

$$a) \quad C = \begin{pmatrix} x_0 & y_0 & z_0 \\ \frac{12}{5} & 0 & 1 & -\frac{12}{5} \\ 0 & 1 & 0 & -\frac{2}{3} \end{pmatrix}$$

$$D = \begin{pmatrix} x_0 & y_0 & z_0 \\ 0 & 1 & 0 & -\frac{2}{3} \end{pmatrix}$$

$$C' = ? \quad D' = ?$$

$$x \mapsto \frac{d}{z} \Rightarrow x'_0 = \frac{-1}{-\frac{12}{5}} = \frac{5}{12}$$

$$x'_D = \frac{-1}{-\frac{2}{3}} = \frac{3}{2}$$

$$y \mapsto \frac{d}{z} \Rightarrow y'_0 = \frac{-1 \cdot 0}{-\frac{12}{5}} = 0$$

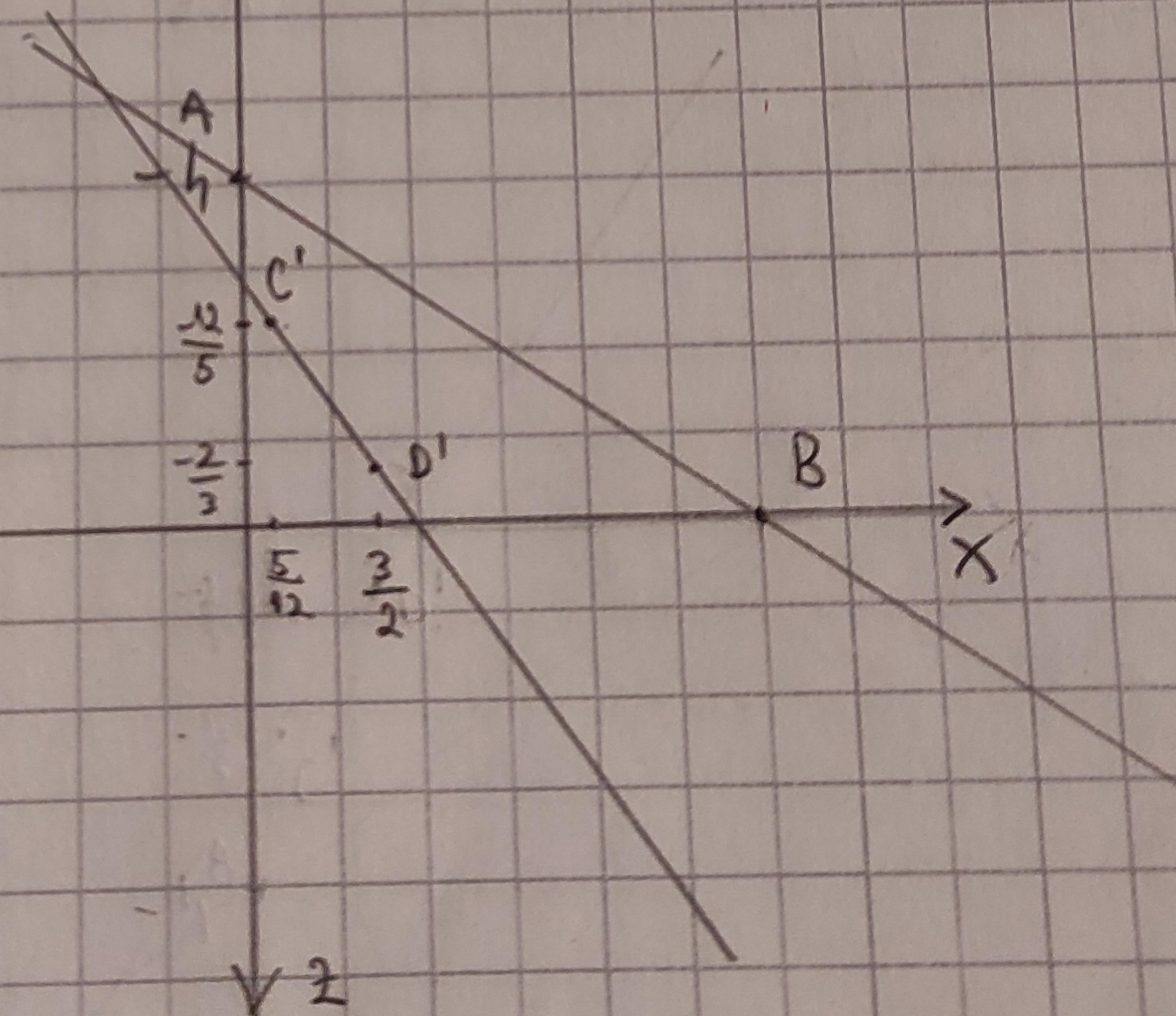
$$y'_D = \frac{-1 \cdot 0}{-\frac{2}{3}} = 0$$

$$z \mapsto z \quad z'_0 = -\frac{12}{5}$$

$$z'_D = -\frac{2}{3}$$

$$C' = \left( \frac{5}{12}, 0, -\frac{12}{5} \right)$$

$$D' = \left( \frac{3}{2}, 0, -\frac{2}{3} \right)$$



Pretpostavimo da su ta dva pravca paralelna. Kad između njih bi trebao biti  $0^\circ$ . Stoga je formula za skalarni produkt ( $\vec{a} \cdot \vec{b} = |\vec{a}| \cdot |\vec{b}| \cdot \cos\alpha$ ) dobivamo:

$$\vec{a} \cdot \vec{b} = |\vec{a}| \cdot |\vec{b}| \quad \text{tj.} \quad \vec{AB'} \cdot \vec{CD'} = |\vec{AB'}| \cdot |\vec{CD'}|$$

$$\vec{AB'} = B' - A' = (6, 0, 4)$$

$$\vec{CD'} = D' - C' = \left(\frac{13}{12}, 0, \frac{26}{15}\right)$$

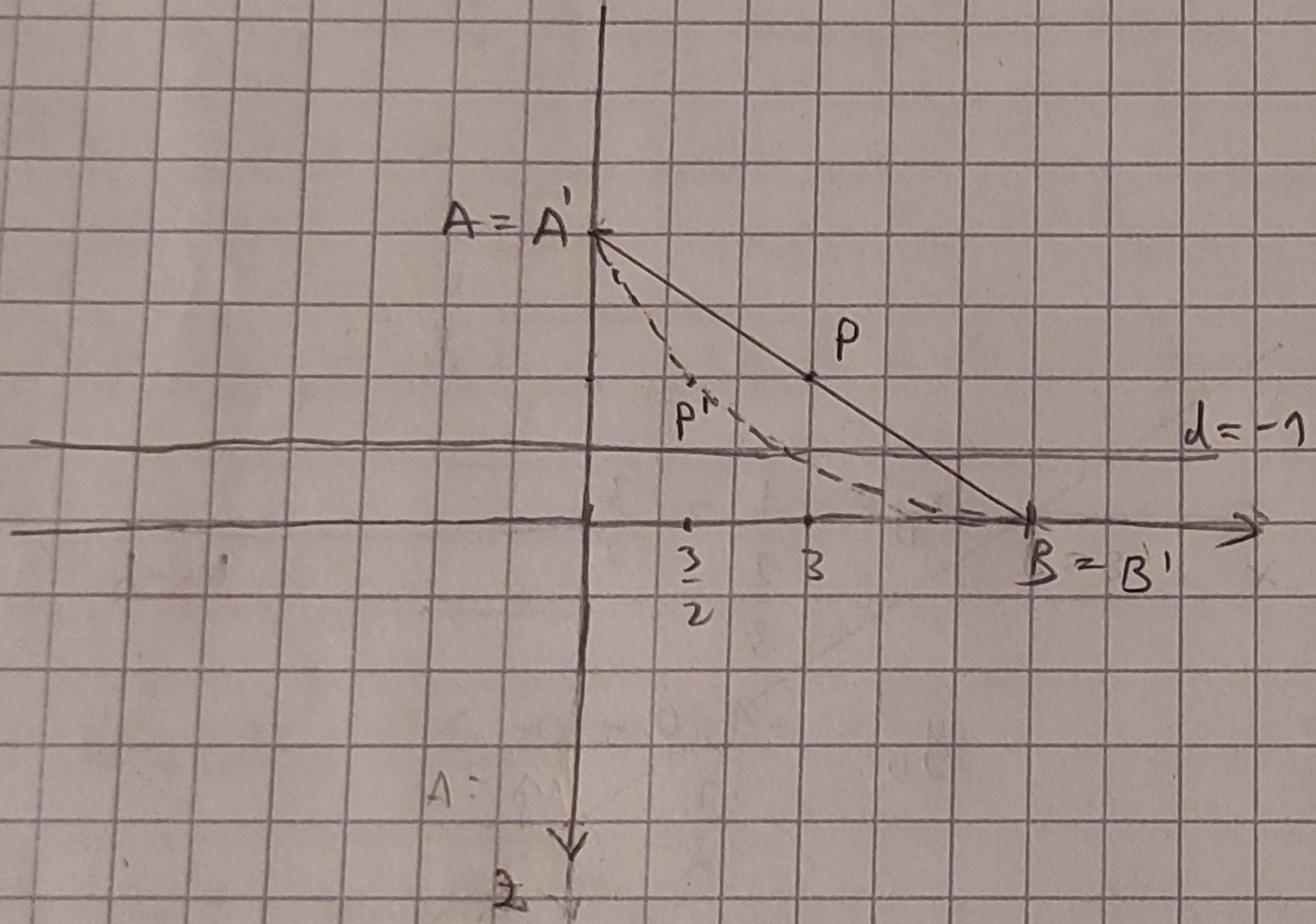
$$\vec{AB'} \cdot \vec{CD'} = |\vec{AB'}| \cdot |\vec{CD'}|$$

$$(6, 0, 4) \cdot \left(\frac{13}{12}, 0, \frac{26}{15}\right) = \sqrt{\left(\frac{13}{12}\right)^2 + \left(\frac{26}{15}\right)^2} \cdot \sqrt{6^2 + 4^2}$$

$$6 \cdot \frac{13}{12} + 4 \cdot \frac{26}{15} = \frac{13\sqrt{85}}{60} \cdot 2\sqrt{13}$$

$$13\sqrt{85} = 17.74$$

b)



$$x_p = \frac{x_A + x_{B'}}{2} = \frac{0 + 6}{2} = 3$$

$$z_p = \frac{z_A + z_{B'}}{2} = \frac{-4 + 0}{2} = -2$$

$$(x_1, y_1, z_1) \mapsto \left( \frac{-d \cdot x}{z}, \frac{-d \cdot y}{z}, z \right)$$

$$x'_p = -\frac{d \cdot x_p}{z} = -\frac{-1 \cdot 3}{-2} = \frac{3}{2}$$

$$z'_p = -2$$