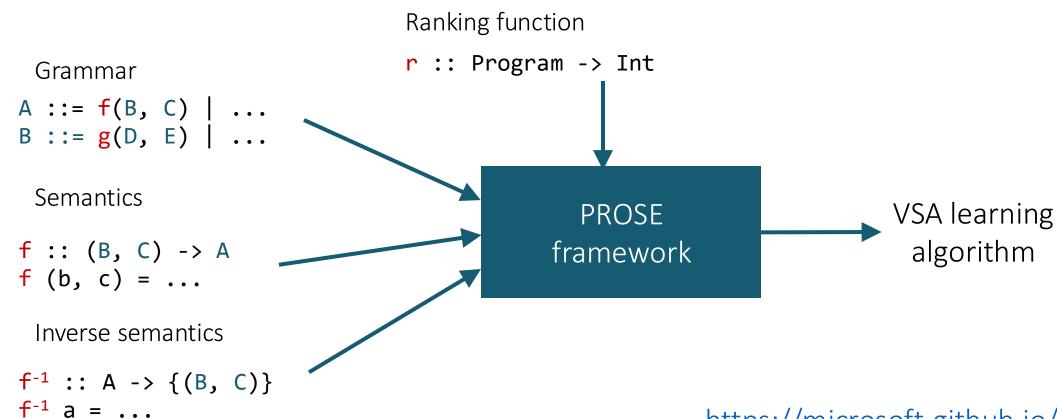
Rosette

A solver-aided language on top of Racket

- Racket's metaprogramming + symbolic variables + solver queries
- Can define full-fledged SDSLs (Solver-aided DSLs)

Let's see how to solver the same problem in Rosette

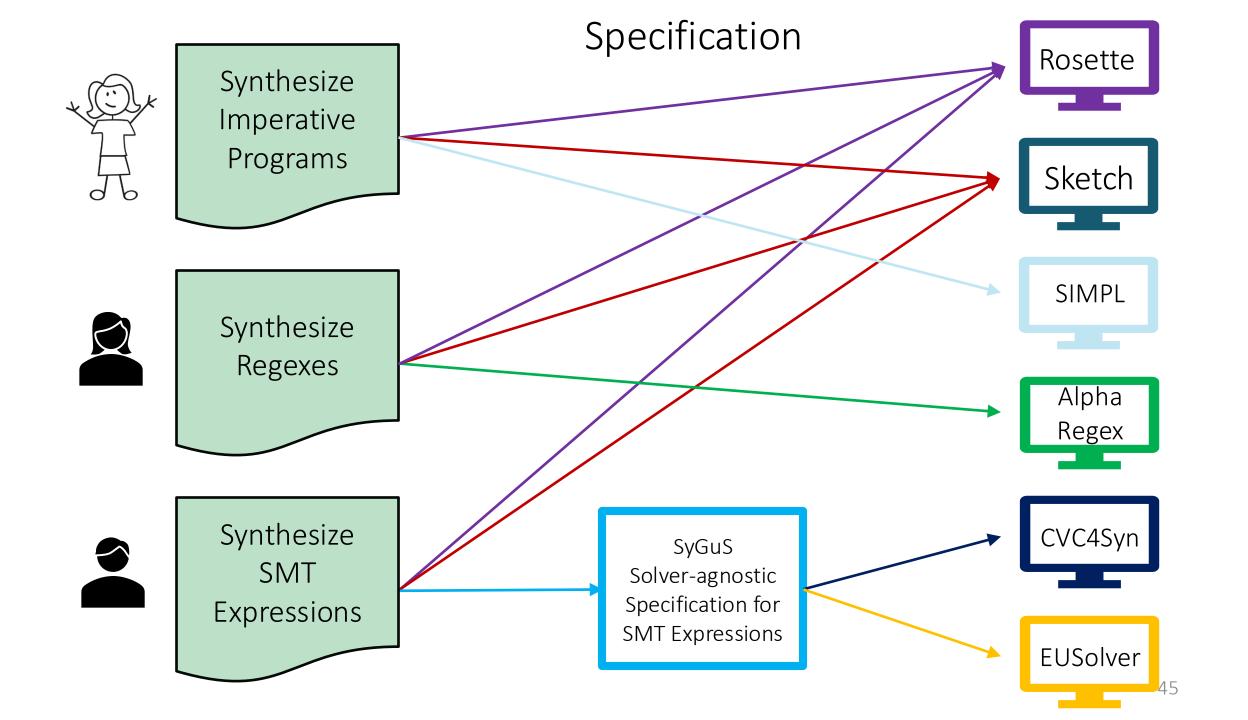
PROSE



https://microsoft.github.io/prose/

SemGuS

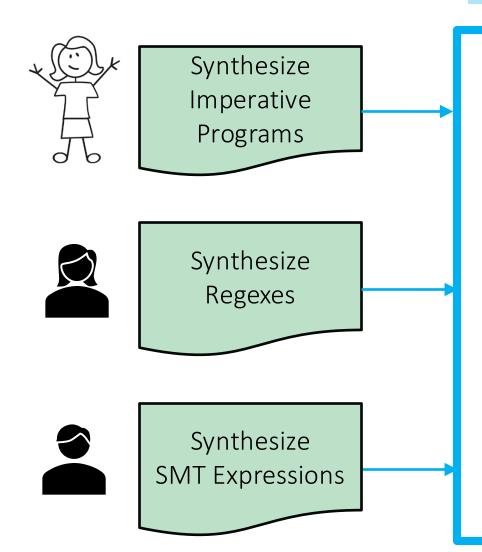
Semantics-guided synthesis



Unified benchmarks!

semgus.org

SemGuS Competition!



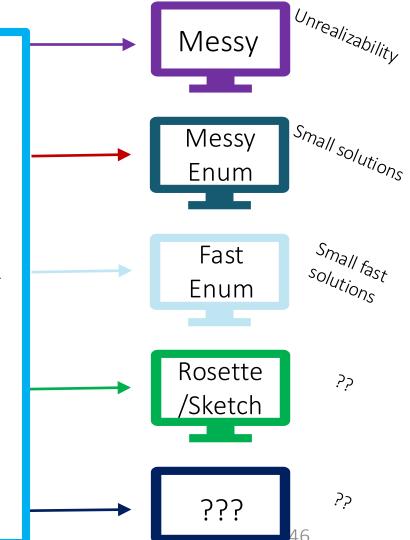
SemGuS

Domain-agnostic Solver-agnostic Specification Framework

Logic

Formal languages

Quantities/Probabilities



Next lectures

Topics:

- Representation-based search
- Stochastic search

Paper: Rishabh Singh: <u>BlinkFill: Semisupervised Programming By Example for Syntactic String Transformations</u>. VLDB'16

Projects:

- Once you have decided on the topic, send me message (one team member)
- If you haven't decided, talk to me after class