

# Real Numbers

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**Definition 1:** [rational\_numbers]/  
dedekind\_cuts

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**Definition 2:** [rational\_numbers, dedekind\_cuts, ordered\_field]/  
real\_numbers

The set of real numbers  $(\mathbb{R}, +, -, *, \leq)$  is an ordered field that can be defined as one of the following:

1. The set of dedekind cuts of the rational numbers.
2. The set of all numbers that can be represented as a decimal number.
3. The unique linearly ordered field that is complete (up to isomorphism).